

# JMAP REGENTS BY TYPE

The NY Algebra II Regents Exams Questions  
from Spring 2015 to January 2020 Sorted by Type

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**Algebra II Multiple Choice Regents Exam Questions**

- 1 The weights of bags of Graseck's Chocolate Candies are normally distributed with a mean of 4.3 ounces and a standard deviation of 0.05 ounces. What is the probability that a bag of these chocolate candies weighs less than 4.27 ounces?
- 1) 0.2257
  - 2) 0.2743
  - 3) 0.7257
  - 4) 0.7757

- 2 Which statement regarding polynomials and their zeros is true?
- 1)  $f(x) = (x^2 - 1)(x + a)$  has zeros of 1 and  $-a$ , only.
  - 2)  $f(x) = x^3 - ax^2 + 16x - 16a$  has zeros of 4 and  $a$ , only.
  - 3)  $f(x) = (x^2 + 25)(x + a)$  has zeros of  $\pm 5$  and  $-a$ .
  - 4)  $f(x) = x^3 - ax^2 - 9x + 9a$  has zeros of  $\pm 3$  and  $a$ .

- 3 The expression  $2 - \frac{x-1}{x+2}$  is equivalent to

- 1)  $1 - \frac{3}{x+2}$
- 2)  $1 + \frac{3}{x+2}$
- 3)  $1 - \frac{1}{x+2}$
- 4)  $1 + \frac{1}{x+2}$

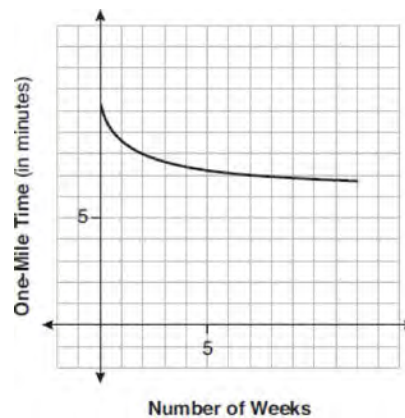
- 4 What is the solution when the equation  $wx^2 + w = 0$  is solved for  $x$ , where  $w$  is a positive integer?

- 1)  $-1$
- 2)  $0$
- 3)  $6$
- 4)  $\pm i$

- 5 There are 440 students at Thomas Paine High School enrolled in U.S. History. On the April report card, the students' grades are approximately normally distributed with a mean of 79 and a standard deviation of 7. Students who earn a grade less than or equal to 64.9 must attend summer school. The number of students who must attend summer school for U.S. History is closest to

- 1) 3
- 2) 5
- 3) 10
- 4) 22

- 6 Irma initially ran one mile in over ten minutes. She then began a training program to reduce her one-mile time. She recorded her one-mile time once a week for twelve consecutive weeks, as modeled in the graph below.



Which statement regarding Irma's one-mile training program is correct?

- 1) Her one-mile speed increased as the number of weeks increased.
- 2) Her one-mile speed decreased as the number of weeks increased.
- 3) If the trend continues, she will run under a six-minute mile by week thirteen.
- 4) She reduced her one-mile time the most between weeks ten and twelve.

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- 7 Stephanie found that the number of white-winged cross bills in an area can be represented by the formula  $C = 550(1.08)^t$ , where  $t$  represents the number of years since 2010. Which equation correctly represents the number of white-winged cross bills in terms of the monthly rate of population growth?
- 1)  $C = 550(1.00643)^t$
  - 2)  $C = 550(1.00643)^{12t}$
  - 3)  $C = 550(1.00643)^{\frac{t}{12}}$
  - 4)  $C = 550(1.00643)^{t+12}$
- 8 The mean intelligence quotient (IQ) score is 100, with a standard deviation of 15, and the scores are normally distributed. Given this information, the approximate percentage of the population with an IQ greater than 130 is closest to
- 1) 2%
  - 2) 31%
  - 3) 48%
  - 4) 95%
- 9 Camryn puts \$400 into a savings account that earns 6% annually. The amount in her account can be modeled by  $C(t) = 400(1.06)^t$  where  $t$  is the time in years. Which expression best approximates the amount of money in her account using a weekly growth rate?
- 1)  $400(1.001153846)^t$
  - 2)  $400(1.001121184)^t$
  - 3)  $400(1.001153846)^{52t}$
  - 4)  $400(1.001121184)^{52t}$
- 10 What is the solution set of  $x = \sqrt{3x + 40}$ ?
- 1)  $\{-5, 8\}$
  - 2)  $\{8\}$
  - 3)  $\{-4, 10\}$
  - 4)  $\{ \}$
- 11 Evan graphed a cubic function,  $f(x) = ax^3 + bx^2 + cx + d$ , and determined the roots of  $f(x)$  to be  $\pm 1$  and 2. What is the value of  $b$ , if  $a = 1$ ?
- 1) 1
  - 2) 2
  - 3) -1
  - 4) -2
- 12 A veterinary pharmaceutical company plans to test a new drug to treat a common intestinal infection among puppies. The puppies are randomly assigned to two equal groups. Half of the puppies will receive the drug, and the other half will receive a placebo. The veterinarians monitor the puppies. This is an example of which study method?
- 1) census
  - 2) observational study
  - 3) survey
  - 4) controlled experiment
- 13 Perry invested in property that cost him \$1500. Five years later it was worth \$3000, and 10 years from his original purchase, it was worth \$6000. Assuming the growth rate remains the same, which type of function could he create to find the value of his investment 30 years from his original purchase?
- 1) exponential function
  - 2) linear function
  - 3) quadratic function
  - 4) trigonometric function

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- 14 Jake wants to buy a car and hopes to save at least \$5000 for a down payment. The table below summarizes the amount of money he plans to save each week.

Week	1	2	3	4	5
Money Saved, in Dollars	2	5	12.5	31.25	...

Based on this plan, which expression should he use to determine how much he has saved in  $n$  weeks?

- 1)  $\frac{2 - 2(2.5^n)}{1 - 2.5}$                       3)  $\frac{1 - 2.5^n}{1 - 2.5}$   
 2)  $\frac{2 - 2(2.5^{n-1})}{1 - 2.5}$                       4)  $\frac{1 - 2.5^{n-1}}{1 - 2.5}$

- 15 Where  $i$  is the imaginary unit, the expression  $(x + 3i)^2 - (2x - 3i)^2$  is equivalent to

- 1)  $-3x^2$   
 2)  $-3x^2 - 18$   
 3)  $-3x^2 + 18xi$   
 4)  $-3x^2 - 6xi - 18$

- 18 A study of black bears in the Adirondacks reveals that their population can be represented by the function  $P(t) = 3500(1.025)^t$ , where  $t$  is the number of years since the study began. Which function is correctly rewritten to reveal the monthly growth rate of the black bear population?

- 1)  $P(t) = 3500(1.00206)^{12t}$   
 2)  $P(t) = 3500(1.00206)^{\frac{t}{12}}$   
 3)  $P(t) = 3500(1.34489)^{12t}$   
 4)  $P(t) = 3500(1.34489)^{\frac{t}{12}}$

- 16 The solution of  $87e^{0.3x} = 5918$ , to the nearest thousandth, is

- 1) 0.583  
 2) 1.945  
 3) 4.220  
 4) 14.066

- 19 The function  $N(x) = 90(0.86)^x + 69$  can be used to predict the temperature of a cup of hot chocolate in degrees Fahrenheit after  $x$  minutes. What is the approximate average rate of change of the temperature of the hot chocolate, in degrees per minute, over the interval  $[0, 6]$ ?

- 1)  $-8.93$   
 2)  $-0.11$   
 3)  $0.11$   
 4)  $8.93$

- 17 Written in simplest form,  $\frac{c^2 - d^2}{d^2 + cd - 2c^2}$  where  $c \neq d$ , is equivalent to

- 1)  $\frac{c + d}{d + 2c}$   
 2)  $\frac{c - d}{d + 2c}$   
 3)  $\frac{-c - d}{d + 2c}$   
 4)  $\frac{-c + d}{d + 2c}$

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20 Consider the data in the table below.

	Right Handed	Left Handed
Male	87	13
Female	89	11

What is the probability that a randomly selected person is male given the person is left handed?

- 1)  $\frac{13}{200}$
- 2)  $\frac{13}{100}$
- 3)  $\frac{13}{50}$
- 4)  $\frac{13}{24}$

21 Which equation represents the equation of the parabola with focus  $(-3,3)$  and directrix  $y = 7$ ?

- 1)  $y = \frac{1}{8}(x + 3)^2 - 5$
- 2)  $y = \frac{1}{8}(x - 3)^2 + 5$
- 3)  $y = -\frac{1}{8}(x + 3)^2 + 5$
- 4)  $y = -\frac{1}{8}(x - 3)^2 + 5$

22 What is the equation of the directrix for the parabola  $-8(y - 3) = (x + 4)^2$ ?

- 1)  $y = 5$
- 2)  $y = 1$
- 3)  $y = -2$
- 4)  $y = -6$

23 If  $f(x) = x^2 + 9$  and  $g(x) = x + 3$ , which operation would not result in a polynomial expression?

- 1)  $f(x) + g(x)$
- 2)  $f(x) - g(x)$
- 3)  $f(x) \cdot g(x)$
- 4)  $f(x) \div g(x)$

24 The scores on a mathematics college-entry exam are normally distributed with a mean of 68 and standard deviation 7.2. Students scoring higher than one standard deviation above the mean will not be enrolled in the mathematics tutoring program. How many of the 750 incoming students can be expected to be enrolled in the tutoring program?

- 1) 631
- 2) 512
- 3) 238
- 4) 119

25 Tides are a periodic rise and fall of ocean water. On a typical day at a seaport, to predict the time of the next high tide, the most important value to have would be the

- 1) time between consecutive low tides
- 2) time when the tide height is 20 feet
- 3) average depth of water over a 24-hour period
- 4) difference between the water heights at low and high tide

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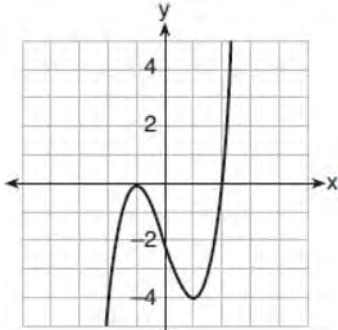
- 26 After Roger's surgery, his doctor administered pain medication in the following amounts in milligrams over four days.

Day (n)	1	2	3	4
Dosage (m)	2000	1680	1411.2	1185.4

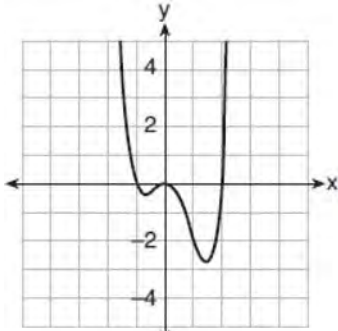
How can this sequence best be modeled recursively?

- 1)  $m_1 = 2000$   
 $m_n = m_{n-1} - 320$
- 2)  $m_n = 2000(0.84)^{n-1}$
- 3)  $m_1 = 2000$   
 $m_n = (0.84)m_{n-1}$
- 4)  $m_n = 2000(0.84)^{n+1}$
- 27 A fast-food restaurant analyzes data to better serve its customers. After its analysis, it discovers that the events  $D$ , that a customer uses the drive-thru, and  $F$ , that a customer orders French fries, are independent. The following data are given in a report:
- $$P(F) = 0.8$$
- $$P(F \cap D) = 0.456$$
- Given this information,  $P(F|D)$  is
- 1) 0.344  
 2) 0.3648  
 3) 0.57  
 4) 0.8
- 28 When a ball bounces, the heights of consecutive bounces form a geometric sequence. The height of the first bounce is 121 centimeters and the height of the third bounce is 64 centimeters. To the nearest centimeter, what is the height of the fifth bounce?
- 1) 25  
 2) 34  
 3) 36  
 4) 42
- 29 Which equation represents a parabola with a focus of  $(-2, 5)$  and a directrix of  $y = 9$ ?
- 1)  $(y - 7)^2 = 8(x + 2)$   
 2)  $(y - 7)^2 = -8(x + 2)$   
 3)  $(x + 2)^2 = 8(y - 7)$   
 4)  $(x + 2)^2 = -8(y - 7)$
- 30 For all values of  $x$  for which the expression is defined,  $\frac{x^3 + 2x^2 - 9x - 18}{x^3 - x^2 - 6x}$ , in simplest form, is equivalent to
- 1) 3  
 2)  $-\frac{17}{2}$   
 3)  $\frac{x+3}{x}$   
 4)  $\frac{x^2 - 9}{x(x-3)}$
- 31 The solution set for the equation  $b = \sqrt{2b^2 - 64}$  is
- 1)  $\{-8\}$   
 2)  $\{8\}$   
 3)  $\{\pm 8\}$   
 4)  $\{ \}$

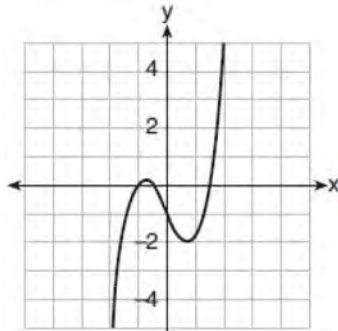
32 Which graph represents a polynomial function that contains  $x^2 + 2x + 1$  as a factor?



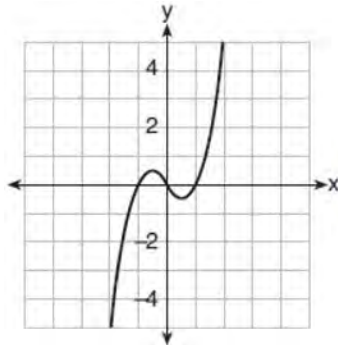
1)



2)



3)



4)

33 For positive values of  $x$ , which expression is

equivalent to  $\sqrt{16x^2} \cdot x^{\frac{2}{3}} + \sqrt[3]{8x^5}$

- 1)  $6\sqrt[5]{x^3}$
- 2)  $6\sqrt[3]{x^5}$
- 3)  $4\sqrt[3]{x^2} + 2\sqrt[3]{x^5}$
- 4)  $4\sqrt{x^3} + 2\sqrt[5]{x^3}$

34 What is the solution set of the following system of equations?

$$y = 3x + 6$$

$$y = (x + 4)^2 - 10$$

- 1)  $\{(-5, -9)\}$
- 2)  $\{(5, 21)\}$
- 3)  $\{(0, 6), (-5, -9)\}$
- 4)  $\{(0, 6), (5, 21)\}$

35 Written in simplest form, the fraction  $\frac{x^3 - 9x}{9 - x^2}$ ,

where  $x \neq \pm 3$ , is equivalent to

- 1)  $-x$
- 2)  $x$
- 3)  $\frac{-x(x + 3)}{(3 + x)}$
- 4)  $\frac{x(x - 3)}{(3 - x)}$

36 Which statement is true about the graph of

$$f(x) = \left(\frac{1}{8}\right)^x ?$$

- 1) The graph is always increasing.
- 2) The graph is always decreasing.
- 3) The graph passes through  $(1, 0)$ .
- 4) The graph has an asymptote,  $x = 0$ .

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- 37 What are the solution(s) to the system of equations shown below?

$$x^2 + y^2 = 5$$

$$y = 2x$$

- 1)  $x = 1$  and  $x = -1$
- 2)  $x = 1$
- 3)  $(1, 2)$  and  $(-1, -2)$
- 4)  $(1, 2)$ , only

- 38 The terminal side of  $\theta$ , an angle in standard

position, intersects the unit circle at  $P\left(-\frac{1}{3}, -\frac{\sqrt{8}}{3}\right)$ .

What is the value of  $\sec \theta$ ?

- 1)  $-3$
- 2)  $-\frac{3\sqrt{8}}{8}$
- 3)  $-\frac{1}{3}$
- 4)  $-\frac{\sqrt{8}}{3}$

- 39 Emmeline is working on one side of a polynomial identity proof used to form Pythagorean triples.

Her work is shown below:

$$(5x)^2 + (5x^2 - 5)^2$$

Step 1:  $25x^2 + (5x^2 - 5)^2$

Step 2:  $25x^2 + 25x^2 + 25$

Step 3:  $50x^2 + 25$

Step 4:  $75x^2$

What statement is true regarding Emmeline's work?

- 1) Emmeline's work is entirely correct.
- 2) There is a mistake in step 2, only.
- 3) There are mistakes in step 2 and step 4.
- 4) There is a mistake in step 4, only.

- 40 After examining the functions  $f(x) = \ln(x + 2)$  and  $g(x) = e^{x-1}$  over the interval  $(-2, 3]$ , Lexi determined that the correct number of solutions to the equation  $f(x) = g(x)$  is

- 1) 1
- 2) 2
- 3) 3
- 4) 0

- 41 If  $f(x) = \log_3 x$  and  $g(x)$  is the image of  $f(x)$  after a translation five units to the left, which equation represents  $g(x)$ ?

- 1)  $g(x) = \log_3(x + 5)$
- 2)  $g(x) = \log_3 x + 5$
- 3)  $g(x) = \log_3(x - 5)$
- 4)  $g(x) = \log_3 x - 5$

- 42 Which expression(s) are equivalent to  $\frac{x^2 - 4x}{2x}$ , where  $x \neq 0$ ?

I.  $\frac{x}{2} - 2$     II.  $\frac{x-4}{2}$     III.  $\frac{x-1}{2} - \frac{3}{2}$

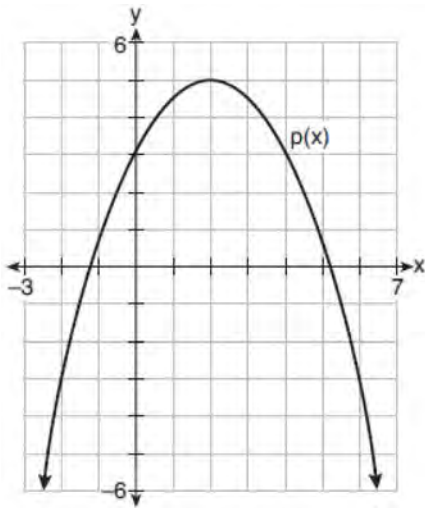
- 1) II, only
- 2) I and II
- 3) II and III
- 4) I, II, and III

- 43 For which values of  $x$ , rounded to the nearest hundredth, will  $|x^2 - 9| - 3 = \log_3 x$ ?

- 1) 2.29 and 3.63
- 2) 2.37 and 3.54
- 3) 2.84 and 3.17
- 4) 2.92 and 3.06



- 44 Consider  $f(x) = 4x^2 + 6x - 3$ , and  $p(x)$  defined by the graph below.



The difference between the values of the maximum of  $p$  and minimum of  $f$  is

- 1) 0.25
  - 2) 1.25
  - 3) 3.25
  - 4) 10.25
- 45 A recursive formula for the sequence 40, 30, 22.5, ... is

- 1)  $g_n = 40\left(\frac{3}{4}\right)^n$
- 2)  $g_1 = 40$   
 $g_n = g_{n-1} - 10$
- 3)  $g_n = 40\left(\frac{3}{4}\right)^{n-1}$
- 4)  $g_1 = 40$   
 $g_n = \frac{3}{4}g_{n-1}$

- 46 If the function  $g(x) = ab^x$  represents exponential growth, which statement about  $g(x)$  is *false*?
- 1)  $a > 0$  and  $b > 1$
  - 2) The  $y$ -intercept is  $(0, a)$ .
  - 3) The asymptote is  $y = 0$ .
  - 4) The  $x$ -intercept is  $(b, 0)$ .

- 47 For  $x > 0$ , which expression is equivalent to

$$\frac{\sqrt[3]{x^2} \cdot \sqrt{x^5}}{\sqrt[6]{x}}?$$

- 1)  $x$
  - 2)  $x^{\frac{3}{2}}$
  - 3)  $x^3$
  - 4)  $x^{10}$
- 48 Judith puts \$5000 into an investment account with interest compounded continuously. Which approximate annual rate is needed for the account to grow to \$9110 after 30 years?
- 1) 2%
  - 2) 2.2%
  - 3) 0.02%
  - 4) 0.022%
- 49 On a given school day, the probability that Nick oversleeps is 48% and the probability he has a pop quiz is 25%. Assuming these two events are independent, what is the probability that Nick oversleeps and has a pop quiz on the same day?
- 1) 73%
  - 2) 36%
  - 3) 23%
  - 4) 12%

50 Which table best represents an exponential relationship?

1) 

x	y
1	8
2	4
3	2
4	1
5	$\frac{1}{2}$

2) 

x	y
8	0
4	1
0	2
-4	3
-8	4

3) 

x	y
0	0
1	1
2	4
3	9
4	16

4) 

x	y
1	1
2	8
3	27
4	64
5	125

51 The value(s) of  $x$  that satisfy

$$\sqrt{x^2 - 4x - 5} = 2x - 10$$

- 1) {5}
- 2) {7}
- 3) {5, 7}
- 4) {3, 5, 7}

52 The profit function,  $p(x)$ , for a company is the cost function,  $c(x)$ , subtracted from the revenue function,  $r(x)$ . The profit function for the Acme Corporation is  $p(x) = -0.5x^2 + 250x - 300$  and the revenue function is  $r(x) = -0.3x^2 + 150x$ . The cost function for the Acme Corporation is

- 1)  $c(x) = 0.2x^2 - 100x + 300$
- 2)  $c(x) = 0.2x^2 + 100x + 300$
- 3)  $c(x) = -0.2x^2 + 100x - 300$
- 4)  $c(x) = -0.8x^2 + 400x - 300$

53 Which investigation technique is most often used to determine if a single variable has an impact on a given population?

- 1) observational study
- 2) random survey
- 3) controlled experiment
- 4) formal interview

54 The solutions to the equation  $5x^2 - 2x + 13 = 9$  are

- 1)  $\frac{1}{5} \pm \frac{\sqrt{21}}{5}$
- 2)  $\frac{1}{5} \pm \frac{\sqrt{19}}{5}i$
- 3)  $\frac{1}{5} \pm \frac{\sqrt{66}}{5}i$
- 4)  $\frac{1}{5} \pm \frac{\sqrt{66}}{5}$

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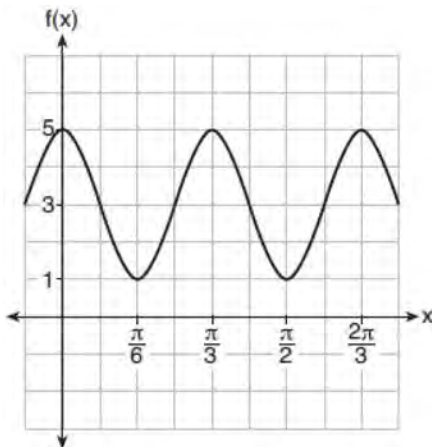
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- 55 The populations of two small towns at the beginning of 2018 and their annual population growth rate are shown in the table below.

Town	Population	Annual Population Growth Rate
Jonesville	1240	6% increase
Williamstown	890	11% increase

Assuming the trend continues, approximately how many years after the beginning of 2018 will it take for the populations to be equal?

- 1) 7  
2) 20  
3) 68  
4) 125
- 56 The function  $f(x) = a \cos bx + c$  is plotted on the graph shown below.



What are the values of  $a$ ,  $b$ , and  $c$ ?

- 1)  $a = 2, b = 6, c = 3$   
2)  $a = 2, b = 3, c = 1$   
3)  $a = 4, b = 6, c = 5$   
4)  $a = 4, b = \frac{\pi}{3}, c = 3$

- 57 If  $x - 1$  is a factor of  $x^3 - kx^2 + 2x$ , what is the value of  $k$ ?

- 1) 0  
2) 2  
3) 3  
4) -3

- 58 The half-life of iodine-131 is 8 days. The percent of the isotope left in the body  $d$  days after being

introduced is  $I = 100 \left( \frac{1}{2} \right)^{\frac{d}{8}}$ . When this equation is

written in terms of the number  $e$ , the base of the natural logarithm, it is equivalent to  $I = 100e^{kd}$ .

What is the approximate value of the constant,  $k$ ?

- 1) -0.087  
2) 0.087  
3) -11.542  
4) 11.542

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- 59 If \$5000 is put into a savings account that pays 3.5% interest compounded monthly, how much money, to the *nearest ten cents*, would be in that account after 6 years, assuming no money was added or withdrawn?
- 1) \$5177.80
  - 2) \$5941.30
  - 3) \$6146.30
  - 4) \$6166.50

- 60 What is the solution set of the equation

$$\frac{2}{x} - \frac{3x}{x+3} = \frac{x}{x+3}?$$

- 1) {3}
- 2)  $\left\{\frac{3}{2}\right\}$
- 3) {-2,3}
- 4)  $\left\{-1, \frac{3}{2}\right\}$

- 61 The parabola described by the equation

$$y = \frac{1}{12}(x-2)^2 + 2$$

has the directrix at  $y = -1$ . The

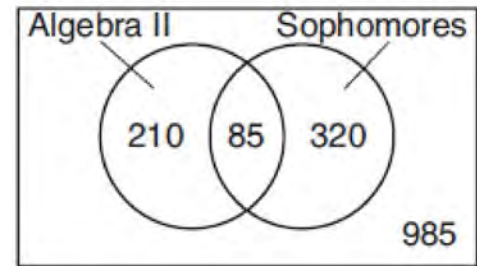
focus of the parabola is

- 1) (2,-1)
- 2) (2,2)
- 3) (2,3)
- 4) (2,5)

- 62 A researcher randomly divides 50 bean plants into two groups. He puts one group by a window to receive natural light and the second group under artificial light. He records the growth of the plants weekly. Which data collection method is described in this situation?

- 1) observational study
- 2) controlled experiment
- 3) survey
- 4) systematic sample

- 63 Data for the students enrolled in a local high school are shown in the Venn diagram below.



If a student from the high school is selected at random, what is the probability that the student is a sophomore given that the student is enrolled in Algebra II?

- 1)  $\frac{85}{210}$
- 2)  $\frac{85}{295}$
- 3)  $\frac{85}{405}$
- 4)  $\frac{85}{1600}$

- 64 Consider the system below.

$$x + y + z = 9$$

$$x - y - z = -1$$

$$x - y + z = 21$$

Which value is *not* in the solution,  $(x,y,z)$ , of the system?

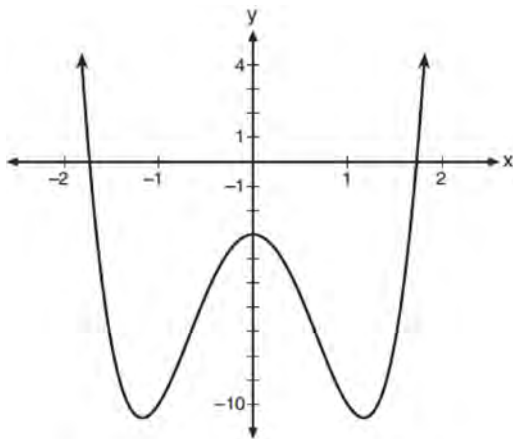
- 1) -8
- 2) -6
- 3) 11
- 4) 4

Algebra II Multiple Choice Regents Exam Questions

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- 65 Which expression is equivalent to  $(2x - i)^2 - (2x - i)(2x + 3i)$  where  $i$  is the imaginary unit and  $x$  is a real number?
- 1)  $-4 - 8xi$
  - 2)  $-4 - 4xi$
  - 3)  $2$
  - 4)  $8x - 4i$
- 66 The completely factored form of  $n^4 - 9n^2 + 4n^3 - 36n - 12n^2 + 108$  is
- 1)  $(n^2 - 9)(n + 6)(n - 2)$
  - 2)  $(n + 3)(n - 3)(n + 6)(n - 2)$
  - 3)  $(n - 3)(n - 3)(n + 6)(n - 2)$
  - 4)  $(n + 3)(n - 3)(n - 6)(n + 2)$
- 67 The first term of a geometric sequence is 8 and the fourth term is 216. What is the sum of the first 12 terms of the corresponding series?
- 1) 236,192
  - 2) 708,584
  - 3) 2,125,760
  - 4) 6,377,288
- 68 A manufacturing plant produces two different-sized containers of peanuts. One container weighs  $x$  ounces and the other weighs  $y$  pounds. If a gift set can hold one of each size container, which expression represents the number of gift sets needed to hold 124 ounces?
- 1)  $\frac{124}{16x + y}$
  - 2)  $\frac{x + 16y}{124}$
  - 3)  $\frac{124}{x + 16y}$
  - 4)  $\frac{16x + y}{124}$
- 69 A random sample of 100 people that would best estimate the proportion of all registered voters in a district who support improvements to the high school football field should be drawn from registered voters in the district at a
- 1) football game
  - 2) supermarket
  - 3) school fund-raiser
  - 4) high school band concert
- 70 The function below models the average price of gas in a small town since January 1st.
- $$G(t) = -0.0049t^4 + 0.0923t^3 - 0.56t^2 + 1.166t + 3.23,$$
- where  $0 \leq t \leq 10$ .  
If  $G(t)$  is the average price of gas in dollars and  $t$  represents the number of months since January 1st, the absolute maximum  $G(t)$  reaches over the given domain is about
- 1) \$1.60
  - 2) \$3.92
  - 3) \$4.01
  - 4) \$7.73
- 71 If  $A = -3 + 5i$ ,  $B = 4 - 2i$ , and  $C = 1 + 6i$ , where  $i$  is the imaginary unit, then  $A - BC$  equals
- 1)  $5 - 17i$
  - 2)  $5 + 27i$
  - 3)  $-19 - 17i$
  - 4)  $-19 + 27i$
- 72 What is the inverse of  $f(x) = \frac{x}{x+2}$ , where  $x \neq -2$ ?
- 1)  $f^{-1}(x) = \frac{2x}{x-1}$
  - 2)  $f^{-1}(x) = \frac{-2x}{x-1}$
  - 3)  $f^{-1}(x) = \frac{x}{x-2}$
  - 4)  $f^{-1}(x) = \frac{-x}{x-2}$

- 73 Consider the function  $p(x) = 3x^3 + x^2 - 5x$  and the graph of  $y = m(x)$  below.



Which statement is true?

- 1)  $p(x)$  has three real roots and  $m(x)$  has two real roots.
  - 2)  $p(x)$  has one real root and  $m(x)$  has two real roots.
  - 3)  $p(x)$  has two real roots and  $m(x)$  has three real roots.
  - 4)  $p(x)$  has three real roots and  $m(x)$  has four real roots.
- 74 The roots of the equation  $3x^2 + 2x = -7$  are
- 1)  $-2, -\frac{1}{3}$
  - 2)  $-\frac{7}{3}, 1$
  - 3)  $-\frac{1}{3} \pm \frac{2i\sqrt{5}}{3}$
  - 4)  $-\frac{1}{3} \pm \frac{\sqrt{11}}{3}$

- 75 Given  $f(x) = \frac{1}{2}x + 8$ , which equation represents the inverse,  $g(x)$ ?

- 1)  $g(x) = 2x - 8$
  - 2)  $g(x) = 2x - 16$
  - 3)  $g(x) = -\frac{1}{2}x + 8$
  - 4)  $g(x) = -\frac{1}{2}x - 16$
- 76 Suppose two sets of test scores have the same mean, but different standard deviations,  $\sigma_1$  and  $\sigma_2$ , with  $\sigma_2 > \sigma_1$ . Which statement best describes the variability of these data sets?
- 1) Data set one has the greater variability.
  - 2) Data set two has the greater variability.
  - 3) The variability will be the same for each data set.
  - 4) No conclusion can be made regarding the variability of either set.

- 77 A sociologist reviews randomly selected surveillance videos from a public park over a period of several years and records the amount of time people spent on a smartphone. The statistical procedure the sociologist used is called

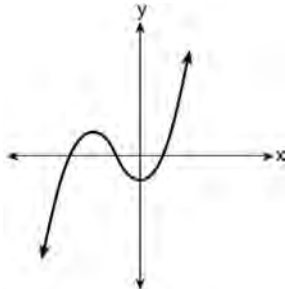
- 1) a census
  - 2) an experiment
  - 3) an observational study
  - 4) a sample survey
- 78 Expressed in simplest  $a + bi$  form,  $(7 - 3i) + (x - 2i)^2 - (4i + 2x^2)$  is
- 1)  $(3 - x^2) - (4x + 7)i$
  - 2)  $(3 + 3x^2) - (4x + 7)i$
  - 3)  $(3 - x^2) - 7i$
  - 4)  $(3 + 3x^2) - 7i$

79 Consider the end behavior description below.

- as  $x \rightarrow -\infty, f(x) \rightarrow \infty$
- as  $x \rightarrow \infty, f(x) \rightarrow -\infty$

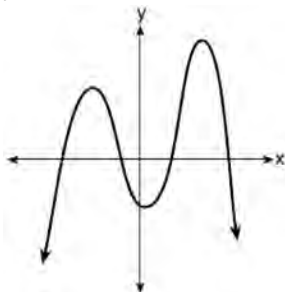
Which function satisfies the given conditions?

1)  $f(x) = x^4 + 2x^2 + 1$



2)

3)  $f(x) = -x^3 + 2x - 6$



4)

80 Which expression is equivalent to

$$\frac{2x^4 + 8x^3 - 25x^2 - 6x + 14}{x + 6}?$$

- 1)  $2x^3 + 4x^2 + x - 12 + \frac{86}{x + 6}$
- 2)  $2x^3 - 4x^2 - x + 14$
- 3)  $2x^3 - 4x^2 - x + \frac{14}{x + 6}$
- 4)  $2x^3 - 4x^2 - x$

81 What is the inverse of  $f(x) = x^3 - 2$ ?

- 1)  $f^{-1}(x) = \sqrt[3]{x} + 2$
- 2)  $f^{-1}(x) = \pm \sqrt[3]{x} + 2$
- 3)  $f^{-1}(x) = \sqrt[3]{x + 2}$
- 4)  $f^{-1}(x) = \pm \sqrt[3]{x + 2}$

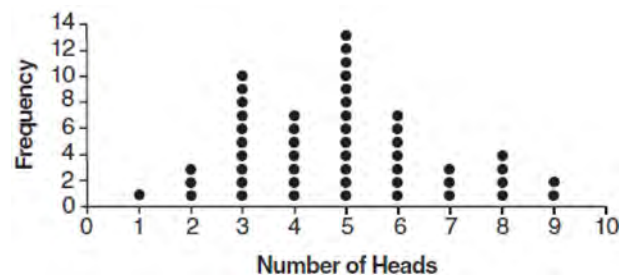
82 If  $(a^3 + 27) = (a + 3)(a^2 + ma + 9)$ , then  $m$  equals

- 1)  $-9$
- 2)  $-3$
- 3)  $3$
- 4)  $6$

83 The expression  $6 - (3x - 2i)^2$  is equivalent to

- 1)  $-9x^2 + 12xi + 10$
- 2)  $9x^2 - 12xi + 2$
- 3)  $-9x^2 + 10$
- 4)  $-9x^2 + 12xi - 4i + 6$

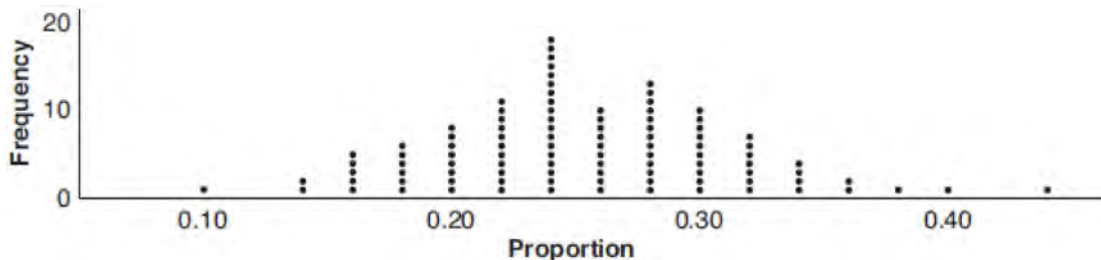
84 The results of simulating tossing a coin 10 times, recording the number of heads, and repeating this 50 times are shown in the graph below.



Based on the results of the simulation, which statement is *false*?

- 1) Five heads occurred most often, which is consistent with the theoretical probability of obtaining a heads.
- 2) Eight heads is unusual, as it falls outside the middle 95% of the data.
- 3) Obtaining three heads or fewer occurred 28% of the time.
- 4) Seven heads is not unusual, as it falls within the middle 95% of the data.

- 85 A group of students was trying to determine the proportion of candies in a bag that are blue. The company claims that 24% of candies in bags are blue. A simulation was run 100 times with a sample size of 50, based on the premise that 24% of the candies are blue. The approximately normal results of the simulation are shown in the dot plot below.

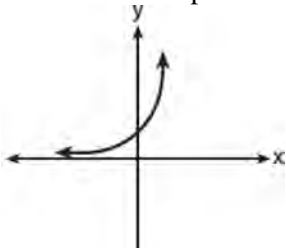
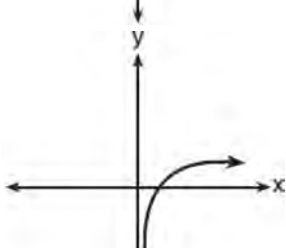
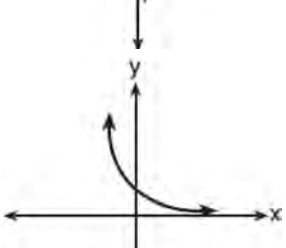
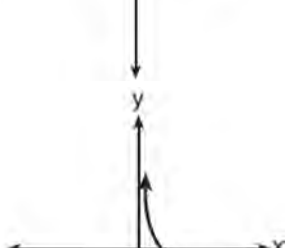


The simulation results in a mean of 0.254 and a standard deviation of 0.060. Based on this simulation, what is a plausible interval containing the middle 95% of the data?

