# JEFFERSON MATH PROJECT REGENTS BY TYPE

The NY Geometry Regents Exams Fall 2007-August 2010 (Answer Key)

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Dear Sir

I have to acknolege the reciept of your favor of May 14. in which you mention that you have finished the 6. first books of Euclid, plane trigonometry, surveying & algebra and ask whether I think a further pursuit of that branch of science would be useful to you. there are some propositions in the latter books of Euclid, & some of Archimedes, which are useful, & I have no doubt you have been made acquainted with them. trigonometry, so far as this, is most valuable to every man, there is scarcely a day in which he will not resort to it for some of the purposes of common life. the science of calculation also is indispensible as far as the extraction of the square & cube roots; Algebra as far as the quadratic equation & the use of logarithms are often of value in ordinary cases: but all beyond these is but a luxury; a delicious luxury indeed; but not to be indulged in by one who is to have a profession to follow for his subsistence. in this light I view the conic sections, curves of the higher orders, perhaps even spherical trigonometry, Algebraical operations beyond the 2d dimension, and fluxions.

Letter from Thomas Jefferson to William G. Munford, Monticello, June 18, 1799.

#### ID: A

# Geometry Multiple Choice Regents Exam Questions Answer Section

1 ANS: 2 A dilation affects distance, not angle measure. PTS: 2 REF: 080906ge **TOP:** Identifying Transformations 2 ANS: 4 PTS: 2 REF: 081023ge TOP: Similarity KEY: perimeter and area 3 ANS: 4 PTS: 2 REF: 061003ge TOP: Solids 4 ANS: 3 2y = -6x + 8 Perpendicular lines have slope the opposite and reciprocal of each other. y = -3x + 4m = -3 $m_{\perp} = \frac{1}{3}$ PTS: 2 REF: 081024ge TOP: Parallel and Perpendicular Lines 5 ANS: 2 The length of the midsegment of a trapezoid is the average of the lengths of its bases.  $\frac{x+30}{2} = 44$ . x + 30 = 88*x* = 58 PTS: 2 REF: 011001ge TOP: Trapezoids 6 ANS: 1 PTS: 2 REF: 081009ge TOP: Equations of Circles 7 ANS: 1  $a^{2} + (5\sqrt{2})^{2} = (2\sqrt{15})^{2}$  $a^{2} + (25 \times 2) = 4 \times 15$  $a^2 + 50 = 60$  $a^2 = 10$  $a = \sqrt{10}$ PTS: 2 REF: 011016ge TOP: Pythagorean Theorem 8 ANS: 1 PTS: 2 REF: 081008ge TOP: Planes 9 ANS: 1 PTS: 2 REF: 061005ge **TOP:** Properties of Transformations 10 ANS: 2  $M_x = \frac{3x+5+x-1}{2} = \frac{4x+4}{2} = 2x+2, \ M_y = \frac{3y+(-y)}{2} = \frac{2y}{2} = y.$ 

PTS: 2REF: 081019geTOP: Midpoint11ANS: 3PTS: 2REF: 081021geTOP: Properties of Transformations



PTS: 2 REF: 081001ge TOP: Trian

TOP: Triangle Congruency

The slope of a line in standard form is  $-\frac{A}{B}$ , so the slope of this line is  $\frac{-2}{-1} = 2$ . A parallel line would also have a slope of 2. Since the answers are in slope intercept form, find the *y*-intercept: y = mx + b-11 = 2(-3) + b-5 = b

PTS: 2 REF: fall0812ge TOP: Parallel and Perpendicular Lines 14 ANS: 2 6+17>22

PTS: 2 REF: 080916ge TOP: Triangle Inequality Theorem 15 ANS: 4

The slope of a line in standard form is  $-\frac{A}{B}$ , so the slope of this line is  $\frac{-4}{2} = -2$ . A parallel line would also have a slope of -2. Since the answers are in slope intercept form, find the *y*-intercept: y = mx + b

3 = -2(7) + b17 = b

PTS: 2 REF: 081010ge TOP: Parallel and Perpendicular Lines  
16 ANS: 3  
PTS: 2 REF: 060902ge TOP: Triangle Congruency  
17 ANS: 3 PTS: 2 REF: fallo816ge TOP: Planes  
18 ANS: 4  
SA = 
$$4\pi r^2$$
  $V = \frac{4}{3}\pi r^3 = \frac{4}{3}\pi \cdot 6^3 = 288\pi$   
 $144\pi = 4\pi r^2$   
 $36 = r^2$   
 $6 = r$   
PTS: 2 REF: 081020ge TOP: Volume and Surface Area

