# JEFFERSON MATH PROJECT REGENTS AT RANDOM

The NY Algebra 2/Trigonometry Regents Exams Fall 2009-June 2011

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Dear Sir

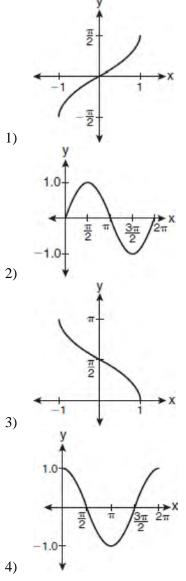
| have to acknolege the reciept of your favor of May 14. in which you mention that you have finished the 6. first books of Euclid, plane trigonometry, surveying  $\xi_{\rightarrow}$  algebra and ask whether | think a further pursuit of that branch of science would be useful to you. there are some propositions in the latter books of Euclid,  $\xi_{\rightarrow}$  some of Archimedes, which are useful,  $\xi_{\rightarrow}$  | have no doubt you have been made acquainted with them. trigonometry, so far as this, is most valuable to every man, there is scarcely a day in which he will not resort to it for some of the purposes of common life. the science of calculation also is indispensible as far as the extraction of the square  $\xi_{\rightarrow}$  cube roots; Algebra as far as the quadratic equation  $\xi_{\rightarrow}$  the use of logarithms are often of value in ordinary cases: but all beyond these is but a luxury; a delicious luxury indeed; but not to be indulged in by one who is to have a profession to follow for his subsistence. in this light | view the conic sections, curves of the higher orders, perhaps even spherical trigonometry, Algebraical operations beyond the 2d dimension, and fluxions.

Letter from Thomas Jefferson to William G. Munford, Monticello, June 18, 1799.

#### Algebra 2/Trigonometry Regents at Random

- 1 Which formula can be used to determine the total number of different eight-letter arrangements that can be formed using the letters in the word *DEADLINE*?
  - 1) 8!
  - 2)  $\frac{8!}{4!}$
  - 3)  $\frac{8!}{2!}$
  - $\frac{5}{2!+2!}$
  - 4)  $\frac{6!}{2! \cdot 2!}$
- 2 Which arithmetic sequence has a common difference of 4?
  - 1)  $\{0, 4n, 8n, 12n, \dots\}$
  - 2)  $\{n, 4n, 16n, 64n, \dots\}$
  - 3)  $\{n+1, n+5, n+9, n+13, \dots\}$
  - 4)  $\{n+4, n+16, n+64, n+256, \dots\}$
- 3 Which task is *not* a component of an observational study?
  - 1) The researcher decides who will make up the sample.
  - 2) The researcher analyzes the data received from the sample.
  - 3) The researcher gathers data from the sample, using surveys or taking measurements.
  - 4) The researcher divides the sample into two groups, with one group acting as a control group.

4 Which graph represents the equation  $y = \cos^{-1} x$ ?

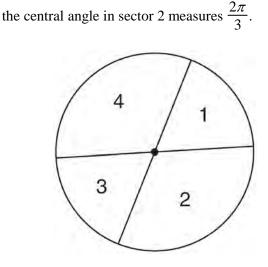


5 The roots of the equation  $2x^2 + 7x - 3 = 0$  are

1) 
$$-\frac{1}{2}$$
 and  $-3$   
2)  $\frac{1}{2}$  and 3  
 $-7 + \sqrt{73}$ 

$$\begin{array}{r} 3) \quad \frac{-7 \pm \sqrt{73}}{4} \\ 4) \quad \frac{7 \pm \sqrt{73}}{4} \end{array}$$

6 A dartboard is shown in the diagram below. The two lines intersect at the center of the circle, and



If darts thrown at this board are equally likely to land anywhere on the board, what is the probability that a dart that hits the board will land in either sector 1 or sector 3?

- $\frac{1}{6}$ 1)
- 2)
- 3)
- $\frac{1}{3}$  $\frac{1}{2}$  $\frac{2}{3}$ 4)

- 7 Express  $\frac{5}{3-\sqrt{2}}$  with a rational denominator, in simplest radical form.
- Which function is *not* one-to-one? 8
  - 1)  $\{(0,1),(1,2),(2,3),(3,4)\}$
  - 2)  $\{(0,0),(1,1),(2,2),(3,3)\}$
  - 3)  $\{(0,1),(1,0),(2,3),(3,2)\}$
  - 4)  $\{(0,1),(1,0),(2,0),(3,2)\}$

9 Express 
$$\left(\frac{2}{3}x-1\right)^2$$
 as a trinomial.

10 What is the radian measure of an angle whose measure is -420°?

1) 
$$-\frac{7\pi}{3}$$
  
2) 
$$-\frac{7\pi}{6}$$
  
3) 
$$\frac{7\pi}{6}$$
  
4) 
$$\frac{7\pi}{3}$$

- 11 The lengths of 100 pipes have a normal distribution with a mean of 102.4 inches and a standard deviation of 0.2 inch. If one of the pipes measures exactly 102.1 inches, its length lies
  - below the 16<sup>th</sup> percentile 1)
  - between the 50<sup>th</sup> and 84<sup>th</sup> percentiles 2)
  - 3) between the 16<sup>th</sup> and 50<sup>th</sup> percentiles
  - 4) above the 84th percentile

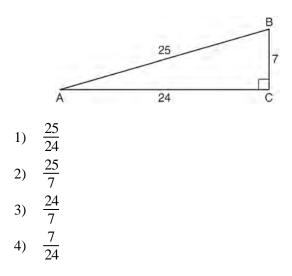
12 Express 
$$\frac{\sqrt{108x^5y^8}}{\sqrt{6xy^5}}$$
 in simplest radical form.

- 13 Find, to the *nearest minute*, the angle whose measure is 3.45 radians.
- 14 Simplify the expression  $\frac{3x^{-4}y^5}{(2x^3y^{-7})^{-2}}$  and write the answer using only positive exponents.
- 15 The expression  $4ab\sqrt{2b} 3a\sqrt{18b^3} + 7ab\sqrt{6b}$ is equivalent to
  - 1)  $2ab\sqrt{6b}$
  - 2)  $16ab\sqrt{2b}$

  - 2)  $16ab \sqrt{2b}$ 3)  $-5ab + 7ab \sqrt{6b}$ 4)  $-5ab \sqrt{2b} + 7ab \sqrt{6b}$
- 16 What is the common difference of the arithmetic sequence 5, 8, 11, 14?
  - $\frac{8}{5}$ 1)
  - 2) -3
  - 3) 3
  - 4) 9

- 17 The minimum point on the graph of the equation y = f(x) is (-1, -3). What is the minimum point on the graph of the equation y = f(x) + 5? 1) (-1,2)
  - (-1, -8)
  - (4, -3)
  - 4) (-6,-3)
- 18 Express  $5\sqrt{3x^3} 2\sqrt{27x^3}$  in simplest radical form.
- 19 An amateur bowler calculated his bowling average for the season. If the data are normally distributed, about how many of his 50 games were within one standard deviation of the mean?
  - 1) 14
  - 17 2)
  - 3) 34
  - 4) 48
- 20 The product of  $(3 + \sqrt{5})$  and  $(3 \sqrt{5})$  is 1)  $4 - 6\sqrt{5}$ 
  - 2)  $14 6\sqrt{5}$
  - 3) 14
  - 4) 4
- 21 Find the total number of different twelve-letter arrangements that can be formed using the letters in the word PENNSYLVANIA.