- |   |  |
|---|--|
| <p>1) (0.194, 0.314)</p> <p>2) (0.134, 0.374)</p> | <p>3) (-0.448, 0.568)</p> <p>4) (0.254, 0.374)</p> |
|---|--|
- 
- 86 What is the solution set of the equation  $\frac{2}{3x+1} = \frac{1}{x} - \frac{6x}{3x+1}$ ?
- |  |   |
|--|---|
| <p>1) <math>\left\{-\frac{1}{3}, \frac{1}{2}\right\}</math></p> <p>2) <math>\left\{-\frac{1}{3}\right\}</math></p> <p>3) <math>\left\{\frac{1}{2}\right\}</math></p> <p>4) <math>\left\{\frac{1}{3}, -2\right\}</math></p> | <p>88 Given the following polynomials</p> $x = (a + b + c)^2$ $y = a^2 + b^2 + c^2$ $z = ab + bc + ac$ <p>Which identity is true?</p> <p>1) <math>x = y - z</math></p> <p>2) <math>x = y + z</math></p> <p>3) <math>x = y - 2z</math></p> <p>4) <math>x = y + 2z</math></p> |
|--|---|
- 
- 87 If  $p(x) = 2x^3 - 3x + 5$ , what is the remainder of  $p(x) \div (x - 5)$ ?
- |   |  |
|---|--|
| <p>1) -230</p> <p>2) 0</p> <p>3) 40</p> <p>4) 240</p> | <p>89 For <math>x \geq 0</math>, which equation is <i>false</i>?</p> <p>1) <math>(x^{\frac{3}{2}})^2 = \sqrt[4]{x^3}</math></p> <p>2) <math>(x^3)^{\frac{1}{4}} = \sqrt[4]{x^3}</math></p> <p>3) <math>(x^{\frac{3}{2}})^{\frac{1}{2}} = \sqrt[4]{x^3}</math></p> <p>4) <math>(x^{\frac{2}{3}})^2 = \sqrt[3]{x^4}</math></p> |
|---|--|



90 Which sketch best represents the graph of  $x = 3^y$ ?

- 1) 
- 2) 
- 3) 
- 4) 

91 Which statement(s) are true for all real numbers?

- I  $(x - y)^2 = x^2 + y^2$   
 II  $(x + y)^3 = x^3 + 3xy + y^3$

- 1) I, only  
 2) II, only  
 3) I and II  
 4) neither I nor II

92 The average monthly temperature of a city can be modeled by a cosine graph. Melissa has been living in Phoenix, Arizona, where the average annual temperature is  $75^\circ\text{F}$ . She would like to move, and live in a location where the average annual temperature is  $62^\circ\text{F}$ . When examining the graphs of the average monthly temperatures for various locations, Melissa should focus on the

- 1) amplitude  
 2) horizontal shift  
 3) period  
 4) midline

93 Which expression can be rewritten as  $(x + 7)(x - 1)$ ?

- 1)  $(x + 3)^2 - 16$   
 2)  $(x + 3)^2 - 10(x + 3) - 2(x + 3) + 20$   
 3)  $\frac{(x - 1)(x^2 - 6x - 7)}{(x + 1)}$   
 4)  $\frac{(x + 7)(x^2 + 4x + 3)}{(x + 3)}$

94 The solutions to  $x + 3 - \frac{4}{x - 1} = 5$  are

- 1)  $\frac{3}{2} \pm \frac{\sqrt{17}}{2}$   
 2)  $\frac{3}{2} \pm \frac{\sqrt{17}}{2} i$   
 3)  $\frac{3}{2} \pm \frac{\sqrt{33}}{2}$   
 4)  $\frac{3}{2} \pm \frac{\sqrt{33}}{2} i$

Algebra II Multiple Choice Regents Exam Questions

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- 95 For the system shown below, what is the value of  $z$ ?

$$y = -2x + 14$$

$$3x - 4z = 2$$

$$3x - y = 16$$

- 1) 5  
 2) 2  
 3) 6  
 4) 4
- 96 Given  $P(x) = x^3 - 3x^2 - 2x + 4$ , which statement is true?  
 1)  $(x - 1)$  is a factor because  $P(-1) = 2$ .  
 2)  $(x + 1)$  is a factor because  $P(-1) = 2$ .  
 3)  $(x + 1)$  is a factor because  $P(1) = 0$ .  
 4)  $(x - 1)$  is a factor because  $P(1) = 0$ .

- 97 A number, minus twenty times its reciprocal, equals eight. The number is  
 1) 10 or  $-2$   
 2) 10 or 2  
 3)  $-10$  or  $-2$   
 4)  $-10$  or 2

- 98 The expression  $\frac{9x^2 - 2}{3x + 1}$  is equivalent to  
 1)  $3x - 1 - \frac{1}{3x + 1}$   
 2)  $3x - 1 + \frac{1}{3x + 1}$   
 3)  $3x + 1 - \frac{1}{3x + 1}$   
 4)  $3x + 1 + \frac{1}{3x + 1}$

- 99 Which description could represent the graph of  $f(x) = 4x^2(x + a) - x - a$ , if  $a$  is an integer?  
 1) As  $x \rightarrow -\infty, f(x) \rightarrow \infty$ , as  $x \rightarrow \infty, f(x) \rightarrow \infty$ , and the graph has 3  $x$ -intercepts.  
 2) As  $x \rightarrow -\infty, f(x) \rightarrow -\infty$ , as  $x \rightarrow \infty, f(x) \rightarrow \infty$ , and the graph has 3  $x$ -intercepts.  
 3) As  $x \rightarrow -\infty, f(x) \rightarrow \infty$ , as  $x \rightarrow \infty, f(x) \rightarrow -\infty$ , and the graph has 4  $x$ -intercepts.  
 4) As  $x \rightarrow -\infty, f(x) \rightarrow -\infty$ , as  $x \rightarrow \infty, f(x) \rightarrow \infty$ , and the graph has 4  $x$ -intercepts.

- 100 Julia deposits \$2000 into a savings account that earns 4% interest per year. The exponential function that models this savings account is  $y = 2000(1.04)^t$ , where  $t$  is the time in years. Which equation correctly represents the amount of money in her savings account in terms of the monthly growth rate?  
 1)  $y = 166.67(1.04)^{0.12t}$   
 2)  $y = 2000(1.01)^t$   
 3)  $y = 2000(1.0032737)^{12t}$   
 4)  $y = 166.67(1.0032737)^t$

- 101 The Fahrenheit temperature,  $F(t)$ , of a heated object at time  $t$ , in minutes, can be modeled by the function below.  $F_s$  is the surrounding temperature,  $F_0$  is the initial temperature of the object, and  $k$  is a constant.

$$F(t) = F_s + (F_0 - F_s)e^{-kt}$$

Coffee at a temperature of  $195^\circ\text{F}$  is poured into a container. The room temperature is kept at a constant  $68^\circ\text{F}$  and  $k = 0.05$ . Coffee is safe to drink when its temperature is, at most,  $120^\circ\text{F}$ . To the *nearest minute*, how long will it take until the coffee is safe to drink?

- 1) 7  
 2) 10  
 3) 11  
 4) 18

Algebra II Multiple Choice Regents Exam Questions

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102 Which expression is *not* a solution to the equation  $2^t = \sqrt{10}$ ?

- 1)  $\frac{1}{2} \log_2 10$
- 2)  $\log_2 \sqrt{10}$
- 3)  $\log_4 10$
- 4)  $\log_{10} 4$

103 Which expression is equivalent to

$$x^6 y^4 (x^4 - 16) - 9(x^4 - 16)?$$

- 1)  $x^{10} y^4 - 16x^6 y^4 - 9x^4 - 144$
- 2)  $(x^6 y^4 - 9)(x + 2)^3 (x - 2)$
- 3)  $(x^3 y^2 + 3)(x^3 y^2 - 3)(x + 2)^2 (x - 2)^2$
- 4)  $(x^3 y^2 + 3)(x^3 y^2 - 3)(x^2 + 4)(x^2 - 4)$

104 The operator of the local mall wants to find out how many of the mall's employees make purchases in the food court when they are working. She hopes to use these data to increase the rent and attract new food vendors. In total, there are 1023 employees who work at the mall. The best method to obtain a random sample of the employees would be to survey

- 1) all 170 employees at each of the larger stores
- 2) 50% of the 90 employees of the food court
- 3) every employee
- 4) every 30th employee entering each mall entrance for one week

105 The graph of  $y = \log_2 x$  is translated to the right 1 unit and down 1 unit. The coordinates of the  $x$ -intercept of the translated graph are

- 1) (0,0)
- 2) (1,0)
- 3) (2,0)
- 4) (3,0)

106 The equation  $t = \frac{1}{0.0105} \ln\left(\frac{A}{5000}\right)$  relates time,  $t$ ,

in years, to the amount of money,  $A$ , earned by a \$5000 investment. Which statement accurately describes the relationship between the average rates of change of  $t$  on the intervals [6000, 8000] and [9000, 12,000]?

- 1) A comparison cannot be made because the intervals are different sizes.
- 2) The average rate of change is equal for both intervals.
- 3) The average rate of change is larger for the interval [6000, 8000].
- 4) The average rate of change is larger for the interval [9000, 12,000].

107 How many solutions exist for

$$\frac{1}{1-x^2} = -|3x-2| + 5?$$

- 1) 1
- 2) 2
- 3) 3
- 4) 4

108 When factoring to reveal the roots of the equation  $x^3 + 2x^2 - 9x - 18 = 0$ , which equations can be used?

- I.  $x^2(x+2) - 9(x+2) = 0$
- II.  $x(x^2-9) + 2(x^2-9) = 0$
- III.  $(x-2)(x^2-9) = 0$

- 1) I and II, only
- 2) I and III, only
- 3) II and III, only
- 4) I, II, and III

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- 109 Sodium iodide-131, used to treat certain medical conditions, has a half-life of 1.8 hours. The data table below shows the amount of sodium iodide-131, rounded to the nearest thousandth, as the dose fades over time.

<b>Number of Half Lives</b>	1	2	3	4	5
<b>Amount of Sodium Iodide-131</b>	139.000	69.500	34.750	17.375	8.688

What approximate amount of sodium iodide-131 will remain in the body after 18 hours?

- 1) 0.001  
2) 0.136  
3) 0.271  
4) 0.543
- 110 The temperature, in degrees Fahrenheit, in Times Square during a day in August can be predicted by the function  $T(x) = 8 \sin(0.3x - 3) + 74$ , where  $x$  is the number of hours after midnight. According to this model, the predicted temperature, to the nearest degree Fahrenheit, at 7 P.M. is  
1) 68  
2) 74  
3) 77  
4) 81
- 111 Given  $y > 0$ , the expression  $\sqrt{3x^2y} \cdot \sqrt[3]{27x^3y^2}$  is equivalent to  
1)  $81x^5y^3$   
2)  $3^{1.5}x^2y$   
3)  $3^{\frac{5}{2}}x^2y^{\frac{5}{3}}$   
4)  $3^{\frac{3}{2}}x^2y^{\frac{7}{6}}$
- 112 The expression  $(x + a)(x + b)$  can *not* be written as  
1)  $a(x + b) + x(x + b)$   
2)  $x^2 + abx + ab$   
3)  $x^2 + (a + b)x + ab$   
4)  $x(x + a) + b(x + a)$
- 113 If  $p(x) = 2 \ln(x) - 1$  and  $m(x) = \ln(x + 6)$ , then what is the solution for  $p(x) = m(x)$ ?  
1) 1.65  
2) 3.14  
3) 5.62  
4) no solution
- 114 What is the inverse of the function  $y = 4x + 5$ ?  
1)  $x = \frac{1}{4}y - \frac{5}{4}$   
2)  $y = \frac{1}{4}x - \frac{5}{4}$   
3)  $y = 4x - 5$   
4)  $y = \frac{1}{4x + 5}$

- 115 A savings account,  $S$ , has an initial value of \$50. The account grows at a 2% interest rate compounded  $n$  times per year,  $t$ , according to the function below.

$$S(t) = 50 \left( 1 + \frac{.02}{n} \right)^{nt}$$

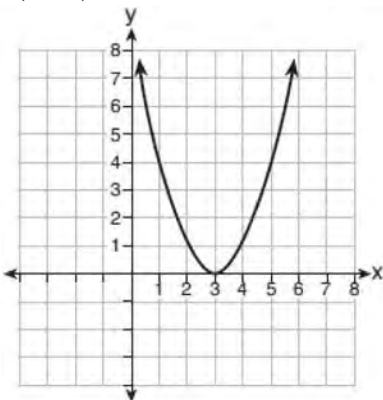
Which statement about the account is correct?

- 1) As the value of  $n$  increases, the amount of interest per year decreases.
- 2) As the value of  $n$  increases, the value of the account approaches the function  $S(t) = 50e^{0.02t}$ .
- 3) As the value of  $n$  decreases to one, the amount of interest per year increases.
- 4) As the value of  $n$  decreases to one, the value of the account approaches the function  $S(t) = 50(1 - 0.02)^t$ .

- 116 Which representation of a quadratic has imaginary roots?

x	y
-2.5	2
-2.0	0
-1.5	-1
-1.0	-1
-0.5	0
0.0	2

- 1)
- 2)  $2(x + 3)^2 = 64$



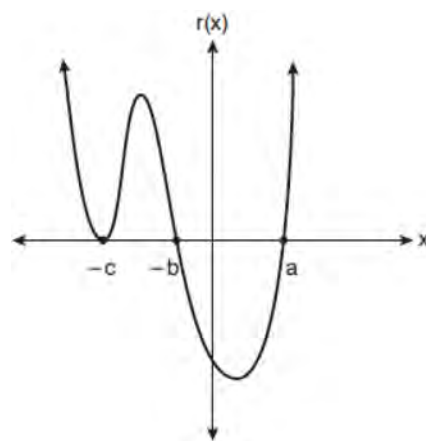
- 3)
- 4)  $2x^2 + 32 = 0$

- 117 Which value, to the nearest tenth, is the smallest solution of  $f(x) = g(x)$  if  $f(x) = 3 \sin\left(\frac{1}{2}x\right) - 1$  and

$$g(x) = x^3 - 2x + 1?$$

- 1) -3.6
- 2) -2.1
- 3) -1.8
- 4) 1.4

- 118 A sketch of  $r(x)$  is shown below.



An equation for  $r(x)$  could be

- 1)  $r(x) = (x - a)(x + b)(x + c)$
- 2)  $r(x) = (x + a)(x - b)(x - c)^2$
- 3)  $r(x) = (x + a)(x - b)(x - c)$
- 4)  $r(x) = (x - a)(x + b)(x + c)^2$

- 119 According to a study, 45% of Americans have type O blood. If a random number generator produces three-digit values from 000 to 999, which values would represent those having type O blood?

- 1) between 000 and 045, inclusive
- 2) between 000 and 444, inclusive
- 3) between 000 and 449, inclusive
- 4) between 000 and 450, inclusive

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120 Suppose events  $A$  and  $B$  are independent and  $P(A \text{ and } B)$  is 0.2. Which statement could be true?

- 1)  $P(A) = 0.4, P(B) = 0.3, P(A \text{ or } B) = 0.5$
- 2)  $P(A) = 0.8, P(B) = 0.25$
- 3)  $P(A|B) = 0.2, P(B) = 0.2$
- 4)  $P(A) = 0.15, P(B) = 0.05$

121 On average, college seniors graduating in 2012 could compute their growing student loan debt using the function  $D(t) = 29,400(1.068)^t$ , where  $t$  is time in years. Which expression is equivalent to  $29,400(1.068)^t$  and could be used by students to identify an approximate daily interest rate on their loans?

- 1)  $29,400 \left( 1.068^{\frac{1}{365}} \right)^t$
- 2)  $29,400 \left( \frac{1.068}{365} \right)^{365t}$
- 3)  $29,400 \left( 1 + \frac{0.068}{365} \right)^t$
- 4)  $29,400 \left( 1.068^{\frac{1}{365}} \right)^{365t}$

122 At her job, Pat earns \$25,000 the first year and receives a raise of \$1000 each year. The explicit formula for the  $n$ th term of this sequence is  $a_n = 25,000 + (n - 1)1000$ . Which rule best represents the equivalent recursive formula?

- 1)  $a_n = 24,000 + 1000n$
- 2)  $a_n = 25,000 + 1000n$
- 3)  $a_1 = 25,000, a_n = a_{n-1} + 1000$
- 4)  $a_1 = 25,000, a_n = a_{n+1} + 1000$

123 Consider the probability statements regarding events  $A$  and  $B$  below.

$$P(A \text{ or } B) = 0.3;$$

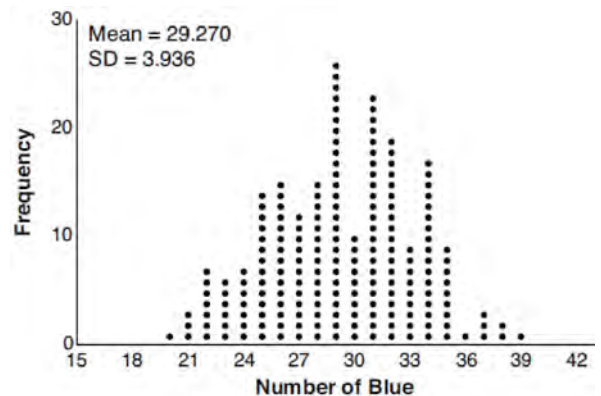
$$P(A \text{ and } B) = 0.2; \text{ and}$$

$$P(A|B) = 0.8$$

What is  $P(B)$ ?

- 1) 0.1
- 2) 0.25
- 3) 0.375
- 4) 0.667

124 The J& B candy company claims that 45% of the candies it produces are blue, 30% are brown, and 25% are yellow. Each bag holds 65 candies. A simulation was run 200 times, each of sample size 65, based on the premise that 45% of the candies are blue. The results of the simulation are shown below.



Bonnie purchased a bag of J& B's candy and counted 24 blue candies. What inference can be made regarding a bag of J& B's with only 24 blue candies?

- 1) The company is not meeting their production standard.
- 2) Bonnie's bag was a rarity and the company should not be concerned.
- 3) The company should change their claim to 37% blue candies are produced.
- 4) Bonnie's bag is within the middle 95% of the simulated data supporting the company's claim.

125 Selected values for the functions  $f$  and  $g$  are shown in the tables below.

$x$	$f(x)$		$x$	$g(x)$
-3.12	-4.88		-2.01	-1.01
0	-6		0	0.58
1.23	-4.77		8.52	2.53
8.52	2.53		13.11	3.01
9.01	3.01		16.52	3.29

A solution to the equation  $f(x) = g(x)$  is

- 1) 0  
 2) 2.53  
 3) 3.01  
 4) 8.52

126 The expression  $\sqrt[4]{81x^8y^6}$  is equivalent to

- 1)  $3x^2y^{\frac{3}{2}}$   
 2)  $3x^4y^2$   
 3)  $9x^2y^{\frac{3}{2}}$   
 4)  $9x^4y^2$

127 Brian deposited 1 cent into an empty non-interest bearing bank account on the first day of the month. He then additionally deposited 3 cents on the second day, 9 cents on the third day, and 27 cents on the fourth day. What would be the total amount of money in the account at the end of the 20th day if the pattern continued?

- 1) \$11,622,614.67  
 2) \$17,433,922.00  
 3) \$116,226,146.80  
 4) \$1,743,392,200.00

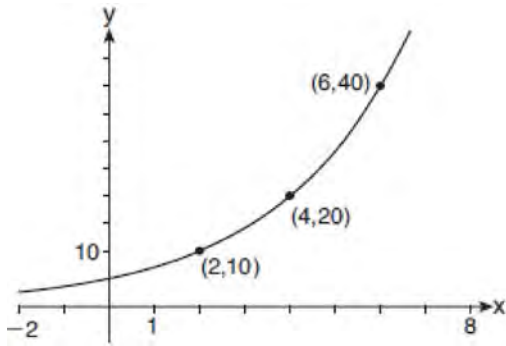
128 What is the inverse of  $f(x) = -6(x - 2)$ ?

- 1)  $f^{-1}(x) = -2 - \frac{x}{6}$   
 2)  $f^{-1}(x) = 2 - \frac{x}{6}$   
 3)  $f^{-1}(x) = \frac{1}{-6(x - 2)}$   
 4)  $f^{-1}(x) = 6(x + 2)$

129 Given  $\cos \theta = \frac{7}{25}$ , where  $\theta$  is an angle in standard position terminating in quadrant IV, and  $\sin^2 \theta + \cos^2 \theta = 1$ , what is the value of  $\tan \theta$ ?

- 1)  $-\frac{24}{25}$   
 2)  $-\frac{24}{7}$   
 3)  $\frac{24}{25}$   
 4)  $\frac{24}{7}$

130 The graph of  $y = f(x)$  is shown below.



Which expression defines  $f(x)$ ?

- 1)  $2x$
- 2)  $5(2^x)$
- 3)  $5(2^{\frac{x}{2}})$
- 4)  $5(2^{2x})$

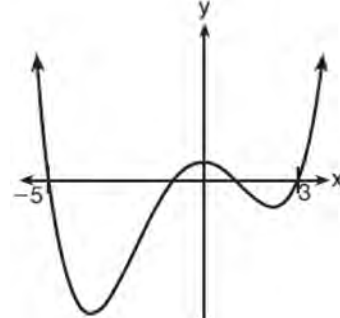
131 What is the quotient when  $10x^3 - 3x^2 - 7x + 3$  is divided by  $2x - 1$ ?

- 1)  $5x^2 + x + 3$
- 2)  $5x^2 - x + 3$
- 3)  $5x^2 - x - 3$
- 4)  $5x^2 + x - 3$

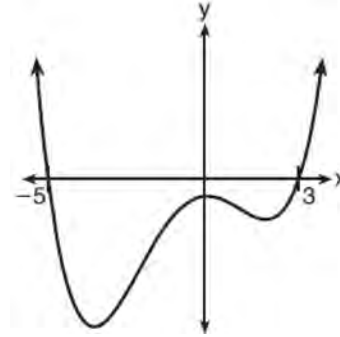
132 If  $n = \sqrt{a^5}$  and  $m = a$ , where  $a > 0$ , an expression for  $\frac{n}{m}$  could be

- 1)  $a^{\frac{5}{2}}$
- 2)  $a^4$
- 3)  $\sqrt[3]{a^2}$
- 4)  $\sqrt{a^3}$

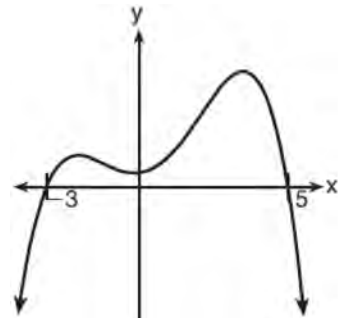
133 A 4th degree polynomial has zeros  $-5$ ,  $3$ ,  $i$ , and  $-i$ . Which graph could represent the function defined by this polynomial?



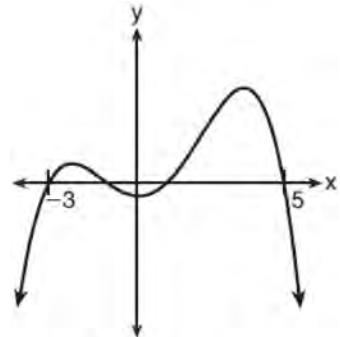
1)



2)



3)



4)



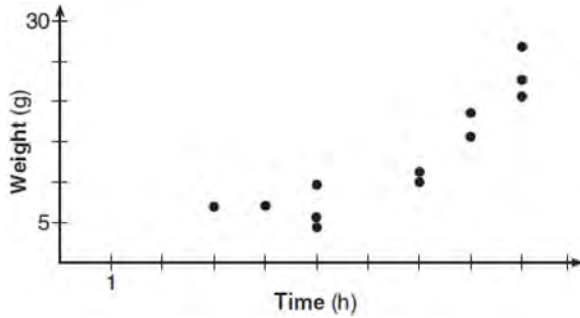
Algebra II Multiple Choice Regents Exam Questions

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- 134 When the expression  $(x+2)^2 + 4(x+2) + 3$  is rewritten as the product of two binomials, the result is
- 1)  $(x+3)(x+1)$
  - 2)  $(x+5)(x+3)$
  - 3)  $(x+2)(x+2)$
  - 4)  $(x+6)(x+1)$
- 135 If  $ae^{bt} = c$ , where  $a$ ,  $b$ , and  $c$  are positive, then  $t$  equals
- 1)  $\ln\left(\frac{c}{ab}\right)$
  - 2)  $\ln\left(\frac{cb}{a}\right)$
  - 3)  $\frac{\ln\left(\frac{c}{a}\right)}{b}$
  - 4)  $\frac{\ln\left(\frac{c}{a}\right)}{\ln b}$
- 136 Given  $c(m) = m^3 - 2m^2 + 4m - 8$ , the solution of  $c(m) = 0$  is
- 1)  $\pm 2$
  - 2) 2, only
  - 3)  $2i, 2$
  - 4)  $\pm 2i, 2$
- 137 As  $\theta$  increases from  $-\frac{\pi}{2}$  to 0 radians, the value of  $\cos \theta$  will
- 1) decrease from 1 to 0
  - 2) decrease from 0 to  $-1$
  - 3) increase from  $-1$  to 0
  - 4) increase from 0 to 1
- 138 Which function's graph has a period of 8 and reaches a maximum height of 1 if at least one full period is graphed?
- 1)  $y = -4\cos\left(\frac{\pi}{4}x\right) - 3$
  - 2)  $y = -4\cos\left(\frac{\pi}{4}x\right) + 5$
  - 3)  $y = -4\cos(8x) - 3$
  - 4)  $y = -4\cos(8x) + 5$
- 139 The graphs of the equations  $y = x^2 + 4x - 1$  and  $y + 3 = x$  are drawn on the same set of axes. One solution of this system is
- 1)  $(-5, -2)$
  - 2)  $(-1, -4)$
  - 3)  $(1, 4)$
  - 4)  $(-2, -1)$
- 140 If  $f(x) = a^x$  where  $a > 1$ , then the inverse of the function is
- 1)  $f^{-1}(x) = \log_x a$
  - 2)  $f^{-1}(x) = a \log x$
  - 3)  $f^{-1}(x) = \log_a x$
  - 4)  $f^{-1}(x) = x \log a$
- 141 The height above ground for a person riding a Ferris wheel after  $t$  seconds is modeled by  $h(t) = 150 \sin\left(\frac{\pi}{45}t + 67.5\right) + 160$  feet. How many seconds does it take to go from the bottom of the wheel to the top of the wheel?
- 1) 10
  - 2) 45
  - 3) 90
  - 4) 150

- 142 Which situation could be modeled using a geometric sequence?
- 1) A cell phone company charges \$30.00 per month for 2 gigabytes of data and \$12.50 for each additional gigabyte of data.
  - 2) The temperature in your car is  $79^\circ$ . You lower the temperature of your air conditioning by  $2^\circ$  every 3 minutes in order to find a comfortable temperature.
  - 3) David's parents have set a limit of 50 minutes per week that he may play online games during the school year. However, they will increase his time by 5% per week for the next ten weeks.
  - 4) Sarah has \$100.00 in her piggy bank and saves an additional \$15.00 each week.
- 143 Savannah just got contact lenses. Her doctor said she can wear them 2 hours the first day, and can then increase the length of time by 30 minutes each day. If this pattern continues, which formula would *not* be appropriate to determine the length of time, in either minutes or hours, she could wear her contact lenses on the  $n$ th day?
- 1)  $a_1 = 120$   
 $a_n = a_{n-1} + 30$
  - 2)  $a_n = 90 + 30n$
  - 3)  $a_1 = 2$   
 $a_n = a_{n-1} + 0.5$
  - 4)  $a_n = 2.5 + 0.5n$
- 144 The hours of daylight,  $y$ , in Utica in days,  $x$ , from January 1, 2013 can be modeled by the equation  $y = 3.06 \sin(0.017x - 1.40) + 12.23$ . How many hours of daylight, to the *nearest tenth*, does this model predict for February 14, 2013?
- 1) 9.4
  - 2) 10.4
  - 3) 12.1
  - 4) 12.2
- 145 A 7-year lease for office space states that the annual rent is \$85,000 for the first year and will increase by 6% each additional year of the lease. What will the total rent expense be for the entire 7-year lease?
- 1) \$42,809.63
  - 2) \$90,425.53
  - 3) \$595,000.00
  - 4) \$713,476.20
- 146 Chet has \$1200 invested in a bank account modeled by the function  $P(n) = 1200(1.002)^n$ , where  $P(n)$  is the value of his account, in dollars, after  $n$  months. Chet's debt is modeled by the function  $Q(n) = 100n$ , where  $Q(n)$  is the value of debt, in dollars, after  $n$  months. After  $n$  months, which function represents Chet's net worth,  $R(n)$ ?
- 1)  $R(n) = 1200(1.002)^n + 100n$
  - 2)  $R(n) = 1200(1.002)^{12n} + 100n$
  - 3)  $R(n) = 1200(1.002)^n - 100n$
  - 4)  $R(n) = 1200(1.002)^{12n} - 100n$
- 147 A certain pain reliever is taken in 220 mg dosages and has a half-life of 12 hours. The function  $A = 220 \left( \frac{1}{2} \right)^{\frac{t}{12}}$  can be used to model this situation, where  $A$  is the amount of pain reliever in milligrams remaining in the body after  $t$  hours. According to this function, which statement is true?
- 1) Every hour, the amount of pain reliever remaining is cut in half.
  - 2) In 12 hours, there is no pain reliever remaining in the body.
  - 3) In 24 hours, there is no pain reliever remaining in the body.
  - 4) In 12 hours, 110 mg of pain reliever is remaining.

- 148 A scatterplot showing the weight,  $w$ , in grams, of each crystal after growing  $t$  hours is shown below.



The relationship between weight,  $w$ , and time,  $t$ , is best modeled by

- 1)  $w = 4^t + 5$
  - 2)  $w = (1.4)^t + 2$
  - 3)  $w = 5(2.1)^t$
  - 4)  $w = 8(.75)^t$
- 149 Kelly-Ann has \$20,000 to invest. She puts half of the money into an account that grows at an annual rate of 0.9% compounded monthly. At the same time, she puts the other half of the money into an account that grows continuously at an annual rate of 0.8%. Which function represents the value of Kelly-Ann's investments after  $t$  years?
- 1)  $f(t) = 10,000(1.9)^t + 10,000e^{0.8t}$
  - 2)  $f(t) = 10,000(1.009)^t + 10,000e^{0.008t}$
  - 3)  $f(t) = 10,000(1.075)^{12t} + 10,000e^{0.8t}$
  - 4)  $f(t) = 10,000(1.00075)^{12t} + 10,000e^{0.008t}$

- 150 What is the solution set of the equation

$$\frac{10}{x^2 - 2x} + \frac{4}{x} = \frac{5}{x - 2}?$$

- 1)  $\{0, 2\}$
- 2)  $\{0\}$
- 3)  $\{2\}$
- 4)  $\{ \}$

- 151 Which situation best describes conditional probability?

- 1) finding the probability of an event occurring two or more times
- 2) finding the probability of an event occurring only once
- 3) finding the probability of two independent events occurring at the same time
- 4) finding the probability of an event occurring given another event had already occurred

- 152 If  $f(x)$  is an even function, which function must also be even?

- 1)  $f(x - 2)$
- 2)  $f(x) + 3$
- 3)  $f(x + 1)$
- 4)  $f(x + 1) + 3$

- 153 Given  $x \neq -2$ , the expression  $\frac{2x^2 + 5x + 8}{x + 2}$  is equivalent to

- 1)  $2x^2 + \frac{9}{x + 2}$
- 2)  $2x + \frac{7}{x + 2}$
- 3)  $2x + 1 + \frac{6}{x + 2}$
- 4)  $2x + 9 - \frac{10}{x + 2}$

- 154 What is the solution set for  $x$  in the equation below?

$$\sqrt{x + 1} - 1 = x$$

- 1)  $\{1\}$
- 2)  $\{0\}$
- 3)  $\{-1, 0\}$
- 4)  $\{0, 1\}$

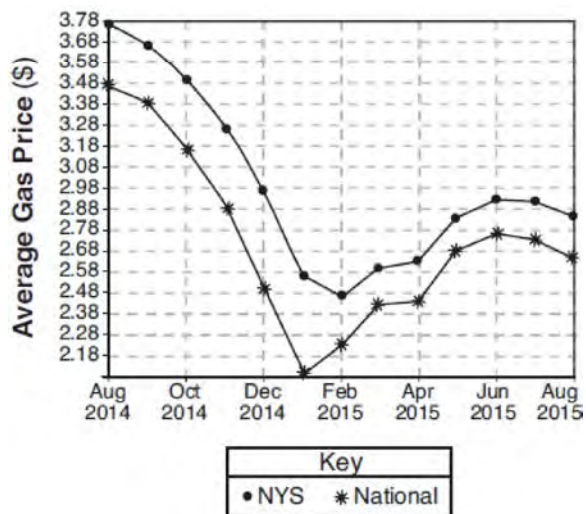
155 Consider the system of equations below:

$$\begin{aligned} x + y - z &= 6 \\ 2x - 3y + 2z &= -19 \\ -x + 4y - z &= 17 \end{aligned}$$

Which number is *not* the value of any variable in the solution of the system?

- 1) -1
- 2) 2
- 3) 3
- 4) -4

156 The graph below represents national and New York State average gas prices.



If New York State's gas prices are modeled by  $G(x)$  and  $C > 0$ , which expression best approximates the national average  $x$  months from August 2014?

- 1)  $G(x + C)$
- 2)  $G(x) + C$
- 3)  $G(x - C)$
- 4)  $G(x) - C$

157 There are 400 students in the senior class at Oak Creek High School. All of these students took the SAT. The distribution of their SAT scores is approximately normal. The number of students who scored within 2 standard deviations of the mean is approximately

- 1) 75
- 2) 95
- 3) 300
- 4) 380

158 The function  $N(t) = 100e^{-0.023t}$  models the number of grams in a sample of cesium-137 that remain after  $t$  years. On which interval is the sample's average rate of decay the fastest?

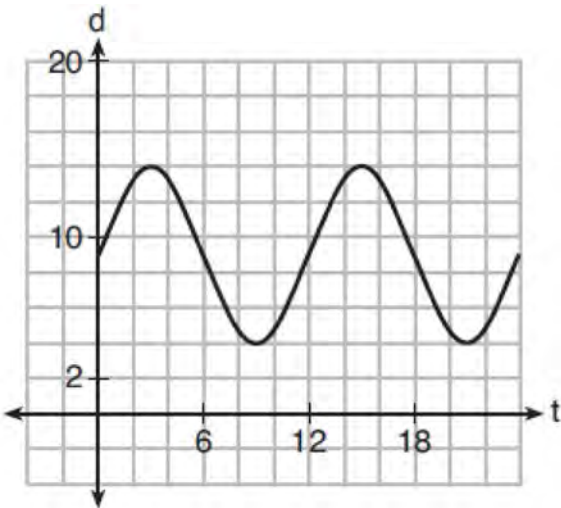
- 1) [1, 10]
- 2) [10, 20]
- 3) [15, 25]
- 4) [1, 30]

159 For a given time,  $x$ , in seconds, an electric current,  $y$ , can be represented by  $y = 2.5(1 - 2.7^{-10x})$ .

Which equation is *not* equivalent?

- 1)  $y = 2.5 - 2.5(2.7^{-10x})$
- 2)  $y = 2.5 - 2.5\left((2.7^2)^{-0.5x}\right)$
- 3)  $y = 2.5 - 2.5\left(\frac{1}{2.7^{10x}}\right)$
- 4)  $y = 2.5 - 2.5(2.7^{-2})(2.7^{0.5x})$

- 160 The depth of the water at a marker 20 feet from the shore in a bay is depicted in the graph below.



If the depth,  $d$ , is measured in feet and time,  $t$ , is measured in hours since midnight, what is an equation for the depth of the water at the marker?

- 1)  $d = 5 \cos\left(\frac{\pi}{6}t\right) + 9$
  - 2)  $d = 9 \cos\left(\frac{\pi}{6}t\right) + 5$
  - 3)  $d = 9 \sin\left(\frac{\pi}{6}t\right) + 5$
  - 4)  $d = 5 \sin\left(\frac{\pi}{6}t\right) + 9$
- 161 Consider the following patterns:
- I. 16, -12, 9, -6.75, ...
  - II. 1, 4, 9, 16, ...
  - III. 6, 18, 30, 42, ...
  - IV.  $\frac{1}{2}, \frac{2}{3}, \frac{3}{4}, \frac{4}{5}, \dots$
- Which pattern is geometric?
- 1) I
  - 2) II
  - 3) III
  - 4) IV

- 162 If a solution of  $2(2x - 1) = 5x^2$  is expressed in simplest  $a + bi$  form, the value of  $b$  is

- 1)  $\frac{\sqrt{6}}{5}i$
- 2)  $\frac{\sqrt{6}}{5}$
- 3)  $\frac{1}{5}i$
- 4)  $\frac{1}{5}$

- 163 The average depreciation rate of a new boat is approximately 8% per year. If a new boat is purchased at a price of \$75,000, which model is a recursive formula representing the value of the boat  $n$  years after it was purchased?

- 1)  $a_n = 75,000(0.08)^n$
- 2)  $a_0 = 75,000$   
 $a_n = (0.92)^n$
- 3)  $a_n = 75,000(1.08)^n$
- 4)  $a_0 = 75,000$   
 $a_n = 0.92(a_{n-1})$

- 164 If  $\cos \theta = -\frac{3}{4}$  and  $\theta$  is in Quadrant III, then  $\sin \theta$  is equivalent to

- 1)  $-\frac{\sqrt{7}}{4}$
- 2)  $\frac{\sqrt{7}}{4}$
- 3)  $-\frac{5}{4}$
- 4)  $\frac{5}{4}$

Algebra II Multiple Choice Regents Exam Questions

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- 165 The expression  $(x + a)^2 + 5(x + a) + 4$  is equivalent to
- 1)  $(a + 1)(a + 4)$
  - 2)  $(x + 1)(x + 4)$
  - 3)  $(x + a + 1)(x + a + 4)$
  - 4)  $x^2 + a^2 + 5x + 5a + 4$

- 166 An estimate of the number of milligrams of a medication in the bloodstream  $t$  hours after 400 mg has been taken can be modeled by the function below.

$$I(t) = 0.5t^4 + 3.45t^3 - 96.65t^2 + 347.7t,$$

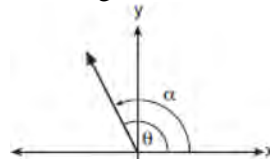
where  $0 \leq t \leq 6$

Over what time interval does the amount of medication in the bloodstream strictly increase?

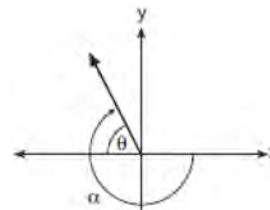
- 1) 0 to 2 hours
  - 2) 0 to 3 hours
  - 3) 2 to 6 hours
  - 4) 3 to 6 hours
- 167 Susan won \$2,000 and invested it into an account with an annual interest rate of 3.2%. If her investment were compounded monthly, which expression best represents the value of her investment after  $t$  years?
- 1)  $2000(1.003)^{12t}$
  - 2)  $2000(1.032)^{\frac{t}{12}}$
  - 3)  $2064^{\frac{t}{12}}$
  - 4)  $\frac{2000(1.032)^t}{12}$

- 168 Which function is even?
- 1)  $f(x) = \sin x$
  - 2)  $f(x) = x^2 - 4$
  - 3)  $f(x) = |x - 2| + 5$
  - 4)  $f(x) = x^4 + 3x^3 + 4$

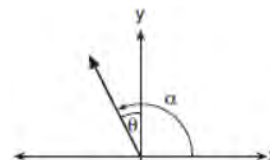
- 169 Which diagram represents an angle,  $\alpha$ , measuring  $\frac{13\pi}{20}$  radians drawn in standard position, and its reference angle,  $\theta$ ?