REF: 060908ge 19 ANS: 3 PTS: 2 **TOP:** Identifying Transformations 20 ANS: 3 PTS: 2 REF: 081026ge TOP: Contrapositive 21 ANS: 1  $\triangle PRT$  and  $\triangle SRQ$  share  $\angle R$  and it is given that  $\angle RPT \cong \angle RSQ$ . PTS: 2 REF: fall0821ge **TOP:** Similarity Proofs 22 ANS: 2  $x^{2} + (x+7)^{2} = 13^{2}$  $x^{2} + x^{2} + 7x + 7x + 49 = 169$  $2x^2 + 14x - 120 = 0$  $x^{2} + 7x - 60 = 0$ (x+12)(x-5) = 0*x* = 5 2x = 10PTS: 2 TOP: Pythagorean Theorem REF: 061024ge 23 ANS: 1 PTS: 2 REF: 061010ge TOP: Angle Side Relationship 24 ANS: 2  $\frac{140 - \overline{RS}}{2} = 40$  $140 - \overline{RS} = 80$  $\overline{RS} = 60$ PTS: 2 REF: 081025ge TOP: Arcs Determined by Angles KEY: outside circle 25 ANS: 4 PTS: 2 REF: 011012ge TOP: Planes 26 ANS: 1 PTS: 2 REF: 081028ge TOP: Centroid, Orthocenter, Incenter and Circumcenter 27 ANS: 4  $x^2 = (4+5) \times 4$  $x^2 = 36$ x = 6PTS: 2 REF: 011008ge TOP: Segments Intercepted by Circle KEY: tangent and secant 28 ANS: 4 REF: 060922ge TOP: Equations of Circles PTS: 2

29 ANS: 3  $4(x+4) = 8^{2}$  4x + 16 = 64x = 12

PTS: 2 REF: 060916ge TOP: Segments Intercepted by Circle KEY: tangent and secant 30 ANS: 4 PTS: 2 REF: 061008ge TOP: Trapezoids 31 ANS: 3 18 11 ĮO 22 PTS: 2 REF: 080920ge **TOP:** Midsegments 32 ANS: 2 REF: 061020ge **TOP:** Constructions PTS: 2 33 ANS: 2 PTS: 2 REF: 081015ge TOP: Properties of Transformations 34 ANS: 4 PTS: 2 REF: 061015ge TOP: Identifying Transformations 35 ANS: 1 PTS: 2 REF: 060903ge **TOP:** Identifying Transformations 36 ANS: 3 The diagonals of an isosceles trapezoid are congruent. 5x + 3 = 11x - 5. 6x = 18x = 3PTS: 2 REF: fall0801ge TOP: Trapezoids 37 ANS: 3 PTS: 2 REF: 061004ge TOP: Isosceles Triangle Theorem 38 ANS: 4  $\triangle ABC \sim \triangle DBE. \quad \frac{\overline{AB}}{\overline{DB}} = \frac{\overline{AC}}{\overline{DE}}$  $\frac{9}{2} = \frac{x}{3}$ *x* = 13.5 PTS: 2 REF: 060927ge TOP: Side Splitter Theorem 39 ANS: 1  $\angle DCB$  and  $\angle ADC$  are supplementary adjacent angles of a parallelogram. 180 - 120 = 60.  $\angle 2 = 60 - 45 = 15$ .

PTS: 2 REF: 080907ge TOP: Parallelograms

The closer a chord is to the center of a circle, the longer the chord.

	PTS: 2	REF: 011005ge	TOP: Chords	
41	ANS: 3	PTS: 2	REF: fall0804ge TOP: Constructions	
42	ANS: 2	PTS: 2	REF: 011003ge TOP: Properties of Transform	ations
43	ANS: 2	PTS: 2	REF: 011006ge TOP: Isometries	
44	ANS: 3	PTS: 2	REF: 011010ge TOP: Equations of Circles	
45	ANS: 2			
	The slope of $y = \frac{1}{2}$	$\frac{1}{2}x + 5$ is $\frac{1}{2}$ . The slope of	of a perpendicular line is $-2$ . $y = mx + b$ .	
			5 = (-2)(-2) + b	
			<i>b</i> = 1	
	PTS: 2	REF: 060907ge	TOP: Parallel and Perpendicular Lines	
46	ANS: 2			
	Because the triang	les are similar, $\frac{\mathbf{m} \angle A}{\mathbf{m} \angle D} =$	1	
	PTS: 2	REF: 011022ge	TOP: Similarity KEY: perimeter and area	
47	ANS: 2	C		
			A B	
	$\angle ACB$ and $\angle ECD$	are congruent vertical a	angles and $\angle CAB \cong \angle CED$ .	
	PTS·2	REF 060917ge	TOP Similarity Proofs	
48	ANS: 1	PTS: 2	REF: 081012ge TOP: Tangents	
-	KEY: two tangent	ts		
49	ANS: 2	PTS: 2	REF: 011004ge TOP: Constructions	
50	ANS: 3			
	PTS: 2	REF: fall0805ge	TOP: Quadratic-Linear Systems	
51	ANS: 3	PTS: 2	REF: 060928ge TOP: Planes	
52	ANS: 2			
	7 + 18 > 6 + 12			
	PTS·2	REF fall0819ge	TOP. Triangle Inequality Theorem	
53	ANS: 4	8-		
	Median $\overline{BF}$ bisects	s $\overline{AC}$ so that $\overline{CF} \cong \overline{FA}$		
	PTS: 2	REF: fall0810ge	TOP: Statements	