22 Which ratio represents csc *A* in the diagram below?



26 Mrs. Hill asked her students to express the sum 1+3+5+7+9+...+39 using sigma notation. Four different student answers were given. Which student answer is correct?

1) 
$$\sum_{k=1}^{20} (2k-1)$$
  
2) 
$$\sum_{k=2}^{40} (k-1)$$
  
3) 
$$\sum_{k=-1}^{37} (k+2)$$
  
4) 
$$\sum_{k=1}^{39} (2k-1)$$

- 27 The letters of any word can be rearranged. Carol believes that the number of different 9-letter arrangements of the word "TENNESSEE" is greater than the number of different 7-letter arrangements of the word "VERMONT." Is she correct? Justify your answer.
- 28 The expression  $2i^2 + 3i^3$  is equivalent to
  - 1) -2-3i
  - 2) 2-3i
  - 3) -2+3i
  - 4) 2+3i

29 The value of the expression  $2\sum_{n=1}^{\infty} (n^2 + 2^n)$  is

- 1) 12
- 2) 22
- 3) 24
- 4) 26

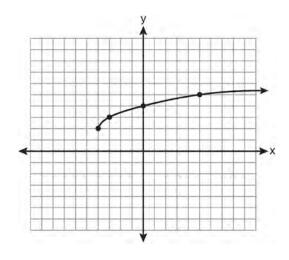
- 23 What is the radian measure of the smaller angle formed by the hands of a clock at 7 o'clock?
  - 1)  $\frac{\pi}{2}$ 2)  $\frac{2\pi}{3}$

$$3) \quad \frac{5\pi}{6}$$

$$4) \quad \frac{7\pi}{6}$$

- 24 If  $\theta$  is an angle in standard position and its terminal side passes through the point (-3,2), find the exact value of csc  $\theta$ .
- 25 Solve the equation  $2\tan C 3 = 3\tan C 4$ algebraically for all values of *C* in the interval  $0^{\circ} \le C < 360^{\circ}$ .

30 What are the domain and the range of the function shown in the graph below?



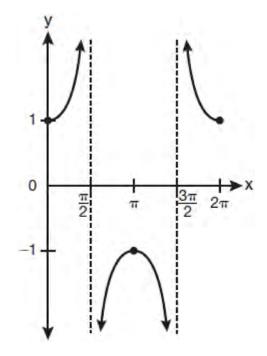
- 1)  $\{x | x > -4\}; \{y | y > 2\}$
- 2)  $\{x | x \ge -4\}; \{y | y \ge 2\}$
- 3)  $\{x | x > 2\}; \{y | y > -4\}$
- 4)  $\{x \mid x \ge 2\}; \{y \mid y \ge -4\}$
- 31 In  $\triangle ABC$ , m $\angle A = 74$ , a = 59.2, and c = 60.3. What are the two possible values for m $\angle C$ , to the *nearest tenth*?
  - 1) 73.7 and 106.3
  - 2) 73.7 and 163.7
  - 3) 78.3 and 101.7
  - 4) 78.3 and 168.3
- 32 If a = 3 and b = -2, what is the value of the expression  $\frac{a^{-2}}{b^{-3}}$ ?

1) 
$$-\frac{9}{8}$$
  
2)  $-1$   
3)  $-\frac{8}{9}$   
4)  $\frac{8}{9}$ 

- 33 In simplest form,  $\sqrt{-300}$  is equivalent to
  - 1)  $3i\sqrt{10}$
  - 2)  $5i\sqrt{12}$
  - 3)  $10i\sqrt{3}$
  - 4)  $12i\sqrt{5}$
- 34 The probability that the Stormville Sluggers will win a baseball game is  $\frac{2}{3}$ . Determine the probability, to the *nearest thousandth*, that the Stormville Sluggers will win *at least* 6 of their next 8 games.
- 35 What is the fifteenth term of the geometric sequence  $-\sqrt{5}, \sqrt{10}, -2\sqrt{5}, \dots$ ?
  - 1)  $-128\sqrt{5}$
  - 2)  $128\sqrt{10}$
  - 3)  $-16384\sqrt{5}$
  - 4)  $16384\sqrt{10}$
- 36 Which values of x are solutions of the equation
  - $x^3 + x^2 2x = 0?$
  - 1) 0,1,2
  - 2) 0, 1, -2
  - 3) 0,-1,24) 0,-1,-2

5

- 37 What is the solution set of the equation
  - |4a+6| 4a = -10?1)  $\emptyset$ 2)  $\{0\}$ 3)  $\left\{\frac{1}{2}\right\}$
  - 4)  $\left\{0,\frac{1}{2}\right\}$
- 38 Which equation is represented by the graph below?



- 1)  $y = \cot x$
- 2)  $y = \csc x$
- 3)  $y = \sec x$
- 4)  $y = \tan x$

39 The table below shows the first-quarter averages for Mr. Harper's statistics class.

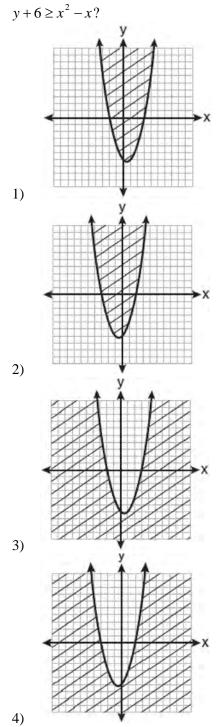
Statistics	Class	Averages
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Quarter Averages	Frequency	
99	1	
97	5	
95	4	
92	4	
90	7	
87	2	
84	6	
81	2	
75	1	
70	2	
65	1	

What is the population variance for this set of data?

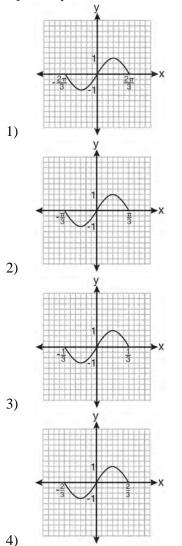
- 1) 8.2
- 8.3
   67.3
- 4) 69.3
- 40 The conjugate of 7-5i is
  - 1) -7-5i
  - 2) -7+5i
  - 3) 7-5i
  - 4) 7 + 5i
- 41 Express the sum  $7 + 14 + 21 + 28 + \ldots + 105$  using sigma notation.