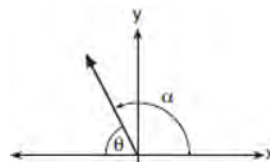
1)



2)



3)



4)

- 170 Which value, to the nearest tenth, is not a solution of  $p(x) = q(x)$  if  $p(x) = x^3 + 3x^2 - 3x - 1$  and  $q(x) = 3x + 8$ ?
- 1) -3.9
  - 2) -1.1
  - 3) 2.1
  - 4) 4.7

**Algebra II Multiple Choice Regents Exam Questions**

171 Consider the system shown below.

$$2x - y = 4$$

$$(x + 3)^2 + y^2 = 8$$

The two solutions of the system can be described as

- 1) both imaginary
- 2) both irrational
- 3) both rational
- 4) one rational and one irrational

172 Sean's team has a baseball game tomorrow. He pitches 50% of the games. There is a 40% chance of rain during the game tomorrow. If the probability that it rains given that Sean pitches is 40%, it can be concluded that these two events are

- 1) independent
- 2) dependent
- 3) mutually exclusive
- 4) complements

173 Which factorization is *incorrect*?

- 1)  $4k^2 - 49 = (2k + 7)(2k - 7)$
- 2)  $a^3 - 8b^3 = (a - 2b)(a^2 + 2ab + 4b^2)$
- 3)  $m^3 + 3m^2 - 4m + 12 = (m - 2)^2(m + 3)$
- 4)  $t^3 + 5t^2 + 6t + t^2 + 5t + 6 = (t + 1)(t + 2)(t + 3)$

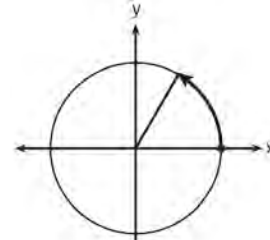
174 What are the zeros of  $P(m) = (m^2 - 4)(m^2 + 1)$ ?

- 1) 2 and -2, only
- 2) 2, -2, and -4
- 3) -4,  $i$ , and  $-i$
- 4) 2, -2,  $i$ , and  $-i$

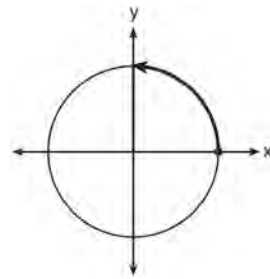
175 Which equation has  $1 - i$  as a solution?

- 1)  $x^2 + 2x - 2 = 0$
- 2)  $x^2 + 2x + 2 = 0$
- 3)  $x^2 - 2x - 2 = 0$
- 4)  $x^2 - 2x + 2 = 0$

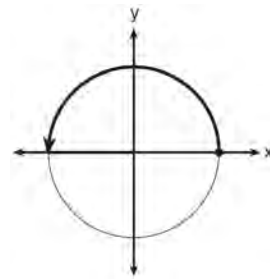
176 Which diagram shows an angle rotation of 1 radian on the unit circle?



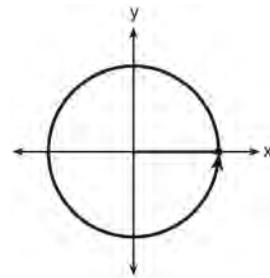
1)



2)



3)



4)

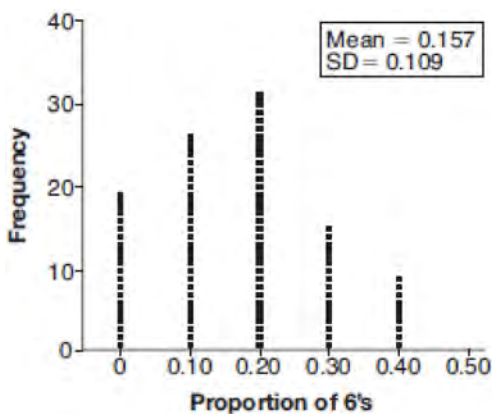
- 177 A game spinner is divided into 6 equally sized regions, as shown in the diagram below.



For Miles to win, the spinner must land on the number 6. After spinning the spinner 10 times, and losing all 10 times, Miles complained that the spinner is unfair. At home, his dad ran 100 simulations of spinning the spinner 10 times,

assuming the probability of winning each spin is  $\frac{1}{6}$ .

The output of the simulation is shown in the diagram below.



Which explanation is appropriate for Miles and his dad to make?

- The spinner was likely unfair, since the number 6 failed to occur in about 20% of the simulations.
- The spinner was likely unfair, since the spinner should have landed on the number 6 by the sixth spin.
- The spinner was likely not unfair, since the number 6 failed to occur in about 20% of the simulations.
- The spinner was likely not unfair, since in the output the player wins once or twice in the majority of the simulations.

- 178 Based on climate data that have been collected in Bar Harbor, Maine, the average monthly temperature, in degrees F, can be modeled by the equation

$B(x) = 23.914 \sin(0.508x - 2.116) + 55.300$ . The same governmental agency collected average monthly temperature data for Phoenix, Arizona, and found the temperatures could be modeled by the equation

$P(x) = 20.238 \sin(0.525x - 2.148) + 86.729$ . Which statement can *not* be concluded based on the average monthly temperature models  $x$  months after starting data collection?

- The average monthly temperature variation is more in Bar Harbor than in Phoenix.
- The midline average monthly temperature for Bar Harbor is lower than the midline temperature for Phoenix.
- The maximum average monthly temperature for Bar Harbor is  $79^\circ$  F, to the nearest degree.
- The minimum average monthly temperature for Phoenix is  $20^\circ$  F, to the nearest degree.

- 179 Given that  $\sin^2 \theta + \cos^2 \theta = 1$  and  $\sin \theta = -\frac{\sqrt{2}}{5}$ , what is a possible value of  $\cos \theta$ ?

- $\frac{5 + \sqrt{2}}{5}$
- $\frac{\sqrt{23}}{5}$
- $\frac{3\sqrt{3}}{5}$
- $\frac{\sqrt{35}}{5}$

- 180 The zeros for  $f(x) = x^4 - 4x^3 - 9x^2 + 36x$  are

- $\{0, \pm 3, 4\}$
- $\{0, 3, 4\}$
- $\{0, \pm 3, -4\}$
- $\{0, 3, -4\}$



Algebra II Multiple Choice Regents Exam Questions

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181 Which expression is equivalent to  $(3k - 2i)^2$ , where  $i$  is the imaginary unit?

- 1)  $9k^2 - 4$
- 2)  $9k^2 + 4$
- 3)  $9k^2 - 12ki - 4$
- 4)  $9k^2 - 12ki + 4$

182 The solution to the equation  $4x^2 + 98 = 0$  is

- 1)  $\pm 7$
- 2)  $\pm 7i$
- 3)  $\pm \frac{7\sqrt{2}}{2}$
- 4)  $\pm \frac{7i\sqrt{2}}{2}$

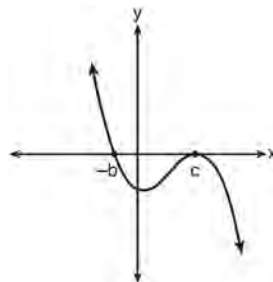
183 If  $p(x) = ab^x$  and  $r(x) = cd^x$ , then  $p(x) \cdot r(x)$  equals

- 1)  $ac(b + d)^x$
- 2)  $ac(b + d)^{2x}$
- 3)  $ac(bd)^x$
- 4)  $ac(bd)^{x^2}$

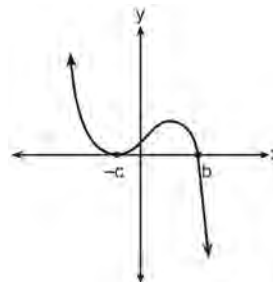
184 An equation to represent the value of a car after  $t$  months of ownership is  $v = 32,000(0.81)^{\frac{t}{12}}$ . Which statement is *not* correct?

- 1) The car lost approximately 19% of its value each month.
- 2) The car maintained approximately 98% of its value each month.
- 3) The value of the car when it was purchased was \$32,000.
- 4) The value of the car 1 year after it was purchased was \$25,920.

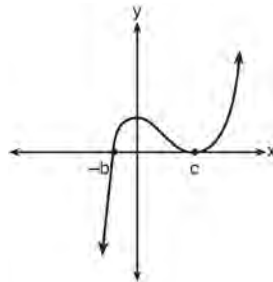
185 If  $a$ ,  $b$ , and  $c$  are all positive real numbers, which graph could represent the sketch of the graph of  $p(x) = -a(x + b)(x^2 - 2cx + c^2)$ ?



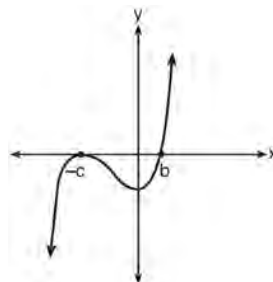
1)



2)



3)



4)

186 Which binomial is a factor of  $x^4 - 4x^2 - 4x + 8$ ?

- 1)  $x - 2$
- 2)  $x + 2$
- 3)  $x - 4$
- 4)  $x + 4$

- 187 Which statement regarding the graphs of the functions below is *untrue*?

$$f(x) = 3 \sin 2x, \text{ from } -\pi < x < \pi$$

$$g(x) = (x - 0.5)(x + 4)(x - 2)$$

$$h(x) = \log_2 x$$

$$j(x) = -|4x - 2| + 3$$

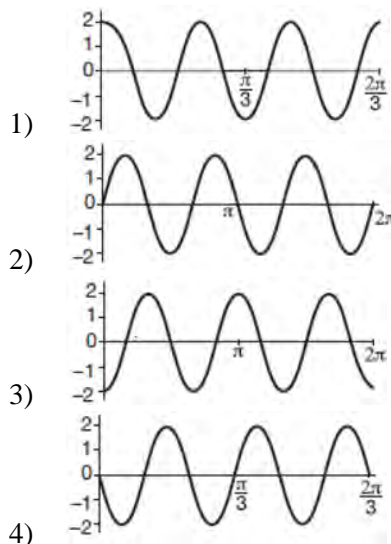
- 1)  $f(x)$  and  $j(x)$  have a maximum  $y$ -value of 3.
  - 2)  $f(x)$ ,  $h(x)$ , and  $j(x)$  have one  $y$ -intercept.
  - 3)  $g(x)$  and  $j(x)$  have the same end behavior as  $x \rightarrow -\infty$ .
  - 4)  $g(x)$ ,  $h(x)$ , and  $j(x)$  have rational zeros.
- 188 The voltage used by most households can be modeled by a sine function. The maximum voltage is 120 volts, and there are 60 cycles *every second*. Which equation best represents the value of the voltage as it flows through the electric wires, where  $t$  is time in seconds?

- 1)  $V = 120 \sin(t)$
- 2)  $V = 120 \sin(60t)$
- 3)  $V = 120 \sin(60\pi t)$
- 4)  $V = 120 \sin(120\pi t)$

- 189 Mallory wants to buy a new window air conditioning unit. The cost for the unit is \$329.99. If she plans to run the unit three months out of the year for an annual operating cost of \$108.78, which function models the cost per year over the lifetime of the unit,  $C(n)$ , in terms of the number of years,  $n$ , that she owns the air conditioner.

- 1)  $C(n) = 329.99 + 108.78n$
- 2)  $C(n) = 329.99 + 326.34n$
- 3)  $C(n) = \frac{329.99 + 108.78n}{n}$
- 4)  $C(n) = \frac{329.99 + 326.34n}{n}$

- 190 Which graph represents a cosine function with no horizontal shift, an amplitude of 2, and a period of  $\frac{2\pi}{3}$ ?



- 191 A solution of the equation  $2x^2 + 3x + 2 = 0$  is

- 1)  $-\frac{3}{4} + \frac{1}{4}i\sqrt{7}$
- 2)  $-\frac{3}{4} + \frac{1}{4}i$
- 3)  $-\frac{3}{4} + \frac{1}{4}\sqrt{7}$
- 4)  $\frac{1}{2}$

- 192 A rabbit population doubles every 4 weeks. There are currently five rabbits in a restricted area. If  $t$  represents the time, in weeks, and  $P(t)$  is the population of rabbits with respect to time, about how many rabbits will there be in 98 days?

- 1) 56
- 2) 152
- 3) 3688
- 4) 81,920

- 193 Which scenario is best described as an observational study?
- 1) For a class project, students in Health class ask every tenth student entering the school if they eat breakfast in the morning.
  - 2) A social researcher wants to learn whether or not there is a link between attendance and grades. She gathers data from 15 school districts.
  - 3) A researcher wants to learn whether or not there is a link between children's daily amount of physical activity and their overall energy level. During lunch at the local high school, she distributed a short questionnaire to students in the cafeteria.
  - 4) Sixty seniors taking a course in Advanced Algebra Concepts are randomly divided into two classes. One class uses a graphing calculator all the time, and the other class never uses graphing calculators. A guidance counselor wants to determine whether there is a link between graphing calculator use and students' final exam grades.

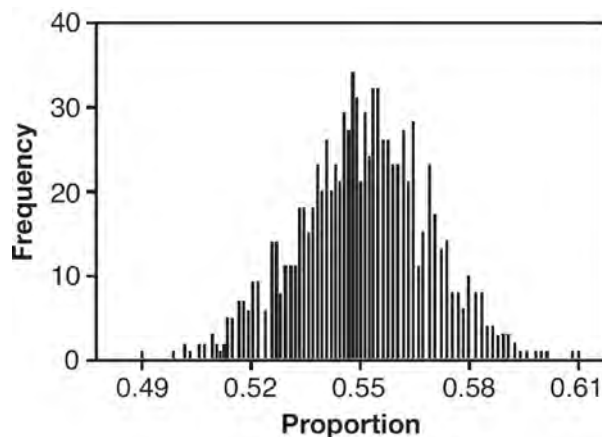
- 194 The focal length,  $F$ , of a camera's lens is related to the distance of the object from the lens,  $J$ , and the distance to the image area in the camera,  $W$ , by the formula below.

$$\frac{1}{J} + \frac{1}{W} = \frac{1}{F}$$

When this equation is solved for  $J$  in terms of  $F$  and  $W$ ,  $J$  equals

- 1)  $F - W$
- 2)  $\frac{FW}{F - W}$
- 3)  $\frac{FW}{W - F}$
- 4)  $\frac{1}{F} - \frac{1}{W}$

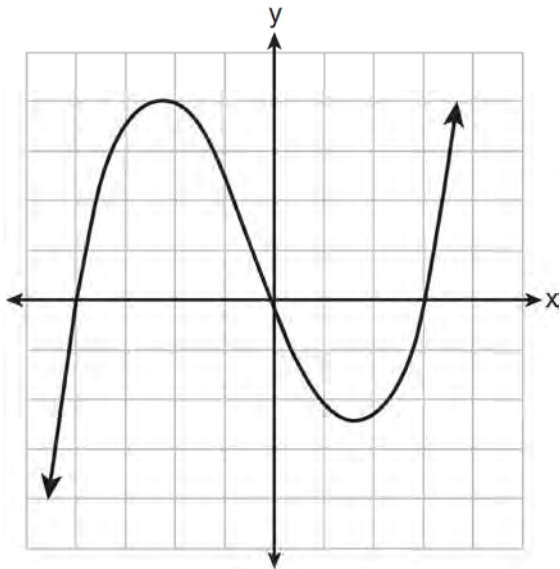
- 195 A candidate for political office commissioned a poll. His staff received responses from 900 likely voters and 55% of them said they would vote for the candidate. The staff then conducted a simulation of 1000 more polls of 900 voters, assuming that 55% of voters would vote for their candidate. The output of the simulation is shown in the diagram below.



Given this output, and assuming a 95% confidence level, the margin of error for the poll is closest to

- 1) 0.01
  - 2) 0.03
  - 3) 0.06
  - 4) 0.12
- 196 Pedro and Bobby each own an ant farm. Pedro starts with 100 ants and says his farm is growing exponentially at a rate of 15% per month. Bobby starts with 350 ants and says his farm is steadily decreasing by 5 ants per month. Assuming both boys are accurate in describing the population of their ant farms, after how many months will they both have approximately the same number of ants?
- 1) 7
  - 2) 8
  - 3) 13
  - 4) 36

197 The graph of  $p(x)$  is shown below.



What is the remainder when  $p(x)$  is divided by  $x + 4$ ?

- 1)  $x - 4$
- 2)  $-4$
- 3)  $0$
- 4)  $4$

198 The equation  $4x^2 - 24x + 4y^2 + 72y = 76$  is equivalent to

- 1)  $4(x - 3)^2 + 4(y + 9)^2 = 76$
- 2)  $4(x - 3)^2 + 4(y + 9)^2 = 121$
- 3)  $4(x - 3)^2 + 4(y + 9)^2 = 166$
- 4)  $4(x - 3)^2 + 4(y + 9)^2 = 436$

199 The completely factored form of  $2d^4 + 6d^3 - 18d^2 - 54d$  is

- 1)  $2d(d^2 - 9)(d + 3)$
- 2)  $2d(d^2 + 9)(d + 3)$
- 3)  $2d(d + 3)^2(d - 3)$
- 4)  $2d(d - 3)^2(d + 3)$

200 Relative to the graph of  $y = 3 \sin x$ , what is the shift of the graph of  $y = 3 \sin\left(x + \frac{\pi}{3}\right)$ ?

- 1)  $\frac{\pi}{3}$  right
- 2)  $\frac{\pi}{3}$  left
- 3)  $\frac{\pi}{3}$  up
- 4)  $\frac{\pi}{3}$  down

201 A circle centered at the origin has a radius of 10 units. The terminal side of an angle,  $\theta$ , intercepts the circle in Quadrant II at point  $C$ . The  $y$ -coordinate of point  $C$  is 8. What is the value of  $\cos \theta$ ?

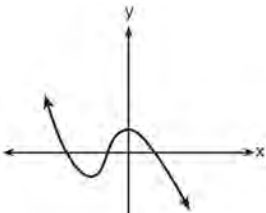
- 1)  $-\frac{3}{5}$
- 2)  $-\frac{3}{4}$
- 3)  $\frac{3}{5}$
- 4)  $\frac{4}{5}$

202 Given  $f^{-1}(x) = -\frac{3}{4}x + 2$ , which equation represents  $f(x)$ ?

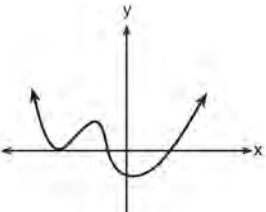
- 1)  $f(x) = \frac{4}{3}x - \frac{8}{3}$
- 2)  $f(x) = -\frac{4}{3}x + \frac{8}{3}$
- 3)  $f(x) = \frac{3}{4}x - 2$
- 4)  $f(x) = -\frac{3}{4}x + 2$

203 Which graph has the following characteristics?

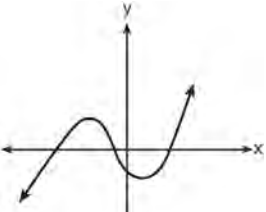
- three real zeros
- as  $x \rightarrow -\infty$ ,  $f(x) \rightarrow -\infty$
- as  $x \rightarrow \infty$ ,  $f(x) \rightarrow \infty$



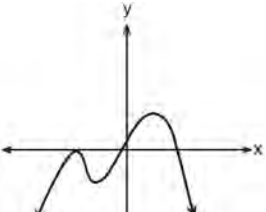
1)



2)



3)



4)

204 The solution set for the equation

$$\sqrt{x+14} - \sqrt{2x+5} = 1$$

- 1)  $\{-6\}$
- 2)  $\{2\}$
- 3)  $\{18\}$
- 4)  $\{2, 22\}$

205 The sequence  $a_1 = 6$ ,  $a_n = 3a_{n-1}$  can also be written as

- 1)  $a_n = 6 \cdot 3^n$
- 2)  $a_n = 6 \cdot 3^{n+1}$
- 3)  $a_n = 2 \cdot 3^n$
- 4)  $a_n = 2 \cdot 3^{n+1}$

206 If  $g(c) = 1 - c^2$  and  $m(c) = c + 1$ , then which statement is *not* true?

- 1)  $g(c) \cdot m(c) = 1 + c - c^2 - c^3$
- 2)  $g(c) + m(c) = 2 + c - c^2$
- 3)  $m(c) - g(c) = c + c^2$
- 4)  $\frac{m(c)}{g(c)} = \frac{-1}{1-c}$

207 A parabola has its focus at  $(1, 2)$  and its directrix is  $y = -2$ . The equation of this parabola could be

- 1)  $y = 8(x+1)^2$
- 2)  $y = \frac{1}{8}(x+1)^2$
- 3)  $y = 8(x-1)^2$
- 4)  $y = \frac{1}{8}(x-1)^2$

208 The distribution of the diameters of ball bearings made under a given manufacturing process is normally distributed with a mean of 4 cm and a standard deviation of 0.2 cm. What proportion of the ball bearings will have a diameter less than 3.7 cm?

- 1) 0.0668
- 2) 0.4332
- 3) 0.8664
- 4) 0.9500

209 What does  $\left(\frac{-54x^9}{y^4}\right)^{\frac{2}{3}}$  equal?

- 1)  $\frac{9ix^6\sqrt[3]{4}}{y\sqrt[3]{y^2}}$
- 2)  $\frac{9ix^6\sqrt[3]{4}}{y^2\sqrt[3]{y^2}}$
- 3)  $\frac{9x^6\sqrt[3]{4}}{y\sqrt[3]{y}}$
- 4)  $\frac{9x^6\sqrt[3]{4}}{y^2\sqrt[3]{y^2}}$

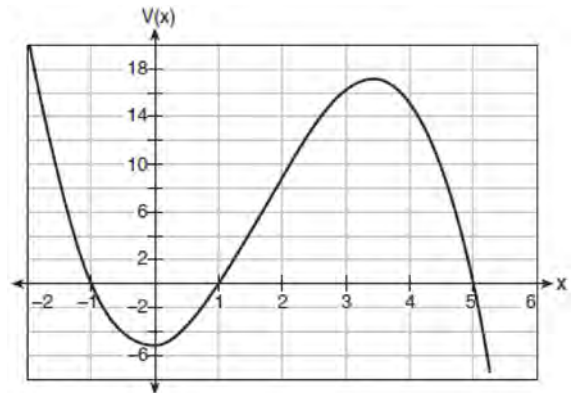
210 The heights of women in the United States are normally distributed with a mean of 64 inches and a standard deviation of 2.75 inches. The percent of women whose heights are between 64 and 69.5 inches, to the *nearest whole percent*, is

- 1) 6
- 2) 48
- 3) 68
- 4) 95

211 Cheap and Fast gas station is conducting a consumer satisfaction survey. Which method of collecting data would most likely lead to a biased sample?

- 1) interviewing every 5th customer to come into the station
- 2) interviewing customers chosen at random by a computer at the checkout
- 3) interviewing customers who call an 800 number posted on the customers' receipts
- 4) interviewing every customer who comes into the station on a day of the week chosen at random out of a hat

212 A cardboard box manufacturing company is building boxes with length represented by  $x + 1$ , width by  $5 - x$ , and height by  $x - 1$ . The volume of the box is modeled by the function below.



Over which interval is the volume of the box changing at the fastest average rate?

- 1) [1,2]
- 2) [1,3.5]
- 3) [1,5]
- 4) [0,3.5]

213 The roots of the equation  $x^2 + 2x + 5 = 0$  are

- 1) -3 and 1
- 2) -1, only
- 3)  $-1 + 2i$  and  $-1 - 2i$
- 4)  $-1 + 4i$  and  $-1 - 4i$

214 For  $x \neq 0$ , which expressions are equivalent to one divided by the sixth root of  $x$ ?

$$\text{I. } \frac{\sqrt[6]{x}}{\sqrt[3]{x}} \quad \text{II. } \frac{x^{\frac{1}{6}}}{x^{\frac{1}{3}}} \quad \text{III. } x^{-\frac{1}{6}}$$

- 1) I and II, only
- 2) I and III, only
- 3) II and III, only
- 4) I, II, and III

Algebra II Multiple Choice Regents Exam Questions

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- 215 Which equation represents a parabola with the focus at  $(0, -1)$  and the directrix of  $y = 1$ ?
- 1)  $x^2 = -8y$
  - 2)  $x^2 = -4y$
  - 3)  $x^2 = 8y$
  - 4)  $x^2 = 4y$
- 216 Which equation represents a parabola with a focus of  $(0, 4)$  and a directrix of  $y = 2$ ?
- 1)  $y = x^2 + 3$
  - 2)  $y = -x^2 + 1$
  - 3)  $y = \frac{x^2}{2} + 3$
  - 4)  $y = \frac{x^2}{4} + 3$
- 217 When  $b > 0$  and  $d$  is a positive integer, the expression  $(3b)^{\frac{2}{d}}$  is equivalent to
- 1)  $\frac{1}{\left(\sqrt[d]{3b}\right)^2}$
  - 2)  $\left(\sqrt{3b}\right)^d$
  - 3)  $\frac{1}{\sqrt{3b^d}}$
  - 4)  $\left(\sqrt[d]{3b}\right)^2$
- 218 The expression  $6xi^3(-4xi + 5)$  is equivalent to
- 1)  $2x - 5i$
  - 2)  $-24x^2 - 30xi$
  - 3)  $-24x^2 + 30x - i$
  - 4)  $26x - 24x^2i - 5i$
- 219 If  $\sin^2(32^\circ) + \cos^2(M) = 1$ , then  $M$  equals
- 1)  $32^\circ$
  - 2)  $58^\circ$
  - 3)  $68^\circ$
  - 4)  $72^\circ$
- 220 Which statement is *incorrect* for the graph of the function  $y = -3 \cos\left[\frac{\pi}{3}(x - 4)\right] + 7$ ?
- 1) The period is 6.
  - 2) The amplitude is 3.
  - 3) The range is  $[4, 10]$ .
  - 4) The midline is  $y = -4$ .
- 221 Julie averaged 85 on the first three tests of the semester in her mathematics class. If she scores 93 on each of the remaining tests, her average will be 90. Which equation could be used to determine how many tests,  $T$ , are left in the semester?
- 1)  $\frac{255 + 93T}{3T} = 90$
  - 2)  $\frac{255 + 90T}{3T} = 93$
  - 3)  $\frac{255 + 93T}{T + 3} = 90$
  - 4)  $\frac{255 + 90T}{T + 3} = 93$
- 222 The expression  $\frac{4x^3 + 5x + 10}{2x + 3}$  is equivalent to
- 1)  $2x^2 + 3x - 7 + \frac{31}{2x + 3}$
  - 2)  $2x^2 - 3x + 7 - \frac{11}{2x + 3}$
  - 3)  $2x^2 + 2.5x + 5 + \frac{15}{2x + 3}$
  - 4)  $2x^2 - 2.5x - 5 - \frac{20}{2x + 3}$

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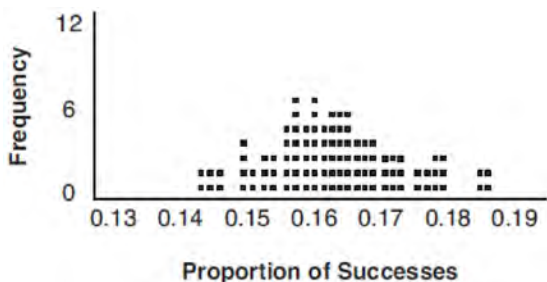
223 Joelle has a credit card that has a 19.2% annual interest rate compounded monthly. She owes a total balance of  $B$  dollars after  $m$  months. Assuming she makes no payments on her account, the table below illustrates the balance she owes after  $m$  months.

$m$	$B$
0	100.00
10	1172.00
19	1352.00
36	1770.80
60	2591.90
69	2990.00
72	3135.80
73	3186.00

Over which interval of time is her average rate of change for the balance on her credit card account the greatest?

- 1) month 10 to month 60
- 2) month 19 to month 69
- 3) month 36 to month 72
- 4) month 60 to month 73

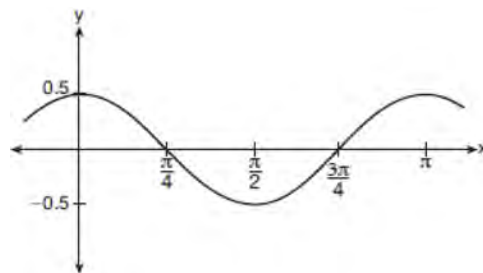
224 A study conducted in 2004 in New York City found that 212 out of 1334 participants had hypertension. Kim ran a simulation of 100 studies based on these data. The output of the simulation is shown in the diagram below.



At a 95% confidence level, the proportion of New York City residents with hypertension and the margin of error are closest to

- 1) proportion  $\approx .16$ ; margin of error  $\approx .01$
- 2) proportion  $\approx .16$ ; margin of error  $\approx .02$
- 3) proportion  $\approx .01$ ; margin of error  $\approx .16$
- 4) proportion  $\approx .02$ ; margin of error  $\approx .16$

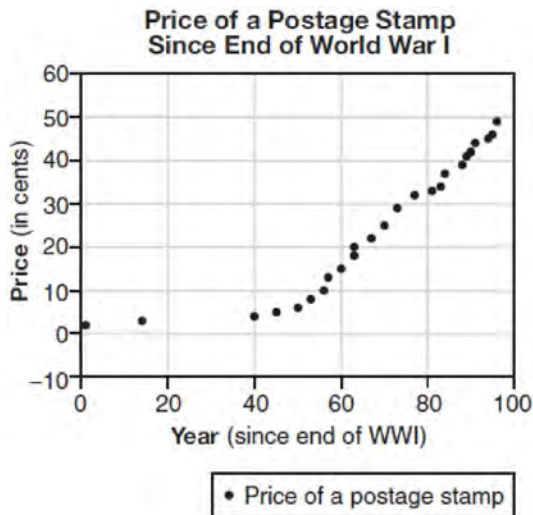
225 Which equation is represented by the graph shown below?



- 1)  $y = \frac{1}{2} \cos 2x$
- 2)  $y = \cos x$
- 3)  $y = \frac{1}{2} \cos x$
- 4)  $y = 2 \cos \frac{1}{2} x$



- 226 The price of a postage stamp in the years since the end of World War I is shown in the scatterplot below.



The equation that best models the price, in cents, of a postage stamp based on these data is

- 1)  $y = 0.59x - 14.82$
  - 2)  $y = 1.04(1.43)^x$
  - 3)  $y = 1.43(1.04)^x$
  - 4)  $y = 24 \sin(14x) + 25$
- 227 The Ferris wheel at the landmark Navy Pier in Chicago takes 7 minutes to make one full rotation. The height,  $H$ , in feet, above the ground of one of the six-person cars can be modeled by

$$H(t) = 70 \sin\left(\frac{2\pi}{7}(t - 1.75)\right) + 80, \text{ where } t \text{ is time,}$$

in minutes. Using  $H(t)$  for one full rotation, this car's minimum height, in feet, is

- 1) 150
- 2) 70
- 3) 10
- 4) 0

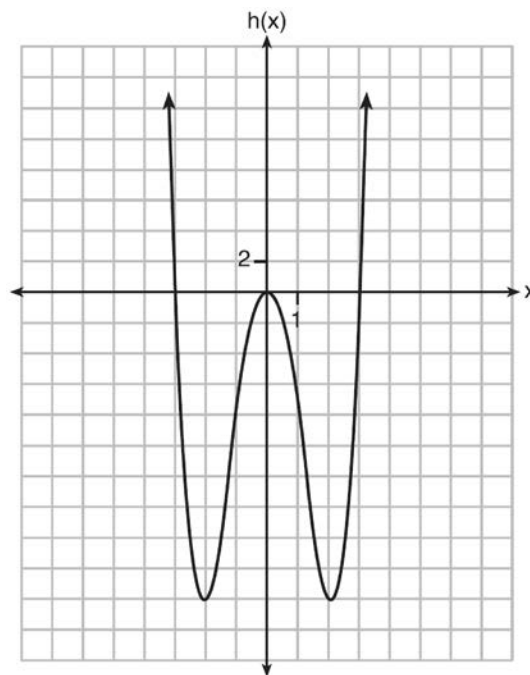
- 228 Which statement about statistical analysis is *false*?

- 1) Experiments can suggest patterns and relationships in data.
- 2) Experiments can determine cause and effect relationships.
- 3) Observational studies can determine cause and effect relationships.
- 4) Observational studies can suggest patterns and relationships in data.

- 229 Functions  $f$ ,  $g$ , and  $h$  are given below.

$$f(x) = \sin(2x)$$

$$g(x) = f(x) + 1$$



Which statement is true about functions  $f$ ,  $g$ , and  $h$ ?

- 1)  $f(x)$  and  $g(x)$  are odd,  $h(x)$  is even.
- 2)  $f(x)$  and  $g(x)$  are even,  $h(x)$  is odd.
- 3)  $f(x)$  is odd,  $g(x)$  is neither,  $h(x)$  is even.
- 4)  $f(x)$  is even,  $g(x)$  is neither,  $h(x)$  is odd.



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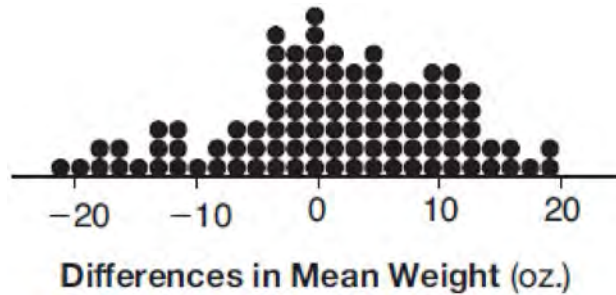
- 235 What is the solution, if any, of the equation  $\frac{2}{x+3} - \frac{3}{4-x} = \frac{2x-2}{x^2-x-12}$ ?
- 1)  $-1$
  - 2)  $-5$
  - 3) all real numbers
  - 4) no real solution
- 236 A public opinion poll was conducted on behalf of Mayor Ortega's reelection campaign shortly before the election. 264 out of 550 likely voters said they would vote for Mayor Ortega; the rest said they would vote for his opponent. Which statement is *least* appropriate to make, according to the results of the poll?
- 1) There is a 48% chance that Mayor Ortega will win the election.
  - 2) The point estimate ( $\hat{p}$ ) of voters who will vote for Mayor Ortega is 48%.
  - 3) It is most likely that between 44% and 52% of voters will vote for Mayor Ortega.
  - 4) Due to the margin of error, an inference cannot be made regarding whether Mayor Ortega or his opponent is most likely to win the election.
- 237 The probability that Gary and Jane have a child with blue eyes is 0.25, and the probability that they have a child with blond hair is 0.5. The probability that they have a child with both blue eyes and blond hair is 0.125. Given this information, the events blue eyes and blond hair are
- I: dependent
  - II: independent
  - III: mutually exclusive
- 1) I, only
  - 2) II, only
  - 3) I and III
  - 4) II and III
- 238 A student studying public policy created a model for the population of Detroit, where the population decreased 25% over a decade. He used the model  $P = 714(0.75)^d$ , where  $P$  is the population, in thousands,  $d$  decades after 2010. Another student, Suzanne, wants to use a model that would predict the population after  $y$  years. Suzanne's model is best represented by
- 1)  $P = 714(0.6500)^y$
  - 2)  $P = 714(0.8500)^y$
  - 3)  $P = 714(0.9716)^y$
  - 4)  $P = 714(0.9750)^y$
- 239 In 2010, the population of New York State was approximately 19,378,000 with an annual growth rate of 1.5%. Assuming the growth rate is maintained for a large number of years, which equation can be used to predict the population of New York State  $t$  years after 2010?
- 1)  $P_t = 19,378,000(1.5)^t$
  - 2)  $P_0 = 19,378,000$   
 $P_t = 19,378,000 + 1.015P_{t-1}$
  - 3)  $P_t = 19,378,000(1.015)^{t-1}$
  - 4)  $P_0 = 19,378,000$   
 $P_t = 1.015P_{t-1}$
- 240 Which value is *not* contained in the solution of the system shown below?
- $$a + 5b - c = -20$$
- $$4a - 5b + 4c = 19$$
- $$-a - 5b - 5c = 2$$
- 1)  $-2$
  - 2)  $2$
  - 3)  $3$
  - 4)  $-3$

Algebra II Multiple Choice Regents Exam Questions

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- 241 The solution set for the equation  $\sqrt{56-x} = x$  is
- 1)  $\{-8, 7\}$
  - 2)  $\{-7, 8\}$
  - 3)  $\{7\}$
  - 4)  $\{ \}$
- 242 A study of the annual population of the red-winged blackbird in Ft. Mill, South Carolina, shows the population,  $B(t)$ , can be represented by the function  $B(t) = 750(1.16)^t$ , where the  $t$  represents the number of years since the study began. In terms of the monthly rate of growth, the population of red-winged blackbirds can be best approximated by the function
- 1)  $B(t) = 750(1.012)^t$
  - 2)  $B(t) = 750(1.012)^{12t}$
  - 3)  $B(t) = 750(1.16)^{12t}$
  - 4)  $B(t) = 750(1.16)^{\frac{t}{12}}$
- 243 What is the inverse of the function  $y = \log_3 x$ ?
- 1)  $y = x^3$
  - 2)  $y = \log_x 3$
  - 3)  $y = 3^x$
  - 4)  $x = 3^y$
- 244 What is the solution to  $8(2^{x+3}) = 48$ ?
- 1)  $x = \frac{\ln 6}{\ln 2} - 3$
  - 2)  $x = 0$
  - 3)  $x = \frac{\ln 48}{\ln 16} - 3$
  - 4)  $x = \ln 4 - 3$
- 245 Which equation represents an odd function?
- 1)  $y = \sin x$
  - 2)  $y = \cos x$
  - 3)  $y = (x + 1)^3$
  - 4)  $y = e^{5x}$
- 246 Last year, the total revenue for Home Style, a national restaurant chain, increased 5.25% over the previous year. If this trend were to continue, which expression could the company's chief financial officer use to approximate their monthly percent increase in revenue? [Let  $m$  represent months.]
- 1)  $(1.0525)^m$
  - 2)  $(1.0525)^{\frac{12}{m}}$
  - 3)  $(1.00427)^m$
  - 4)  $(1.00427)^{\frac{m}{12}}$
- 247 Kristin wants to increase her running endurance. According to experts, a gradual mileage increase of 10% per week can reduce the risk of injury. If Kristin runs 8 miles in week one, which expression can help her find the total number of miles she will have run over the course of her 6-week training program?
- 1)  $\sum_{n=1}^6 8(1.10)^{n-1}$
  - 2)  $\sum_{n=1}^6 8(1.10)^n$
  - 3)  $\frac{8 - 8(1.10)^6}{0.90}$
  - 4)  $\frac{8 - 8(0.10)^n}{1.10}$

- 248 Gabriel performed an experiment to see if planting 13 tomato plants in black plastic mulch leads to larger tomatoes than if 13 plants are planted without mulch. He observed that the average weight of the tomatoes from tomato plants grown in black plastic mulch was 5 ounces greater than those from the plants planted without mulch. To determine if the observed difference is statistically significant, he rerandomized the tomato groups 100 times to study these random differences in the mean weights. The output of his simulation is summarized in the dotplot below.