54 ANS: 3 PTS: 2 REF: 080924ge **TOP:** Negations 55 ANS: 2 PTS: 2 REF: 061007ge TOP: Parallel Lines and Transversals 56 ANS: 3 PTS: 2 REF: fall0814ge TOP: Equations of Circles 57 ANS: 2 REF: fall0806ge PTS: 2 TOP: Planes 58 ANS: 2 PTS: 2 REF: 061022ge TOP: Parallel and Perpendicular Lines 59 ANS: 3  $m = \frac{-A}{R} = -\frac{3}{4}$ PTS: 2 REF: 011025ge TOP: Parallel and Perpendicular Lines 60 ANS: 1 Translations and reflections do not affect distance. PTS: 2 REF: 080908ge **TOP:** Properties of Transformations 61 ANS: 1 After the translation, the coordinates are A'(-1,5) and B'(3,4). After the dilation, the coordinates are A''(-2,10)and B''(6,8). PTS: 2 REF: fall0823ge **TOP:** Compositions of Transformations 62 ANS: 2 PTS: 2 REF: 080921ge TOP: Equations of Circles 63 ANS: 2 PTS: 2 REF: 060910ge TOP: Equations of Circles 64 ANS: 2 The slope of a line in standard form is  $-\frac{A}{B}$  so the slope of this line is  $-\frac{5}{3}$  Perpendicular lines have slope that are the opposite and reciprocal of each other. REF: fall0828ge PTS: 2 TOP: Parallel and Perpendicular Lines 65 ANS: 1  $(x,y) \rightarrow (x+3,y+1)$ PTS: 2 REF: fall0803ge **TOP:** Translations 66 ANS: 4  $d = \sqrt{\left(-3 - 1\right)^2 + \left(2 - 0\right)^2} = \sqrt{16 + 4} = \sqrt{20} = \sqrt{4} \cdot \sqrt{5} = 2\sqrt{5}$ PTS: 2 REF: 011017ge TOP: Distance 67 ANS: 3 REF: 081002ge PTS: 2 TOP: Planes PTS: 2 68 ANS: 3 REF: 080913ge TOP: Triangle Congruency 69 ANS: 2 PTS: 2 REF: 081007ge TOP: Triangle Congruency

70 ANS: 4 
$$180 - (40 + 40) = 100$$

PTS: 2 REF: 080903ge TOP: Isosceles Triangle Theorem

71 ANS: 4

The marked 60° angle and the angle above it are on the same straight line and supplementary. This unmarked supplementary angle is 120°. Because the unmarked 120° angle and the marked 120° angle are alternate exterior angles and congruent,  $d \parallel e$ .

PTS: 2 REF: 080901ge TOP: Parallel Lines and Transversals 72 ANS: 3  $m = \frac{-A}{B} = \frac{5}{2}$ .  $m = \frac{-A}{B} = \frac{10}{4} = \frac{5}{2}$ PTS: 2 REF: 011014ge TOP: Parallel and Perpendicular Lines 73 ANS: 1



PTS: 2	REF: 060923ge	TOP: Quadratic-Linear Systems
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74 ANS: 2

Adjacent sides of a rectangle are perpendicular and have opposite and reciprocal slopes.

79 ANS: 3 PTS: 2 REF: fall0825ge TOP: Centroid, Orthocenter, Incenter and Circumcenter 80 ANS: 2 REF: 080927ge PTS: 2 TOP: Planes 81 ANS: 1  $3x^2 + 18x + 24$  $3(x^2 + 6x + 8)$ 3(x+4)(x+2)PTS: 2 REF: fall0815ge TOP: Volume 82 ANS: 1 Since  $AC \cong BC$ ,  $m \angle A = m \angle B$  under the Isosceles Triangle Theorem. PTS: 2 REF: fall0809ge TOP: Triangles in the Coordinate Plane 83 ANS: 4 PTS: 2 REF: 080915ge TOP: Identifying Transformations 84 ANS: 4 sum of interior  $\angle s = \text{sum of exterior } \angle s$  $(n-2)180 = n \left( 180 - \frac{(n-2)180}{n} \right)$ 180n - 360 = 180n - 180n + 360180n = 720*n* = 4 PTS: 2 TOP: Interior and Exterior Angles of Polygons REF: 081016ge 85 ANS: 1 PTS: 2 REF: 061013ge TOP: Tangents KEY: point of tangency 86 ANS: 1  $\overline{GC} = 2\overline{FG}$ The centroid divides each median into segments whose lengths are in the ratio 2 : 1.  $\overline{GC} + \overline{FG} = 24$  $2\overline{FG} + \overline{FG} = 24$  $3\overline{FG} = 24$  $\overline{FG} = 8$ PTS: 2 REF: 081018ge TOP: Centroid 87 ANS: 1 PTS: 2 REF: 060920ge **TOP:** Graphing Circles 88 ANS: 1 If  $\angle A$  is at minimum (50°) and  $\angle B$  is at minimum (90°),  $\angle C$  is at maximum of 40° (180° - (50° + 90°)). If  $\angle A$  is at maximum (60°) and  $\angle B$  is at maximum (100°),  $\angle C$  is at minimum of 20° (180° - (60° + 100°)).