42 Which graph best represents the inequality



- 43 Akeem invests \$25,000 in an account that pays 4.75% annual interest compounded continuously. Using the formula  $A = Pe^{rt}$ , where A = the amount in the account after *t* years, P = principal invested, and *r* = the annual interest rate, how many years, to the *nearest tenth*, will it take for Akeem's investment to triple?
  - 1) 10.0
  - 2) 14.6
  - 3) 23.1
  - 4) 24.0
- 44 If  $\tan A = \frac{2}{3}$  and  $\sin B = \frac{5}{\sqrt{41}}$  and angles A and B are in Quadrant I, find the value of  $\tan(A + B)$ .
- 45 For which equation does the sum of the roots equal  $\frac{3}{4}$  and the product of the roots equal -2?
  - 1)  $4x^2 8x + 3 = 0$
  - 2)  $4x^2 + 8x + 3 = 0$
  - 3)  $4x^2 3x 8 = 0$
  - 4)  $4x^2 + 3x 2 = 0$
- 46 What is a formula for the *n*th term of sequence *B* shown below?
  - $B = 10, 12, 14, 16, \ldots$
  - 1)  $b_n = 8 + 2n$
  - 2)  $b_n = 10 + 2n$
  - 3)  $b_n = 10(2)^n$
  - 4)  $b_n = 10(2)^{n-1}$

47 Which graph represents one complete cycle of the equation  $y = \sin 3\pi x$ ?



48 The members of a men's club have a choice of wearing black or red vests to their club meetings. A study done over a period of many years determined that the percentage of black vests worn is 60%. If there are 10 men at a club meeting on a given night, what is the probability, to the *nearest thousandth*, that *at least* 8 of the vests worn will be black?

49 What is the formula for the *n*th term of the sequence  $54, 18, 6, \ldots$ ?

1) 
$$a_{n} = 6\left(\frac{1}{3}\right)^{n}$$
  
2) 
$$a_{n} = 6\left(\frac{1}{3}\right)^{n-1}$$
  
3) 
$$a_{n} = 54\left(\frac{1}{3}\right)^{n}$$
  
4) 
$$a_{n} = 54\left(\frac{1}{3}\right)^{n-1}$$

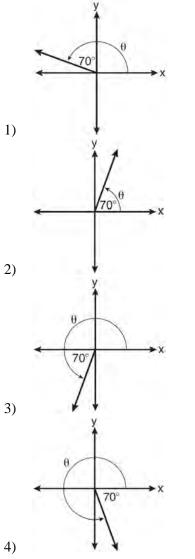
50 The table below shows the results of an experiment involving the growth of bacteria.

Time (x) (in minutes)	1	3	5	7	9	11
Number of Bacteria (y)	2	25	81	175	310	497

Write a power regression equation for this set of data, rounding all values to *three decimal places*. Using this equation, predict the bacteria's growth, to the *nearest integer*, after 15 minutes.

51 A study shows that 35% of the fish caught in a local lake had high levels of mercury. Suppose that 10 fish were caught from this lake. Find, to the *nearest tenth of a percent*, the probability that *at least* 8 of the 10 fish caught did *not* contain high levels of mercury.

52 In which graph is  $\theta$  coterminal with an angle of  $-70^{\circ}$ ?



- 53 What is the principal value of  $\cos^{-1}\left(-\frac{\sqrt{3}}{2}\right)$ ?
  - 1) -30°
  - 2) 60°
  - 3) 150°
  - 4) 240°

- 54 What are the values of  $\theta$  in the interval  $0^{\circ} \le \theta < 360^{\circ}$  that satisfy the equation  $\tan \theta - \sqrt{3} = 0$ ? 1) 60°, 240° 2) 72°, 252°
  - 3) 72°, 108°, 252°, 288°
  - 4) 60°, 120°, 240°, 300°
- 55 Solve the following systems of equations algebraically: 5 = y x

$$4x^2 = -17x + y + 4$$

56 The number of minutes students took to complete a quiz is summarized in the table below.

Minutes	14	15	16	17	18	19	20
Number of Students	5	3	x	5	2	10	1

If the mean number of minutes was 17, which equation could be used to calculate the value of x?

1) 
$$17 = \frac{119 + x}{x}$$

2) 
$$17 = \frac{119 + 16x}{x}$$

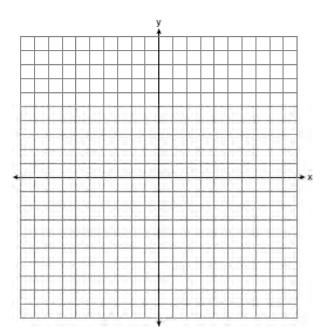
3) 
$$17 = \frac{446 + x}{26 + x}$$

4) 
$$17 = \frac{446 + 16x}{26 + x}$$

- 57 The sides of a parallelogram measure 10 cm and 18 cm. One angle of the parallelogram measures 46 degrees. What is the area of the parallelogram, to the *nearest square centimeter*?
  - 1) 65
  - 2) 125
  - 3) 129
  - 4) 162
- 58 The graph of the equation  $y = \left(\frac{1}{2}\right)^x$  has an

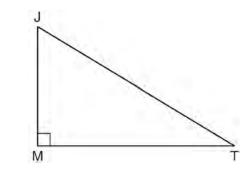
asymptote. On the grid below, sketch the graph of

 $y = \left(\frac{1}{2}\right)^x$  and write the equation of this asymptote.

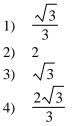


59 Find all values of  $\theta$  in the interval  $0^{\circ} \le \theta < 360^{\circ}$  that satisfy the equation  $\sin 2\theta = \sin \theta$ .

- 60 Use the discriminant to determine all value of k that would result in the equation  $x^2 kx + 4 = 0$  having equal roots.
- 61 In the diagram below of right triangle *JTM*, JT = 12, JM = 6, and  $m \angle JMT = 90$ .



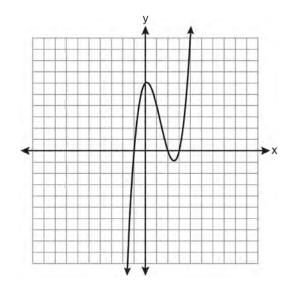
What is the value of  $\cot J$ ?



- 62 A doctor wants to test the effectiveness of a new drug on her patients. She separates her sample of patients into two groups and administers the drug to only one of these groups. She then compares the results. Which type of study *best* describes this situation?
  - 1) census
  - 2) survey
  - 3) observation
  - 4) controlled experiment

- 63 Solve algebraically for *x*:  $16^{2x+3} = 64^{x+2}$
- 64 Factor completely:  $10ax^2 23ax 5a$
- 65 Factored completely, the expression  $12x^4 + 10x^3 12x^2$  is equivalent to
  - 1)  $x^{2}(4x+6)(3x-2)$
  - 2)  $2(2x^2 + 3x)(3x^2 2x)$
  - 3)  $2x^2(2x-3)(3x+2)$
  - 4)  $2x^2(2x+3)(3x-2)$
- 66 Express as a single fraction the exact value of sin 75°.
- 67 The function  $f(x) = \tan x$  is defined in such a way that  $f^{-1}(x)$  is a function. What can be the domain of f(x)?
  - $1) \quad \{x \mid 0 \le x \le \pi\}$
  - 2)  $\{x \mid 0 \le x \le 2\pi\}$ 3)  $\left\{x \mid -\frac{\pi}{2} < x < \frac{\pi}{2}\right\}$ 4)  $\left\{x \mid -\frac{\pi}{2} < x < \frac{3\pi}{2}\right\}$

68 The graph of  $y = x^3 - 4x^2 + x + 6$  is shown below.

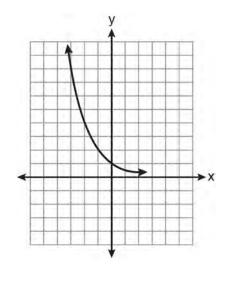


What is the product of the roots of the equation  $x^3 - 4x^2 + x + 6 = 0$ ?