Given these results, what is an appropriate inference that can be drawn?

- |   |   |
|---|---|
| <p>1) There was no effect observed between the two groups.</p> <p>2) There was an effect observed that could be due to the random assignment of plants to the groups.</p> | <p>3) There is strong evidence to support the hypothesis that tomatoes from plants planted in black plastic mulch are larger than those planted without mulch.</p> <p>4) There is strong evidence to support the hypothesis that tomatoes from plants planted without mulch are larger than those planted in black plastic mulch.</p> |
|---|---|
- 
- 249 Given  $f(9) = -2$ , which function can be used to generate the sequence  $-8, -7.25, -6.5, -5.75, \dots$ ?
- 1)  $f(n) = -8 + 0.75n$
  - 2)  $f(n) = -8 - 0.75(n - 1)$
  - 3)  $f(n) = -8.75 + 0.75n$
  - 4)  $f(n) = -0.75 + 8(n - 1)$
- 
- 250 To the *nearest tenth*, the value of  $x$  that satisfies  $2^x = -2x + 11$  is
- 1) 2.5
  - 2) 2.6
  - 3) 5.8
  - 4) 5.9
- 
- 251 The solution to the equation  $18x^2 - 24x + 87 = 0$  is
- 1)  $-\frac{2}{3} \pm 6i\sqrt{158}$
  - 2)  $-\frac{2}{3} \pm \frac{1}{6}i\sqrt{158}$
  - 3)  $\frac{2}{3} \pm 6i\sqrt{158}$
  - 4)  $\frac{2}{3} \pm \frac{1}{6}i\sqrt{158}$

Algebra II Multiple Choice Regents Exam Questions

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- 252 If  $f(x) = 3|x| - 1$  and  $g(x) = 0.03x^3 - x + 1$ , an approximate solution for the equation  $f(x) = g(x)$  is
- 1) 1.96
  - 2) 11.29
  - 3)  $(-0.99, 1.96)$
  - 4)  $(11.29, 32.87)$
- 253 The expression  $\frac{x^3 + 2x^2 + x + 6}{x + 2}$  is equivalent to
- 1)  $x^2 + 3$
  - 2)  $x^2 + 1 + \frac{4}{x + 2}$
  - 3)  $2x^2 + x + 6$
  - 4)  $2x^2 + 1 + \frac{4}{x + 2}$
- 254 The function  $f(x) = 2^{-0.25x} \cdot \sin\left(\frac{\pi}{2}x\right)$  represents a damped sound wave function. What is the average rate of change for this function on the interval  $[-7, 7]$ , to the nearest hundredth?
- 1) -3.66
  - 2) -0.30
  - 3) -0.26
  - 4) 3.36
- 255 In 2013, approximately 1.6 million students took the Critical Reading portion of the SAT exam. The mean score, the modal score, and the standard deviation were calculated to be 496, 430, and 115, respectively. Which interval reflects 95% of the Critical Reading scores?
- 1)  $430 \pm 115$
  - 2)  $430 \pm 230$
  - 3)  $496 \pm 115$
  - 4)  $496 \pm 230$
- 256 The lifespan of a 60-watt lightbulb produced by a company is normally distributed with a mean of 1450 hours and a standard deviation of 8.5 hours. If a 60-watt lightbulb produced by this company is selected at random, what is the probability that its lifespan will be between 1440 and 1465 hours?
- 1) 0.3803
  - 2) 0.4612
  - 3) 0.8415
  - 4) 0.9612
- 257 What is the solution set of the equation  $\frac{3x + 25}{x + 7} - 5 = \frac{3}{x}$ ?
- 1)  $\left\{\frac{3}{2}, 7\right\}$
  - 2)  $\left\{\frac{7}{2}, -3\right\}$
  - 3)  $\left\{-\frac{3}{2}, 7\right\}$
  - 4)  $\left\{-\frac{7}{2}, -3\right\}$
- 258 A ball is dropped from a height of 32 feet. It bounces and rebounds 80% of the height from which it was falling. What is the total downward distance, in feet, the ball traveled up to the 12th bounce?
- 1) 29
  - 2) 58
  - 3) 120
  - 4) 149

Algebra II Multiple Choice Regents Exam Questions

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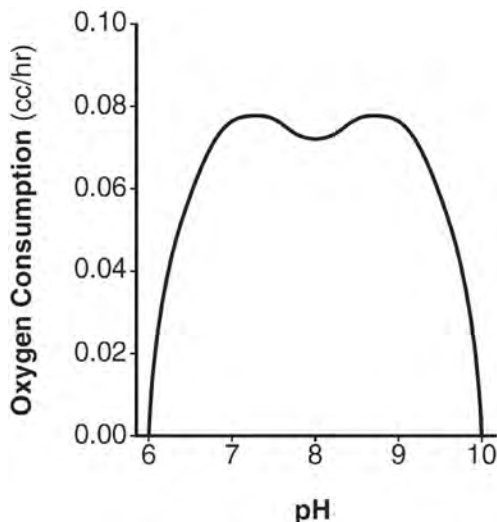
- 259 The loudness of sound is measured in units called decibels (dB). These units are measured by first assigning an intensity  $I_0$  to a very soft sound that is called the threshold sound. The sound to be measured is assigned an intensity,  $I$ , and the decibel rating,  $d$ , of this sound is found using  $d = 10 \log \frac{I}{I_0}$ . The threshold sound audible to the average person is  $1.0 \times 10^{-12}$  W/m<sup>2</sup> (watts per square meter). Consider the following sound level classifications:

Moderate	45-69 dB
Loud	70-89 dB
Very loud	90-109 dB
Deafening	>110 dB

How would a sound with intensity  $6.3 \times 10^{-3}$  W/m<sup>2</sup> be classified?

- 1) moderate  
2) loud  
3) very loud  
4) deafening
- 260 Given  $i$  is the imaginary unit,  $(2 - yi)^2$  in simplest form is
- 1)  $y^2 - 4yi + 4$   
2)  $-y^2 - 4yi + 4$   
3)  $-y^2 + 4$   
4)  $y^2 + 4$
- 261 The expression  $\frac{6x^3 + 17x^2 + 10x + 2}{2x + 3}$  equals
- 1)  $3x^2 + 4x - 1 + \frac{5}{2x + 3}$   
2)  $6x^2 + 8x - 2 + \frac{5}{2x + 3}$   
3)  $6x^2 - x + 13 - \frac{37}{2x + 3}$   
4)  $3x^2 + 13x + \frac{49}{2} + \frac{151}{2x + 3}$
- 262 Sally's high school is planning their spring musical. The revenue,  $R$ , generated can be determined by the function  $R(t) = -33t^2 + 360t$ , where  $t$  represents the price of a ticket. The production cost,  $C$ , of the musical is represented by the function  $C(t) = 700 + 5t$ . What is the highest ticket price, to the nearest dollar, they can charge in order to *not* lose money on the event?
- 1)  $t = 3$   
2)  $t = 5$   
3)  $t = 8$   
4)  $t = 11$
- 263 Which expression has been rewritten correctly to form a true statement?
- 1)  $(x + 2)^2 + 2(x + 2) - 8 = (x + 6)x$   
2)  $x^4 + 4x^2 + 9x^2y^2 - 36y^2 = (x + 3y)^2(x - 2)^2$   
3)  $x^3 + 3x^2 - 4xy^2 - 12y^2 = (x - 2y)(x + 3)^2$   
4)  $(x^2 - 4)^2 - 5(x^2 - 4) - 6 = (x^2 - 7)(x^2 - 6)$

- 264 There was a study done on oxygen consumption of snails as a function of pH, and the result was a degree 4 polynomial function whose graph is shown below.



Which statement about this function is *incorrect*?

- 1) The degree of the polynomial is even.
  - 2) There is a positive leading coefficient.
  - 3) At two pH values, there is a relative maximum value.
  - 4) There are two intervals where the function is decreasing.
- 265 When  $g(x)$  is divided by  $x + 4$ , the remainder is 0. Given  $g(x) = x^4 + 3x^3 - 6x^2 - 6x + 8$ , which conclusion about  $g(x)$  is true?
- 1)  $g(4) = 0$
  - 2)  $g(-4) = 0$
  - 3)  $x - 4$  is a factor of  $g(x)$ .
  - 4) No conclusion can be made regarding  $g(x)$ .

- 266 Factored completely,  $m^5 + m^3 - 6m$  is equivalent to
- 1)  $(m + 3)(m - 2)$
  - 2)  $(m^2 + 3m)(m^2 - 2)$
  - 3)  $m(m^4 + m^2 - 6)$
  - 4)  $m(m^2 + 3)(m^2 - 2)$

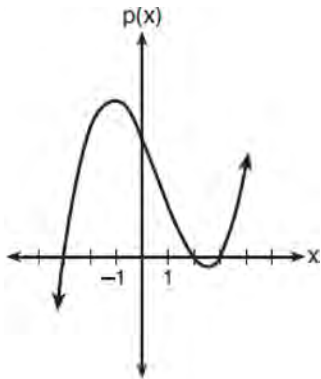
- 267 The eighth and tenth terms of a sequence are 64 and 100. If the sequence is either arithmetic or geometric, the ninth term can *not* be
- 1) -82
  - 2) -80
  - 3) 80
  - 4) 82

- 268 A manufacturing company has developed a cost model,  $C(x) = 0.15x^3 + 0.01x^2 + 2x + 120$ , where  $x$  is the number of items sold, in thousands. The sales price can be modeled by  $S(x) = 30 - 0.01x$ . Therefore, revenue is modeled by  $R(x) = x \cdot S(x)$ . The company's profit,  $P(x) = R(x) - C(x)$ , could be modeled by
- 1)  $0.15x^3 + 0.02x^2 - 28x + 120$
  - 2)  $-0.15x^3 - 0.02x^2 + 28x - 120$
  - 3)  $-0.15x^3 + 0.01x^2 - 2.01x - 120$
  - 4)  $-0.15x^3 + 32x + 120$

- 269 To solve  $\frac{2x}{x-2} - \frac{11}{x} = \frac{8}{x^2-2x}$ , Ren multiplied both sides by the least common denominator. Which statement is true?
- 1) 2 is an extraneous solution.
  - 2)  $\frac{7}{2}$  is an extraneous solution.
  - 3) 0 and 2 are extraneous solutions.
  - 4) This equation does not contain any extraneous solutions.



270 The graph of the function  $p(x)$  is sketched below.



Which equation could represent  $p(x)$ ?

- 1)  $p(x) = (x^2 - 9)(x - 2)$
- 2)  $p(x) = x^3 - 2x^2 + 9x + 18$
- 3)  $p(x) = (x^2 + 9)(x - 2)$
- 4)  $p(x) = x^3 + 2x^2 - 9x - 18$

271 The Rickerts decided to set up an account for their daughter to pay for her college education. The day their daughter was born, they deposited \$1000 in an account that pays 1.8% compounded annually. Beginning with her first birthday, they deposit an additional \$750 into the account on each of her birthdays. Which expression correctly represents the amount of money in the account  $n$  years after their daughter was born?

- 1)  $a_n = 1000(1.018)^n + 750$
- 2)  $a_n = 1000(1.018)^n + 750n$
- 3)  $a_0 = 1000$   
 $a_n = a_{n-1}(1.018) + 750$
- 4)  $a_0 = 1000$   
 $a_n = a_{n-1}(1.018) + 750n$

272 A sine function increasing through the origin can be used to model light waves. Violet light has a wavelength of 400 nanometers. Over which interval is the height of the wave *decreasing*, only?

- 1)  $(0, 200)$
- 2)  $(100, 300)$
- 3)  $(200, 400)$
- 4)  $(300, 400)$

273 As  $x$  increases from 0 to  $\frac{\pi}{2}$ , the graph of the equation  $y = 2 \tan x$  will

- 1) increase from 0 to 2
- 2) decrease from 0 to  $-2$
- 3) increase without limit
- 4) decrease without limit

274 The formula below can be used to model which scenario?

$$a_1 = 3000$$

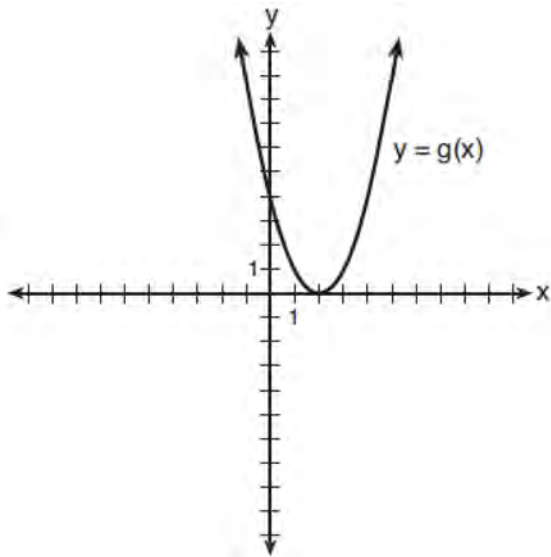
$$a_n = 0.80a_{n-1}$$

- 1) The first row of a stadium has 3000 seats, and each row thereafter has 80 more seats than the row in front of it.
- 2) The last row of a stadium has 3000 seats, and each row before it has 80 fewer seats than the row behind it.
- 3) A bank account starts with a deposit of \$3000, and each year it grows by 80%.
- 4) The initial value of a specialty toy is \$3000, and its value each of the following years is 20% less.

275 The inverse of the function  $f(x) = \frac{x+1}{x-2}$  is

- 1)  $f^{-1}(x) = \frac{x+1}{x+2}$
- 2)  $f^{-1}(x) = \frac{2x+1}{x-1}$
- 3)  $f^{-1}(x) = \frac{x+1}{x-2}$
- 4)  $f^{-1}(x) = \frac{x-1}{x+1}$

276 What is the solution to the system of equations  $y = 3x - 2$  and  $y = g(x)$  where  $g(x)$  is defined by the function below?



- 1)  $\{(0, -2)\}$
- 2)  $\{(0, -2), (1, 6)\}$
- 3)  $\{(1, 6)\}$
- 4)  $\{(1, 1), (6, 16)\}$

277 Which binomial is *not* a factor of the expression  $x^3 - 11x^2 + 16x + 84$ ?

- 1)  $x + 2$
- 2)  $x + 4$
- 3)  $x - 6$
- 4)  $x - 7$

278 Which expression is equivalent to  $\frac{4x^3 + 9x - 5}{2x - 1}$ ,

where  $x \neq \frac{1}{2}$ ?

- 1)  $2x^2 + x + 5$
- 2)  $2x^2 + \frac{11}{2} + \frac{1}{2(2x - 1)}$
- 3)  $2x^2 - x + 5$
- 4)  $2x^2 - x + 4 + \frac{1}{2x - 1}$

279 Which statement about the graph of  $c(x) = \log_6 x$  is *false*?

- 1) The asymptote has equation  $y = 0$ .
- 2) The graph has no  $y$ -intercept.
- 3) The domain is the set of positive reals.
- 4) The range is the set of all real numbers.

280 Which function represents exponential decay?

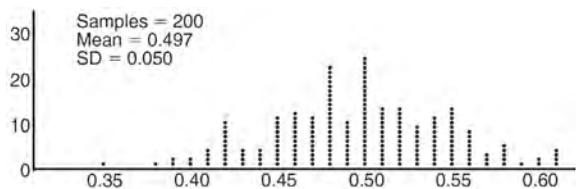
- 1)  $y = 2^{0.3t}$
- 2)  $y = 1.2^{3t}$
- 3)  $y = \left(\frac{1}{2}\right)^{-t}$
- 4)  $y = 5^{-t}$

Algebra II Multiple Choice Regents Exam Questions

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- 281 The solutions to the equation  $-\frac{1}{2}x^2 = -6x + 20$  are
- 1)  $-6 \pm 2i$
  - 2)  $-6 \pm 2\sqrt{19}$
  - 3)  $6 \pm 2i$
  - 4)  $6 \pm 2\sqrt{19}$
- 282 When  $g(x) = \frac{2}{x+2}$  and  $h(x) = \log(x+1) + 3$  are graphed on the same set of axes, which coordinates best approximate their point of intersection?
- 1)  $(-0.9, 1.8)$
  - 2)  $(-0.9, 1.9)$
  - 3)  $(1.4, 3.3)$
  - 4)  $(1.4, 3.4)$
- 283 The expression  $\frac{-3x^2 - 5x + 2}{x^3 + 2x^2}$  can be rewritten as
- 1)  $\frac{-3x-3}{x^2+2x}$
  - 2)  $\frac{-3x-1}{x^2}$
  - 3)  $-3x^{-1} + 1$
  - 4)  $-3x^{-1} + x^{-2}$
- 284 What is the completely factored form of  $k^4 - 4k^2 + 8k^3 - 32k + 12k^2 - 48$ ?
- 1)  $(k-2)(k-2)(k+3)(k+4)$
  - 2)  $(k-2)(k-2)(k+6)(k+2)$
  - 3)  $(k+2)(k-2)(k+3)(k+4)$
  - 4)  $(k+2)(k-2)(k+6)(k+2)$
- 285 The function  $f(x) = \frac{x-3}{x^2+2x-8}$  is undefined when  $x$  equals
- 1) 2 or  $-4$
  - 2) 4 or  $-2$
  - 3) 3, only
  - 4) 2, only
- 286 The population of Jamesburg for the years 2010-2013, respectively, was reported as follows: 250,000 250,937 251,878 252,822  
How can this sequence be recursively modeled?
- 1)  $j_n = 250,000(1.00375)^{n-1}$
  - 2)  $j_n = 250,000 + 937^{(n-1)}$
  - 3)  $j_1 = 250,000$   
 $j_n = 1.00375j_{n-1}$
  - 4)  $j_1 = 250,000$   
 $j_n = j_{n-1} + 937$
- 287 Iridium-192 is an isotope of iridium and has a half-life of 73.83 days. If a laboratory experiment begins with 100 grams of Iridium-192, the number of grams,  $A$ , of Iridium-192 present after  $t$  days would be  $A = 100\left(\frac{1}{2}\right)^{\frac{t}{73.83}}$ . Which equation approximates the amount of Iridium-192 present after  $t$  days?
- 1)  $A = 100\left(\frac{73.83}{2}\right)^t$
  - 2)  $A = 100\left(\frac{1}{147.66}\right)^t$
  - 3)  $A = 100(0.990656)^t$
  - 4)  $A = 100(0.116381)^t$

- 288 Anne has a coin. She does not know if it is a fair coin. She flipped the coin 100 times and obtained 73 heads and 27 tails. She ran a computer simulation of 200 samples of 100 fair coin flips. The output of the proportion of heads is shown below.



Given the results of her coin flips and of her computer simulation, which statement is most accurate?

- 1) 73 of the computer's next 100 coin flips will be heads.
  - 2) 50 of her next 100 coin flips will be heads.
  - 3) Her coin is not fair.
  - 4) Her coin is fair.
- 289 A polynomial equation of degree three,  $p(x)$ , is used to model the volume of a rectangular box. The graph of  $p(x)$  has  $x$  intercepts at  $-2$ ,  $10$ , and  $14$ . Which statements regarding  $p(x)$  could be true?
- A. The equation of  $p(x) = (x - 2)(x + 10)(x + 14)$ .
  - B. The equation of  $p(x) = -(x + 2)(x - 10)(x - 14)$ .
  - C. The maximum volume occurs when  $x = 10$ .
  - D. The maximum volume of the box is approximately 56.
- 1) A and C
  - 2) A and D
  - 3) B and C
  - 4) B and D

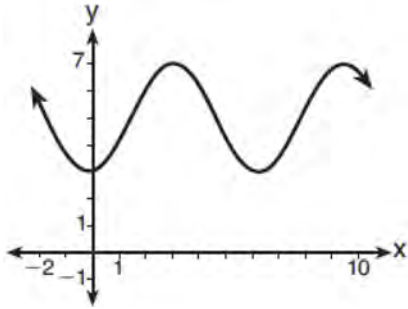
- 290 Which statement(s) about statistical studies is true?

- I. A survey of all English classes in a high school would be a good sample to determine the number of hours students throughout the school spend studying.
  - II. A survey of all ninth graders in a high school would be a good sample to determine the number of student parking spaces needed at that high school.
  - III. A survey of all students in one lunch period in a high school would be a good sample to determine the number of hours adults spend on social media websites.
  - IV. A survey of all Calculus students in a high school would be a good sample to determine the number of students throughout the school who don't like math.
- 1) I, only
  - 2) II, only
  - 3) I and III
  - 4) III and IV

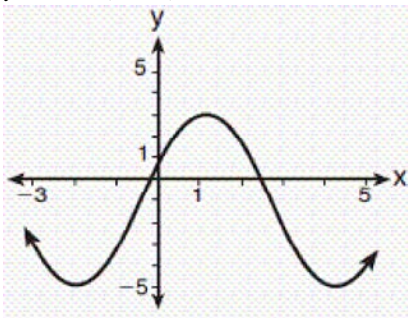
- 291 A recursive formula for the sequence  $18, 9, 4.5, \dots$  is

- 1)  $g_1 = 18$   
 $g_n = \frac{1}{2}g_{n-1}$
- 2)  $g_n = 18\left(\frac{1}{2}\right)^{n-1}$
- 3)  $g_1 = 18$   
 $g_n = 2g_{n-1}$
- 4)  $g_n = 18(2)^{n-1}$

292 Which sinusoid has the greatest amplitude?



- 1)
- 2)  $y = 3 \sin(\theta - 3) + 5$



- 3)
- 4)  $y = -5 \sin(\theta - 1) - 3$

293 The expression  $\left(\frac{m^2}{m^{\frac{1}{3}}}\right)^{-\frac{1}{2}}$  is equivalent to

- 1)  $-\sqrt[6]{m^5}$
- 2)  $\frac{1}{\sqrt[6]{m^5}}$
- 3)  $-m^5\sqrt{m}$
- 4)  $\frac{1}{m^5\sqrt{m}}$

294 Given the parent function  $p(x) = \cos x$ , which phrase best describes the transformation used to obtain the graph of  $g(x) = \cos(x + a) - b$ , if  $a$  and  $b$  are positive constants?

- 1) right  $a$  units, up  $b$  units
- 2) right  $a$  units, down  $b$  units
- 3) left  $a$  units, up  $b$  units
- 4) left  $a$  units, down  $b$  units

295 The value of a new car depreciates over time. Greg purchased a new car in June 2011. The value,  $V$ , of his car after  $t$  years can be modeled by the equation

$$\log_{0.8} \left( \frac{V}{17000} \right) = t.$$

What is the average decreasing rate of change per year of the value of the car from June 2012 to June 2014, to the nearest ten dollars per year?

- 1) 1960
- 2) 2180
- 3) 2450
- 4) 2770

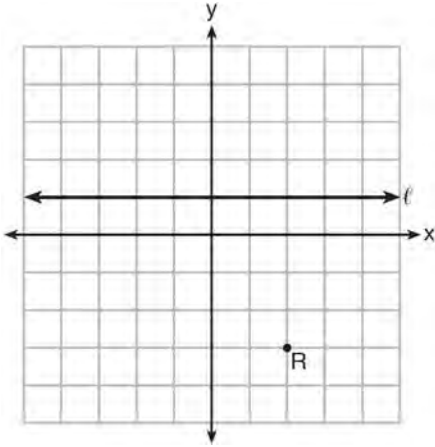
296 The function  $p(t) = 110e^{0.03922t}$  models the population of a city, in millions,  $t$  years after 2010. As of today, consider the following two statements:

- I. The current population is 110 million.
- II. The population increases continuously by approximately 3.9% per year.

This model supports

- 1) I, only
- 2) II, only
- 3) both I and II
- 4) neither I nor II

- 297 Which equation represents the set of points equidistant from line  $\ell$  and point  $R$  shown on the graph below?



- 1)  $y = -\frac{1}{8}(x+2)^2 + 1$
  - 2)  $y = -\frac{1}{8}(x+2)^2 - 1$
  - 3)  $y = -\frac{1}{8}(x-2)^2 + 1$
  - 4)  $y = -\frac{1}{8}(x-2)^2 - 1$
- 298 If the terminal side of angle  $\theta$ , in standard position, passes through point  $(-4, 3)$ , what is the numerical value of  $\sin \theta$ ?

- 1)  $\frac{3}{5}$
- 2)  $\frac{4}{5}$
- 3)  $-\frac{3}{5}$
- 4)  $-\frac{4}{5}$

**Algebra II 2 Point Regents Exam Questions**

299 The results of a poll of 200 students are shown in the table below:

	Preferred Music Style		
	Techno	Rap	Country
Female	54	25	27
Male	36	40	18

For this group of students, do these data suggest that gender and preferred music styles are independent of each other? Justify your answer.

300 An orange-juice processing plant receives a truckload of oranges. The quality control team randomly chooses three pails of oranges, each containing 50 oranges, from the truckload. Identify the sample and the population in the given scenario. State *one* conclusion that the quality control team could make about the population if 5% of the sample was found to be unsatisfactory.

301 A study was designed to test the effectiveness of a new drug. Half of the volunteers received the drug. The other half received a sugar pill. The probability of a volunteer receiving the drug and getting well was 40%. What is the probability of a volunteer getting well, given that the volunteer received the drug?

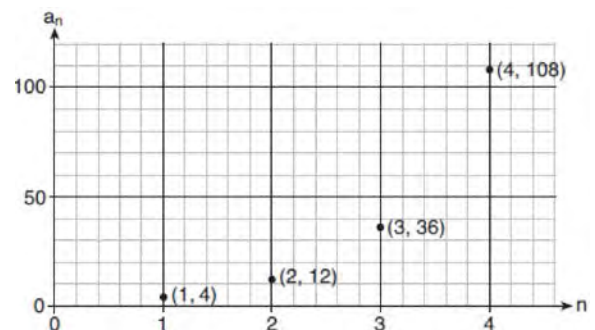
302 The volume of air in a person's lungs, as the person breathes in and out, can be modeled by a sine graph. A scientist is studying the differences in this volume for people at rest compared to people told to take a deep breath. When examining the graphs, should the scientist focus on the amplitude, period, or midline? Explain your choice.

303 Over the set of integers, factor the expression  $4x^3 - x^2 + 16x - 4$  completely.

304 Express  $(1 - i)^3$  in  $a + bi$  form.

305 Rewrite the expression  $(4x^2 + 5x)^2 - 5(4x^2 + 5x) - 6$  as a product of four linear factors.

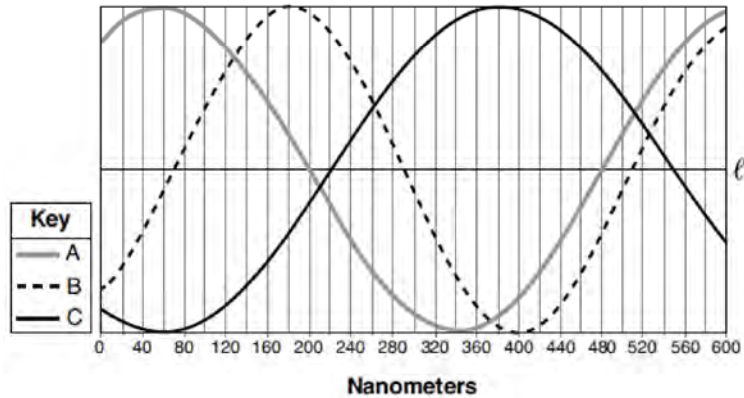
306 Write a recursive formula,  $a_n$ , to describe the sequence graphed below.



Algebra II 2 Point Regents Exam Questions

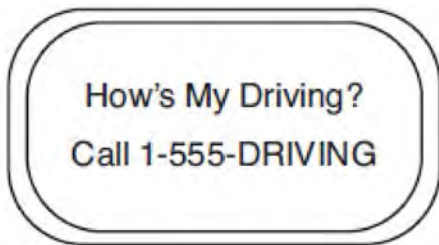
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- 307 Visible light can be represented by sinusoidal waves. Three visible light waves are shown in the graph below. The midline of each wave is labeled  $\ell$ .



Based on the graph, which light wave has the longest period? Justify your answer.

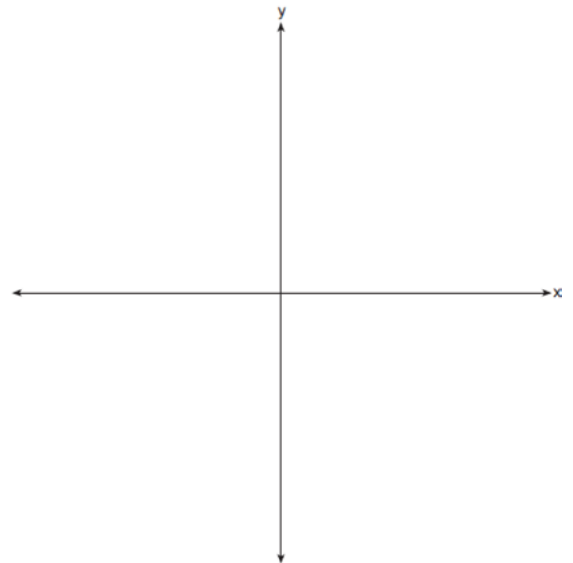
- 308 Chuck's Trucking Company has decided to initiate an Employee of the Month program. To determine the recipient, they put the following sign on the back of each truck.



The driver who receives the highest number of positive comments will win the recognition. Explain *one* statistical bias in this data collection method.

- 309 Given events  $A$  and  $B$ , such that  $P(A) = 0.6$ ,  $P(B) = 0.5$ , and  $P(A \cup B) = 0.8$ , determine whether  $A$  and  $B$  are independent or dependent.

- 310 Sketch the graphs of  $r(x) = \frac{1}{x}$  and  $a(x) = |x| - 3$  on the set of axes below. Determine, to the *nearest tenth*, the positive solution of  $r(x) = a(x)$ .

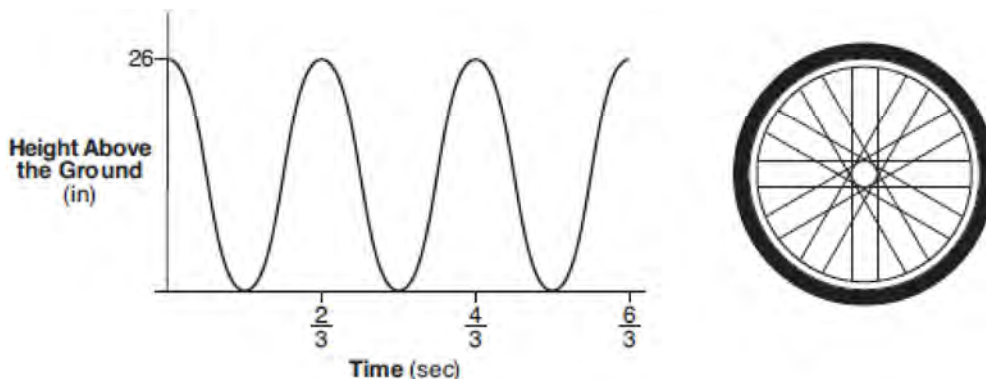




Algebra II 2 Point Regents Exam Questions

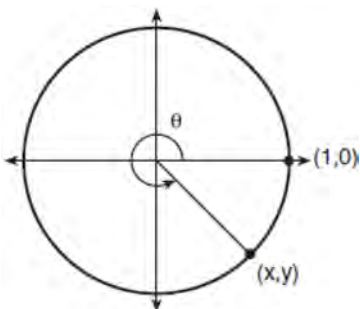
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- 311 The graph below represents the height above the ground,  $h$ , in inches, of a point on a triathlete's bike wheel during a training ride in terms of time,  $t$ , in seconds.



Identify the period of the graph and describe what the period represents in this context.

- 312 Using the unit circle below, explain why  $\csc \theta = \frac{1}{y}$ .



- 315 The probability that a resident of a housing community opposes spending money for community improvement on plumbing issues is 0.8. The probability that a resident favors spending money on improving walkways given that the resident opposes spending money on plumbing issues is 0.85. Determine the probability that a randomly selected resident opposes spending money on plumbing issues and favors spending money on walkways.

- 313 In New York State, the minimum wage has grown exponentially. In 1966, the minimum wage was \$1.25 an hour and in 2015, it was \$8.75. Algebraically determine the rate of growth to the nearest percent.

- 316 Algebraically prove that  $\frac{x^3 + 9}{x^3 + 8} = 1 + \frac{1}{x^3 + 8}$ , where  $x \neq -2$ .

- 314 Algebraically determine whether the function  $j(x) = x^4 - 3x^2 - 4$  is odd, even, or neither.

- 317 Given the equal terms  $\sqrt[3]{x^5}$  and  $y^{\frac{5}{6}}$ , determine and state  $y$ , in terms of  $x$ .

318 Data collected about jogging from students with two older siblings are shown in the table below.

	<b>Neither Sibling Jogs</b>	<b>One Sibling Jogs</b>	<b>Both Siblings Jog</b>
<b>Student Does Not Jog</b>	1168	1823	1380
<b>Student Jogs</b>	188	416	400

Using these data, determine whether a student with two older siblings is more likely to jog if one sibling jogs or if both siblings jog. Justify your answer.

319 Consider the function  $h(x) = 2\sin(3x) + 1$  and the function  $q$  represented in the table below.

$x$	$q(x)$
-2	-8
-1	0
0	0
1	-2
2	0

Determine which function has the *smaller* minimum value for the domain  $[-2, 2]$ . Justify your answer.

320 Explain how  $(-8)^{\frac{4}{3}}$  can be evaluated using properties of rational exponents to result in an integer answer.

323 Using the identity  $\sin^2 \theta + \cos^2 \theta = 1$ , find the value of  $\tan \theta$ , to the *nearest hundredth*, if  $\cos \theta$  is  $-0.7$  and  $\theta$  is in Quadrant II.

321 A house purchased 5 years ago for \$100,000 was just sold for \$135,000. Assuming exponential growth, approximate the annual growth rate, to the *nearest percent*.

324 Write a recursive formula for the sequence 6, 9, 13.5, 20.25, ...

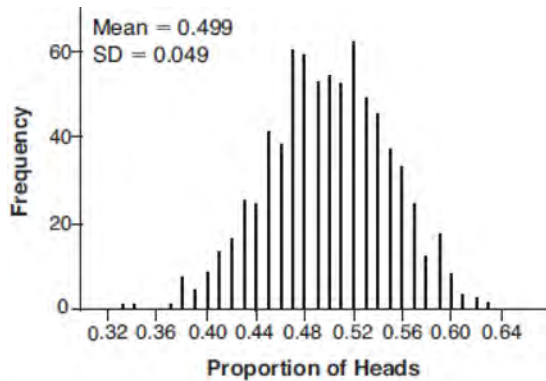
322 Over the set of integers, factor the expression  $x^4 - 4x^2 - 12$ .

325 The scores of a recent test taken by 1200 students had an approximately normal distribution with a mean of 225 and a standard deviation of 18. Determine the number of students who scored between 200 and 245.

Algebra II 2 Point Regents Exam Questions

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- 326 Robin flips a coin 100 times. It lands heads up 43 times, and she wonders if the coin is unfair. She runs a computer simulation of 750 samples of 100 fair coin flips. The output of the proportion of heads is shown below.



Do the results of the simulation provide strong evidence that Robin's coin is unfair? Explain your answer.

- 327 Solve algebraically for all values of  $x$ :

$$\sqrt{x-4} + x = 6$$

- 328 Researchers in a local area found that the population of rabbits with an initial population of 20 grew continuously at the rate of 5% per month. The fox population had an initial value of 30 and grew continuously at the rate of 3% per month. Find, to the *nearest tenth of a month*, how long it takes for these populations to be equal.

- 329 Determine the quotient and remainder when  $(6a^3 + 11a^2 - 4a - 9)$  is divided by  $(3a - 2)$ .

Express your answer in the form  $q(a) + \frac{r(a)}{d(a)}$ .

- 330 Write  $\sqrt[3]{x} \cdot \sqrt{x}$  as a single term with a rational exponent.

- 331 Algebraically prove that the difference of the squares of any two consecutive integers is an odd integer.

- 332 Elizabeth waited for 6 minutes at the drive thru at her favorite fast-food restaurant the last time she visited. She was upset about having to wait that long and notified the manager. The manager assured her that her experience was very unusual and that it would not happen again. A study of customers commissioned by this restaurant found an approximately normal distribution of results. The mean wait time was 226 seconds and the standard deviation was 38 seconds. Given these data, and using a 95% level of confidence, was Elizabeth's wait time unusual? Justify your answer.

- 333 Given  $\tan \theta = \frac{7}{24}$ , and  $\theta$  terminates in Quadrant III, determine the value of  $\cos \theta$ .

- 334 Determine for which polynomial(s)  $(x + 2)$  is a factor. Explain your answer.

$$P(x) = x^4 - 3x^3 - 16x - 12$$

$$Q(x) = x^3 - 3x^2 - 16x - 12$$

- 335 Algebraically solve for  $x$ :  $\frac{7}{2x} - \frac{2}{x+1} = \frac{1}{4}$

Algebra II 2 Point Regents Exam Questions

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- 336 The results of a survey of the student body at Central High School about television viewing preferences are shown below.

	Comedy Series	Drama Series	Reality Series	Total
Males	95	65	70	230
Females	80	70	110	260
Total	175	135	180	490

Are the events “student is a male” and “student prefers reality series” independent of each other? Justify your answer.

- 337 Use the properties of rational exponents to determine the value of  $y$  for the equation:

$$\frac{\sqrt[3]{x^8}}{(x^4)^{\frac{1}{3}}} = x^y, \quad x > 1$$

- 338 The Wells family is looking to purchase a home in a suburb of Rochester with a 30-year mortgage that has an annual interest rate of 3.6%. The house the family wants to purchase is \$152,500 and they will make a \$15,250 down payment and borrow the remainder. Use the formula below to determine their monthly payment, to the *nearest dollar*.

$$M = \frac{P\left(\frac{r}{12}\right)\left(1 + \frac{r}{12}\right)^n}{\left(1 + \frac{r}{12}\right)^n - 1}$$

$M$  = monthly payment

$P$  = amount borrowed

$r$  = annual interest rate

$n$  = total number of monthly payments

- 339 Describe how a controlled experiment can be created to examine the effect of ingredient  $X$  in a toothpaste.