PTS: 2 REF: 060901ge TOP: Interior and Exterior Angles of Triangles

89 ANS: 2  $\frac{3}{7} = \frac{6}{x}$ 3x = 42*x* = 14 PTS: 2 REF: 081027ge TOP: Side Splitter Theorem 90 ANS: 4  $d = \sqrt{(-6-2)^2 + (4-(-5))^2} = \sqrt{64+81} = \sqrt{145}$ TOP: Distance PTS: 2 REF: 081013ge 91 ANS: 2 (d+4)4 = 12(6)4d + 16 = 72d = 14r = 7REF: 061023ge TOP: Segments Intercepted by Circle PTS: 2 KEY: two secants 92 ANS: 4 180 - (50 + 30) = 100PTS: 2 REF: 081006ge TOP: Similarity KEY: basic 93 ANS: 3 PTS: 2 REF: 011028ge **TOP:** Conditional Statements 94 ANS: 4 PTS: 2 REF: 060913ge **TOP:** Conditional Statements 95 ANS: 2  $x^2 = 3(x+18)$  $x^2 - 3x - 54 = 0$ (x-9)(x+6) = 0x = 9PTS: 2 REF: fall0817ge TOP: Segments Intercepted by Circle KEY: tangent and secant 96 ANS: 3 The slope of y = x + 2 is 1. The slope of y - x = -1 is  $\frac{-A}{B} = \frac{-(-1)}{1} = 1$ . PTS: 2 REF: 080909ge TOP: Parallel and Perpendicular Lines



104 ANS: 2  $M_x = \frac{-2+6}{2} = 2$ .  $M_y = \frac{-4+2}{2} = -1$ PTS: 2 REF: 080910ge TOP: Midpoint 105 ANS: 3 ς 20 15  $\frac{36-20}{2}$  $\sqrt{17^2 - 8^2} = 15$ 8 36 A = 8. PTS: 2 REF: 061016ge TOP: Trapezoids 106 ANS: 1 x + 2x + 2 + 3x + 4 = 1806x + 6 = 180x = 29PTS: 2 REF: 011002ge TOP: Interior and Exterior Angles of Triangles 107 ANS: 4 PTS: 2 REF: fall0824ge TOP: Tangents KEY: common tangency 108 ANS: 1  $V = \pi r^2 h$  $1000 = \pi r^2 \cdot 8$  $r^2 = \frac{1000}{8\pi}$  $r \approx 6.3$ PTS: 2 REF: 080926ge TOP: Volume 109 ANS: 4 PTS: 2 REF: fall0818ge TOP: Analytical Representations of Transformations 110 ANS: 1 PTS: 2 REF: 060918ge TOP: Planes 111 ANS: 1 Opposite sides of a parallelogram are congruent. 4x - 3 = x + 3. SV = (2) + 3 = 5. 3x = 6x = 2PTS: 2 REF: 011013ge TOP: Parallelograms 112 ANS: 2 PTS: 2 REF: 011011ge TOP: Locus

Parallel lines intercept congruent arcs.



PTS: 2 REF: 081017ge TOP: Segments Intercepted by Circle KEY: two chords

115 ANS: 4

The slope of y = -3x + 2 is -3. The perpendicular slope is  $\frac{1}{3}$ .  $-1 = \frac{1}{3}(3) + b$ -1 = 1 + bb = -2



120 ANS: 4 3y + 1 = 6x + 4. 2y + 1 = x - 93y = 6x + 3 2y = x - 10 $y = 2x + 1 \qquad \qquad y = \frac{1}{2}x - 5$ REF: fall0822ge PTS: 2 TOP: Parallel and Perpendicular Lines 121 ANS: 1  $M_x = \frac{-2+6}{2} = 2$ .  $M_y = \frac{3+3}{2} = 3$ . The center is (2,3).  $d = \sqrt{(-2-6)^2 + (3-3)^2} = \sqrt{64+0} = 8$ . If the diameter is 8, the radius is 4 and  $r^2 = 16$ . PTS: 2 REF: fall0820ge TOP: Equations of Circles 122 ANS: 3 PTS: 2 REF: 060925ge TOP: Constructions 123 ANS: 1  $\angle A = \frac{(n-2)180}{n} = \frac{(5-2)180}{5} = 108 \ \angle AEB = \frac{180-108}{2} = 36$ PTS: 2 REF: 081022ge TOP: Interior and Exterior Angles of Polygons 124 ANS: 1 In an equilateral triangle, each interior angle is 60° and each exterior angle is 120° (180° - 120°). The sum of the three interior angles is 180° and the sum of the three exterior angles is 360°. PTS: 2 REF: 060909ge TOP: Interior and Exterior Angles of Triangles 125 ANS: 2 Parallel chords intercept congruent arcs.  $\widehat{mAC} = \widehat{mBD} = 30$ . 180 - 30 - 30 = 120. PTS: 2 REF: 080904ge TOP: Chords 126 ANS: 4  $L = 2\pi rh = 2\pi \cdot 5 \cdot 11 \approx 345.6$ REF: 061006ge **PTS: 2** TOP: Volume 127 ANS: 4 (n-2)180 = (8-2)180 = 1080.  $\frac{1080}{8} = 135.$ PTS: 2 REF: fall0827ge TOP: Interior and Exterior Angles of Polygons 128 ANS: 4 PTS: 2 REF: fall0802ge TOP: Negations 129 ANS: 1 PTS: 2 REF: 061009ge TOP: Converse 130 ANS: 2  $M_x = \frac{2 + (-4)}{2} = -1$ .  $M_y = \frac{-3 + 6}{2} = \frac{3}{2}$ . PTS: 2 REF: fall0813ge TOP: Midpoint