- 1) -36
- 2) -6
- 3) 6
- 4) 4
- 69 Solve algebraically for x:  $\log_{x+3} \frac{x^3 + x 2}{x} = 2$

70 When  $x^{-1} - 1$  is divided by x - 1, the quotient is 1) -12)  $-\frac{1}{x}$ 3)  $\frac{1}{x^2}$ 4)  $\frac{1}{(x-1)^2}$ 

- 71 The solution set of the inequality  $x^2 3x > 10$  is
  - 1)  $\{x \mid -2 < x < 5\}$
  - 2)  $\{x \mid 0 < x < 3\}$
  - 3)  $\{x \mid x < -2 \text{ or } x > 5\}$
  - 4)  $\{x \mid x < -5 \text{ or } x > 2\}$
- 72 Which equation is represented by the graph below?



- 1)  $y = 5^x$
- $2) \quad y = 0.5^x$
- 3)  $y = 5^{-x}$
- 4)  $y = 0.5^{-x}$
- 73 The equation  $x^2 + y^2 2x + 6y + 3 = 0$  is equivalent to
  - 1)  $(x-1)^2 + (y+3)^2 = -3$
  - 2)  $(x-1)^2 + (y+3)^2 = 7$
  - 3)  $(x+1)^2 + (y+3)^2 = 7$
  - 4)  $(x+1)^2 + (y+3)^2 = 10$

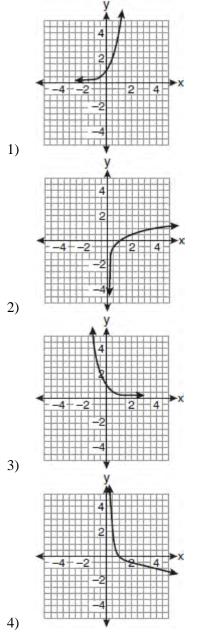
74 Three marbles are to be drawn at random, without replacement, from a bag containing 15 red marbles, 10 blue marbles, and 5 white marbles. Which expression can be used to calculate the probability of drawing 2 red marbles and 1 white marble from the bag?

1) 
$$\frac{{}_{15}C_2 \cdot {}_5C_1}{{}_{30}C_3}$$
  
2) 
$$\frac{{}_{15}P_2 \cdot {}_5P_1}{{}_{30}C_3}$$
  
3) 
$$\frac{{}_{15}C_2 \cdot {}_5C_1}{{}_{30}P_3}$$
  
4) 
$$\frac{{}_{15}P_2 \cdot {}_5P_1}{{}_{30}P_3}$$

75 The expression 
$$(x^2 - 1)^{-\frac{2}{3}}$$
 is equivalent to  
1)  $\sqrt[3]{(x^2 - 1)^2}$   
2)  $\frac{1}{\sqrt[3]{(x^2 - 1)^2}}$   
3)  $\sqrt{(x^2 - 1)^3}$   
4)  $\frac{1}{\sqrt{(x^2 - 1)^3}}$ 

76 Starting with  $\sin^2 A + \cos^2 A = 1$ , derive the formula  $\tan^2 A + 1 = \sec^2 A$ .

77 If a function is defined by the equation  $f(x) = 4^x$ , which graph represents the inverse of this function?



78 If  $r = \sqrt[3]{\frac{A^2B}{C}}$ , then  $\log r$  can be represented by 1)  $\frac{1}{6}\log A + \frac{1}{3}\log B - \log C$ 2)  $3(\log A^2 + \log B - \log C)$ 3)  $\frac{1}{3}\log(A^2 + B) - C$ 4)  $\frac{2}{3}\log A + \frac{1}{3}\log B - \frac{1}{3}\log C$ 

79 If 
$$\sin^{-1}\left(\frac{5}{8}\right) = A$$
, then  
1)  $\sin A = \frac{5}{8}$   
2)  $\sin A = \frac{8}{5}$   
3)  $\cos A = \frac{5}{8}$   
4)  $\cos A = \frac{8}{5}$ 

- 80 If  $f(x) = x^2 6$  and  $g(x) = 2^x 1$ , determine the value of  $(g \circ f)(-3)$ .
- 81 Find, to the *nearest tenth of a degree*, the angle whose measure is 2.5 radians.
- 82 What is the coefficient of the fourth term in the expansion of  $(a-4b)^9$ ?
  - 1) -5,376
  - 2) -336
  - 3) 336
  - 4) 5,376

83 The expression 
$$\log_5\left(\frac{1}{25}\right)$$
 is equivalent to  
1)  $\frac{1}{2}$   
2) 2  
3)  $-\frac{1}{2}$   
4) -2

84 The expression  $\log_8 64$  is equivalent to

- 1) 8 2 2)
- $\frac{1}{2}$ 3)
- $\frac{1}{8}$
- 4)

4)

85 Graph the inequality -3|6-x| < -15 for x. Graph the solution on the line below.

86 Which graph represents the solution set of  $|6x - 7| \le 5?$ 1) 2) 3)

- 87 Twenty different cameras will be assigned to several boxes. Three cameras will be randomly selected and assigned to box A. Which expression can be used to calculate the number of ways that three cameras can be assigned to box A? 1) 20!
  - 20! 2)
  - 3!
  - 3)  $_{20}C_{3}$
  - 4)  $_{20}P_{3}$

88 How many distinct triangles can be formed if  $m \angle A = 35$ , a = 10, and b = 13?

- 1) 1
- 2 2)
- 3) 3
- 4) 0

89 If  $\sin A = \frac{2}{3}$  where  $0^{\circ} < A < 90^{\circ}$ , what is the value of sin 2A?

1) 
$$\frac{2\sqrt{5}}{3}$$
2) 
$$\frac{2\sqrt{5}}{9}$$
3) 
$$\frac{4\sqrt{5}}{9}$$
4) 
$$-\frac{4\sqrt{5}}{9}$$

90 What is the fourth term in the expansion of

$$(3x-2)^{5}$$
?

- 1)  $-720x^2$
- 2) –240*x*
- 3)  $720x^2$
- 4)  $1,080x^3$
- 91 The scores of one class on the Unit 2 mathematics test are shown in the table below.

Test Score	Frequency		
96	1		
92	2		
84	5		
80	3		
76	6		
72	3		
68	2		

Unit 2 Mathematics Test

Find the population standard deviation of these scores, to the *nearest tenth*.

- 92 Two forces of 25 newtons and 85 newtons acting on a body form an angle of 55°. Find the magnitude of the resultant force, to the *nearest hundredth of a newton*. Find the measure, to the *nearest degree*, of the angle formed between the resultant and the larger force.
- 93 In  $\triangle ABC$ , m $\angle A = 32$ , a = 12, and b = 10. Find the measures of the missing angles and side of  $\triangle ABC$ . Round each measure to the *nearest tenth*.