- 340 Given:  $h(x) = \frac{2}{9}x^3 + \frac{8}{9}x^2 - \frac{16}{13}x + 2$

$$k(x) = -|0.7x| + 5$$

State the solutions to the equation  $h(x) = k(x)$ , rounded to the *nearest hundredth*.

- 341 Rowan is training to run in a race. He runs 15 miles in the first week, and each week following, he runs 3% more than the week before. Using a geometric series formula, find the total number of miles Rowan runs over the first ten weeks of training, rounded to the *nearest thousandth*.

- 342 Use an appropriate procedure to show that  $x - 4$  is a factor of the function  $f(x) = 2x^3 - 5x^2 - 11x - 4$ . Explain your answer.

- 343 Given the geometric series  $300 + 360 + 432 + 518.4 + \dots$ , write a geometric series formula,  $S_n$ , for the sum of the first  $n$  terms. Use the formula to find the sum of the first 10 terms, to the *nearest tenth*.

Algebra II 2 Point Regents Exam Questions

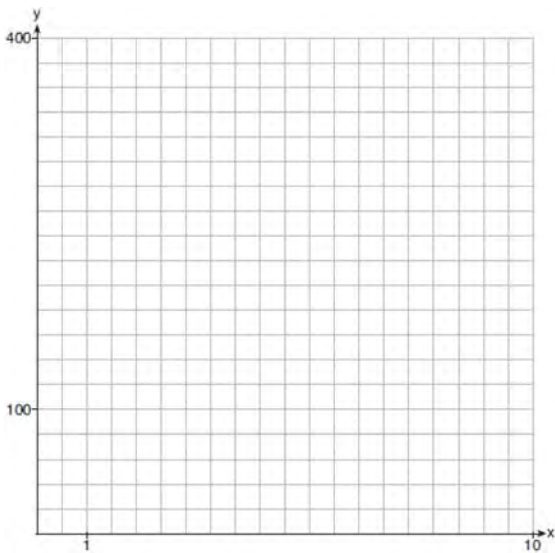
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344 The  $x$ -value of which function's  $x$ -intercept is larger,  $f$  or  $h$ ? Justify your answer.

$$f(x) = \log(x - 4)$$

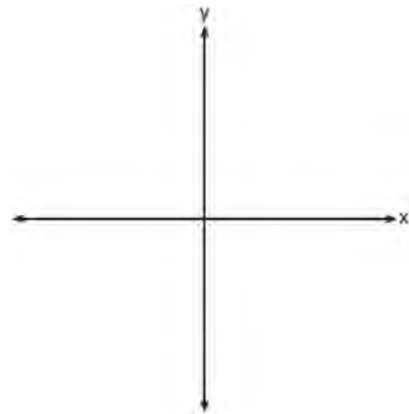
$x$	$h(x)$
-1	6
0	4
1	2
2	0
3	-2

345 Graph  $y = 400(.85)^{2x} - 6$  on the set of axes below.



347 Explain why  $81^{\frac{3}{4}}$  equals 27.

348 On the axes below, sketch a possible function  $p(x) = (x - a)(x - b)(x + c)$ , where  $a$ ,  $b$ , and  $c$  are positive,  $a > b$ , and  $p(x)$  has a positive  $y$ -intercept of  $d$ . Label all intercepts.



346 The recursive formula to describe a sequence is shown below.

$$a_1 = 3$$

$$a_n = 1 + 2a_{n-1}$$

State the first four terms of this sequence. Can this sequence be represented using an explicit geometric formula? Justify your answer.

349 Biologists are studying a new bacterium. They create a culture with 100 of the bacteria and anticipate that the number of bacteria will double every 30 hours. Write an equation for the number of bacteria,  $B$ , in terms of the number of hours,  $t$ , since the experiment began.

Algebra II 2 Point Regents Exam Questions

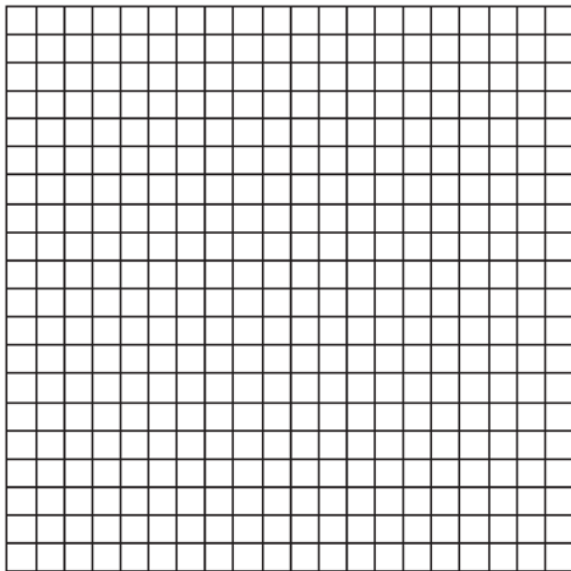
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350 A person's lung capacity can be modeled by the function  $C(t) = 250 \sin\left(\frac{2\pi}{5} t\right) + 2450$ , where  $C(t)$  represents the volume in mL present in the lungs after  $t$  seconds. State the maximum value of this function over one full cycle, and explain what this value represents.

351 Solve algebraically for all values of  $x$ :

$$\sqrt{x-5} + x = 7$$

352 The parabola  $y = -\frac{1}{20}(x-3)^2 + 6$  has its focus at  $(3, 1)$ . Determine and state the equation of the directrix. (The use of the grid below is optional.)

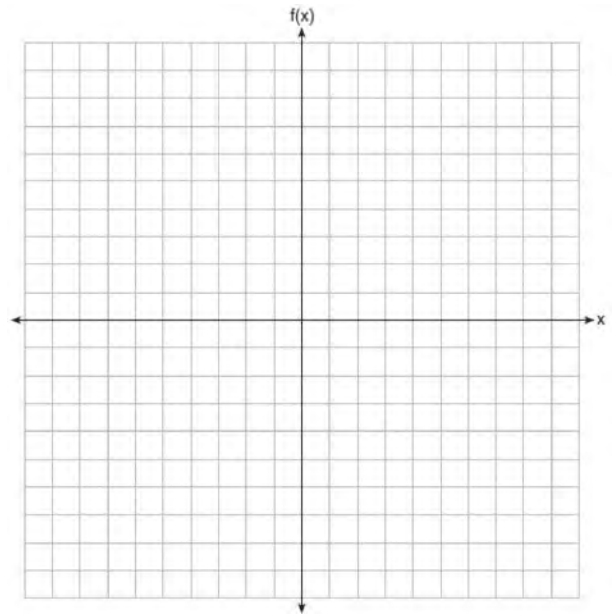


353 Algebraically determine the values of  $x$  that satisfy the system of equations below.

$$y = -2x + 1$$

$$y = -2x^2 + 3x + 1$$

354 Graph  $f(x) = \log_2(x + 6)$  on the set of axes below.



355 Erin and Christa were working on cubing binomials for math homework. Erin believed they could save time with a shortcut. She wrote down the rule below for Christa to follow.

$$(a + b)^3 = a^3 + b^3$$

Does Erin's shortcut always work? Justify your result algebraically.

356 On July 21, 2016, the water level in Puget Sound, WA reached a high of 10.1 ft at 6 a.m. and a low of  $-2$  ft at 12:30 p.m. Across the country in Long Island, NY, Shinnecock Bay's water level reached a high of 2.5 ft at 10:42 p.m. and a low of  $-0.1$  ft at 5:31 a.m. The water levels of both locations are affected by the tides and can be modeled by sinusoidal functions. Determine the difference in amplitudes, in feet, for these two locations.

357 The table below shows the number of hours of daylight on the first day of each month in Rochester, NY.

Month	Hours of Daylight
Jan.	9.4
Feb.	10.6
March	11.9
April	13.9
May	14.7
June	15.4
July	15.1
Aug.	13.9
Sept.	12.5
Oct.	11.1
Nov.	9.7
Dec.	9.0

Given the data, what is the average rate of change in hours of daylight per month from January 1st to April 1st? Interpret what this means in the context of the problem.

358 Explain what a rational exponent, such as  $\frac{5}{2}$  means.

Use this explanation to evaluate  $9^{\frac{5}{2}}$ .

361 For the function  $f(x) = (x - 3)^3 + 1$ , find  $f^{-1}(x)$ .

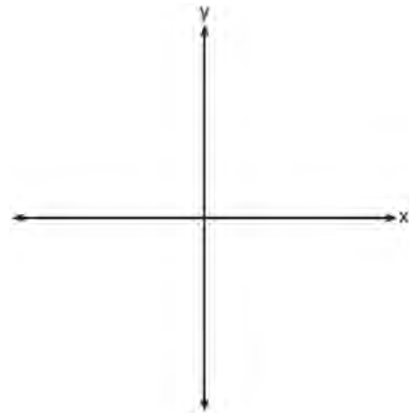
362 The zeros of a quartic polynomial function are 2, -2, 4, and -4. Use the zeros to construct a possible sketch of the function, on the set of axes below.

359 Solve the following system of equations algebraically.  $x^2 + y^2 = 400$

$$y = x - 28$$

360 Justify why  $\frac{\sqrt[3]{x^2 y^5}}{\sqrt[4]{x^3 y^4}}$  is equivalent to  $x^{-\frac{1}{12}} y^{\frac{2}{3}}$  using

properties of rational exponents, where  $x \neq 0$  and  $y \neq 0$ .



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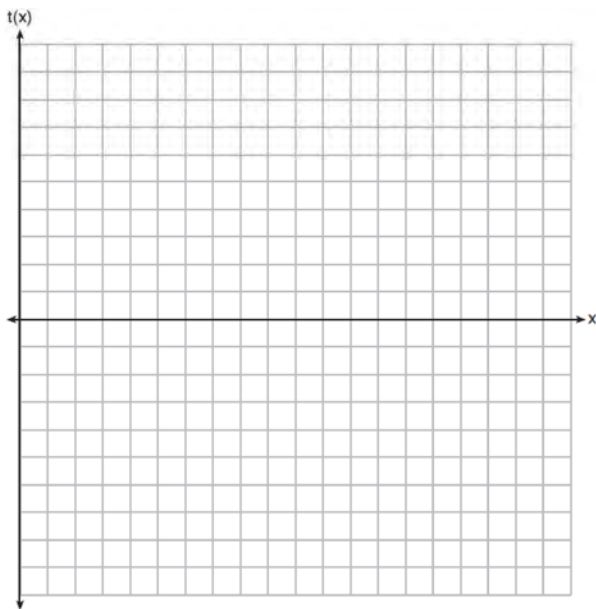
- 363 A runner is using a nine-week training app to prepare for a "fun run." The table below represents the amount of the program completed,  $A$ , and the distance covered in a session,  $D$ , in miles.

<b>A</b>	$\frac{4}{9}$	$\frac{5}{9}$	$\frac{6}{9}$	$\frac{8}{9}$	1
<b>D</b>	2	2	2.25	3	3.25

Based on these data, write an exponential regression equation, rounded to the *nearest thousandth*, to model the distance the runner is able to complete in a session as she continues through the nine-week program.

364 Algebraically solve for  $x$ :  $\frac{-3}{x+3} + \frac{1}{2} = \frac{x}{6} - \frac{1}{2}$

- 365 Graph  $t(x) = 3 \sin(2x) + 2$  over the domain  $[0, 2\pi]$  on the set of axes below.



- 366 Kenzie believes that for  $x \geq 0$ , the expression  $\left(\sqrt[7]{x^2}\right)\left(\sqrt[5]{x^3}\right)$  is equivalent to  $\sqrt[35]{x^6}$ . Is she correct? Justify your response algebraically.

- 367 The weight of a bag of pears at the local market averages 8 pounds with a standard deviation of 0.5 pound. The weights of all the bags of pears at the market closely follow a normal distribution. Determine what percentage of bags, to the *nearest integer*, weighed *less* than 8.25 pounds.

- 368 At Andrew Jackson High School, students are only allowed to enroll in AP U.S. History if they have already taken AP World History or AP European History. Out of 825 incoming seniors, 165 took AP World History, 66 took AP European History, and 33 took both. Given this information, determine the probability a randomly selected incoming senior is allowed to enroll in AP U.S. History.

- 369 Simplify  $xi(i - 7i)^2$ , where  $i$  is the imaginary unit.

- 370 A suburban high school has a population of 1376 students. The number of students who participate in sports is 649. The number of students who participate in music is 433. If the probability that a student participates in either sports or music is  $\frac{974}{1376}$ , what is the probability that a student participates in both sports and music?



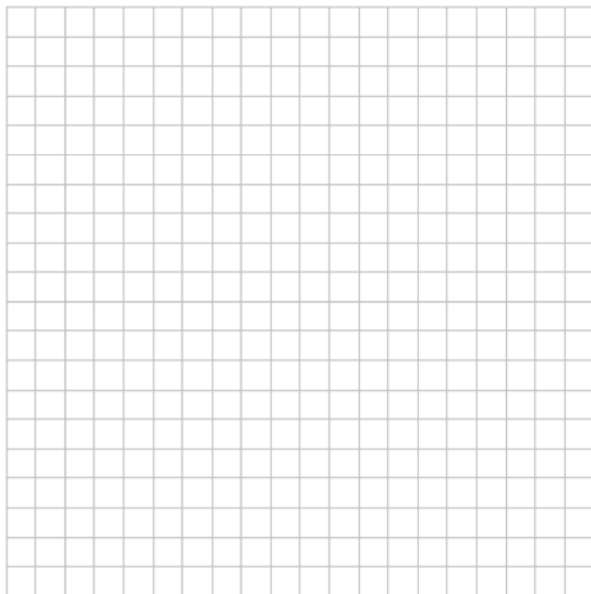
Algebra II 2 Point Regents Exam Questions

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371 Mrs. Jones had hundreds of jelly beans in a bag that contained equal numbers of six different flavors. Her student randomly selected four jelly beans and they were all black licorice. Her student complained and said "What are the odds I got all of that kind?" Mrs. Jones replied, "simulate rolling a die 250 times and tell me if four black licorice jelly beans is unusual." Explain how this simulation could be used to solve the problem.

372 Solve for  $x$ :  $\frac{1}{x} - \frac{1}{3} = -\frac{1}{3x}$

373 On the grid below, sketch a cubic polynomial whose zeros are 1, 3, and -2.



374 Point  $M\left(t, \frac{4}{7}\right)$  is located in the second quadrant on the unit circle. Determine the exact value of  $t$ .

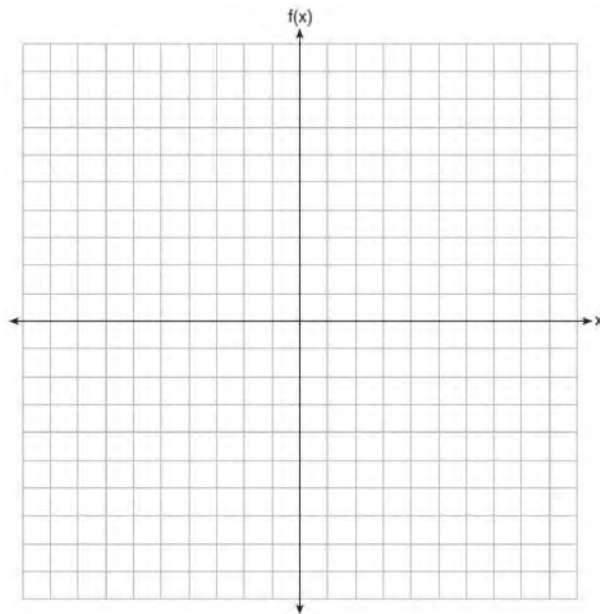
375 Given  $f(x) = 3x^2 + 7x - 20$  and  $g(x) = x - 2$ , state the quotient and remainder of  $\frac{f(x)}{g(x)}$ , in the form

$$q(x) + \frac{r(x)}{g(x)}.$$

376 Solve the equation  $2x^2 + 5x + 8 = 0$ . Express the answer in  $a + bi$  form.

377 Show why  $x - 3$  is a factor of  $m(x) = x^3 - x^2 - 5x - 3$ . Justify your answer.

378 On the grid below, graph the function  $f(x) = x^3 - 6x^2 + 9x + 6$  on the domain  $-1 \leq x \leq 4$ .



Algebra II 2 Point Regents Exam Questions

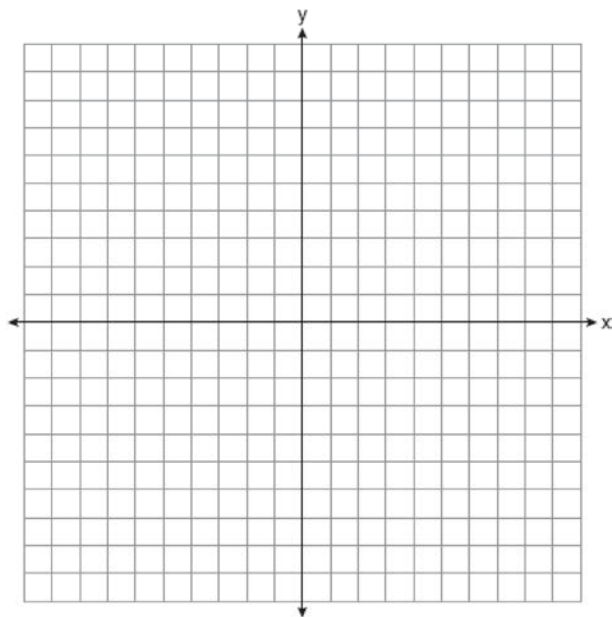
[www.jmap.org](http://www.jmap.org)

- 379 A survey about television-viewing preferences was given to randomly selected freshmen and seniors at Fairport High School. The results are shown in the table below.

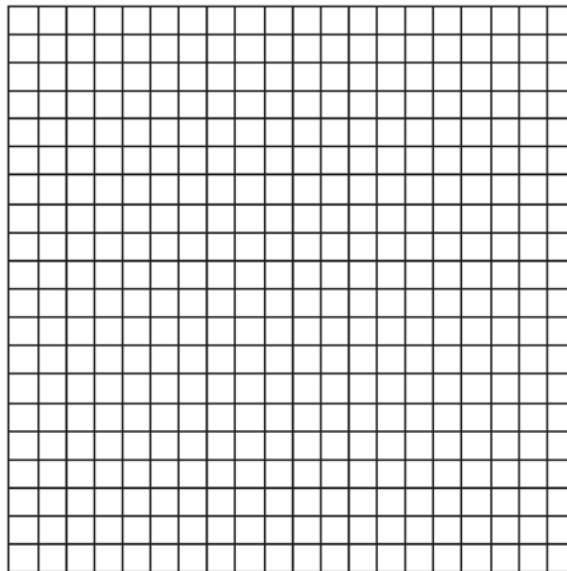
Favorite Type of Program			
	Sports	Reality Show	Comedy Series
Senior	83	110	67
Freshmen	119	103	54

A student response is selected at random from the results. State the *exact* probability the student response is from a freshman, given the student prefers to watch reality shows on television.

- 380 Graph  $y = x^3 - 4x^2 + 2x + 7$  on the set of axes below.



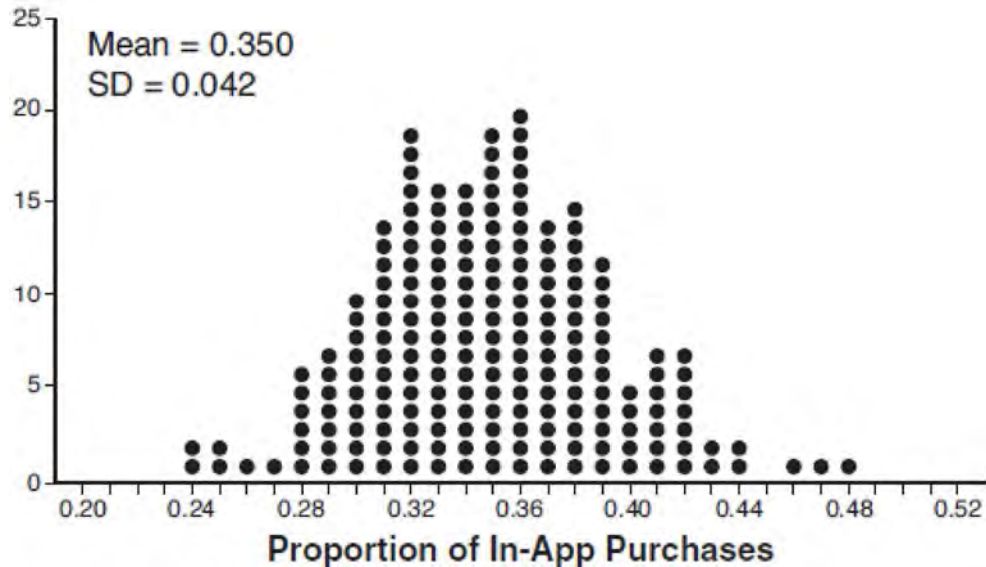
- 382 The zeros of a quartic polynomial function  $h$  are  $-1, \pm 2,$  and  $3$ . Sketch a graph of  $y = h(x)$  on the grid below.



- 381 When the function  $p(x)$  is divided by  $x - 1$  the quotient is  $x^2 + 7 + \frac{5}{x - 1}$ . State  $p(x)$  in standard form.

- 383 Describe the transformation applied to the graph of  $p(x) = 2^x$  that forms the new function  $q(x) = 2^{x-3} + 4$ .

- 384 Some smart-phone applications contain "in-app" purchases, which allow users to purchase special content within the application. A random sample of 140 users found that 35 percent made in-app purchases. A simulation was conducted with 200 samples of 140 users assuming 35 percent of the samples make in-app purchases. The approximately normal results are shown below.



Considering the middle 95% of the data, determine the margin of error, to the *nearest hundredth*, for the simulated results. In the given context, explain what this value represents.

- 385 The distance needed to stop a car after applying the brakes varies directly with the square of the car's speed. The table below shows stopping distances for various speeds.

<b>Speed (mph)</b>	10	20	30	40	50	60	70
<b>Distance (ft)</b>	6.25	25	56.25	100	156.25	225	306.25

Determine the average rate of change in braking distance, in ft/mph, between one car traveling at 50 mph and one traveling at 70 mph. Explain what this rate of change means as it relates to braking distance.

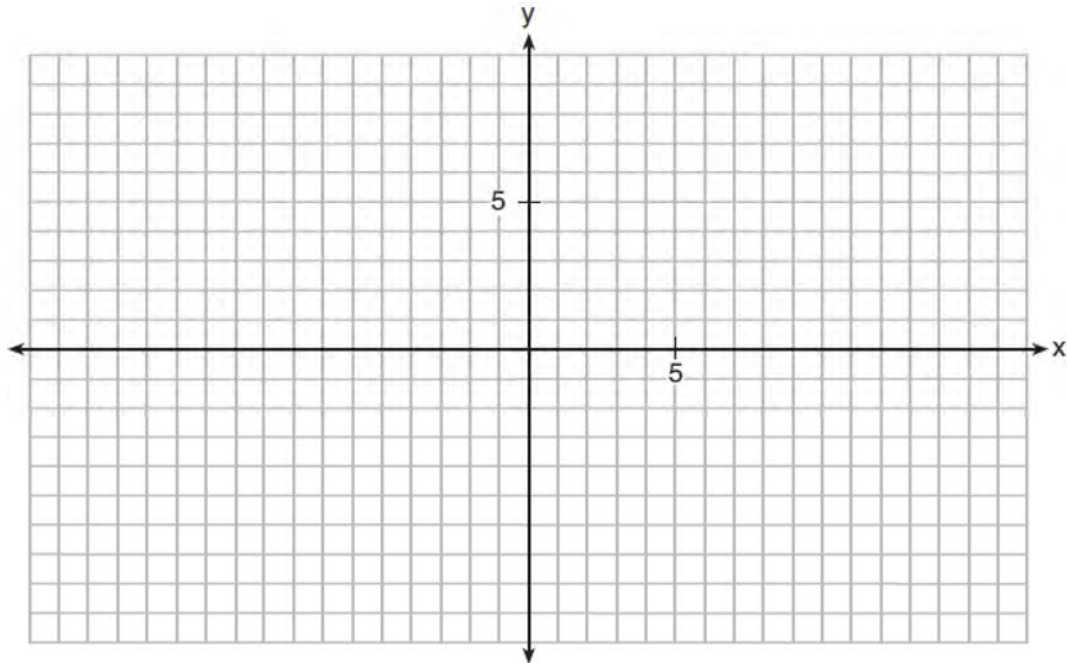
- 386 Express the fraction  $\frac{2x^{\frac{3}{2}}}{(16x^4)^{\frac{1}{4}}}$  in simplest radical form.

- 387 Completely factor the following expression:  
 $x^2 + 3xy + 3x^3 + y$

Algebra II 2 Point Regents Exam Questions

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388 On the grid below, graph the function  $y = \log_2(x - 3) + 1$



389 Determine if  $x - 5$  is a factor of  $2x^3 - 4x^2 - 7x - 10$ . Explain your answer.

390 An angle,  $\theta$ , is in standard position and its terminal side passes through the point  $(2, -1)$ . Find the *exact* value of  $\sin \theta$ .

391 Write  $-\frac{1}{2}i^3(\sqrt{-9} - 4) - 3i^2$  in simplest  $a + bi$  form.

392 The directrix of the parabola  $12(y + 3) = (x - 4)^2$  has the equation  $y = -6$ . Find the coordinates of the focus of the parabola.

393 Elizabeth tried to find the product of  $(2 + 4i)$  and  $(3 - i)$ , and her work is shown below.

$$\begin{aligned} & (2 + 4i)(3 - i) \\ &= 6 - 2i + 12i - 4i^2 \\ &= 6 + 10i - 4i^2 \\ &= 6 + 10i - 4(1) \\ &= 6 + 10i - 4 \\ &= 2 + 10i \end{aligned}$$

Identify the error in the process shown and determine the correct product of  $(2 + 4i)$  and  $(3 - i)$ .

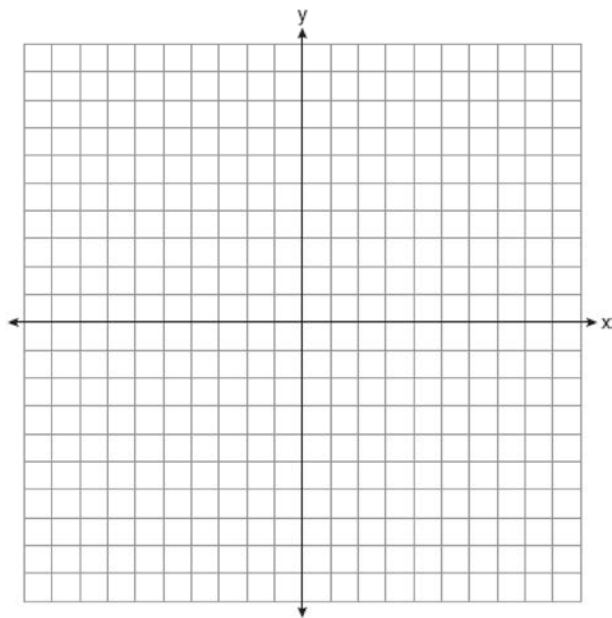
394 Write  $(5 + 2yi)(4 - 3i) - (5 - 2yi)(4 - 3i)$  in  $a + bi$  form, where  $y$  is a real number.

Algebra II 2 Point Regents Exam Questions

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395 Explain how  $\left(3\frac{1}{5}\right)^2$  can be written as the equivalent radical expression  $\sqrt[5]{9}$ .

396 On the axes below, graph *one* cycle of a cosine function with amplitude 3, period  $\frac{\pi}{2}$ , midline  $y = -1$ , and passing through the point  $(0, 2)$ .



397 For  $n$  and  $p > 0$ , is the expression

$$\left(p^2 n^{\frac{1}{2}}\right)^8 \sqrt{p^5 n^4} \text{ equivalent to } p^{18} n^6 \sqrt{p}?$$

Justify your answer.

398 Verify the following Pythagorean identity for all values of  $x$  and  $y$ :

$$(x^2 + y^2)^2 = (x^2 - y^2)^2 + (2xy)^2$$

399 While experimenting with her calculator, Candy creates the sequence 4, 9, 19, 39, 79, .... Write a recursive formula for Candy's sequence. Determine the eighth term in Candy's sequence.

400 The function  $M(t)$  represents the mass of radium over time,  $t$ , in years.

$$M(t) = 100e^{\frac{\left(\ln \frac{1}{2}\right)t}{1590}}$$

Determine if the function  $M(t)$  represents growth or decay. Explain your reasoning.

401 A formula for work problems involving two people is shown below.

$$\frac{1}{t_1} + \frac{1}{t_2} = \frac{1}{t_b}$$

$t_1$  = the time taken by the first person to complete the job

$t_2$  = the time taken by the second person to complete the job

$t_b$  = the time it takes for them working together to complete the job

Fred and Barney are carpenters who build the same model desk. It takes Fred eight hours to build the desk while it only takes Barney six hours. Write an equation that can be used to find the time it would take both carpenters working together to build a desk. Determine, to the *nearest tenth of an hour*, how long it would take Fred and Barney working together to build a desk.

## Algebra II 2 Point Regents Exam Questions

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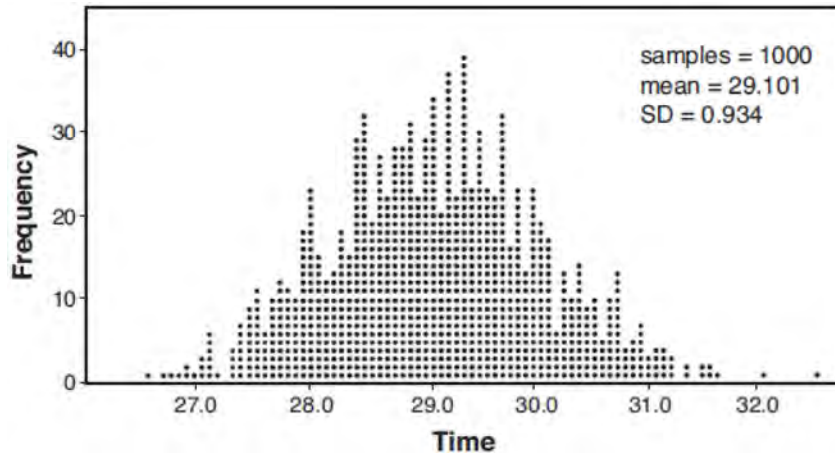
- 402 Given  $r(x) = x^3 - 4x^2 + 4x - 6$ , find the value of  $r(2)$ . What does your answer tell you about  $x - 2$  as a factor of  $r(x)$ ? Explain.
- 403 The average monthly high temperature in Buffalo, in degrees Fahrenheit, can be modeled by the function  $B(t) = 25.29 \sin(0.4895t - 1.9752) + 55.2877$ , where  $t$  is the month number (January = 1). State, to the *nearest tenth*, the average monthly rate of temperature change between August and November. Explain its meaning in the given context.
- 404 The world population was 2560 million people in 1950 and 3040 million in 1960 and can be modeled by the function  $p(t) = 2560e^{0.017185t}$ , where  $t$  is time in years after 1950 and  $p(t)$  is the population in millions. Determine the average rate of change of  $p(t)$  in millions of people per year, from  $4 \leq t \leq 8$ . Round your answer to the *nearest hundredth*.

**Algebra II 4 Point Regents Exam Questions**

- 405 A radio station claims to its advertisers that the mean number of minutes commuters listen to the station is 30. The station conducted a survey of 500 of their listeners who commute. The sample statistics are shown below.

$\bar{x}$	29.11
$s_x$	20.718

A simulation was run 1000 times based upon the results of the survey. The results of the simulation appear below.



Based on the simulation results, is the claim that commuters listen to the station on average 30 minutes plausible? Explain your response including an interval containing the middle 95% of the data, rounded to the *nearest hundredth*.

- 406 Jim is looking to buy a vacation home for \$172,600 near his favorite southern beach. The formula to compute a mortgage payment,  $M$ , is

$$M = P \cdot \frac{r(1+r)^N}{(1+r)^N - 1}$$

where  $P$  is the principal

amount of the loan,  $r$  is the monthly interest rate, and  $N$  is the number of monthly payments. Jim's bank offers a monthly interest rate of 0.305% for a 15-year mortgage. With no down payment, determine Jim's mortgage payment, rounded to the *nearest dollar*. Algebraically determine and state the down payment, rounded to the *nearest dollar*, that Jim needs to make in order for his mortgage payment to be \$1100.

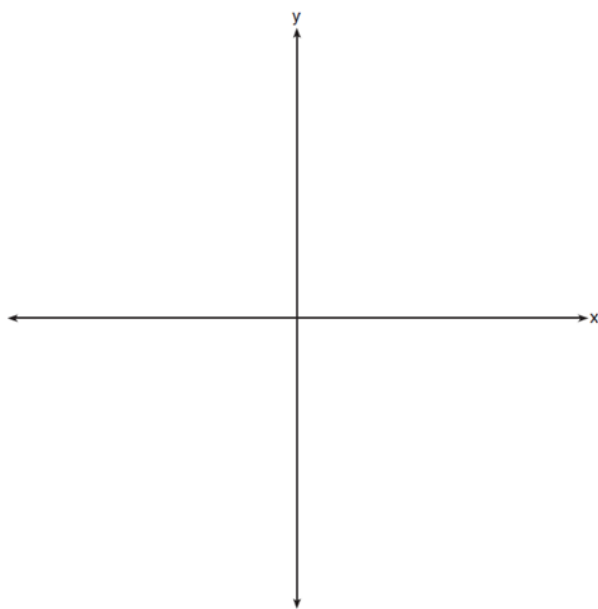
- 407 Carla wants to start a college fund for her daughter Lila. She puts \$63,000 into an account that grows at a rate of 2.55% per year, compounded monthly. Write a function,  $C(t)$ , that represents the amount of money in the account  $t$  years after the account is opened, given that no more money is deposited into or withdrawn from the account. Calculate algebraically the number of years it will take for the account to reach \$100,000, to the *nearest hundredth of a year*.

Algebra II 4 Point Regents Exam Questions

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408 Two versions of a standardized test are given, an April version and a May version. The statistics for the April version show a mean score of 480 and a standard deviation of 24. The statistics for the May version show a mean score of 510 and a standard deviation of 20. Assume the scores are normally distributed. Joanne took the April version and scored in the interval 510-540. What is the probability, to the *nearest ten thousandth*, that a test paper selected at random from the April version scored in the same interval? Maria took the May version. In what interval must Maria score to claim she scored as well as Joanne?

409 a) On the axes below, sketch *at least one* cycle of a sine curve with an amplitude of 2, a midline at  $y = -\frac{3}{2}$ , and a period of  $2\pi$ .



b) Explain any differences between a sketch of  $y = 2 \sin\left(x - \frac{\pi}{3}\right) - \frac{3}{2}$  and the sketch from part a.

410 After sitting out of the refrigerator for a while, a turkey at room temperature ( $68^\circ\text{F}$ ) is placed into an oven at 8 a.m., when the oven temperature is  $325^\circ\text{F}$ . Newton's Law of Heating explains that the temperature of the turkey will increase proportionally to the difference between the temperature of the turkey and the temperature of the oven, as given by the formula below:

$$T = T_a + (T_0 - T_a)e^{-kt}$$

$T_a$  = the temperature surrounding the object

$T_0$  = the initial temperature of the object

$t$  = the time in hours

$T$  = the temperature of the object after  $t$  hours

$k$  = decay constant

The turkey reaches the temperature of approximately  $100^\circ\text{F}$  after 2 hours. Find the value of  $k$ , to the *nearest thousandth*, and write an equation to determine the temperature of the turkey after  $t$  hours. Determine the Fahrenheit temperature of the turkey, to the *nearest degree*, at 3 p.m.

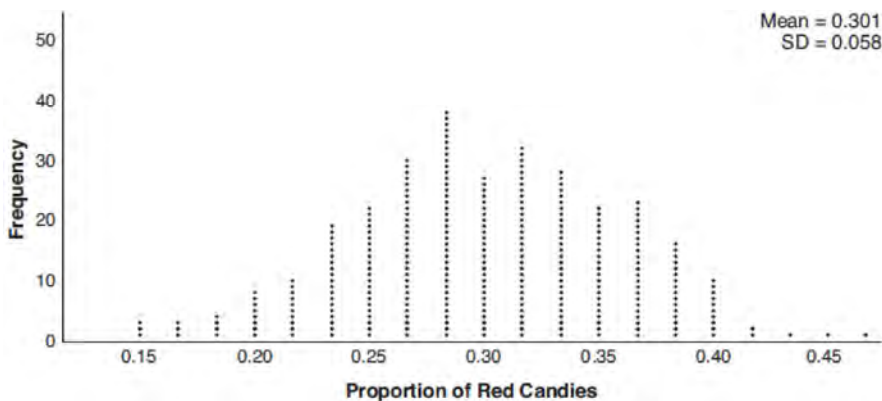
411 A student is chosen at random from the student body at a given high school. The probability that the student selects Math as the favorite subject is  $\frac{1}{4}$ . The probability that the student chosen is a junior is  $\frac{116}{459}$ . If the probability that the student selected is a junior or that the student chooses Math as the favorite subject is  $\frac{47}{108}$ , what is the exact probability that the student selected is a junior whose favorite subject is Math? Are the events "the student is a junior" and "the student's favorite subject is Math" independent of each other? Explain your answer.



Algebra II 4 Point Regents Exam Questions

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- 412 Mary bought a pack of candy. The manufacturer claims that 30% of the candies manufactured are red. In her pack, 14 of the 60 candies are red. She ran a simulation of 300 samples, assuming the manufacturer is correct. The results are shown below.



Based on the simulation, determine the middle 95% of plausible values that the proportion of red candies in a pack is within. Based on the simulation, is it unusual that Mary’s pack had 14 red candies out of a total of 60? Explain.

- 413 Using the formula below, determine the monthly payment on a 5-year car loan with a monthly percentage rate of 0.625% for a car with an original cost of \$21,000 and a \$1000 down payment, to the nearest cent.

$$P_n = PMT \left( \frac{1 - (1 + i)^{-n}}{i} \right)$$

$P_n$  = present amount borrowed

$n$  = number of monthly pay periods

$PMT$  = monthly payment

$i$  = interest rate per month

The affordable monthly payment is \$300 for the same time period. Determine an appropriate down payment, to the nearest dollar.