131	ANS: 3 $\frac{36+20}{2} = 28$						
132	PTS: 2 KEY: inside circle ANS: 2 4(4x-3) = 3(2x+8)	REF:	061019ge	TOP:	Arcs Determi	ned by .	Angles
	16x - 12 = 6x + 24						
	10x = 36						
	x = 3.6						
	PTS: 2 KEY: two chords	REF:	080923ge	TOP:	Segments Inte	ercepted	l by Circle
133	ANS: 4	PTS:	2	REF:	060912ge	TOP:	Locus
134	ANS: 3	PTS:	2	REF:	060905ge	TOP:	Reflections
	KEY: basic						
135	ANS: 2						
	The centroid divides	s each m	edian into segr	nents w	hose lengths a	re in the	eratio 2 : 1.
	PTS: 2	REF:	060914ge	TOP:	Centroid		
136	ANS: 4	PTS:	2	REF:	080905ge	TOP:	Triangle Congruency
137	ANS: 4	PTS:	2	REF:	080914ge	TOP:	Planes
138	ANS: 4	PTS:	2	REF:	011019ge	TOP:	Similarity Proofs
139	ANS: 4				_		
	The slope of $y = -\frac{2}{3}x - 5$ is $-\frac{2}{3}$ . Perpendicular lines have slope that are opposite reciprocals.						
	PTS: 2	REF:	080917ge	TOP:	Parallel and P	erpendi	cular Lines
140	ANS: 4		C			1	
	Corresponding angles of similar triangles are congruent.						
	PTS: 2	REF:	fall0826ge	TOP:	Similarity	KEY:	perimeter and area
141	ANS: 3	PTS:	2	REF:	011007ge	TOP:	Isosceles Triangle Theorem
142	ANS: 4						
	(4) is not true if $\angle Pg$	<i>QR</i> is ol	otuse.				
	PTS: 2	REF:	060924ge	TOP:	Exterior Angl	e Theor	rem
143	ANS: 3		-		C		
	The lateral edges of	a prism	are parallel.				
	PTS: 2	REF:	fall0808ge	TOP:	Solids		

144 ANS: 1  $V = \frac{1}{3} \pi r^2 h = \frac{1}{3} \pi \cdot 4^2 \cdot 12 \approx 201$ PTS: 2 REF: 060921ge TOP: Volume and Lateral Area 145 ANS: 2 The slope of 2x + 3y = 12 is  $-\frac{A}{B} = -\frac{2}{3}$ . The slope of a perpendicular line is  $\frac{3}{2}$ . Rewritten in slope intercept form, (2) becomes  $y = \frac{3}{2}x + 3$ . REF: 060926ge PTS: 2 TOP: Parallel and Perpendicular Lines 146 ANS: 4 Let  $\overline{AD} = x$ .  $36x = 12^2$ x = 4TOP: Similarity REF: 080922ge KEY: leg PTS: 2 147 ANS: 4 y+x=4.  $x^2-6x+10=-x+4$ . y+x=4. y+2=4y = -x + 4  $x^2 - 5x + 6 = 0$  y + 3 = 4 y = 2(x-3)(x-2) = 0 y = 1x = 3 or 2PTS: 2 REF: 080912ge TOP: Quadratic-Linear Systems 148 ANS: 4 PTS: 2 REF: 081005ge **TOP:** Constructions 149 ANS: 3  $V = \pi r^2 h = \pi \cdot 6^2 \cdot 27 = 972\pi$ TOP: Volume PTS: 2 REF: 011027ge 150 ANS: 1 PTS: 2 REF: 061012ge TOP: Constructions

158 ANS: 4

159 ANS: 1

160 ANS: 1

PTS: 2



PTS: 2

PTS: 2

TOP: Centroid, Orthocenter, Incenter and Circumcenter

REF: 080919ge

 $d = \sqrt{(-4-2)^2 + (5-(-5))^2} = \sqrt{36+100} = \sqrt{136} = \sqrt{4} \cdot \sqrt{34} = 2\sqrt{34}.$ 