94 What is the period of the function  $y = \frac{1}{2} \sin\left(\frac{x}{3} - \pi\right)?$ 

1) 
$$\frac{1}{2}$$
  
2)  $\frac{1}{3}$   
3)  $\frac{2}{3}\pi$   
4)  $6\pi$ 

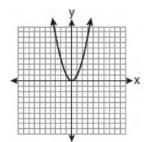
95 If 
$$f(x) = \frac{x}{x^2 - 16}$$
, what is the value of f(-10)?  
1)  $-\frac{5}{2}$   
2)  $-\frac{5}{42}$   
3)  $\frac{5}{58}$   
4)  $\frac{5}{18}$ 

- 96 A circle has a radius of 4 inches. In inches, what is the length of the arc intercepted by a central angle of 2 radians?
  - 1) 2*π*
  - 2) 2
  - 3) 8*π*
  - 4) 8

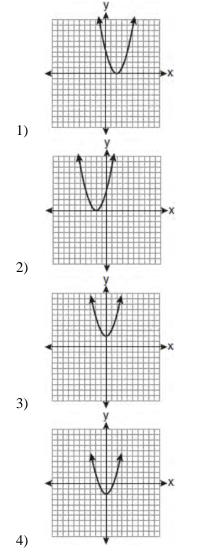
97 What is the solution of the equation  $2\log_4(5x) = 3$ ?

- 1) 6.4
- 2) 2.56
- 3)  $\frac{9}{5}$
- 4)  $\frac{8}{5}$

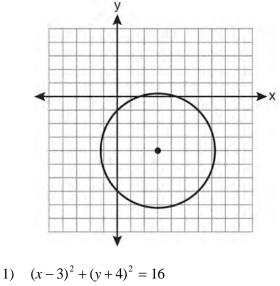
98 The graph below shows the function f(x).



Which graph represents the function f(x + 2)?



99 Which equation represents the circle shown in the graph below that passes through the point (0,-1)?



- 2)  $(x-3)^2 + (y+4)^2 = 18$
- 3)  $(x+3)^2 + (y-4)^2 = 16$
- 4)  $(x+3)^2 + (y-4)^2 = 18$
- 100 What is the value of x in the equation  $\log_5 x = 4$ ?
  - 1) 1.16
  - 2) 20
  - 3) 625
  - 4) 1,024
- 101 A four-digit serial number is to be created from the digits 0 through 9. How many of these serial numbers can be created if 0 can not be the first digit, no digit may be repeated, and the last digit must be 5?
  - 448 1)
  - 2) 504
  - 3) 2,240
  - 4) 2,520

102 What is the common ratio of the geometric sequence whose first term is 27 and fourth term is 64?

1) 
$$\frac{3}{4}$$

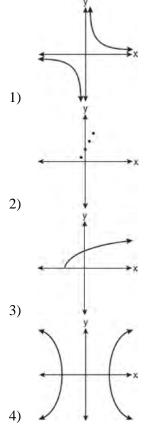
2) 
$$\frac{64}{81}$$

3) 
$$\frac{4}{3}$$
  
1)  $\frac{37}{3}$ 

4) 
$$\frac{37}{3}$$

- 103 The expression  $\frac{4}{5 \sqrt{13}}$  is equivalent to 1)  $\frac{4\sqrt{13}}{5\sqrt{13} - 13}$ 2)  $\frac{4(5 - \sqrt{13})}{38}$ 3)  $\frac{5 + \sqrt{13}}{3}$ 4)  $\frac{4(5 + \sqrt{13})}{38}$
- 104 Ms. Bell's mathematics class consists of 4 sophomores, 10 juniors, and 5 seniors. How many different ways can Ms. Bell create a four-member committee of juniors if each junior has an equal chance of being selected?
  - 1) 210
  - 2) 3,876
  - 3) 5,040
  - 4) 93,024

105 Which graph does *not* represent a function?



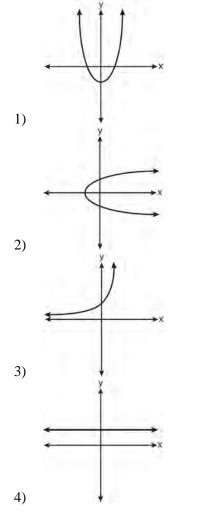
106 The product of  $i^7$  and  $i^5$  is equivalent to

- 1) 1
- 2) -13) *i*
- 4) -i

107 What is the number of degrees in an angle whose radian measure is  $\frac{11\pi}{12}$ ?

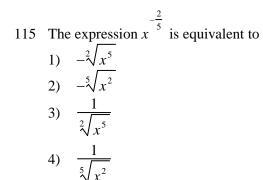
- 2) 165
- 3) 330
- 4) 518

- 108 What is the fifteenth term of the sequence
  - $5,-10,20,-40,80,\ldots?$
  - 1) -163,840
  - 2) -81,920 3) 81,920
  - $3) \quad 81,920$
  - 4) 327,680
- 109 Which graph represents a one-to-one function?

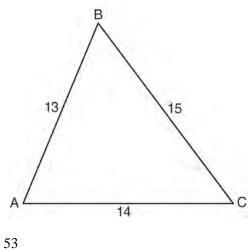


- 110 If  $f(x) = x^2 5$  and g(x) = 6x, then g(f(x)) is equal to 1)  $6x^3 - 30x$ 2)  $6x^2 - 30$ 
  - 3)  $36x^2 5$
  - 4)  $x^2 + 6x 5$
- 111 Solve algebraically for *x*:  $\frac{1}{x+3} \frac{2}{3-x} = \frac{4}{x^2 9}$
- 112 When  $\frac{3}{2}x^2 \frac{1}{4}x 4$  is subtracted from  $\frac{5}{2}x^2 - \frac{3}{4}x + 1$ , the difference is 1)  $-x^2 + \frac{1}{2}x - 5$ 2)  $x^2 - \frac{1}{2}x + 5$ 3)  $-x^2 - x - 3$ 4)  $x^2 - x - 3$
- 113 An auditorium has 21 rows of seats. The first row has 18 seats, and each succeeding row has two more seats than the previous row. How many seats are in the auditorium?
  - 1) 540
  - 2) 567
  - 3) 760
  - 4) 798

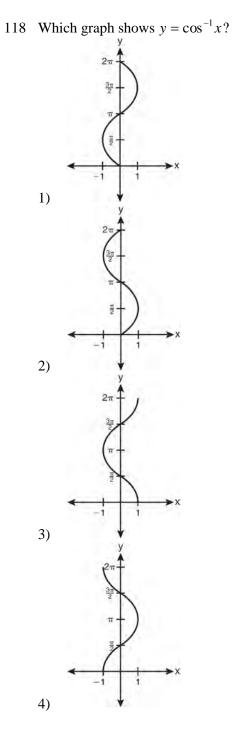
114 Solve for x: 
$$\frac{4x}{x-3} = 2 + \frac{12}{x-3}$$



- 116 Write the binomial expansion of  $(2x-1)^5$  as a polynomial in simplest form.
- 117 In  $\triangle ABC$ , a = 15, b = 14, and c = 13, as shown in the diagram below. What is the m $\angle C$ , to the *nearest degree*?



- 1) 53 2) 59
- 3) 67
- 4) 127



119 The table below shows the number of new stores in a coffee shop chain that opened during the years 1986 through 1994.