- 414 Solve the following system of equations algebraically for all values of  $x$ ,  $y$ , and  $z$ :

$$x + y + z = 1$$

$$2x + 4y + 6z = 2$$

$$-x + 3y - 5z = 11$$

- 415 Sonja is cutting wire to construct a mobile. She cuts 100 inches for the first piece, 80 inches for the second piece, and 64 inches for the third piece. Assuming this pattern continues, write an explicit equation for  $a_n$ , the length in inches of the  $n$ th piece. Sonja only has 40 feet of wire to use for the project and wants to cut 20 pieces total for the mobile using her pattern. Will she have enough wire? Justify your answer.

Algebra II 4 Point Regents Exam Questions

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- 416 Juan and Filipe practice at the driving range before playing golf. The number of wins and corresponding practice times for each player are shown in the table below.

	Juan Wins	Felipe Wins
Short Practice Time	8	10
Long Practice Time	15	12

Given that the practice time was long, determine the exact probability that Filipe wins the next match. Determine whether or not the two events “Filipe wins” and “long practice time” are independent. Justify your answer.

- 417 The half-life of a radioactive substance is 15 years. Write an equation that can be used to determine the amount,  $s(t)$ , of 200 grams of this substance that remains after  $t$  years. Determine algebraically, to the *nearest year*, how long it will take for  $\frac{1}{10}$  of this substance to remain.

- 420 Solve the following system of equations algebraically for all values of  $x$ ,  $y$ , and  $z$ :

$$x + 3y + 5z = 45$$

$$6x - 3y + 2z = -10$$

$$-2x + 3y + 8z = 72$$

- 418 One of the medical uses of Iodine-131 (I-131), a radioactive isotope of iodine, is to enhance x-ray images. The half-life of I-131 is approximately 8.02 days. A patient is injected with 20 milligrams of I-131. Determine, to the *nearest day*, the amount of time needed before the amount of I-131 in the patient’s body is approximately 7 milligrams.

- 421 Monthly mortgage payments can be found using the formula below:

$$M = \frac{P\left(\frac{r}{12}\right)\left(1 + \frac{r}{12}\right)^n}{\left(1 + \frac{r}{12}\right)^n - 1}$$

$M$  = monthly payment

$P$  = amount borrowed

$r$  = annual interest rate

$n$  = number of monthly payments

- 419 Write an explicit formula for  $a_n$ , the  $n$ th term of the recursively defined sequence below.

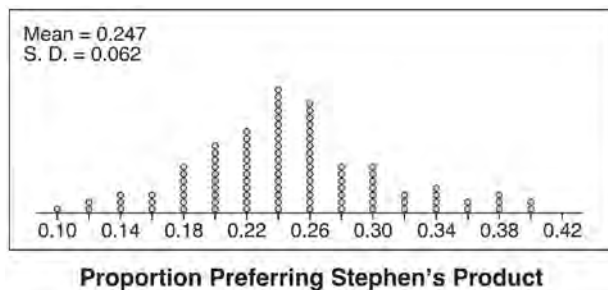
$$a_1 = x + 1$$

$$a_n = x(a_{n-1})$$

For what values of  $x$  would  $a_n = 0$  when  $n > 1$ ?

The Banks family would like to borrow \$120,000 to purchase a home. They qualified for an annual interest rate of 4.8%. Algebraically determine the *fewest* number of whole years the Banks family would need to include in the mortgage agreement in order to have a monthly payment of no more than \$720.

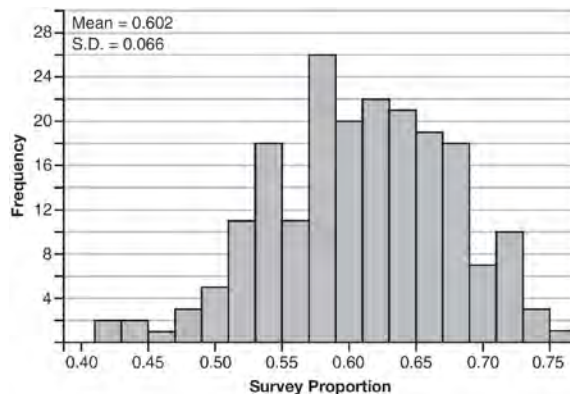
- 422 Stephen's Beverage Company is considering whether to produce a new brand of cola. The company will launch the product if at least 25% of cola drinkers will buy the product. Fifty cola drinkers are randomly selected to take a blind taste-test of products  $A$ ,  $B$ , and the new product. Nine out of fifty participants preferred Stephen's new cola to products  $A$  and  $B$ . The company then devised a simulation based on the requirement that 25% of cola drinkers will buy the product. Each dot in the graph shown below represents the proportion of people who preferred Stephen's new product, each of sample size 50, simulated 100 times.



Assume the set of data is approximately normal and the company wants to be 95% confident of its results. Does the sample proportion obtained from the blind taste-test, nine out of fifty, fall within the margin of error developed from the simulation? Justify your answer. The company decides to continue developing the product even though only nine out of fifty participants preferred its brand of cola in the taste-test. Describe how the simulation data could be used to support this decision.

- 423 A population of 950 bacteria grows continuously at a rate of 4.75% per day. Write an exponential function,  $N(t)$ , that represents the bacterial population after  $t$  days and explain the reason for your choice of base. Determine the bacterial population after 36 hours, to the *nearest bacterium*.

- 424 Given  $z(x) = 6x^3 + bx^2 - 52x + 15$ ,  $z(2) = 35$ , and  $z(-5) = 0$ , algebraically determine all the zeros of  $z(x)$ .
- 425 Fifty-five students attending the prom were randomly selected to participate in a survey about the music choice at the prom. Sixty percent responded that a DJ would be preferred over a band. Members of the prom committee thought that the vote would have 50% for the DJ and 50% for the band. A simulation was run 200 times, each of sample size 55, based on the premise that 60% of the students would prefer a DJ. The approximate normal simulation results are shown below.



Using the results of the simulation, determine a plausible interval containing the middle 95% of the data. Round all values to the *nearest hundredth*. Members of the prom committee are concerned that a vote of all students attending the prom may produce a 50% – 50% split. Explain what statistical evidence supports this concern.

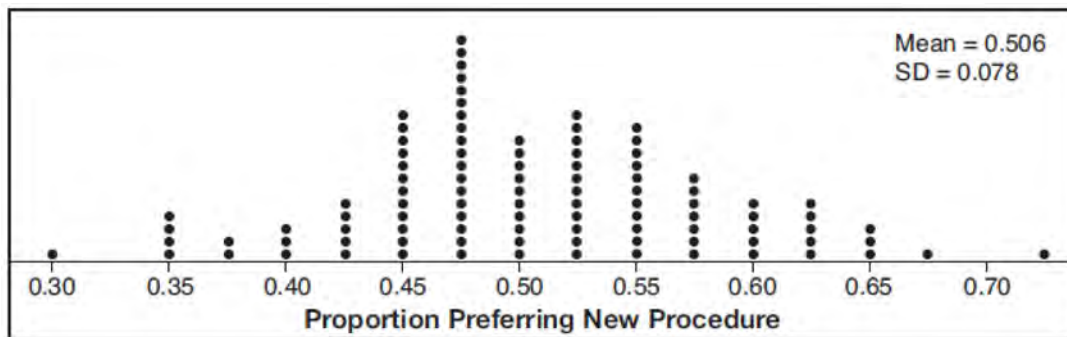
- 426 Solve the given equation algebraically for all values of  $x$ .  $3\sqrt{x} - 2x = -5$

427 The table below gives air pressures in kPa at selected altitudes above sea level measured in kilometers.

<b>x</b>	<b>Altitude (km)</b>	0	1	2	3	4	5
<b>y</b>	<b>Air Pressure (kPa)</b>	101	90	79	70	62	54

Write an exponential regression equation that models these data rounding all values to the *nearest thousandth*. Use this equation to algebraically determine the altitude, to the *nearest hundredth* of a kilometer, when the air pressure is 29 kPa.

428 Charlie's Automotive Dealership is considering implementing a new check-in procedure for customers who are bringing their vehicles for routine maintenance. The dealership will launch the procedure if 50% or more of the customers give the new procedure a favorable rating when compared to the current procedure. The dealership devises a simulation based on the minimal requirement that 50% of the customers prefer the new procedure. Each dot on the graph below represents the proportion of the customers who preferred the new check-in procedure, each of sample size 40, simulated 100 times.



Assume the set of data is approximately normal and the dealership wants to be 95% confident of its results. Determine an interval containing the plausible sample values for which the dealership will launch the new procedure. Round your answer to the *nearest hundredth*. Forty customers are selected randomly to undergo the new check-in procedure and the proportion of customers who prefer the new procedure is 32.5%. The dealership decides *not* to implement the new check-in procedure based on the results of the study. Use statistical evidence to explain this decision.

429 Solve the system of equations shown below algebraically.

$$(x - 3)^2 + (y + 2)^2 = 16$$

$$2x + 2y = 10$$

430 Solve the following system of equations algebraically for all values of  $x$ ,  $y$ , and  $z$ :

$$2x + 3y - 4z = -1$$

$$x - 2y + 5z = 3$$

$$-4x + y + z = 16$$

Algebra II 4 Point Regents Exam Questions

[www.jmap.org](http://www.jmap.org)

- 431 Using a microscope, a researcher observed and recorded the number of bacteria spores on a large sample of uniformly sized pieces of meat kept at room temperature. A summary of the data she recorded is shown in the table below.

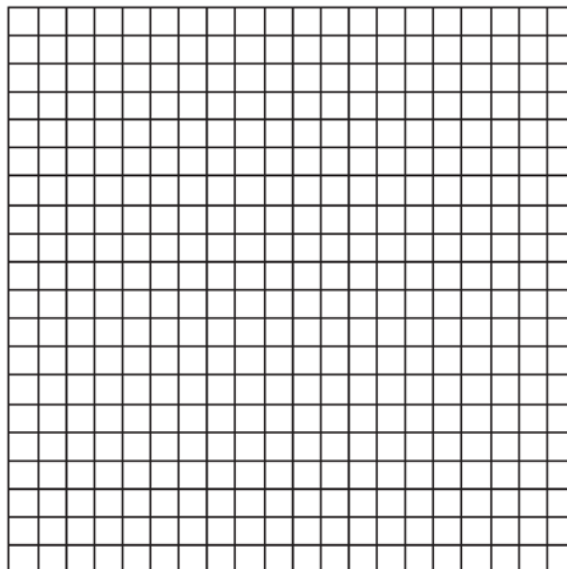
Hours (x)	Average Number of Spores (y)
0	4
0.5	10
1	15
2	60
3	260
4	1130
6	16,380

Using these data, write an exponential regression equation, rounding all values to the *nearest thousandth*. The researcher knows that people are likely to suffer from food-borne illness if the number of spores exceeds 100. Using the exponential regression equation, determine the maximum amount of time, to the *nearest quarter hour*, that the meat can be kept at room temperature safely.

- 432 Factor completely over the set of integers:  $16x^4 - 81$ . Sara graphed the polynomial  $y = 16x^4 - 81$  and stated “All the roots of  $y = 16x^4 - 81$  are real.” Is Sara correct? Explain your reasoning.

- 434 Write an equation for a sine function with an amplitude of 2 and a period of  $\frac{\pi}{2}$ . On the grid below, sketch the graph of the equation in the interval 0 to  $2\pi$ .

- 433 Simon lost his library card and has an overdue library book. When the book was 5 days late, he owed \$2.25 to replace his library card and pay the fine for the overdue book. When the book was 21 days late, he owed \$6.25 to replace his library card and pay the fine for the overdue book. Suppose the total amount Simon owes when the book is  $n$  days late can be determined by an arithmetic sequence. Determine a formula for  $a_n$ , the  $n$ th term of this sequence. Use the formula to determine the amount of money, in dollars, Simon needs to pay when the book is 60 days late.

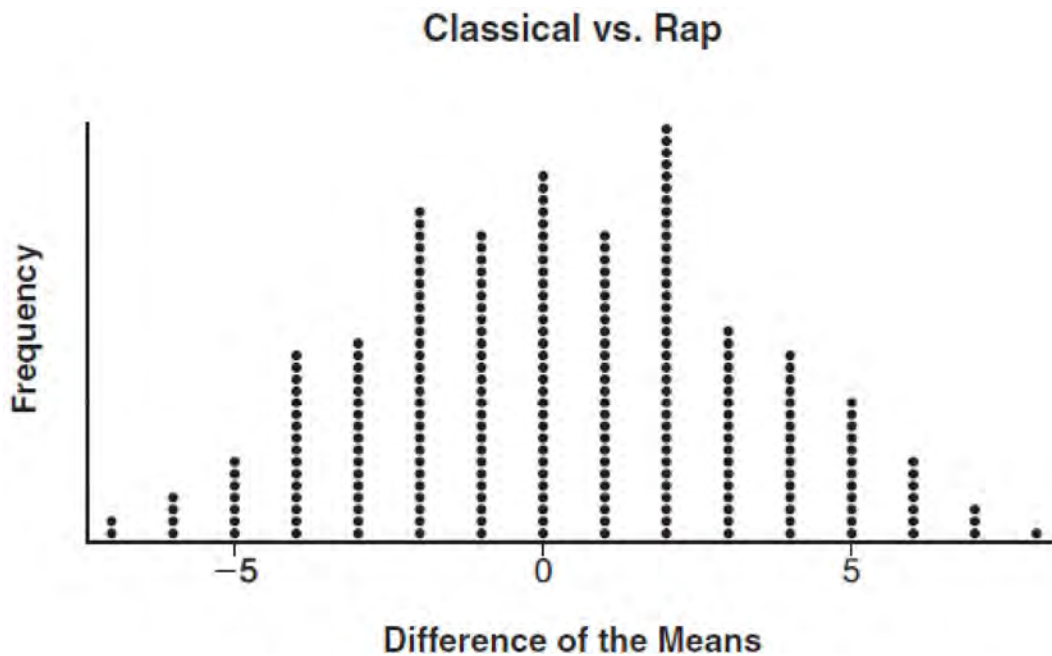


- 435 To determine if the type of music played while taking a quiz has a relationship to results, 16 students were randomly assigned to either a room softly playing classical music or a room softly playing rap music. The results on the quiz were as follows:

Classical: 74, 83, 77, 77, 84, 82, 90, 89

Rap: 77, 80, 78, 74, 69, 72, 78, 69

John correctly rounded the difference of the means of his experimental groups as 7. How did John obtain this value and what does it represent in the given context? Justify your answer. To determine if there is any significance in this value, John rerandomized the 16 scores into two groups of 8, calculated the difference of the means, and simulated this process 250 times as shown below.



Does the simulation support the theory that there may be a significant difference in quiz scores? Explain.

- 436 Given  $a(x) = x^4 + 2x^3 + 4x - 10$  and  $b(x) = x + 2$ , determine  $\frac{a(x)}{b(x)}$  in the form  $q(x) + \frac{r(x)}{b(x)}$ . Is  $b(x)$  a factor of  $a(x)$ ? Explain.

- 437 Algebraically solve the following system of equations.

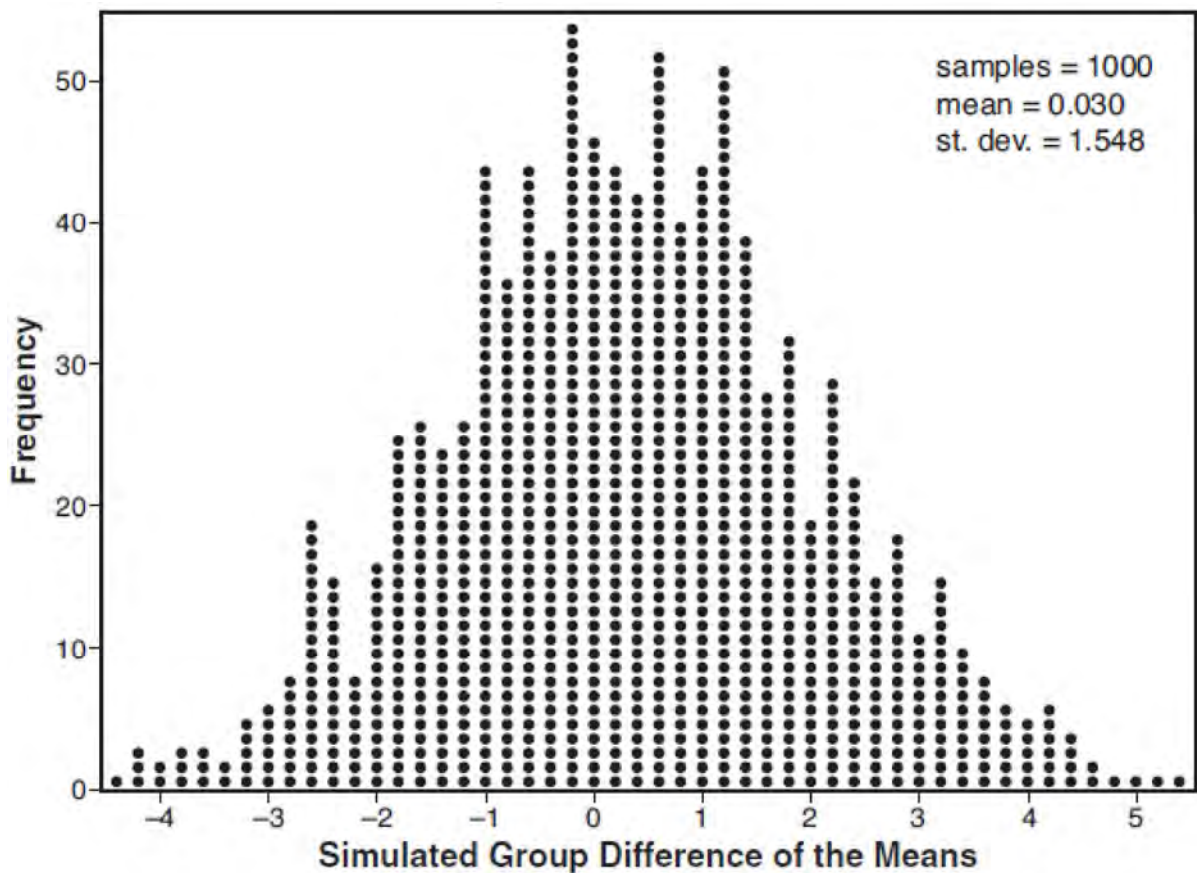
$$(x - 2)^2 + (y - 3)^2 = 16$$

$$x + y - 1 = 0$$

438 Joseph was curious to determine if scent improves memory. A test was created where better memory is indicated by higher test scores. A controlled experiment was performed where one group was given the test on scented paper and the other group was given the test on unscented paper. The summary statistics from the experiment are given below.

	Scented Paper	Unscented Paper
$\bar{x}$	23	18
$s_x$	2.898	2.408

Calculate the difference in means in the experimental test grades (scented -unscented). A simulation was conducted in which the subjects' scores were rerandomized into two groups 1000 times. The differences of the group means were calculated each time. The results are shown below.



Use the simulation results to determine the interval representing the middle 95% of the difference in means, to the nearest hundredth. Is the difference in means in Joseph's experiment statistically significant based on the simulation? Explain.

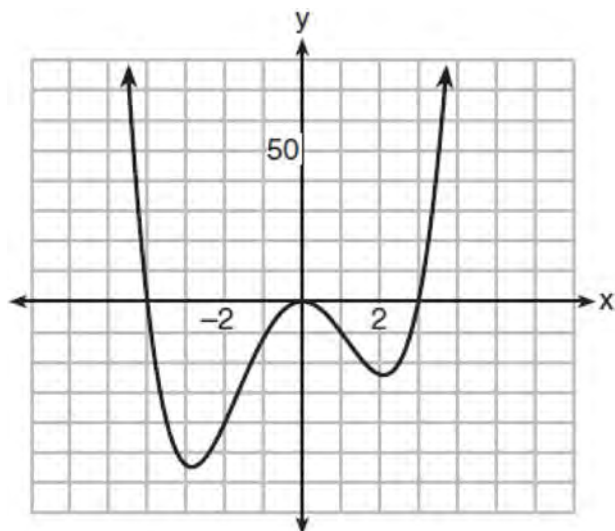


Algebra II 4 Point Regents Exam Questions

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439 Solve for all values of  $p$ :  $\frac{3p}{p-5} - \frac{2}{p+3} = \frac{p}{p+3}$

440 The graph of  $y = f(x)$  is shown below. The function has a leading coefficient of 1.



Write an equation for  $f(x)$ . The function  $g$  is formed by translating function  $f$  left 2 units. Write an equation for  $g(x)$ .

441 In contract negotiations between a local government agency and its workers, it is estimated that there is a 50% chance that an agreement will be reached on the salaries of the workers. It is estimated that there is a 70% chance that there will be an agreement on the insurance benefits. There is a 20% chance that no agreement will be reached on either issue. Find the probability that an agreement will be reached on *both* issues. Based on this answer, determine whether the agreement on salaries and the agreement on insurance are independent events. Justify your answer.

442 Solve the following system of equations algebraically for all values of  $a$ ,  $b$ , and  $c$ .

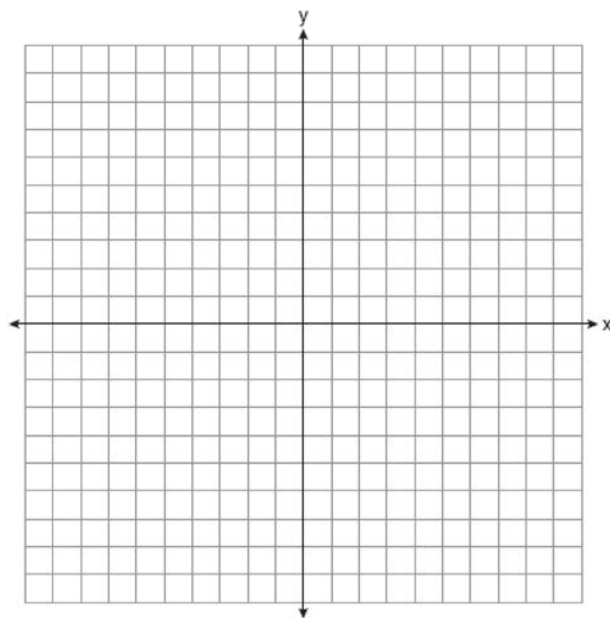
$$a + 4b + 6c = 23$$

$$a + 2b + c = 2$$

$$6b + 2c = a + 14$$

443 Graph the following function on the axes below.

$$f(x) = \log_3(2 - x)$$



State the domain of  $f$ . State the equation of the asymptote.

444 Alexa earns \$33,000 in her first year of teaching and earns a 4% increase in each successive year. Write a geometric series formula,  $S_n$ , for Alexa's total earnings over  $n$  years. Use this formula to find Alexa's total earnings for her first 15 years of teaching, to the *nearest cent*.



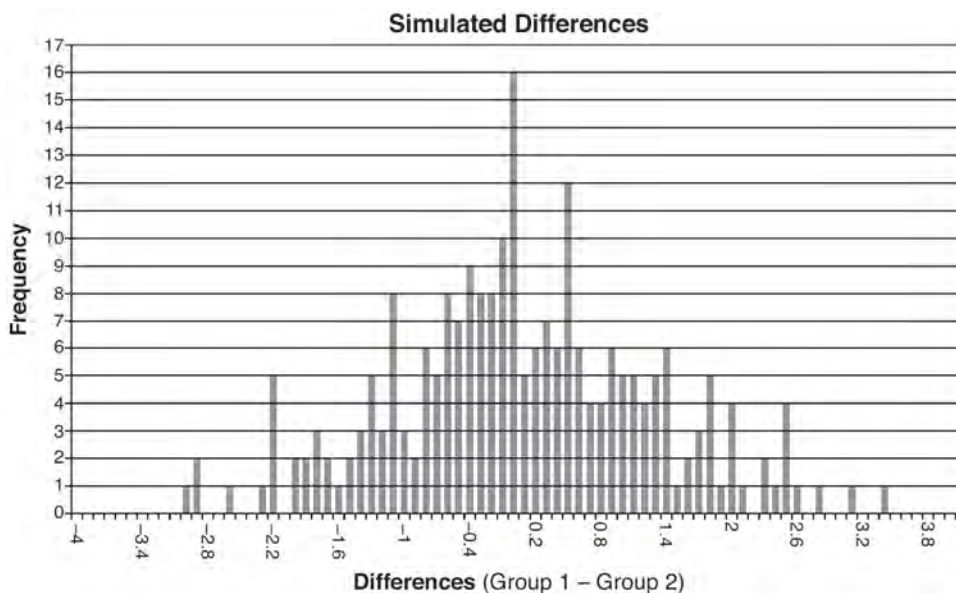
Algebra II 4 Point Regents Exam Questions

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- 445 Ayva designed an experiment to determine the effect of a new energy drink on a group of 20 volunteer students. Ten students were randomly selected to form group 1 while the remaining 10 made up group 2. Each student in group 1 drank one energy drink, and each student in group 2 drank one cola drink. Ten minutes later, their times were recorded for reading the same paragraph of a novel. The results of the experiment are shown below.

Group 1 (seconds)	Group 2 (seconds)
17.4	23.3
18.1	18.8
18.2	22.1
19.6	12.7
18.6	16.9
16.2	24.4
16.1	21.2
15.3	21.2
17.8	16.3
19.7	14.5
Mean = 17.7	Mean = 19.1

Ayva thinks drinking energy drinks makes students read faster. Using information from the experimental design or the results, explain why Ayva’s hypothesis may be *incorrect*. Using the given results, Ayva randomly mixes the 20 reading times, splits them into two groups of 10, and simulates the difference of the means 232 times.

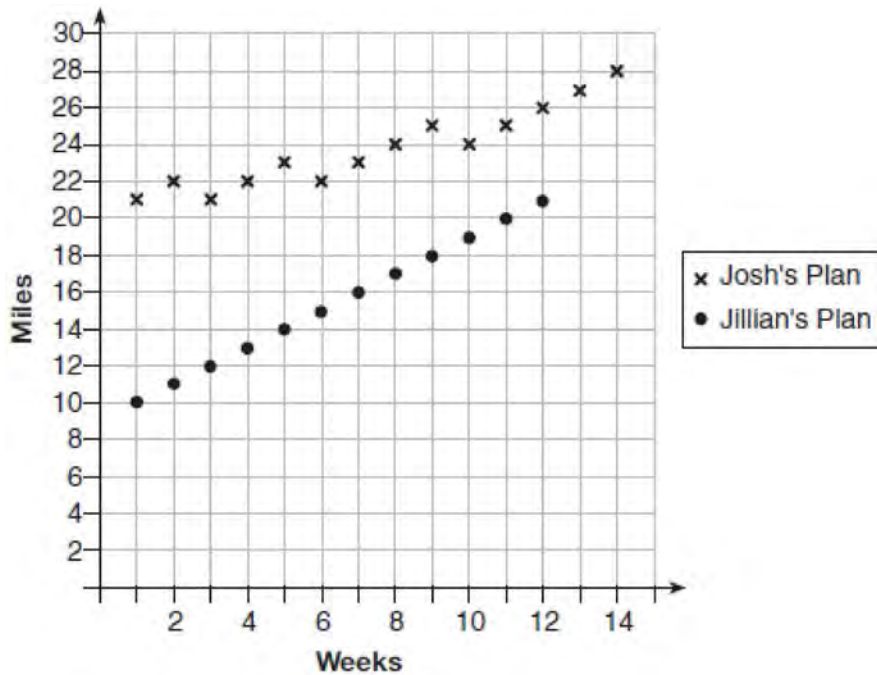


Ayva has decided that the difference in mean reading times is not an unusual occurrence. Support her decision using the results of the simulation. Explain your reasoning.

Algebra II 4 Point Regents Exam Questions

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- 446 Elaina has decided to run the Buffalo half-marathon in May. She researched training plans on the Internet and is looking at two possible plans: Jillian's 12-week plan and Josh's 14-week plan. The number of miles run per week for each plan is plotted below.



Which one of the plans follows an arithmetic pattern? Explain how you arrived at your answer. Write a recursive definition to represent the number of miles run each week for the duration of the plan you chose. Jillian's plan has an alternative if Elaina wanted to train instead for a full 26-mile marathon. Week one would start at 13 miles and follow the same pattern for the half-marathon, but it would continue for 14 weeks. Write an explicit formula, in *simplest form*, to represent the number of miles run each week for the full-marathon training plan.

- 447 Algebraically determine the values of  $h$  and  $k$  to correctly complete the identity stated below.  

$$2x^3 - 10x^2 + 11x - 7 = (x - 4)(2x^2 + hx + 3) + k$$

- 449 Solve the equation  $\sqrt{2x - 7} + x = 5$  algebraically, and justify the solution set.

- 448 Given:  $f(x) = 2x^2 + x - 3$  and  $g(x) = x - 1$   
 Express  $f(x) \cdot g(x) - [f(x) + g(x)]$  as a polynomial in standard form.

- 450 Evaluate  $j(-1)$  given  
 $j(x) = 2x^4 - x^3 - 35x^2 + 16x + 48$ . Explain what your answer tells you about  $x + 1$  as a factor. Algebraically find the remaining zeros of  $j(x)$ .

Algebra II 4 Point Regents Exam Questions

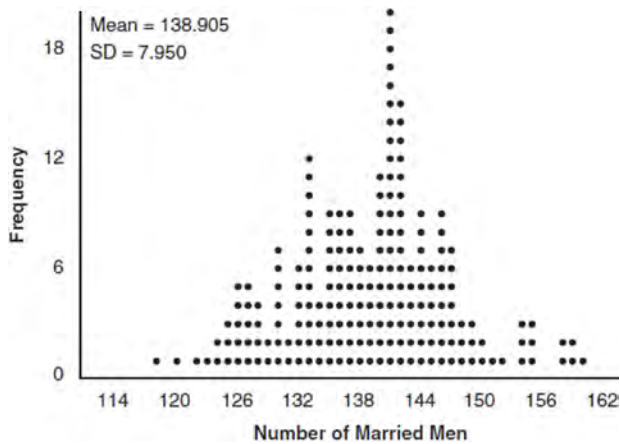
[www.jmap.org](http://www.jmap.org)

451 Which function shown below has a greater average rate of change on the interval  $[-2,4]$ ? Justify your answer.

$x$	$f(x)$
-4	0.3125
-3	0.625
-2	1.25
-1	2.5
0	5
1	10
2	20
3	40
4	80
5	160
6	320

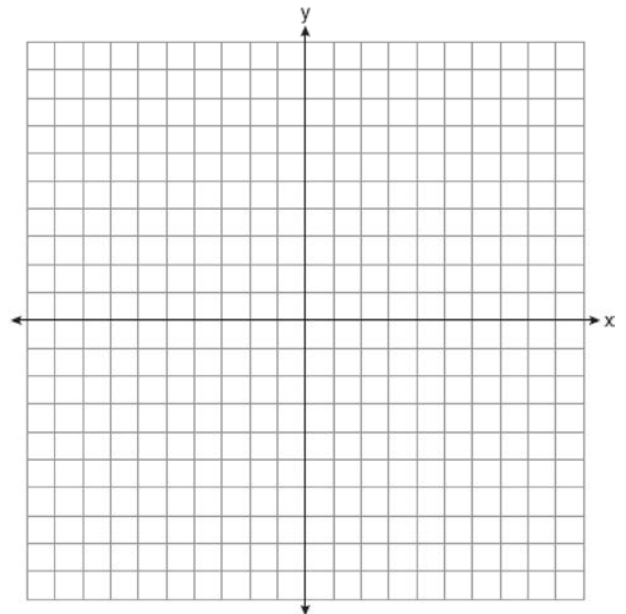
$$g(x) = 4x^3 - 5x^2 + 3$$

452 In a random sample of 250 men in the United States, age 21 or older, 139 are married. The graph below simulated samples of 250 men, 200 times, assuming that 139 of the men are married.



- Based on the simulation, create an interval in which the middle 95% of the number of married men may fall. Round your answer to the *nearest integer*.
- A study claims "50 percent of men 21 and older in the United States are married." Do your results from part a contradict this claim? Explain.

453 Graph  $y = \log_2(x + 3) - 5$  on the set of axes below. Use an appropriate scale to include *both* intercepts.



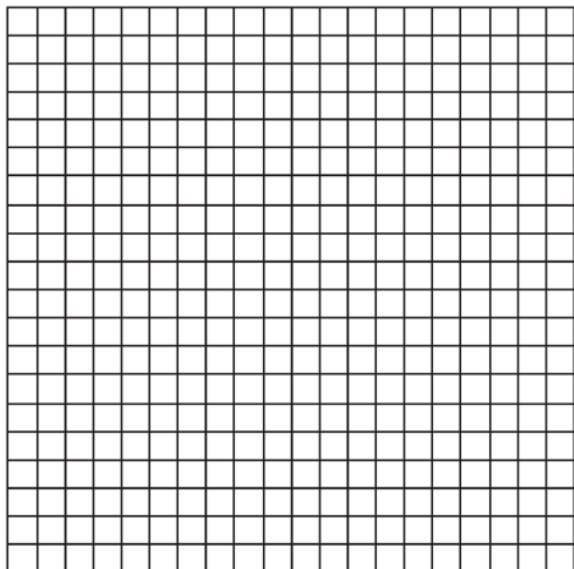
Describe the behavior of the given function as  $x$  approaches  $-3$  and as  $x$  approaches positive infinity.

Algebra II 4 Point Regents Exam Questions

[www.jmap.org](http://www.jmap.org)

454 The guidance department has reported that of the senior class, 2.3% are members of key club,  $K$ , 8.6% are enrolled in AP Physics,  $P$ , and 1.9% are in both. Determine the probability of  $P$  given  $K$ , to the *nearest tenth of a percent*. The principal would like a basic interpretation of these results. Write a statement relating your calculated probabilities to student enrollment in the given situation.

455 Determine an equation for the parabola with focus  $(4, -1)$  and directrix  $y = -5$ . (Use of the grid below is optional.)



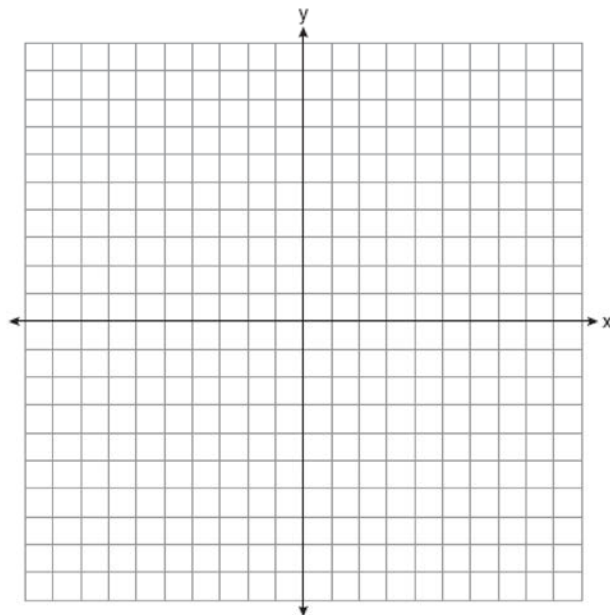
456 The height,  $h(t)$  in cm, of a piston, is given by the equation  $h(t) = 12 \cos\left(\frac{\pi}{3} t\right) + 8$ , where  $t$  represents the number of seconds since the measurements began. Determine the average rate of change, in cm/sec, of the piston's height on the interval  $1 \leq t \leq 2$ . At what value(s) of  $t$ , to the *nearest tenth of a second*, does  $h(t) = 0$  in the interval  $1 \leq t \leq 5$ ? Justify your answer.

457 Solve algebraically for all values of  $x$ :

$$\sqrt{6 - 2x} + x = 2(x + 15) - 9$$

458 Find algebraically the zeros for

$p(x) = x^3 + x^2 - 4x - 4$ . On the set of axes below, graph  $y = p(x)$ .



459 a) Algebraically determine the roots, in simplest  $a + bi$  form, to the equation below.

$$x^2 - 2x + 7 = 4x - 10$$

b) Consider the system of equations below.

$$y = x^2 - 2x + 7$$

$$y = 4x - 10$$

The graph of this system confirms the solution from part a is imaginary. Explain why.

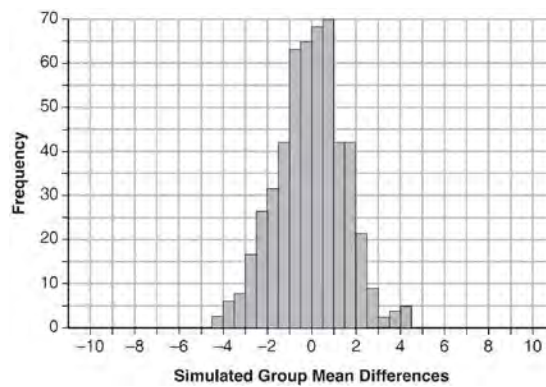
Algebra II 4 Point Regents Exam Questions

[www.jmap.org](http://www.jmap.org)

- 460 Seventy-two students are randomly divided into two equally-sized study groups. Each member of the first group (group 1) is to meet with a tutor after school twice each week for one hour. The second group (group 2), is given an online subscription to a tutorial account that they can access for a maximum of two hours each week. Students in both groups are given the same tests during the year. A summary of the two groups' final grades is shown below:

	Group 1	Group 2
$\bar{x}$	80.16	83.8
$S_x$	6.9	5.2

Calculate the mean difference in the final grades (group 1 – group 2) and explain its meaning in the context of the problem. A simulation was conducted in which the students' final grades were rerandomized 500 times. The results are shown below.



Use the simulation to determine if there is a significant difference in the final grades. Explain your answer.

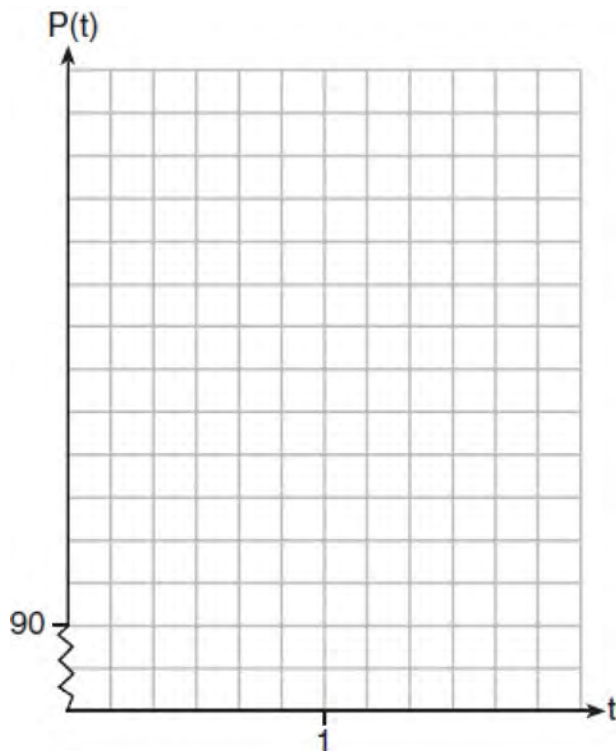
- 461 Determine, to the *nearest tenth of a year*, how long it would take an investment to double at a  $3\frac{3}{4}\%$  interest rate, compounded continuously.