PTS: 2 REF: 011021ge TOP: Exterior Angle Theorem 152 ANS: 2 Parallel chords intercept congruent arcs.  $\widehat{mAD} = \widehat{mBC} = 60$ .  $\underline{m\angle CDB} = \frac{1}{2} \widehat{mBC} = 30$ . PTS: 2 REF: 060906ge TOP: Chords 153 ANS: 1 A'(2,4)PTS: 2 REF: 011023ge TOP: Compositions of Transformations KEY: basic 154 ANS: 1 TOP: Special Quadrilaterals PTS: 2 REF: 080918ge 155 ANS: 2 PTS: 2 REF: 011020ge **TOP:** Graphing Circles 156 ANS: 4  $\overline{BG}$  is also an angle bisector since it intersects the concurrence of  $\overline{CD}$  and  $\overline{AE}$ PTS: 2 REF: 061025ge KEY: Centroid, Orthocenter, Incenter and Circumcenter 157 ANS: 3 Because OC is a radius, its length is 5. Since CE = 2 OE = 3.  $\triangle EDO$  is a 3-4-5 triangle. If ED = 4, BD = 8. PTS: 2 REF: fall0811ge TOP: Chords

REF: 080925ge

TOP: Distance

REF: 080911ge

TOP: Equations of Circles

x = 12



### **Geometry 2 Point Regents Exam Questions**

### **Answer Section**

1 ANS:  

$$y = \frac{2}{3}x - 9$$
. The slope of  $2x - 3y = 11$  is  $-\frac{A}{B} = \frac{-2}{-3} = \frac{2}{3}$ .  $-5 = \left(\frac{2}{3}\right)(6) + b$   
 $-5 = 4 + b$   
 $b = -9$ 

PTS: 2 REF: 080931ge TOP: Parallel and Perpendicular Lines 2 ANS: 20. 5x + 10 = 4x + 30x = 20

PTS: 2 REF: 060934ge TOP: Similarity KEY: basic 3 ANS: 18.  $V = \frac{1}{3}Bh = \frac{1}{3}lwh$   $288 = \frac{1}{3} \cdot 8 \cdot 6 \cdot h$  288 = 16h 18 = h4 ANS:  $(x+1)^2 + (y-2)^2 = 36$ PTS: 2 REF: 081034ge TOP: Equations of Circles

20. The sides of the triangle formed by connecting the midpoints are half the sides of the original triangle.



PTS: 2 REF: 060929ge TOP: Midsegments

6 ANS:

True. The first statement is true and the second statement is false. In a disjunction, if either statement is true, the disjunction is true.

PTS: 2 REF: 060933ge TOP: Compound Statements KEY: disjunction 7 ANS:

$$67. \ \frac{180 - 46}{2} = 67$$

PTS: 2 REF: 011029ge TOP: Isosceles Triangle Theorem

8 ANS:

6. The centroid divides each median into segments whose lengths are in the ratio 2 : 1.  $\overline{TD} = 6$  and  $\overline{DB} = 3$ 

PTS: 2 REF: 011034ge TOP: Centroid

9 ANS:



PTS: 2 REF: 081032ge TOP: Constructions

10 ANS:

452.  $SA = 4\pi r^2 = 4\pi \cdot 6^2 = 144\pi \approx 452$ 

PTS:	2	REF:	061029ge	TOP:	Volume and Surface Area
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PTS: 2 REF: fall0832ge TOP: Constructions 13 ANS: 4.  $l_1w_1h_1 = l_2w_2h_2$ 

$$10 \times 2 \times h = 5 \times w_2 \times h$$
$$20 = 5w_2$$
$$w_2 = 4$$

PTS: 2 REF: 011030ge TOP: Volume 14 ANS:

PTS: 2 REF: 080932ge TOP: Constructions 15 ANS:

y = -2x + 14. The slope of 2x + y = 3 is  $\frac{-A}{B} = \frac{-2}{1} = -2$ . y = mx + b. 4 = (-2)(5) + bb = 14

PTS: 2 REF: 060931ge TOP: Parallel and Perpendicular Lines

- 16 <u>ANS</u>: <u>AC</u>. m $\angle BCA = 63$  and m $\angle ABC = 80$ . <u>AC</u> is the longest side as it is opposite the largest angle.
  - PTS: 2 REF: 080934ge TOP: Angle Side Relationship
- 17 ANS:  $375\pi \ L = \pi r l = \pi (15)(25) = 375\pi$

PTS: 2 REF: 081030ge TOP: Volume and Lateral Area



PTS: 2 REF: 061033ge TOP: Locus 19 ANS: 34. 2x - 12 + x + 90 = 180 3x + 78 = 90 3x = 102x = 34

PTS: 2 REF: 061031ge TOP: Interior and Exterior Angles of Triangles 20 ANS:



PTS: 2 REF: 060930ge TOP: Constructions

21 ANS:

Contrapositive-If two angles of a triangle are not congruent, the sides opposite those angles are not congruent.