Year	Number of New Stores			
1986	14			
1987	27			
1988	48			
1989	80			
1990	110			
1991	153			
1992	261			
1993	403			
1994	681			

Using x = 1 to represent the year 1986 and y to represent the number of new stores, write the exponential regression equation for these data. Round all values to the *nearest thousandth*.

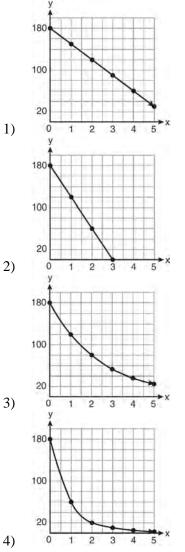
120 Written in simplest form, the expression  $\frac{\frac{x}{4} - \frac{1}{x}}{\frac{1}{2x} + \frac{1}{4}}$  is

equivalent to

- 1) x 1
- 2) x-23) x-2
- 3)  $\frac{x-2}{2}$

4) 
$$\frac{x^2 - 4}{x + 2}$$

- 121 Express the product of  $\left(\frac{1}{2}y^2 \frac{1}{3}y\right)$  and  $\left(12y + \frac{3}{5}\right)$  as a trinomial.
- 122 On January 1, a share of a certain stock cost \$180. Each month thereafter, the cost of a share of this stock decreased by one-third. If x represents the time, in months, and y represents the cost of the stock, in dollars, which graph best represents the cost of a share over the following 5 months?

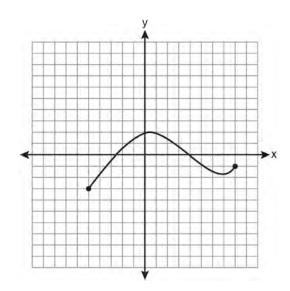


- 123 The expression  $(3-7i)^2$  is equivalent to
  - 1) -40 + 0i
  - 2) -40 42i
  - 3) 58 + 0i
  - 4) 58 42i
- 124 For which equation does the sum of the roots equal -3 and the product of the roots equal 2?
  - 1)  $x^2 + 2x 3 = 0$
  - 2)  $x^2 3x + 2 = 0$
  - 3)  $2x^2 + 6x + 4 = 0$
  - 4)  $2x^2 6x + 4 = 0$
- 125 The expression  $\cos^2 \theta \cos 2\theta$  is equivalent to
  - 1)  $\sin^2 \theta$

1) 1 2) 2 3) 5 4) -10

- 2)  $-\sin^2\theta$
- 3)  $\cos^2\theta + 1$
- 4)  $-\cos^2\theta 1$

- 128 For a given set of rectangles, the length is inversely proportional to the width. In one of these rectangles, the length is 12 and the width is 6. For this set of rectangles, calculate the width of a rectangle whose length is 9.
- 129 The solution set of  $\sqrt{3x+16} = x+2$  is
  - 1) {-3,4}
  - 2)  $\{-4,3\}$
  - 3) {3}
  - 4) {-4}
- 130 What is the conjugate of -2 + 3i?
  - 1) -3+2i
  - 2) -2-3i
  - 3) 2-3i
  - 4) 3+2i
- 131 The graph below represents the function y = f(x).

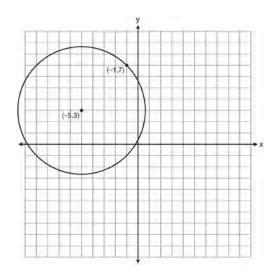


State the domain and range of this function.

126 The value of x in the equation  $4^{2x+5} = 8^{3x}$  is

- 127 The solution set of  $4^{x^2 + 4x} = 2^{-6}$  is
  - 1) {1,3}
  - 2) {-1,3}
  - 3) {-1,-3}
  - 4) {1,-3}

- 132 If  $f(x) = \frac{1}{2}x 3$  and g(x) = 2x + 5, what is the value of  $(g \circ f)(4)$ ? 1) -13
  - 2) 3.5
     3) 3
  - 3) 3 4) 6
- 133 Two sides of a parallelogram are 24 feet and 30 feet. The measure of the angle between these sides is 57°. Find the area of the parallelogram, to the *nearest square foot*.
- 134 Factor the expression  $12t^8 75t^4$  completely.
- 135 A circle shown in the diagram below has a center of (-5,3) and passes through point (-1,7).



Write an equation that represents the circle.

- 136 Write a quadratic equation such that the sum of its roots is 6 and the product of its roots is -27.
- 137 Howard collected fish eggs from a pond behind his house so he could determine whether sunlight had an effect on how many of the eggs hatched. After he collected the eggs, he divided them into two tanks. He put both tanks outside near the pond, and he covered one of the tanks with a box to block out all sunlight. State whether Howard's investigation was an example of a controlled experiment, an observation, or a survey. Justify your response.
- 138 A survey completed at a large university asked 2,000 students to estimate the average number of hours they spend studying each week. Every tenth student entering the library was surveyed. The data showed that the mean number of hours that students spend studying was 15.7 per week. Which characteristic of the survey could create a bias in the results?
  - 1) the size of the sample
  - 2) the size of the population
  - 3) the method of analyzing the data
  - 4) the method of choosing the students who were surveyed

139 Evaluate: 
$$10 + \sum_{n=1}^{5} (n^3 - 1)$$

140 Which values of x are in the solution set of the following system of equations? y = 3x - 6

$$y = x^2 - x - 6$$

- 1) 0, -4
- 2) 0,4
- 3) 6, -2
- 4) -6, 2
- 141 Which two functions are inverse functions of each other?
  - 1)  $f(x) = \sin x$  and  $g(x) = \cos(x)$
  - 2) f(x) = 3 + 8x and g(x) = 3 8x
  - 3)  $f(x) = e^x$  and  $g(x) = \ln x$
  - 4) f(x) = 2x 4 and  $g(x) = -\frac{1}{2}x + 4$

142 The expression 
$$\frac{2x+4}{\sqrt{x+2}}$$
 is equivalent to  
1)  $\frac{(2x+4)\sqrt{x-2}}{x-2}$   
2)  $\frac{(2x+4)\sqrt{x-2}}{x-4}$   
3)  $2\sqrt{x-2}$   
4)  $2\sqrt{x+2}$ 

- 143 Which value of *r* represents data with a strong negative linear correlation between two variables?
  - 1) -1.07
  - 2) -0.89
  - 3) -0.14
  - 4) 0.92

144 In  $\triangle ABC$ , a = 3, b = 5, and c = 7. What is m $\angle C$ ? 1) 22 2) 38 3) 60

4) 120

145 Which expression is equivalent to  $\frac{\sqrt{3}+5}{\sqrt{3}-5}$ ?

1) 
$$-\frac{14+5\sqrt{3}}{11}$$
  
2)  $-\frac{17+5\sqrt{3}}{11}$   
3)  $\frac{14+5\sqrt{3}}{14}$   
4)  $\frac{17+5\sqrt{3}}{14}$ 

146 If  $x^2 + 2 = 6x$  is solved by completing the square, an intermediate step would be

- 1)  $(x+3)^2 = 7$
- 2)  $(x-3)^2 = 7$
- 3)  $(x-3)^2 = 11$
- 4)  $(x-6)^2 = 34$
- 147 The roots of the equation  $x^2 10x + 25 = 0$  are
  - 1) imaginary
  - 2) real and irrational
  - 3) real, rational, and equal
  - 4) real, rational, and unequal

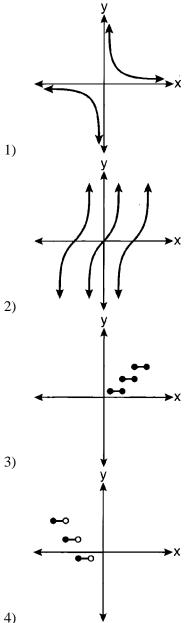
- 148 Expressed as a function of a positive acute angle,  $\cos(-305^\circ)$  is equal to
  - 1)  $-\cos 55^{\circ}$
  - 2)  $\cos 55^\circ$
  - $3) -\sin 55^{\circ}$
  - 4)  $\sin 55^\circ$
- 149 Which relation is *not* a function?