**Algebra II 6 Point Regents Exam Questions**

- 462 The resting blood pressure of an adult patient can be modeled by the function  $P$  below, where  $P(t)$  is the pressure in millimeters of mercury after time  $t$  in seconds.

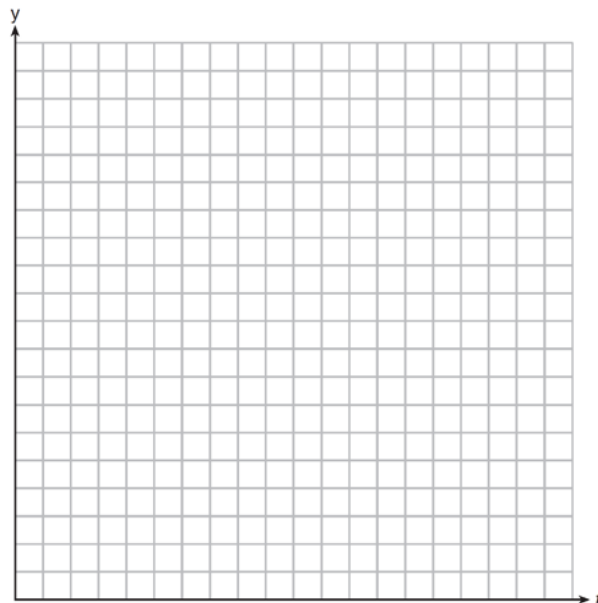
$$P(t) = 24\cos(3\pi t) + 120$$

On the set of axes below, graph  $y = P(t)$  over the domain  $0 \leq t \leq 2$ .



Determine the period of  $P$ . Explain what this value represents in the given context. Normal resting blood pressure for an adult is 120 over 80. This means that the blood pressure oscillates between a maximum of 120 and a minimum of 80. Adults with high blood pressure (above 140 over 90) and adults with low blood pressure (below 90 over 60) may be at risk for health disorders. Classify the given patient's blood pressure as low, normal, or high and explain your reasoning.

- 463 Drugs break down in the human body at different rates and therefore must be prescribed by doctors carefully to prevent complications, such as overdosing. The breakdown of a drug is represented by the function  $N(t) = N_0(e)^{-rt}$ , where  $N(t)$  is the amount left in the body,  $N_0$  is the initial dosage,  $r$  is the decay rate, and  $t$  is time in hours. Patient A,  $A(t)$ , is given 800 milligrams of a drug with a decay rate of 0.347. Patient B,  $B(t)$ , is given 400 milligrams of another drug with a decay rate of 0.231. Write two functions,  $A(t)$  and  $B(t)$ , to represent the breakdown of the respective drug given to each patient. Graph each function on the set of axes below.



To the *nearest hour*,  $t$ , when does the amount of the given drug remaining in patient B begin to exceed the amount of the given drug remaining in patient A? The doctor will allow patient A to take another 800 milligram dose of the drug once only 15% of the original dose is left in the body. Determine, to the *nearest tenth of an hour*, how long patient A will have to wait to take another 800 milligram dose of the drug.

Algebra II 6 Point Regents Exam Questions

[www.jmap.org](http://www.jmap.org)

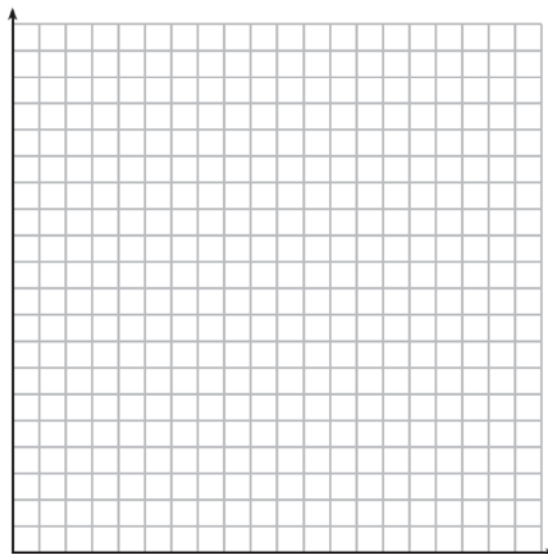
- 464 A radioactive substance has a mass of 140 g at 3 p.m. and 100 g at 8 p.m. Write an equation in the

form  $A = A_0 \left( \frac{1}{2} \right)^{\frac{t}{h}}$  that models this situation,

where  $h$  is the constant representing the number of hours in the half-life,  $A_0$  is the initial mass, and  $A$  is the mass  $t$  hours after 3 p.m. Using this equation, solve for  $h$ , to the *nearest ten thousandth*. Determine when the mass of the radioactive substance will be 40 g. Round your answer to the *nearest tenth of an hour*.

- 465 The value of a certain small passenger car based on its use in years is modeled by

$V(t) = 28482.698(0.684)^t$ , where  $V(t)$  is the value in dollars and  $t$  is the time in years. Zach had to take out a loan to purchase the small passenger car. The function  $Z(t) = 22151.327(0.778)^t$ , where  $Z(t)$  is measured in dollars, and  $t$  is the time in years, models the unpaid amount of Zach's loan over time. Graph  $V(t)$  and  $Z(t)$  over the interval  $0 \leq t \leq 5$ , on the set of axes below.



State when  $V(t) = Z(t)$ , to the *nearest hundredth*, and interpret its meaning in the context of the problem. Zach takes out an insurance policy that requires him to pay a \$3000 deductible in case of a collision. Zach will cancel the collision policy when the value of his car equals his deductible. To the *nearest year*, how long will it take Zach to cancel this policy? Justify your answer.

Algebra II 6 Point Regents Exam Questions

[www.jmap.org](http://www.jmap.org)

466 Seth's parents gave him \$5000 to invest for his 16th birthday. He is considering two investment options. Option *A* will pay him 4.5% interest compounded annually. Option *B* will pay him 4.6% compounded quarterly. Write a function of option *A* and option *B* that calculates the value of each account after  $n$  years. Seth plans to use the money after he graduates from college in 6 years. Determine how much more money option *B* will earn than option *A* to the *nearest cent*. Algebraically determine, to the *nearest tenth of a year*, how long it would take for option *B* to double Seth's initial investment.

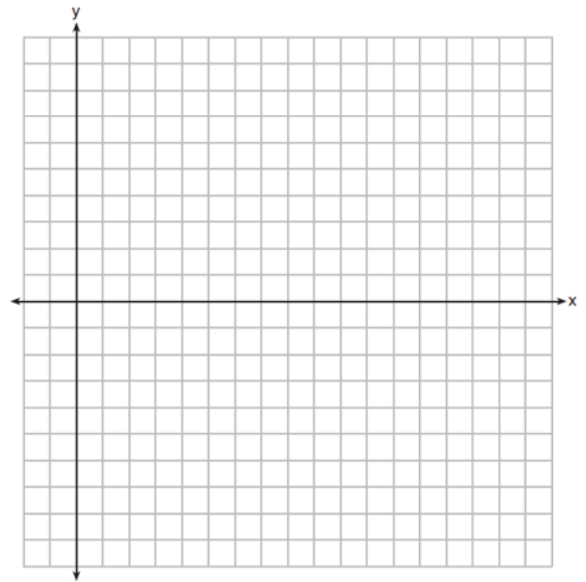
467 The speed of a tidal wave,  $s$ , in hundreds of miles per hour, can be modeled by the equation  $s = \sqrt{t} - 2t + 6$ , where  $t$  represents the time from its origin in hours. Algebraically determine the time when  $s = 0$ . How much faster was the tidal wave traveling after 1 hour than 3 hours, to the *nearest mile per hour*? Justify your answer.

468 A major car company analyzes its revenue,  $R(x)$ , and costs  $C(x)$ , in millions of dollars over a fifteen-year period. The company represents its revenue and costs as a function of time, in years,  $x$ , using the given functions.

$$R(x) = 550x^3 - 12,000x^2 + 83,000x + 7000$$

$$C(x) = 880x^3 - 21,000x^2 + 150,000x - 160,000$$

The company's profits can be represented as the difference between its revenue and costs. Write the profit function,  $P(x)$ , as a polynomial in standard form. Graph  $y = P(x)$  on the set of axes below over the domain  $2 \leq x \leq 16$ .



Over the given domain, state when the company was the least profitable and the most profitable, to the *nearest year*. Explain how you determined your answer.



Algebra II 6 Point Regents Exam Questions

[www.jmap.org](http://www.jmap.org)

- 469 The Beaufort Wind Scale was devised by British Rear Admiral Sir Francis Beaufort, in 1805 based upon observations of the effects of the wind. Beaufort numbers,  $B$ , are determined by the equation  $B = 1.69\sqrt{s + 4.45} - 3.49$ , where  $s$  is the speed of the wind in mph, and  $B$  is rounded to the nearest integer from 0 to 12.

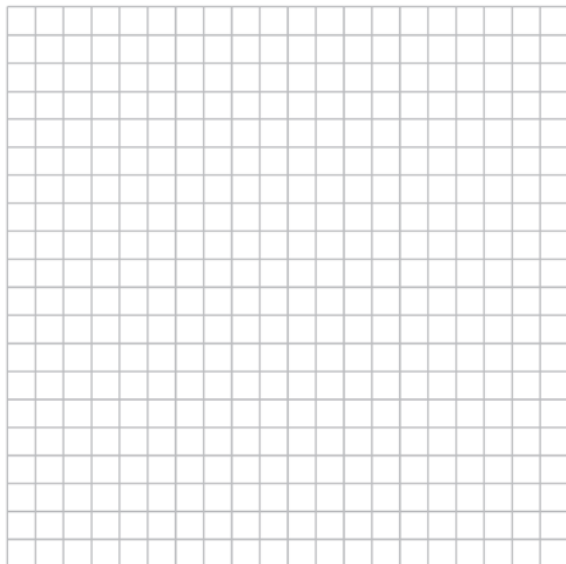
Beaufort Wind Scale	
Beaufort Number	Force of Wind
0	Calm
1	Light air
2	Light breeze
3	Gentle breeze
4	Moderate breeze
5	Fresh breeze
6	Steady breeze
7	Moderate gale
8	Fresh gale
9	Strong gale
10	Whole gale
11	Storm
12	Hurricane

Using the table above, classify the force of wind at a speed of 30 mph. Justify your answer. In 1946, the scale was extended to accommodate strong hurricanes. A strong hurricane received a  $B$  value of exactly 15. Algebraically determine the value of  $s$ , to the *nearest mph*. Any  $B$  values that round to 10 receive a Beaufort number of 10. Using technology, find an approximate range of wind speeds, to the *nearest mph*, associated with a Beaufort number of 10.

Algebra II 6 Point Regents Exam Questions

[www.jmap.org](http://www.jmap.org)

- 470 The ocean tides near Carter Beach follow a repeating pattern over time, with the amount of time between each low and high tide remaining relatively constant. On a certain day, low tide occurred at 8:30 a.m. and high tide occurred at 3:00 p.m. At high tide, the water level was 12 inches above the average local sea level; at low tide it was 12 inches below the average local sea level. Assume that high tide and low tide are the maximum and minimum water levels each day, respectively. Write a cosine function of the form  $f(t) = A \cos(Bt)$ , where  $A$  and  $B$  are real numbers, that models the water level,  $f(t)$ , in inches above or below the average Carter Beach sea level, as a function of the time measured in  $t$  hours since 8:30 a.m. On the grid below, graph one cycle of this function.



People who fish in Carter Beach know that a certain species of fish is most plentiful when the water level is increasing. Explain whether you would recommend fishing for this species at 7:30 p.m. or 10:30 p.m. using evidence from the given context.

- 471 Sarah is fighting a sinus infection. Her doctor prescribed a nasal spray and an antibiotic to fight the infection. The active ingredients, in milligrams, remaining in the bloodstream from the nasal spray,  $n(t)$ , and the antibiotic,  $a(t)$ , are modeled in the functions below, where  $t$  is the time in hours since the medications were taken.

$$n(t) = \frac{t+1}{t+5} + \frac{18}{t^2 + 8t + 15}$$

$$a(t) = \frac{9}{t+3}$$

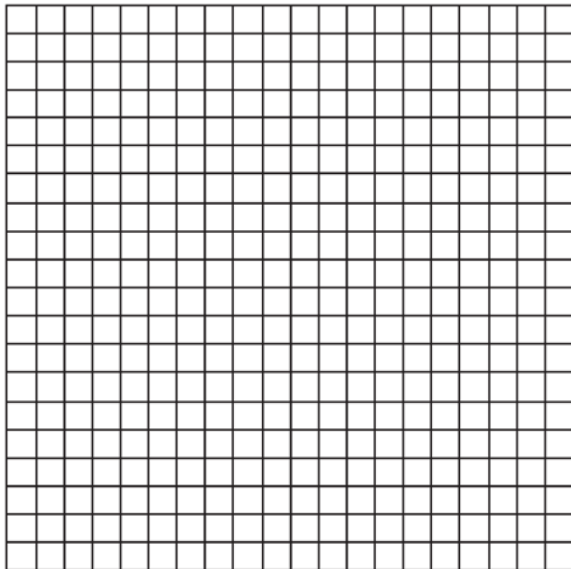
Determine which drug is made with a greater initial amount of active ingredient. Justify your answer. Sarah's doctor told her to take both drugs at the same time. Determine algebraically the number of hours after taking the medications when both medications will have the same amount of active ingredient remaining in her bloodstream.

- 472 Titanium-44 is a radioactive isotope such that every 63 years, its mass decreases by half. For a sample of titanium-44 with an initial mass of 100 grams, write a function that will give the mass of the sample remaining after any amount of time. Define all variables. Scientists sometimes use the average yearly decrease in mass for estimation purposes. Use the average yearly decrease in mass of the sample between year 0 and year 10 to predict the amount of the sample remaining after 40 years. Round your answer to the *nearest tenth*. Is the actual mass of the sample or the estimated mass greater after 40 years? Justify your answer.

Algebra II 6 Point Regents Exam Questions

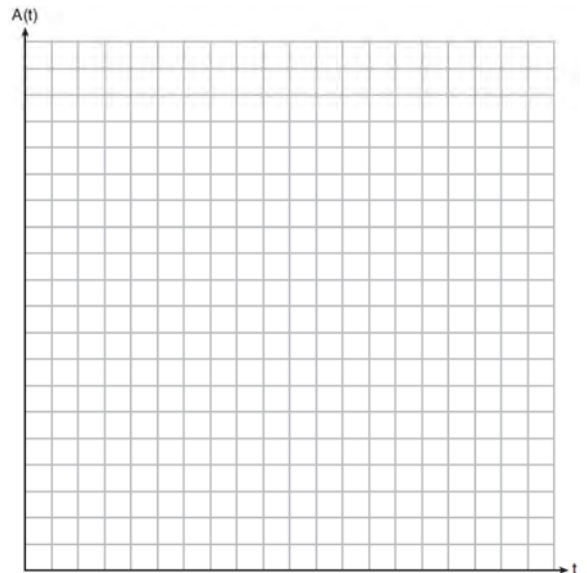
[www.jmap.org](http://www.jmap.org)

- 473 Griffin is riding his bike down the street in Churchville, N.Y. at a constant speed, when a nail gets caught in one of his tires. The height of the nail above the ground, in inches, can be represented by the trigonometric function  $f(t) = -13 \cos(0.8\pi t) + 13$ , where  $t$  represents the time (in seconds) since the nail first became caught in the tire. Determine the period of  $f(t)$ . Interpret what the period represents in this context. On the grid below, graph *at least one* cycle of  $f(t)$  that includes the  $y$ -intercept of the function.



Does the height of the nail ever reach 30 inches above the ground? Justify your answer.

- 474 Tony is evaluating his retirement savings. He currently has \$318,000 in his account, which earns an interest rate of 7% compounded annually. He wants to determine how much he will have in the account in the future, even if he makes no additional contributions to the account. Write a function,  $A(t)$ , to represent the amount of money that will be in his account in  $t$  years. Graph  $A(t)$  where  $0 \leq t \leq 20$  on the set of axes below.

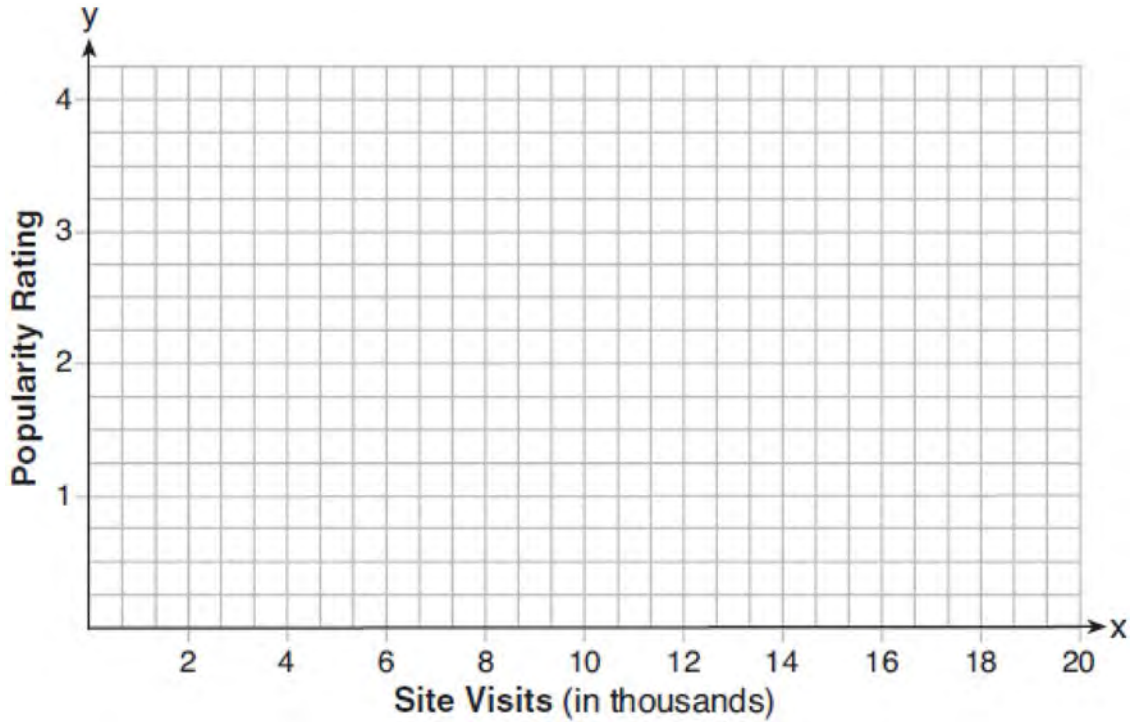


Tony's goal is to save \$1,000,000. Determine algebraically, to the *nearest year*, how many years it will take for him to achieve his goal. Explain how your graph of  $A(t)$  confirms your answer.

Algebra II 6 Point Regents Exam Questions

[www.jmap.org](http://www.jmap.org)

- 475 Website popularity ratings are often determined using models that incorporate the number of visits per week a website receives. One model for ranking websites is  $P(x) = \log(x - 4)$ , where  $x$  is the number of visits per week in thousands and  $P(x)$  is the website's popularity rating. According to this model, if a website is visited 16,000 times in one week, what is its popularity rating, rounded to the *nearest tenth*? Graph  $y = P(x)$  on the axes below.



An alternative rating model is represented by  $R(x) = \frac{1}{2}x - 6$ , where  $x$  is the number of visits per week in thousands. Graph  $R(x)$  on the same set of axes. For what number of weekly visits will the two models provide the same rating?

## Algebra II Multiple Choice Regents Exam Questions Answer Section

1 ANS: 2



REF: 061817aia NAT: S.ID.A.4 TOP: Normal Distributions

KEY: probability

2 ANS: 4

1)  $-1$  is also a zero. 2)  $x^2(x-a) + 16(x-a) = (x^2 + 16)(x-a)$   $a$  is the only zero. 3)  $-a$  is the only zero. 4)  $x^2(x-a) - 9(x-a) = (x^2 - 9)(x-a)$ .

REF: 012019aia NAT: A.APR.B.3 TOP: Solving Polynomial Equations

3 ANS: 2

$$2 - \frac{x-1}{x+2}$$

$$1 + \frac{x+2}{x+2} - \frac{x-1}{x+2}$$

$$1 + \frac{x+2-(x-1)}{x+2}$$

$$1 + \frac{3}{x+2}$$

REF: 081907aia NAT: A.APR.D.7 TOP: Addition and Subtraction of Rationals

4 ANS: 4

$$wx^2 + w = 0$$

$$w(x^2 + 1) = 0$$

$$x^2 = -1$$

$$x = \pm i$$

REF: 061912aia NAT: A.REI.B.4 TOP: Solving Quadratics

KEY: complex solutions | taking square roots

5 ANS: 3

$$440 \times 2.3\% \approx 10$$

REF: 011807aia NAT: S.ID.A.4 TOP: Normal Distributions

KEY: predict

6 ANS: 1 REF: 061904aai NAT: F.IF.B.6 TOP: Rate of Change

7 ANS: 2  
 $1.00643^{12} \approx 1.08$

REF: 081808aai NAT: A.SSE.B.3 TOP: Modeling Exponential Functions

8 ANS: 1



REF: 081919aai NAT: S.ID.A.4 TOP: Normal Distributions

KEY: percent

9 ANS: 4

$$1.06^{\frac{1}{52}}$$

REF: 061924aai NAT: F.BF.A.1 TOP: Modeling Exponential Functions

10 ANS: 2

$$x^2 = 3x + 40. \quad x = -5 \text{ is an extraneous solution.}$$

$$x^2 - 3x - 40 = 0$$

$$(x - 8)(x + 5) = 0$$

$$x = 8, -5$$

REF: 012010aai NAT: A.REI.A.2 TOP: Solving Radicals

KEY: extraneous solutions

11 ANS: 4

$$f(x) = (x + 1)(x - 1)(x - 2) = (x^2 - 1)(x - 2) = x^3 - 2x^2 - x + 2$$

REF: 081921aai NAT: A.APR.B.3 TOP: Graphing Polynomial Functions

12 ANS: 4 REF: 081906aai NAT: S.IC.B.3 TOP: Analysis of Data

KEY: type

13 ANS: 1 REF: 081903aai NAT: F.LE.A.2 TOP: Families of Functions

14 ANS: 1 REF: 081813aai NAT: A.SSE.B.4 TOP: Series

15 ANS: 3

$$(x + 3i)^2 - (2x - 3i)^2 = x^2 + 6xi + 9i^2 - (4x^2 - 12xi + 9i^2) = -3x^2 + 18xi$$

REF: 061805aai NAT: N.CN.A.2 TOP: Operations with Complex Numbers

16 ANS: 4

$$\ln e^{0.3x} = \ln \frac{5918}{87}$$

$$x = \frac{\ln \frac{5918}{87}}{0.3}$$

REF: 081801aai NAT: F.LE.A.4 TOP: Exponential Equations

KEY: without common base

17 ANS: 3

$$\frac{c^2 - d^2}{d^2 + cd - 2c^2} = \frac{(c+d)(c-d)}{(d+2c)(d-c)} = \frac{-(c+d)}{d+2c} = \frac{-c-d}{d+2c}$$

REF: 011818aai NAT: A.APR.D.6 TOP: Rational Expressions

KEY: factoring

18 ANS: 1

$$1.025^{\frac{1}{12}} \approx 1.00206$$

REF: 081924aai NAT: A.SSE.B.3 TOP: Modeling Exponential Functions

19 ANS: 1

$$\frac{N(6) - N(0)}{6 - 0} \approx -8.93$$

REF: 012012aai NAT: F.IF.B.6 TOP: Rate of Change

20 ANS: 4

$$\frac{13}{13+11} = \frac{13}{24}$$

REF: 012011aai NAT: S.CP.A.4 TOP: Conditional Probability

21 ANS: 3

The vertex is  $(-3,5)$  and  $p = 2$ .  $y = \frac{-1}{4(2)}(x+3)^2 + 5$

REF: 011914aai NAT: G.GPE.A.2 TOP: Graphing Quadratic Functions

22 ANS: 1

In vertex form, the parabola is  $y = -\frac{1}{4(2)}(x+4)^2 + 3$ . The vertex is  $(-4,3)$  and  $p = 2$ .  $3 + 2 = 5$

REF: 011816aai NAT: G.GPE.A.2 TOP: Graphing Quadratic Functions

23 ANS: 4

REF: 081803aai NAT: F.BF.A.1 TOP: Operations with Functions

24 ANS: 1

$$84.1\% \times 750 \approx 631$$

REF: 011923aai NAT: S.ID.A.4 TOP: Normal Distributions

KEY: predict

25 ANS: 1

The time of the next high tide will be the midpoint of consecutive low tides.

REF: 011907aii NAT: F.IF.C.7 TOP: Graphing Trigonometric Functions

KEY: mixed

26 ANS: 3

REF: 081909aii

NAT: F.BF.A.2

TOP: Sequences

KEY: recursive

27 ANS: 4

REF: 081824aii

NAT: S.CP.A.3

TOP: Conditional Probability

28 ANS: 2

$$121(b)^2 = 64 \quad 64\left(\frac{8}{11}\right)^2 \approx 34$$

$$b = \frac{8}{11}$$

REF: 011904aii

NAT: F.IF.A.3

TOP: Sequences

KEY: explicit

29 ANS: 4

$$\frac{5+9}{2} = 7, \text{ vertex: } (-2, 7); p = 7 - 9 = -2, y = \frac{1}{4(-2)}(x+2)^2 + 7$$

$$y - 7 = \frac{1}{-8}(x+2)^2$$

$$-8(y - 7) = (x+2)^2$$

REF: 061821aii

NAT: G.GPE.A.2

TOP: Graphing Quadratic Functions

30 ANS: 3

$$\frac{x^2(x+2) - 9(x+2)}{x(x^2 - x - 6)} = \frac{(x^2 - 9)(x+2)}{x(x-3)(x+2)} = \frac{(x+3)(x-3)}{x(x-3)} = \frac{x+3}{x}$$

REF: 061803aii

NAT: A.APR.D.6

TOP: Rational Expressions

KEY: factoring

31 ANS: 2

$$b^2 = 2b^2 - 64 \quad -8 \text{ is extraneous.}$$

$$-b^2 = -64$$

$$b = \pm 8$$

REF: 061919aii

NAT: A.REI.A.2

TOP: Solving Radicals

KEY: extraneous solutions

32 ANS: 1

$$x^2 + 2x + 1 = (x+1)^2$$

REF: 011919aii

NAT: A.APR.B.3

TOP: Graphing Polynomial Functions



33 ANS: 2

$$4x \cdot x^{\frac{2}{3}} + 2x^{\frac{5}{3}} = 4x^{\frac{5}{3}} + 2x^{\frac{5}{3}} = 6x^{\frac{5}{3}} = 6\sqrt[3]{x^5}$$

REF: 061820aii NAT: N.RN.A.2 TOP: Operations with Radicals

KEY: with variables, index &gt; 2

34 ANS: 3

$$(x+4)^2 - 10 = 3x+6 \quad y = 3(-5)+6 = -9$$

$$x^2 + 8x + 16 - 10 = 3x + 6 \quad y = 3(0) + 6 = 6$$

$$x^2 + 5x = 0$$

$$x(x+5) = 0$$

$$x = -5, 0$$

REF: 061903aii NAT: A.REI.C.7 TOP: Quadratic-Linear Systems

35 ANS: 1

$$\frac{x(x^2-9)}{-(x^2-9)} = -x$$

REF: 012023aii NAT: A.APR.D.6 TOP: Rational Expressions

KEY: factoring

36 ANS: 2 REF: 061802aii NAT: F.IF.C.7 TOP: Graphing Exponential Functions

37 ANS: 3

$$x^2 + (2x)^2 = 5 \quad y = 2x = \pm 2$$

$$x^2 + 4x^2 = 5$$

$$5x^2 = 5$$

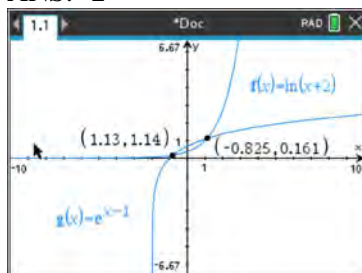
$$x = \pm 1$$

REF: 081916aii NAT: A.REI.C.7 TOP: Quadratic-Linear Systems

38 ANS: 1 REF: 011815aii NAT: F.TF.A.2 TOP: Unit Circle

39 ANS: 3 REF: 012003aii NAT: A.APR.C.4 TOP: Polynomial Identities

40 ANS: 2



REF: 081920aii NAT: A.REI.D.11 TOP: Other Systems

41 ANS: 1 REF: 011902aii NAT: F.IF.C.7 TOP: Graphing Logarithmic Functions

42 ANS: 4

$$\frac{x^2 - 4x}{2x} = \frac{x(x-4)}{2x} = \frac{x-4}{2} = \frac{x}{2} - 2 = \frac{x-1}{2} - \frac{3}{2} = \frac{x-1-3}{2} = \frac{x-4}{2}$$

REF: 011921aai NAT: A.APR.D.6 TOP: Rational Expressions

KEY: factoring

43 ANS: 1 REF: 011814aai NAT: A.REI.D.11 TOP: Other Systems

44 ANS: 4

The maximum of  $p$  is 5. The minimum of  $f$  is  $-\frac{21}{4}$  ( $x = \frac{-6}{2(4)} = -\frac{3}{4}$ )

$$f\left(-\frac{3}{4}\right) = 4\left(-\frac{3}{4}\right)^2 + 6\left(-\frac{3}{4}\right) - 3 = 4\left(\frac{9}{16}\right) - \frac{18}{4} - \frac{12}{4} = -\frac{21}{4}, \quad \frac{20}{4} - \left(-\frac{21}{4}\right) = \frac{41}{4} = 10.25$$

REF: 011922aai NAT: F.IF.C.9 TOP: Comparing Functions

45 ANS: 4

(1) and (3) are not recursive

REF: 012013aai NAT: F.LE.A.2 TOP: Sequences KEY: recursive

46 ANS: 4

There is no  $x$ -intercept.

REF: 011823aai NAT: F.IF.C.7 TOP: Graphing Exponential Functions

47 ANS: 3

$$\frac{x^{\frac{2}{3}} \cdot x^{\frac{5}{2}}}{x^{\frac{1}{6}}} = \frac{x^{\frac{4}{6}} \cdot x^{\frac{15}{6}}}{x^{\frac{1}{6}}} = x^{\frac{18}{6}} = x^3$$

REF: 081812aai NAT: N.RN.A.2 TOP: Operations with Radicals

KEY: with variables, index &gt; 2

48 ANS: 1

$$9110 = 5000e^{30r}$$

$$\ln \frac{911}{500} = \ln e^{30r}$$

$$\frac{\ln \frac{911}{500}}{30} = r$$

$$r \approx .02$$

REF: 011810aai NAT: F.LE.A.4 TOP: Exponential Growth

49 ANS: 4

$$0.48 \cdot 0.25 = 0.12$$

REF: 061811aai NAT: S.CP.A.2 TOP: Probability of Compound Events

KEY: probability

- 50 ANS: 1  
2) linear, 3) quadratic, 4) cubic

REF: 061920aai NAT: F.LE.A.2 TOP: Families of Functions

- 51 ANS: 3

$$x^2 - 4x - 5 = 4x^2 - 40x + 100$$

$$3x^2 - 36x + 105 = 0$$

$$x^2 - 12x + 35 = 0$$

$$(x - 7)(x - 5) = 0$$

$$x = 5, 7$$

REF: 081807aai NAT: A.REI.A.2 TOP: Solving Radicals

KEY: extraneous solutions

- 52 ANS: 1

$$p(x) = r(x) - c(x)$$

$$-0.5x^2 + 250x - 300 = -0.3x^2 + 150x - c(x)$$

$$c(x) = 0.2x^2 - 100x + 300$$

REF: 061813aai NAT: F.BF.A.1 TOP: Operations with Functions

- 53 ANS: 3 REF: 012015aai NAT: S.IC.B.3 TOP: Analysis of Data

KEY: type

- 54 ANS: 2

$$x = \frac{2 \pm \sqrt{(-2)^2 - 4(5)(4)}}{2(5)} = \frac{2 \pm \sqrt{-76}}{10} = \frac{2 \pm i\sqrt{4}\sqrt{19}}{10} = \frac{1}{5} \pm \frac{i\sqrt{19}}{5}$$

REF: 011905aai NAT: A.REI.B.4 TOP: Solving Quadratics

KEY: complex solutions | quadratic formula

- 55 ANS: 1

$$1240(1.06)^x = 890(1.11)^x$$

$$x \approx 7$$

REF: 061814aai NAT: A.REI.D.11 TOP: Other Systems

- 56 ANS: 1

The cosine function has been translated +3. Since the maximum is 5 and the minimum is 1, the amplitude is 2.

$$\frac{\pi}{3} = \frac{2\pi}{b}$$

$$b = 6$$

REF: 011913aai NAT: F.TF.B.5 TOP: Modeling Trigonometric Functions

57 ANS: 3

$$1^3 - k(1)^2 + 2(1) = 0$$

$$k = 3$$

REF: 061812aai NAT: A.APR.B.2 TOP: Remainder Theorem

58 ANS: 1

$$100\left(\frac{1}{2}\right)^{\frac{d}{8}} = 100e^{kd}$$

$$\left(\frac{1}{2}\right)^{\frac{1}{8}} = e^k$$

$$k \approx -0.087$$

REF: 061818aai NAT: A.SSE.B.3 TOP: Modeling Exponential Functions

59 ANS: 4

$$5000\left(1 + \frac{.035}{12}\right)^{12 \cdot 6} \approx 6166.50$$

REF: 081917aai NAT: A.CED.A.1 TOP: Exponential Growth

60 ANS: 4

$$\frac{2}{x} = \frac{4x}{x+3}$$

$$2x + 6 = 4x^2$$

$$4x^2 - 2x - 6 = 0$$

$$2(2x^2 - x - 3) = 0$$

$$(2x - 3)(x + 1) = 0$$

$$x = \frac{3}{2}, -1$$

REF: 061809aai NAT: A.REI.A.2 TOP: Solving Rationals

61 ANS: 4

The vertex is (2,2) and  $p = 3$ .  $3 + 2 = 5$ 

REF: 081823aai NAT: G.GPE.A.2 TOP: Graphing Quadratic Functions

62 ANS: 2

REF: 081802aai NAT: S.IC.B.3 TOP: Analysis of Data

KEY: type

63 ANS: 2

$$\frac{85}{210 + 85}$$

REF: 081818aai NAT: S.CP.A.1 TOP: Venn Diagrams

64 ANS: 1

$$x + y + z = 9 \quad 4 - y - z = -1 \quad 4 - 6 + z = 9$$

$$\underline{x - y - z = -1} \quad 4 - y + z = 21 \quad z = 11$$

$$2x = 8 \quad -y - z = -5$$

$$x = 4 \quad \underline{-y + z = 17}$$

$$-2y = 12$$

$$y = -6$$

REF: 012018aai NAT: A.REI.C.6 TOP: Solving Linear Systems

KEY: three variables

65 ANS: 1

$$(2x - i)^2 - (2x - i)(2x + 3i)$$

$$(2x - i)[(2x - i) - (2x + 3i)]$$

$$(2x - i)(-4i)$$

$$-8xi + 4i^2$$

$$-8xi - 4$$

REF: 011911aai NAT: N.CN.A.2 TOP: Operations with Complex Numbers

66 ANS: 2

$$n^2(n^2 - 9) + 4n(n^2 - 9) - 12(n^2 - 9)$$

$$(n^2 + 4n - 12)(n^2 - 9)$$

$$(n + 6)(n - 2)(n + 3)(n - 3)$$

REF: 061911aai NAT: A.SSE.A.2 TOP: Factoring Polynomials

KEY: factoring by grouping

67 ANS: 3

$$8r^3 = 216 \quad S_{12} = \frac{8 - 8(3)^{12}}{1 - 3} = 2125760$$

$$r^3 = 27$$

$$r = 3$$

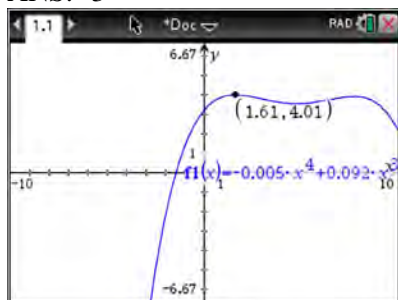
REF: 081902aai NAT: A.SSE.B.4 TOP: Series

68 ANS: 3 REF: 061824aai NAT: A.CED.A.1 TOP: Modeling Rationals

69 ANS: 2 REF: 011910aai NAT: S.IC.B.3 TOP: Analysis of Data

KEY: bias

70 ANS: 3



REF: 011817aai NAT: F.IF.B.4 TOP: Graphing Polynomial Functions

71 ANS: 3

$$-3 + 5i - (4 + 24i - 2i - 12i^2) = -3 + 5i - (16 + 22i) = -19 - 17i$$

REF: 081815aai NAT: N.CN.A.2 TOP: Operations with Complex Numbers

72 ANS: 2

$$x = \frac{y}{y+2}$$

$$xy + 2x = y$$

$$xy - y = -2x$$

$$y(x-1) = -2x$$

$$y = \frac{-2x}{x-1}$$

REF: 081924aai NAT: F.BF.B.4 TOP: Inverse of Functions

KEY: other

73 ANS: 1

REF: 081804aai

NAT: F.IF.C.9

TOP: Comparing Functions

74 ANS: 3

$$x = \frac{-2 \pm \sqrt{2^2 - 4(3)(7)}}{2(3)} = \frac{-2 \pm \sqrt{-80}}{6} = \frac{-2 \pm i\sqrt{16}\sqrt{5}}{6} = -\frac{1}{3} \pm \frac{2i\sqrt{5}}{3}$$

REF: 081809aai NAT: A.REI.B.4 TOP: Solving Quadratics

KEY: complex solutions | quadratic formula

75 ANS: 2

$$y = \frac{1}{2}x + 8 \quad x = \frac{1}{2}y + 8$$

$$2x = y + 16$$

$$y = 2x - 16$$

REF: 081806aai NAT: F.BF.B.4 TOP: Inverse of Functions

KEY: linear

76 ANS: 2

REF: 011901aai

NAT: S.ID.A.4

TOP: Normal Distributions

KEY: mean and standard deviation

77 ANS: 3 REF: 061901aai NAT: S.IC.B.3 TOP: Analysis of Data  
KEY: type

78 ANS: 1  
 $7 - 3i + x^2 - 4xi + 4i^2 - 4i - 2x^2 = 7 - 7i - x^2 - 4xi - 4 = 3 - x^2 - 4xi - 7i = (3 - x^2) - (4x + 7)i$