PTS: 2 REF: fall0834ge TOP: Conditional Statements

- 22 ANS:
  - 3. The non-parallel sides of an isosceles trapezoid are congruent. 2x + 5 = 3x + 2

x = 3

PTS: 2 REF: 080929ge TOP: Trapezoids 23 ANS: 6x + 20 = x + 40 + 4x - 5110. 6x + 20 = 5x + 35x = 156((15) + 20 = 110)PTS: 2 REF: 081031ge TOP: Isosceles Triangle Theorem 24 ANS: 37. Since  $\overline{DE}$  is a midsegment, AC = 14. 10 + 13 + 14 = 37PTS: 2 REF: 061030ge TOP: Midsegments 25 ANS: 70. 3x + 5 + 3x + 5 + 2x + 2x = 18010x + 10 = 36010x = 350*x* = 35 2x = 70PTS: 2 REF: 081029ge TOP: Trapezoids 26 ANS: 5.  $\frac{3}{x} = \frac{6+3}{15}$ 9x = 45x = 5PTS: 2 REF: 011033ge TOP: Side Splitter Theorem 27 ANS: (6,-4).  $C_x = \frac{Q_x + R_x}{2}$ .  $C_y = \frac{Q_y + R_y}{2}$ .  $3.5 = \frac{1 + R_x}{2} \qquad 2 = \frac{8 + R_y}{2}$  $7 = 1 + R_x \qquad 4 = 8 + R_y$  $6 = R_x \qquad -4 = R_y$ 

PTS: 2 REF: 011031ge TOP: Midpoint



PTS: 2 REF: fall0830ge TOP: Properties of Transformations 32 ANS:

25. 
$$d = \sqrt{(-3-4)^2 + (1-25)^2} = \sqrt{49+576} = \sqrt{625} = 25.$$

PTS: 2 REF: fall0831ge TOP: Distance

33 ANS: 22.4.  $V = \pi r^2 h$ 12566.4 =  $\pi r^2 \cdot 8$   $r^2 = \frac{12566.4}{8\pi}$  $r \approx 22.4$ 

PTS: 2 REF: fall0833ge TOP: Volume 34 ANS:

2016. 
$$V = \frac{1}{3}Bh = \frac{1}{3}s^2h = \frac{1}{3}12^2 \cdot 42 = 2016$$

PTS: 2 REF: 080930ge TOP: Volume 35 ANS:



PTS: 2 REF: 061032ge TOP: Reflections KEY: grids 36 ANS:



### Geometry 4 Point Regents Exam Questions Answer Section

1 ANS:

Yes,  $m\angle ABD = m\angle BDC = 44\ 180 - (93 + 43) = 44\ x + 19 + 2x + 6 + 3x + 5 = 180$ . Because alternate interior

6x + 30 = 1806x = 150x = 25x + 19 = 44

angles  $\angle ABD$  and  $\angle CDB$  are congruent,  $\overline{AB}$  is parallel to  $\overline{DC}$ .

PTS: 4 REF: 081035ge TOP: Parallel Lines and Transversals 2 ANS:

2.4.  $5a = 4^2$   $5b = 3^2$   $h^2 = ab$ a = 3.2 b = 1.8  $h^2 = 3.2 \cdot 1.8$  $h = \sqrt{5.76} = 2.4$ 

PTS: 4 REF: 081037ge TOP: Similarity KEY: altitude 3 ANS:

36, because a dilation does not affect angle measure. 10, because a dilation does affect distance.

PTS: 4 REF: 011035ge TOP: Properties of Transformations 4 ANS: Midpoint:  $\left(\frac{-4+4}{2}, \frac{2+(-4)}{2}\right) = (0,-1)$ . Distance:  $d = \sqrt{(-4-4)^2 + (2-(-4))^2} = \sqrt{100} = 10$  r = 5  $r^2 = 25$  $x^2 + (v+1)^2 = 25$ 

PTS: 2 REF: 061037ge TOP: Equations of Circles

5 ANS:  $y = \frac{4}{3}x - 6$ .  $M_x = \frac{-1+7}{2} = 3$  The perpendicular bisector goes through (3,-2) and has a slope of  $\frac{4}{3}$ .  $M_y = \frac{1+(-5)}{2} = -2$   $m = \frac{1-(-5)}{-1-7} = -\frac{3}{4}$  $y - y_M = m(x - x_M)$ .

$$y-1=\frac{4}{3}(x-2)$$

PTS: 4 REF: 080935ge TOP: Perpendicular Bisector

6 ANS:



PTS: 4 REF: fall0835ge TOP: Midsegments 7 ANS:

 $\angle D$ ,  $\angle G$  and 24° or  $\angle E$ ,  $\angle F$  and 84°.  $\widehat{mFE} = \frac{2}{15} \times 360 = 48$ . Since the chords forming  $\angle D$  and  $\angle G$  are intercepted by  $\widehat{FE}$ , their measure is 24°.  $\widehat{mGD} = \frac{7}{15} \times 360 = 168$ . Since the chords forming  $\angle E$  and  $\angle F$  are intercepted by  $\widehat{GD}$ , their measure is 84°.