1) 
$$(x-2)^2 + y^2 = 4$$

- 2)  $x^2 + 4x + y = 4$
- 3) x + y = 4
- 4) xy = 4
- 150 A committee of 5 members is to be randomly selected from a group of 9 teachers and 20 students. Determine how many different committees can be formed if 2 members must be teachers and 3 members must be students.
- 151 The temperature, *T*, of a given cup of hot chocolate after it has been cooling for *t* minutes can best be modeled by the function below, where  $T_0$  is the temperature of the room and *k* is a constant.  $\ln(T - T_0) = -kt + 4.718$

A cup of hot chocolate is placed in a room that has a temperature of  $68^{\circ}$ . After 3 minutes, the temperature of the hot chocolate is  $150^{\circ}$ . Compute the value of *k* to the nearest thousandth. [Only an algebraic solution can receive full credit.] Using this value of *k*, find the temperature, *T*, of this cup of hot chocolate if it has been sitting in this room for a total of 10 minutes. Express your answer to the *nearest degree*. [Only an algebraic solution can receive full credit.]

- 152 In a triangle, two sides that measure 6 cm and 10 cm form an angle that measures 80°. Find, to the *nearest degree*, the measure of the smallest angle in the triangle.
- 153 Which graph represents a relation that is *not* a function?



- 154 Assume that the ages of first-year college students are normally distributed with a mean of 19 years and standard deviation of 1 year. To the *nearest integer*, find the percentage of first-year college students who are between the ages of 18 years and 20 years, inclusive. To the *nearest integer*, find the percentage of first-year college students who are 20 years old or older.
- 155 The expression  $2\log x (3\log y + \log z)$  is equivalent to

1) 
$$\log \frac{x^2}{y^3 z}$$
  
2)  $\log \frac{x^2 z}{y^3}$   
3)  $\log \frac{2x}{3yz}$ 

- 4)  $\log \frac{2xz}{3y}$
- 156 The solution set of the equation  $\sqrt{x+3} = 3-x$  is
  - 1) {1}
  - 2) {0}
  - 3) {1,6}
  - 4) {2,3}
- 157 Factored completely, the expression  $6x x^3 x^2$  is equivalent to
  - 1) x(x+3)(x-2)
  - 2) x(x-3)(x+2)
  - 3) -x(x-3)(x+2)
  - 4) -x(x+3)(x-2)

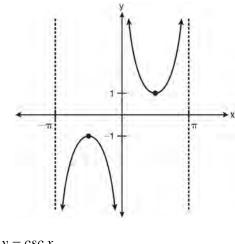
158 The fraction 
$$\frac{3}{\sqrt{3a^2b}}$$
 is equivalent to  
1)  $\frac{1}{a\sqrt{b}}$   
2)  $\frac{\sqrt{b}}{ab}$   
3)  $\frac{\sqrt{3b}}{ab}$   
4)  $\frac{\sqrt{3}}{a}$ 

- 159 If  $f(x) = x^2 6$ , find  $f^{-1}(x)$ .
- 160 Brian correctly used a method of completing the square to solve the equation  $x^2 + 7x 11 = 0$ . Brian's first step was to rewrite the equation as  $x^2 + 7x = 11$ . He then added a number to both sides of the equation. Which number did he add? 1)  $\frac{7}{2}$ 
  - 1)  $\frac{7}{2}$ 2)  $\frac{49}{4}$
  - 3)  $\frac{49}{2}$
  - 4) 49
- 161 Express in simplest form:  $\frac{\frac{1}{2} \frac{4}{d}}{\frac{1}{d} + \frac{3}{2d}}$

- 162 The equation  $y 2\sin\theta = 3$  may be rewritten as
  - 1)  $f(y) = 2\sin x + 3$
  - 2)  $f(y) = 2\sin\theta + 3$
  - 3)  $f(x) = 2\sin\theta + 3$
  - 4)  $f(\theta) = 2\sin\theta + 3$
- 163 The expression  $\sqrt[4]{16x^2y^7}$  is equivalent to
  - 1)  $2x^{\frac{1}{2}}y^{\frac{7}{4}}$
  - 2)  $2x^8y^{28}$

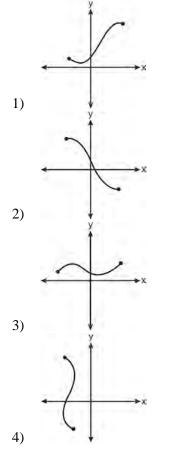
  - 3)  $4x^{\frac{1}{2}}y^{\frac{7}{4}}$
  - $4x^8y^{28}$ 4)
- 164 Find the sum and product of the roots of the equation  $5x^2 + 11x - 3 = 0$ .
- 165 The expression  $\frac{\sin^2 \theta + \cos^2 \theta}{1 \sin^2 \theta}$  is equivalent to
  - 1)  $\cos^2\theta$
  - 2)  $\sin^2 \theta$
  - 3)  $\sec^2 \theta$
  - 4)  $\csc^2 \theta$

166 Which equation is sketched in the diagram below?



- 1)  $y = \csc x$ 2)  $y = \sec x$ 3)  $y = \cot x$ 4)  $y = \tan x$
- 167 The expression  $\frac{a^2b^{-3}}{a^{-4}b^2}$  is equivalent to 1)  $\frac{a^6}{b^5}$ 2)  $\frac{b^5}{a^6}$ 3)  $\frac{a^2}{b}$ 4)  $a^{-2}b^{-1}$

168 Which graph does *not* represent a function?



- 170 The value of  $\tan 126^{\circ}43'$  to the *nearest ten-thousandth* is
  - 1) -1.3407
  - 2) -1.3408
  - 3) -1.3548
  - 4) -1.3549
- 171 In a study of 82 video game players, the researchers found that the ages of these players were normally distributed, with a mean age of 17 years and a standard deviation of 3 years. Determine if there were 15 video game players in this study over the age of 20. Justify your answer.
- 172 The roots of the equation  $9x^2 + 3x 4 = 0$  are
  - imaginary 1)
  - 2) real, rational, and equal
  - 3) real, rational, and unequal
  - 4) real, irrational, and unequal
- 173 Four points on the graph of the function f(x) are shown below.