PTS: 4 REF: fall0836ge TOP: Arcs Determined by Angles KEY: inscribed



- PTS: 4
- REF: 080937ge T

TOP: Properties of Transformations

9 ANS:



PTS: 4 REF: 060936ge 10 ANS:



TOP: Triangles in the Coordinate Plane

F: 011037ge TOP: Locus

11 ANS:  

$$y = \frac{2}{3}x + 1$$
.  $2y + 3x = 6$ .  $y = mx + b$   
 $2y = -3x + 6$   $5 = \frac{2}{3}(6) + b$   
 $y = -\frac{3}{2}x + 3$   $5 = 4 + b$   
 $m = -\frac{3}{2}$   $1 = b$   
 $m_{\perp} = \frac{2}{3}$   $y = \frac{2}{3}x + 1$ 

PTS: 4 REF: 061036ge 12 ANS:





PTS: 4 REF: 060937ge TOP: Compositions of Transformations KEY: grids

13 ANS:

18. If the ratio of *TA* to *AC* is 1:3, the ratio of *TE* to *ES* is also 1:3. x + 3x = 24. 3(6) = 18.

x = 6

PTS: 4 REF: 060935ge TOP: Tangents KEY: common tangency 14 ANS:



PTS: 4 REF: fall0837ge TOP: Locus

 $\overline{JK} \cong \overline{LM}$  because opposite sides of a parallelogram are congruent.  $\overline{LM} \cong \overline{LN}$  because of the Isosceles Triangle Theorem.  $\overline{LM} \cong \overline{JM}$  because of the transitive property. JKLM is a rhombus because all sides are congruent.

- PTS: 4 REF: 011036ge TOP: Special Quadrilaterals
- 16 ANS:

 $\overline{BD} \cong \overline{DB}$  (Reflexive Property);  $\triangle ABD \cong \triangle CDB$  (SSS);  $\angle BDC \cong \angle ABD$  (CPCTC).









PTS: 4 REF: 080936ge TOP: Locus

## Geometry 6 Point Regents Exam Questions Answer Section

1 ANS:



 $\overrightarrow{AF} \cong \overrightarrow{CE} \text{ (Substitution); } \overrightarrow{AF} \cong \overrightarrow{FE} \text{ (Reflexive Property); } \overrightarrow{AE} - \overrightarrow{FE} \cong \overrightarrow{FC} - \overrightarrow{EF} \text{ (Line Segment Subtraction Theorem); } \overrightarrow{AF} \cong \overrightarrow{CE} \text{ (Substitution); } \angle BFA \cong \angle DEC \text{ (All right angles are congruent); } \triangle BFA \cong \triangle DEC \text{ (AAS); } \overrightarrow{AB} \cong \overrightarrow{CD} \text{ and } \overrightarrow{BF} \cong \overrightarrow{DE} \text{ (CPCTC); } \angle BFC \cong \angle DEA \text{ (All right angles are congruent); } \triangle BFC \cong \triangle DEA \text{ (SAS); } \overrightarrow{AD} \cong \overrightarrow{CB} \text{ (CPCTC); } ABCD \text{ is a parallelogram (opposite sides of quadrilateral ABCD are congruent)}$ 

PTS: 6 REF: 080938ge TOP: Special Quadrilaterals

2 ANS:

Because  $\overline{AB} \parallel \overline{DC}$ ,  $\overline{AD} \cong \widehat{BC}$  since parallel chords intersect congruent arcs.  $\angle BDC \cong \angle ACD$  because inscribed angles that intercept congruent arcs are congruent.  $\overline{AD} \cong \overline{BC}$  since congruent chords intersect congruent arcs.  $\overline{DC} \cong \overline{CD}$  because of the reflexive property. Therefore,  $\triangle ACD \cong \triangle BDC$  because of SAS.

- PTS: 6 REF: fall0838ge TOP: Circle Proofs
- 3 ANS:





4 ANS:

 $\overline{AC} \cong \overline{EC}$  and  $\overline{DC} \cong \overline{BC}$  because of the definition of midpoint.  $\angle ACB \cong \angle ECD$  because of vertical angles.  $\triangle ABC \cong \triangle EDC$  because of SAS.  $\angle CDE \cong \angle CBA$  because of CPCTC.  $\overline{BD}$  is a transversal intersecting  $\overline{AB}$  and

 $\overline{ED}$ . Therefore  $\overline{AB} \parallel \overline{DE}$  because  $\angle CDE$  and  $\angle CBA$  are congruent alternate interior angles.

PTS: 6 REF: 060938ge TOP: Triangle Proofs

(5y - 2)°

= MLTAS

5 ANS:

A	M-O B
	d=11
d=V92+22 M= I	m - 9 d = 1;3
* 13	
	M-O \
D	dill

 $\overline{AB} \| \overline{CD} \text{ and } \overline{AD} \| \overline{CB}$  because their slopes are equal. *ABCD* is a parallelogram because opposite side are parallel.  $\overline{AB} \neq \overline{BC}$ . *ABCD* is not a rhombus because all sides are not equal.  $\overline{AB} \sim \bot \overline{BC}$  because their slopes are not opposite reciprocals. *ABCD* is not a rectangle because  $\angle ABC$  is not a right angle.

PTS: 4 REF: 081038ge TOP: Quadrilaterals in the Coordinate Plane 6 ANS:  $\frac{3x + 30}{\sqrt{3x + 30}}$ 



PTS: 6 REF: 061038ge TOP: Special Parallelograms