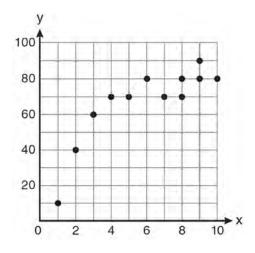
 $\{(0,1),(1,2),(2,4),(3,8)\}$ 

Which equation represents f(x)?

- $f(x) = 2^x$ 1)
- 2) f(x) = 2x
- 3) f(x) = x + 1
- 4)  $f(x) = \log_2 x$
- 169 What is the period of the function  $f(\theta) = -2\cos 3\theta$ ?
  - 1) π
  - $\frac{2\pi}{3}$ 2)

  - $\frac{3\pi}{2}$ 3)
  - 4)  $2\pi$

174 Samantha constructs the scatter plot below from a set of data.



Based on her scatter plot, which regression model would be most appropriate?

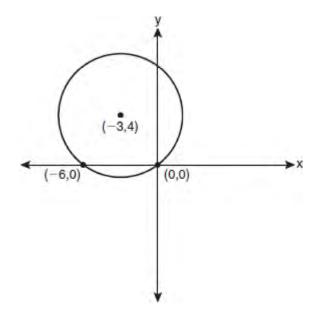
- 1) exponential
- 2) linear
- 3) logarithmic
- 4) power
- 175 Solve the equation  $8x^3 + 4x^2 18x 9 = 0$ algebraically for all values of *x*.
- 176 What is the range of  $f(x) = (x+4)^2 + 7?$ 
  - 1)  $y \ge -4$
  - 2)  $y \ge 4$
  - 3) y = 7
  - 4)  $y \ge 7$

177 Find the first four terms of the recursive sequence defined below.

$$a_1 = -3$$
$$a_n = a_{(n-1)} - n$$

- 178 What is the domain of the function  $f(x) = \sqrt{x-2} + 3?$ 
  - $1(x) = \sqrt{x 2}$  $1) \quad (-\infty, \infty)$
  - 2) (2,∞)
  - 3) [2,∞)
  - 4) [3,∞)
- 179 The value of the expression  $\sum_{r=3}^{5} (-r^2 + r)$  is
  - 1) -38
  - 2) -12
  - 3) 26
  - 4) 62
- 180 The expression  $\cos 4x \cos 3x + \sin 4x \sin 3x$  is equivalent to
  - 1)  $\sin x$
  - 2)  $\sin 7x$
  - 3)  $\cos x$
  - 4)  $\cos 7x$
- 181 Solve  $2x^2 12x + 4 = 0$  by completing the square, expressing the result in simplest radical form.

182 Write an equation of the circle shown in the graph below.



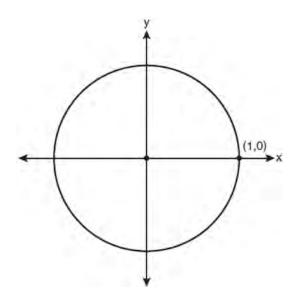
183 When simplified, the expression  $\left(\frac{w^{-5}}{w^{-9}}\right)^{\frac{1}{2}}$  is

equivalent to

- $w^{-7}$ 1)
- $w^2$ 2)
- 3)  $w^7$
- $w^{14}$ 4)
- 184 The principal would like to assemble a committee of 8 students from the 15-member student council. How many different committees can be chosen?
  - 1) 120 2) 6,435
  - 3) 32,432,400

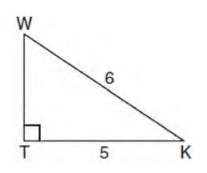
  - 259,459,200 4)

- 185 Evaluate  $e^{x \ln y}$  when x = 3 and y = 2.
- 186 On the unit circle shown in the diagram below, sketch an angle, in standard position, whose degree measure is 240 and find the exact value of sin 240°.



187 If  $\angle A$  is acute and  $\tan A = \frac{2}{3}$ , then 1)  $\cot A = \frac{2}{3}$ 2)  $\cot A = \frac{1}{3}$ 3)  $\cot(90^\circ - A) = \frac{2}{3}$ 4)  $\cot(90^\circ - A) = \frac{1}{3}$ 

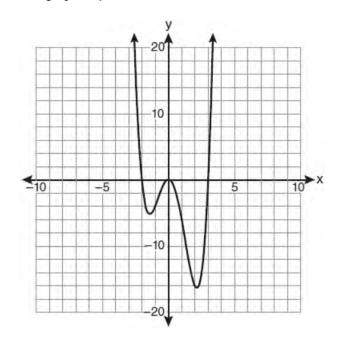
- 188 The probability that a professional baseball player will get a hit is  $\frac{1}{3}$ . Calculate the exact probability that he will get at least 3 hits in 5 attempts.
- 189 In the diagram below of right triangle *KTW*, KW = 6, KT = 5, and  $m \angle KTW = 90$ .



What is the measure of  $\angle K$ , to the *nearest minute*?

- 33°33' 1)
- 2) 33°34'
- 3) 33°55'
- 4) 33°56'
- 190 In  $\triangle ABC$ , m $\angle A = 120$ , b = 10, and c = 18. What is the area of  $\triangle ABC$  to the *nearest square inch*?
  - 52 1)
  - 78 2)
  - 90 3)
  - 4) 156

191 The graph of y = f(x) is shown below.



Which set lists all the real solutions of f(x) = 0?

- $\{-3,2\}$ 1)
- 2)  $\{-2,3\}$
- $\{-3,0,2\}$ 3)
- 4)  $\{-2,0,3\}$
- 192 What is the value of x in the equation  $9^{3x+1} = 27^{x+2}$ ? 1) 1
  - 2)
  - $\frac{1}{2}$  $\frac{4}{3}$

 $\frac{1}{3}$ 

- 3)
- 4)

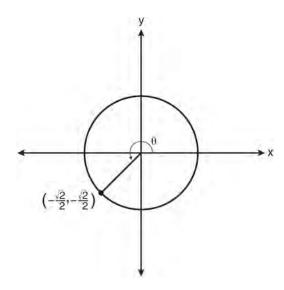
- 193 Matt places \$1,200 in an investment account earning an annual rate of 6.5%, compounded continuously. Using the formula  $V = Pe^{rt}$ , where V is the value of the account in t years, P is the principal initially invested, e is the base of a natural logarithm, and r is the rate of interest, determine the amount of money, to the *nearest cent*, that Matt will have in the account after 10 years.
- 195 The solutions of the equation  $y^2 3y = 9$  are

1) 
$$\frac{3\pm 3i\sqrt{3}}{2}$$
  
2) 
$$\frac{3\pm 3i\sqrt{5}}{2}$$
  
3) 
$$\frac{-3\pm 3\sqrt{5}}{2}$$
  
4) 
$$\frac{3\pm 3\sqrt{5}}{2}$$

194 In the diagram below of a unit circle, the ordered  $\left( \sqrt{2} - \sqrt{2} \right)$ 

pair  $\left(-\frac{\sqrt{2}}{2}, -\frac{\sqrt{2}}{2}\right)$  represents the point where the

terminal side of  $\theta$  intersects the unit circle.



What is  $m \angle \theta$ ?

- 1) 45
- 2) 135
- 3) 225
- 4) 240