REF: 012022aai NAT: N.CN.A.2 TOP: Operations with Complex Numbers

79 ANS: 3 REF: 012005aai NAT: F.IF.B.4 TOP: Graphing Polynomial Functions

80 ANS: 3

$$\begin{array}{r}
 2x^3 - 4x^2 - x + \frac{14}{x+6} \\
 x+6 \overline{) 2x^4 + 8x^3 - 25x^2 - 6x + 14} \\
 \underline{2x^4 + 12x^3} \phantom{- 25x^2 - 6x + 14} \\
 -4x^3 - 25x^2 \phantom{- 6x + 14} \\
 \underline{-4x^3 - 24x^2} \phantom{- 6x + 14} \\
 -x^2 - 6x + 14 \\
 \underline{-x^2 - 6x} \phantom{+ 14} \\
 14
 \end{array}$$

REF: 081805aai NAT: A.APR.D.6 TOP: Rational Expressions

KEY: division

81 ANS: 3

$$y = x^3 - 2$$

$$x = y^3 - 2$$

$$x + 2 = y^3$$

$$\sqrt[3]{x+2} = y$$

REF: 061815aai NAT: F.BF.B.4 TOP: Inverse of Functions

KEY: other

82 ANS: 2 REF: 081904aai NAT: A.SSE.A.2 TOP: Factoring Polynomials

KEY: higher power

83 ANS: 1

$$6 - (3x - 2i)(3x - 2i) = 6 - (9x^2 - 12xi + 4i^2) = 6 - 9x^2 + 12xi + 4 = -9x^2 + 12xi + 10$$

REF: 061915aai NAT: N.CN.A.2 TOP: Operations with Complex Numbers

84 ANS: 2 REF: 011820aai NAT: S.IC.A.2 TOP: Analysis of Data

85 ANS: 2

$$0.254 \pm 2(0.060) \rightarrow (0.134, 0.374)$$

REF: 061913aai NAT: S.IC.B.5 TOP: Analysis of Data

86 ANS: 3

$$\frac{2}{3x+1} = \frac{1}{x} - \frac{6x}{3x+1} - \frac{1}{3} \text{ is extraneous.}$$

$$\frac{6x+2}{3x+1} = \frac{1}{x}$$

$$6x^2 + 2x = 3x + 1$$

$$6x^2 - x - 1 = 0$$

$$(2x - 1)(3x + 1) = 0$$

$$x = \frac{1}{2}, -\frac{1}{3}$$

REF: 011915aai NAT: A.REI.A.2 TOP: Solving Rationals

87 ANS: 4

$$p(5) = 2(5)^3 - 3(5) + 5 = 240$$

REF: 011819aai NAT: A.APR.B.2 TOP: Remainder Theorem

88 ANS: 4

$$(a + b + c)^2 = a^2 + ab + ac + ab + b^2 + bc + ac + ab + c^2$$

$$x = a^2 + b^2 + c^2 + 2(ab + bc + ac)$$

$$x = y + 2z$$

REF: 061822aai NAT: A.APR.C.4 TOP: Polynomial Identities

89 ANS: 1

$$(x^{\frac{3}{2}})^2 = x^3$$

REF: 061908aai NAT: N.RN.A.2 TOP: Radicals and Rational Exponents

KEY: variables

90 ANS: 2 REF: 081816aai NAT: F.IF.C.7 TOP: Graphing Logarithmic Functions

KEY: bimodalgraph

91 ANS: 4

$$(x - y)^2 = x^2 - 2xy + y^2 \quad (x + y)^3 = x^3 + 3x^2y + 3xy^2 + y^3$$

REF: 061902aai NAT: A.APR.C.4 TOP: Polynomial Identities

92 ANS: 4 REF: 081912aai NAT: F.IF.C.7 TOP: Graphing Trigonometric Functions

KEY: mixed

93 ANS: 1

$$(x + 7)(x - 1) = x^2 + 6x - 7 = x^2 + 6x + 9 - 7 - 9 = (x + 3)^2 - 16$$

REF: 061808aai NAT: A.APR.C.4 TOP: Polynomial Identities



94 ANS: 1

$$x - \frac{4}{x-1} = 2 \quad x = \frac{3 \pm \sqrt{(-3)^2 - 4(1)(-2)}}{2(1)} = \frac{3 \pm \sqrt{17}}{2}$$

$$x(x-1) - 4 = 2(x-1)$$

$$x^2 - x - 4 = 2x - 2$$

$$x^2 - 3x - 2 = 0$$

REF: 011812aii NAT: A.REI.A.2 TOP: Solving Rationals

KEY: rational solutions

95 ANS: 4

$$3x - (-2x + 14) = 16 \quad 3(6) - 4z = 2$$

$$5x = 30 \quad -4z = -16$$

$$x = 6 \quad z = 4$$

REF: 011803aii NAT: A.REI.C.6 TOP: Solving Linear Systems

KEY: three variables

96 ANS: 4

REF: 061907aii

NAT: A.APR.B.2

TOP: Remainder Theorem

97 ANS: 1

$$x - \frac{20}{x} = 8$$

$$x^2 - 8x - 20 = 0$$

$$(x-10)(x+2) = 0$$

$$x = 10, -2$$

REF: 061916aii NAT: A.CED.A.1 TOP: Modeling Rationals

98 ANS: 1

$$\begin{array}{r} 3x-1 \\ 3x+1 \overline{) 9x^2 + 0x - 2} \end{array}$$

$$\underline{9x^2 + 3x}$$

$$-3x - 2$$

$$\underline{-3x - 1}$$

$$-1$$

REF: 081910aii NAT: A.APR.D.6 TOP: Rational Expressions

KEY: division

99 ANS: 2

REF: 081908aii

NAT: F.IF.B.4

TOP: Graphing Polynomial Functions

100 ANS: 3

$$1.04^{\frac{1}{12}} \approx 1.0032737$$

REF: 011906aai NAT: A.SSE.B.3 TOP: Modeling Exponential Functions

101 ANS: 4

$$120 = 68 + (195 - 68)e^{-0.05t}$$

$$52 = 127e^{-0.05t}$$

$$\ln \frac{52}{127} = \ln e^{-0.05t}$$

$$\ln \frac{52}{127} = -0.05t$$

$$\frac{\ln \frac{52}{127}}{-0.05} = t$$

$$18 \approx t$$

REF: 081918aai NAT: F.LE.A.4 TOP: Exponential Decay

102 ANS: 4

$$\log 2^t = \log \sqrt{10} \quad 2) \frac{\log \sqrt{10}}{\log 2} = \log_2 \sqrt{10}, \quad 1) \log_2 \sqrt{10} = \log_2 10^{\frac{1}{2}} = \frac{1}{2} \log_2 10, \quad 3) \log_4 10 = \frac{\log_2 10}{\log_2 4} = \frac{1}{2} \log_2 10$$

$$t \log 2 = \log \sqrt{10}$$

$$t = \frac{\log \sqrt{10}}{\log 2}$$

REF: 012009aai NAT: F.LE.A.4 TOP: Exponential Equations

KEY: without common base

103 ANS: 4

$$(x^6 y^4 - 9)(x^4 - 16)$$

$$(x^3 y^2 + 3)(x^3 y^2 - 3)(x^2 + 4)(x^2 - 4)$$

REF: 081814aai NAT: A.SSE.A.2 TOP: Factoring Polynomials

KEY: factoring by grouping

104 ANS: 4

REF: 011801aai

NAT: S.IC.B.3

TOP: Analysis of Data

KEY: bias

105 ANS: 4

$$\log_2(x-1) - 1 = 0$$

$$\log_2(x-1) = 1$$

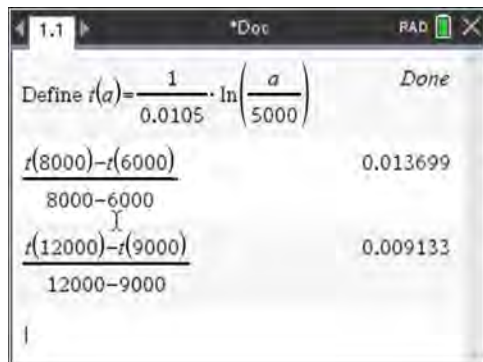
$$x-1 = 2^1$$

$$x = 3$$

REF: 061819aai NAT: F.IF.C.7

TOP: Graphing Logarithmic Functions

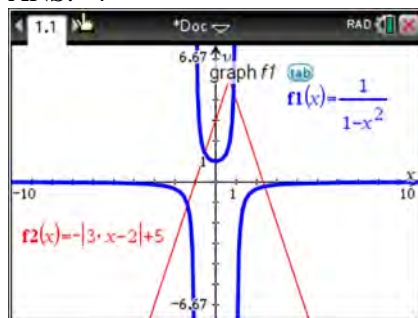
106 ANS: 3



REF: 081922aai NAT: F.IF.B.6

TOP: Rate of Change

107 ANS: 4



REF: 011924aai NAT: A.REI.D.11 TOP: Other Systems

108 ANS: 1

$$x^3 + 2x^2 - 9x - 18 = 0 \quad x^3 - 9x + 2x^2 - 18 = 0 \quad x^3 - 9x + 2x^2 - 18 = 0$$

$$x^2(x+2) - 9(x+2) = 0 \quad x(x^2-9) + 2(x^2-9) = 0 \quad x(x^2-9) + 2(x^2-9) = 0$$

$$(x+2)(x^2-9) = 0$$

REF: 011903aai NAT: A.APR.B.3 TOP: Solving Polynomial Equations

109 ANS: 3

$$y = 278(0.5)^{\frac{18}{1.8}} \approx 0.271$$

REF: 011920aai NAT: F.LE.A.2

TOP: Modeling Exponential Functions

110 ANS: 3

$$T(19) = 8 \sin(0.3(19) - 3) + 74 \approx 77$$

REF: 061922aai NAT: F.TF.A.2 TOP: Determining Trigonometric Functions

KEY: radians

111 ANS: 4

$$\sqrt{3x^2y} \cdot \sqrt[3]{27x^3y^2} = 3^{\frac{1}{2}}x^{\frac{1}{2}}y^{\frac{1}{2}} \cdot 3^{\frac{2}{3}}x^{\frac{2}{3}}y^{\frac{2}{3}} = 3^{\frac{3}{2}}x^2y^{\frac{7}{6}}$$

REF: 081914aai NAT: N.RN.A.2 TOP: Operations with Radicals

KEY: with variables, index &gt; 2

112 ANS: 2

REF: 011806aai

NAT: A.APR.C.4

TOP: Polynomial Identities

113 ANS: 3

REF: 081819aai

NAT: A.REI.D.11

TOP: Other Systems

114 ANS: 2

$$x = 4y + 5$$

$$x - 5 = 4y$$

$$\frac{1}{4}x - \frac{5}{4} = y$$

REF: 061909aai

NAT: F.BF.B.4

TOP: Inverse of Functions

KEY: linear

115 ANS: 2

REF: 061917aai

NAT: F.LE.B.5

TOP: Modeling Exponential Functions

116 ANS: 4

(1) quadratic has two roots and both are real  $(-2,0)$  and  $(-0.5,0)$ , (2)  $x = \pm\sqrt{32} - 3$ , (3) the real root is 3, with a multiplicity of 2, (4)  $x = \pm 4i$

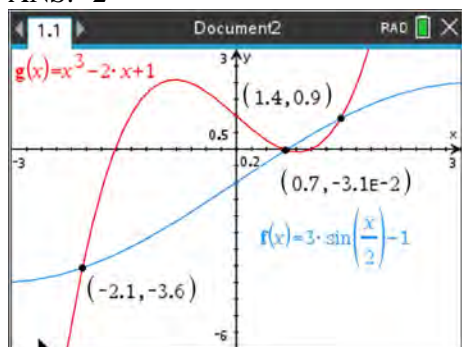
REF: 011909aai

NAT: A.REI.B.4

TOP: Using the Discriminant

KEY: determine nature of roots given equation, graph, table

117 ANS: 2



REF: 012021aai

NAT: A.REI.D.11

TOP: Other Systems

118 ANS: 4

REF: 061921aai

NAT: A.APR.B.3

TOP: Graphing Polynomial Functions

119 ANS: 3

between 000 and 449, inclusive  $\rightarrow \frac{450}{1000} = 45\%$

REF: 012024aai NAT: S.IC.B.3 TOP: Analysis of Data

KEY: type

120 ANS: 2

(1)  $0.4 \cdot 0.3 \neq 0.2$ , (2)  $0.8 \cdot 0.25 = 0.2$ , (3)  $P(A|B) = P(A) = 0.2$ , (4)  $0.2 \neq 0.15 \cdot 0.05$

$$0.2 \neq 0.2 \cdot 0.2$$

REF: 011912aai NAT: S.CP.A.3 TOP: Conditional Probability

121 ANS: 4

1 year = 365 days

REF: 061823aai NAT: A.SSE.B.3 TOP: Modeling Exponential Functions

122 ANS: 3 REF: 011824aai NAT: F.BF.A.2 TOP: Sequences

123 ANS: 2

$P(B) \cdot P(A|B) = P(A \text{ and } B)$

$$P(B) \cdot 0.8 = 0.2$$

$$P(B) = 0.25$$

REF: 081913aai NAT: S.CP.A.3 TOP: Conditional Probability

124 ANS: 4 REF: 012014aai NAT: S.IC.B.5 TOP: Analysis of Data

125 ANS: 4 REF: 061914aai NAT: A.REI.D.11 TOP: Other Systems

126 ANS: 1

$$\sqrt[4]{81x^8y^6} = 81^{\frac{1}{4}} x^{\frac{8}{4}} y^{\frac{6}{4}} = 3x^2y^{\frac{3}{2}}$$

REF: 012001aai NAT: N.RN.A.2 TOP: Radicals and Rational Exponents

KEY: variables

127 ANS: 2

$$S_{20} = \frac{.01 - .01(3)^{20}}{1 - 3} = 17,433,922$$

REF: 011822aai NAT: A.SSE.B.4 TOP: Series

128 ANS: 2

$$x = -6(y - 2)$$

$$-\frac{x}{6} = y - 2$$

$$-\frac{x}{6} + 2 = y$$

REF: 011821aai NAT: F.BF.B.4 TOP: Inverse of Functions

KEY: linear

129 ANS: 2

$$\text{If } \cos \theta = \frac{7}{25}, \sin \theta = \pm \frac{24}{25}, \text{ and } \tan \theta = \frac{\sin \theta}{\cos \theta} = \frac{-\frac{24}{25}}{\frac{7}{25}} = -\frac{24}{7}$$

REF: 081811aii NAT: F.TF.C.8 TOP: Determining Trigonometric Functions

130 ANS: 3 REF: 061906aii NAT: F.LE.A.2 TOP: Families of Functions

131 ANS: 4

$$\begin{array}{r} 5x^2 + x - 3 \\ 2x - 1 \overline{) 10x^3 - 3x^2 - 7x + 3} \\ \underline{10x^3 - 5x^2} \phantom{+ 3} \\ 2x^2 - 7x \phantom{+ 3} \\ \underline{2x^2 - x} \phantom{+ 3} \\ -6x + 3 \\ \underline{-6x + 3} \phantom{+ 3} \end{array}$$

REF: 011809aii NAT: A.APR.D.6 TOP: Rational Expressions

KEY: division

132 ANS: 4

$$\frac{n}{m} = \frac{\sqrt{a^5}}{a} = \frac{a^{\frac{5}{2}}}{a^{\frac{2}{2}}} = a^{\frac{3}{2}} = \sqrt{a^3}$$

REF: 011811aii NAT: N.RN.A.2 TOP: Radicals and Rational Exponents

KEY: variables

133 ANS: 2 REF: 061816aii NAT: F.IF.C.7 TOP: Graphing Polynomial Functions

KEY: bimodalgraph

134 ANS: 2

$$\begin{array}{l} u = x + 2 \quad u^2 + 4u + 3 \\ (u + 3)(u + 1) \\ (x + 2 + 3)(x + 2 + 1) \\ (x + 5)(x + 3) \end{array}$$

REF: 081901aii NAT: A.SSE.A.2 TOP: Factoring Polynomials

KEY: higher power

135 ANS: 3

$$e^{bt} = \frac{c}{a}$$

$$\ln e^{bt} = \ln \frac{c}{a}$$

$$bt \ln e = \ln \frac{c}{a}$$

$$t = \frac{\ln \frac{c}{a}}{b}$$

REF: 011813aai NAT: F.LE.A.4 TOP: Exponential Growth

136 ANS: 4

$$m^3 - 2m^2 + 4m - 8 = 0$$

$$m^2(m-2) + 4(m-2) = 0$$

$$(m^2 + 4)(m-2) = 0$$

REF: 081821aai NAT: A.APR.B.3 TOP: Solving Polynomial Equations

137 ANS: 4 REF: 012016aai NAT: F.IF.B.4 TOP: Graphing Trigonometric Functions

KEY: increasing/decreasing

138 ANS: 1

$$-4(-1) - 3 = 1 \quad 8 = \frac{2\pi}{b}$$

$$b = \frac{\pi}{4}$$

REF: 081820aai NAT: F.IF.B.4 TOP: Graphing Trigonometric Functions

KEY: maximum/minimum

139 ANS: 2

$$x^2 + 4x - 1 = x - 3 \quad y + 3 = -1$$

$$x^2 + 3x + 2 = 0 \quad y = -4$$

$$(x+2)(x+1) = 0$$

$$x = -2, -1$$

REF: 061801aai NAT: A.REI.C.7 TOP: Quadratic-Linear Systems

140 ANS: 3 REF: 011917aai NAT: F.BF.B.4 TOP: Inverse of Functions

KEY: other

141 ANS: 2

$$P = \frac{2\pi}{\frac{\pi}{45}} = 90$$

REF: 081822aii NAT: F.IF.C.7 TOP: Graphing Trigonometric Functions

KEY: period

142 ANS: 3 REF: 061910aii NAT: F.BF.A.2 TOP: Sequences

143 ANS: 4

$$a_1 = 2.5 + 0.5(1) = 3$$

REF: 011916aii NAT: F.BF.A.2 TOP: Sequences

144 ANS: 2 REF: 011804aii NAT: F.TF.A.2 TOP: Determining Trigonometric Functions

KEY: radians

145 ANS: 4

$$S_7 = \frac{85000 - 85000(1.06)^7}{1 - 1.06} \approx 713476.20$$

REF: 061905aii NAT: A.SSE.B.4 TOP: Series

146 ANS: 3 REF: 012002aii NAT: F.BF.A.1 TOP: Operations with Functions

147 ANS: 4 REF: 011805aii NAT: F.LE.B.5 TOP: Modeling Exponential Functions

148 ANS: 2 REF: 061804aii NAT: S.ID.B.6 TOP: Regression

KEY: choose model

149 ANS: 4

$$1 + \frac{.009}{12} = 1.00075$$

REF: 011918aii NAT: A.SSE.B.3 TOP: Modeling Exponential Functions

150 ANS: 4

$$x(x-2) \left( \frac{10}{x^2-2x} + \frac{4}{x} = \frac{5}{x-2} \right) \quad 2 \text{ is extraneous.}$$

$$10 + 4(x-2) = 5x$$

$$10 + 4x - 8 = 5x$$

$$2 = x$$

REF: 081915aii NAT: A.REI.A.2 TOP: Solving Rationals

KEY: rational solutions

151 ANS: 4 REF: 012008aii NAT: S.CP.A.3 TOP: Conditional Probability

152 ANS: 2 REF: 081911aii NAT: F.BF.B.3 TOP: Even and Odd Functions



153 ANS: 3

$$\begin{array}{r} 2x+1 \\ x+2 \overline{) 2x^2+5x+8} \\ \underline{2x^2+4x} \phantom{+8} \\ x+8 \\ \underline{x+2} \\ 6 \end{array}$$

REF: 012007aai NAT: A.APR.D.6 TOP: Rational Expressions  
KEY: division

154 ANS: 3

$$\begin{aligned} \sqrt{x+1} &= x+1 \\ x+1 &= x^2+2x+1 \\ 0 &= x^2+x \\ 0 &= x(x+1) \\ x &= -1, 0 \end{aligned}$$

REF: 011802aai NAT: A.REI.A.2 TOP: Solving Radicals  
KEY: extraneous solutions

155 ANS: 2

$$\begin{aligned} x+y-z &= 6 & 2x+2y-2z &= 12 & 5y-4z &= 31 & 5y-2(-4) &= 23 & x+3-(-4) &= 6 \\ -x+4y-z &= 17 & 2x-3y+2z &= -19 & 5y-2z &= 23 & 5y &= 15 & x &= -1 \\ 5y-2z &= 23 & 5y-4z &= 31 & -2z &= 8 & y &= 3 \\ & & & & z &= -4 \end{aligned}$$

REF: 061923aai NAT: A.REI.C.6 TOP: Solving Linear Systems  
KEY: three variables

156 ANS: 4 REF: 081817aai NAT: F.BF.B.3 TOP: Transformations with Functions

157 ANS: 4  
 $400 \cdot .954 \approx 380$ 

REF: 061918aai NAT: S.ID.A.4 TOP: Normal Distributions  
KEY: predict

158 ANS: 1

$$\frac{N(10)-N(1)}{10-1} \approx -2.03, \frac{N(20)-N(10)}{20-10} \approx -1.63, \frac{N(25)-N(15)}{25-15} \approx -1.46, \frac{N(30)-N(1)}{30-1} \approx -1.64$$

REF: 061807aai NAT: F.IF.B.6 TOP: Rate of Change

159 ANS: 4 REF: 011808aai NAT: A.SSE.B.3 TOP: Modeling Exponential Functions

160 ANS: 4

$$a = \frac{14-4}{2} = 5, d = \frac{14+4}{2} = 9$$

REF: 061810aai NAT: F.TF.B.5 TOP: Modeling Trigonometric Functions

161 ANS: 1

$$\frac{-12}{16} = \frac{9}{-12} = \frac{-6.75}{9}$$

REF: 012017aai NAT: F.IF.A.3 TOP: Sequences KEY: difference or ratio

162 ANS: 2

$$5x^2 - 4x + 2 = 0 \quad \frac{4 \pm \sqrt{(-4)^2 - 4(5)(2)}}{2(5)} = \frac{4 \pm \sqrt{-24}}{10} = \frac{4 \pm 2i\sqrt{6}}{10} = \frac{2 \pm i\sqrt{6}}{5}$$

REF: 012020aai NAT: A.REI.B.4 TOP: Solving Quadratics

KEY: complex solutions | quadratic formula

163 ANS: 4 REF: 081810aai NAT: F.BF.A.2 TOP: Sequences

164 ANS: 1

$$-\sqrt{1 - \left(-\frac{3}{4}\right)^2} = -\sqrt{\frac{16}{16} - \frac{9}{16}} = -\sqrt{\frac{7}{16}} = -\frac{\sqrt{7}}{4}$$

REF: 081905aai NAT: F.TF.C.8 TOP: Determining Trigonometric Functions

165 ANS: 3

$$(x+a)^2 + 5(x+a) + 4 \quad \text{let } u = x+a$$

$$u^2 + 5u + 4$$

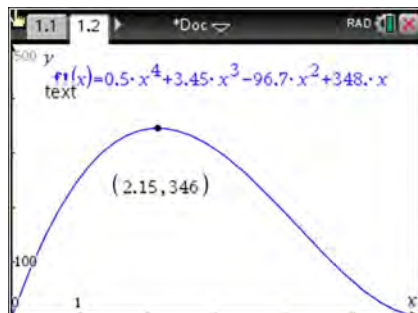
$$(u+4)(u+1)$$

$$(x+a+4)(x+a+1)$$

REF: 012006aai NAT: A.SSE.A.2 TOP: Factoring Polynomials

KEY: multivariable

166 ANS: 1



REF: 011908aai NAT: F.IF.B.4 TOP: Graphing Polynomial Functions

167 ANS: 1

$$2000 \left( 1 + \frac{.032}{12} \right)^{12t} \approx 2000(1.003)^{12t}$$

REF: 012004aia NAT: F.BF.A.1 TOP: Modeling Exponential Functions

168 ANS: 2

$$f(x) = f(-x)$$

$$x^2 - 4 = (-x)^2 - 4$$

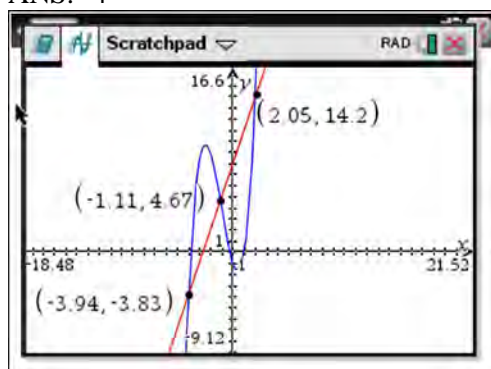
$$x^2 - 4 = x^2 - 4$$

REF: 061806aia NAT: F.BF.B.3 TOP: Even and Odd Functions

169 ANS: 4 REF: 081707aia NAT: F.TF.A.2 TOP: Reference Angles

KEY: bimodalgraph

170 ANS: 4



REF: 061622aia NAT: A.REI.D.11 TOP: Other Systems

## Algebra II Multiple Choice Regents Exam Questions

### Answer Section

171 ANS: 1

$$(x+3)^2 + (2x-4)^2 = 8 \quad b^2 - 4ac$$

$$x^2 + 6x + 9 + 4x^2 - 16x + 16 = 8 \quad 100 - 4(5)(17) < 0$$

$$5x^2 - 10x + 17 = 0$$

REF: 081719aai NAT: A.REI.C.7 TOP: Quadratic-Linear Systems

172 ANS: 1

The probability of rain equals the probability of rain, given that Sean pitches.

REF: 061611aai NAT: S.CP.A.3 TOP: Conditional Probability

173 ANS: 3

$$(m-2)^2(m+3) = (m^2 - 4m + 4)(m+3) = m^3 + 3m^2 - 4m^2 - 12m + 4m + 12 = m^3 - m^2 - 8m + 12$$

REF: 081605aai NAT: A.SSE.A.2 TOP: Factoring Polynomials

KEY: factoring by grouping

174 ANS: 4 REF: 081708aai NAT: A.APR.B.3 TOP: Solving Polynomial Equations

175 ANS: 4

If  $1-i$  is one solution, the other is  $1+i$ .  $(x-(1-i))(x-(1+i)) = 0$ 

$$x^2 - x - ix - x + ix + (1-i^2) = 0$$

$$x^2 - 2x + 2 = 0$$

REF: 081601aai NAT: A.REI.B.4 TOP: Complex Conjugate Root Theorem

176 ANS: 1 REF: 081616aai NAT: F.TF.A.1 TOP: Unit Circle

KEY: bimodalgraph

177 ANS: 3 REF: 061710aai NAT: S.IC.A.2 TOP: Analysis of Data

178 ANS: 4

	Bar Harbor	Phoenix
<b>Minimum</b>	31.386	66.491
<b>Midline</b>	55.3	86.729
<b>Maximum</b>	79.214	106.967
<b>Range</b>	47.828	40.476

REF: 061715aai NAT: F.IF.B.4 TOP: Graphing Trigonometric Functions

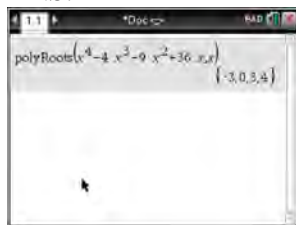
KEY: maximum/minimum

179 ANS: 2

$$\cos \theta = \pm \sqrt{1 - \left(\frac{-\sqrt{2}}{5}\right)^2} = \pm \sqrt{\frac{25}{25} - \frac{2}{25}} = \pm \frac{\sqrt{23}}{5}$$

REF: 061712aai NAT: F.TF.C.8 TOP: Determining Trigonometric Functions

180 ANS: 1



$$x^4 - 4x^3 - 9x^2 + 36x = 0$$

$$x^3(x - 4) - 9x(x - 4) = 0$$

$$(x^3 - 9x)(x - 4) = 0$$

$$x(x^2 - 9)(x - 4) = 0$$

$$x(x + 3)(x - 3)(x - 4) = 0$$

$$x = 0, \pm 3, 4$$

REF: 061606aai NAT: A.APR.B.3 TOP: Solving Polynomial Equations

181 ANS: 3

$$(3k - 2i)^2 = 9k^2 - 12ki + 4i^2 = 9k^2 - 12ki - 4$$

REF: 081702aai NAT: N.CN.A.2 TOP: Operations with Complex Numbers

182 ANS: 4

$$4x^2 = -98$$

$$x^2 = -\frac{98}{4}$$

$$x^2 = -\frac{49}{2}$$

$$x = \pm \sqrt{-\frac{49}{2}} = \pm \frac{7i}{\sqrt{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}} = \pm \frac{7i\sqrt{2}}{2}$$

REF: 061707aai NAT: A.REI.B.4 TOP: Solving Quadratics

KEY: complex solutions | taking square roots

183 ANS: 3 REF: 011710aai NAT: F.BF.A.1 TOP: Operations with Functions

184 ANS: 1

The car lost approximately 19% of its value each year.

REF: 081613aai NAT: F.LE.B.5 TOP: Modeling Exponential Functions

185 ANS: 1

The zeros of the polynomial are at  $-b$ , and  $c$ . The sketch of a polynomial of degree 3 with a negative leading coefficient should have end behavior showing as  $x$  goes to negative infinity,  $f(x)$  goes to positive infinity. The multiplicities of the roots are correctly represented in the graph.

REF: spr1501aai NAT: F.IF.C.7 TOP: Graphing Polynomial Functions

KEY: bimodalgraph

186 ANS: 1

$$\begin{array}{r|rrrrr} 2 & 1 & 0 & -4 & -4 & 8 \\ & & 2 & 4 & 0 & -8 \\ \hline & 1 & 2 & 0 & -4 & 0 \end{array}$$

Since there is no remainder when the quartic is divided by  $x - 2$ , this binomial is a factor.

REF: 061711aai NAT: A.APR.B.2 TOP: Remainder Theorem

187 ANS: 2

$h(x)$  does not have a  $y$ -intercept.

REF: 011719aai NAT: F.IF.C.9 TOP: Comparing Functions

188 ANS: 4

$$\text{period} = \frac{2\pi}{B}$$

$$\frac{1}{60} = \frac{2\pi}{B}$$

$$B = 120\pi$$

REF: 061624aai NAT: F.TF.B.5 TOP: Modeling Trigonometric Functions

189 ANS: 3

REF: 061722aai

NAT: A.CED.A.1 TOP: Modeling Rationals

190 ANS: 3

(3) repeats 3 times over  $2\pi$ .

REF: 011722aai NAT: F.IF.C.7 TOP: Graphing Trigonometric Functions

KEY: recognize | bimodalgraph

191 ANS: 1

$$x = \frac{-3 \pm \sqrt{3^2 - 4(2)(2)}}{2(2)} = \frac{-3 \pm \sqrt{-7}}{4} = -\frac{3}{4} \pm \frac{i\sqrt{7}}{4}$$

REF: 061612aai NAT: A.REI.B.4 TOP: Solving Quadratics

KEY: complex solutions | quadratic formula

192 ANS: 1

$$P(28) = 5(2)^{\frac{98}{28}} \approx 56$$

REF: 011702aai NAT: F.LE.A.2 TOP: Modeling Exponential Functions

193 ANS: 2

REF: 081717aai

NAT: S.IC.B.3 TOP: Analysis of Data

KEY: type

194 ANS: 3

$$\frac{1}{J} = \frac{1}{F} - \frac{1}{W}$$

$$\frac{1}{J} = \frac{W-F}{FW}$$

$$J = \frac{FW}{W-F}$$

REF: 081617aia NAT: A.REI.A.2 TOP: Solving Rationals

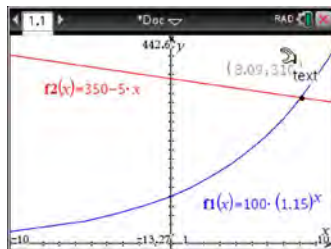
KEY: rational solutions

195 ANS: 2

$$ME = \left( z \sqrt{\frac{p(1-p)}{n}} \right) = \left( 1.96 \sqrt{\frac{(0.55)(0.45)}{900}} \right) \approx 0.03 \text{ or } \frac{1}{\sqrt{900}} \approx 0.03$$

REF: 081612aia NAT: S.IC.B.4 TOP: Analysis of Data

196 ANS: 2



REF: 011716aia NAT: A.REI.D.11 TOP: Other Systems

197 ANS: 3

Since  $x + 4$  is a factor of  $p(x)$ , there is no remainder.

REF: 081621aia NAT: A.APR.B.2 TOP: Remainder Theorem

198 ANS: 4

$$4(x^2 - 6x + 9) + 4(y^2 + 18y + 81) = 76 + 36 + 324$$

$$4(x - 3)^2 + 4(y + 9)^2 = 436$$

REF: 061619aia NAT: G.GPE.A.1 TOP: Equations of Circles

KEY: completing the square

199 ANS: 3

$$2d(d^3 + 3d^2 - 9d - 27)$$

$$2d(d^2(d+3) - 9(d+3))$$

$$2d(d^2 - 9)(d+3)$$

$$2d(d+3)(d-3)(d+3)$$

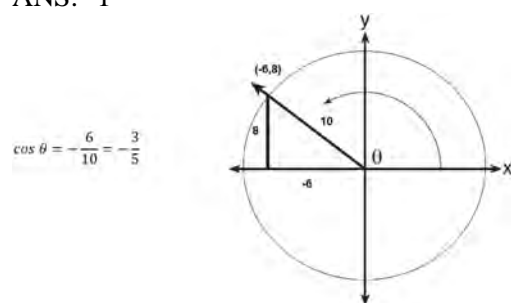
$$2d(d+3)^2(d-3)$$

REF: 081615aia NAT: A.SSE.A.2 TOP: Factoring Polynomials

KEY: factoring by grouping

200 ANS: 2 REF: 011701aia NAT: F.IF.B.4 TOP: Graphing Trigonometric Functions

201 ANS: 1



REF: 061617aia NAT: F.TF.A.2 TOP: Determining Trigonometric Functions

KEY: extension to reals

202 ANS: 2

$$x = -\frac{3}{4}y + 2$$

$$-4x = 3y - 8$$

$$-4x + 8 = 3y$$

$$-\frac{4}{3}x + \frac{8}{3} = y$$

REF: 061616aia NAT: F.BF.B.4 TOP: Inverse of Functions

KEY: linear

203 ANS: 3

The graph shows three real zeros, and has end behavior matching the given end behavior.

REF: 061604aia NAT: F.IF.C.7 TOP: Graphing Polynomial Functions

KEY: bimodalgraph



204 ANS: 2

$$\sqrt{x+14} = \sqrt{2x+5} + 1 \qquad \sqrt{22+14} - \sqrt{2(22)+5} = 1$$

$$x+14 = 2x+5+2\sqrt{2x+5}+1 \qquad 6-7 \neq 1$$

$$-x+8 = 2\sqrt{2x+5}$$

$$x^2 - 16x + 64 = 8x + 20$$

$$x^2 - 24x + 44 = 0$$

$$(x-22)(x-2) = 0$$

$$x = 2, 22$$

REF: 081704aii NAT: A.REI.A.2 TOP: Solving Radicals

KEY: advanced

205 ANS: 3

REF: 081618aii NAT: F.LE.A.2 TOP: Sequences

KEY: recursive

206 ANS: 4

$$\frac{m(c)}{g(c)} = \frac{c+1}{1-c^2} = \frac{c+1}{(1+c)(1-c)} = \frac{1}{1-c}$$

REF: 061608aii NAT: F.BF.A.1 TOP: Operations with Functions

207 ANS: 4

The vertex is (1,0) and  $p = 2$ .  $y = \frac{1}{4(2)}(x-1)^2 + 0$

REF: 061717aii NAT: G.GPE.A.2 TOP: Graphing Quadratic Functions

208 ANS: 1



REF: 081711aii NAT: S.ID.A.4 TOP: Normal Distributions

KEY: percent

209 ANS: 4

$$\left( \frac{-54x^9}{y^4} \right)^{\frac{2}{3}} = \frac{(2 \cdot -27)^{\frac{2}{3}} x^{\frac{18}{3}}}{y^{\frac{8}{3}}} = \frac{2^{\frac{2}{3}} \cdot 9x^6}{y^2 \cdot y^{\frac{2}{3}}} = \frac{9x^6 \sqrt[3]{4}}{y^2 \sqrt[3]{y^2}}$$

REF: 081723aii NAT: N.RN.A.2 TOP: Radicals and Rational Exponents

KEY: variables

210 ANS: 2



$\bar{x} + 2\sigma$  represents approximately 48% of the data.

REF: 061609aia NAT: S.ID.A.4 TOP: Normal Distributions

KEY: percent

211 ANS: 3

Self selection causes bias.

REF: 061703aia NAT: S.IC.B.3 TOP: Analysis of Data

KEY: bias

212 ANS: 1

$$(1) \frac{9-0}{2-1} = 9 \quad (2) \frac{17-0}{3.5-1} = 6.8 \quad (3) \frac{0-0}{5-1} = 0 \quad (4) \frac{17--5}{3.5-1} \approx 6.3$$

REF: 011724aia NAT: F.IF.B.6 TOP: Rate of Change

213 ANS: 3

$$x^2 + 2x + 1 = -5 + 1$$

$$(x + 1)^2 = -4$$

$$x + 1 = \pm 2i$$

$$x = -1 \pm 2i$$

REF: 081703aia NAT: A.REI.B.4 TOP: Solving Quadratics

KEY: complex solutions | completing the square

214 ANS: 4 REF: 061716aia NAT: N.RN.A.2 TOP: Radicals and Rational Exponents

KEY: variables

215 ANS: 2

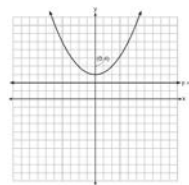
The vertex of the parabola is (0,0). The distance,  $p$ , between the vertex and the focus or the vertex and thedirectrix is 1.  $y = \frac{-1}{4p}(x-h)^2 + k$ 

$$y = \frac{-1}{4(1)}(x-0)^2 + 0$$

$$y = -\frac{1}{4}x^2$$

REF: 081706aia NAT: G.GPE.A.2 TOP: Graphing Quadratic Functions

216 ANS: 4



A parabola with a focus of  $(0,4)$  and a directrix of  $y = 2$  is sketched as follows: By inspection, it is determined that the vertex of the parabola is  $(0,3)$ . It is also evident that the distance,  $p$ , between the vertex and the focus is 1. It is possible to use the formula  $(x - h)^2 = 4p(y - k)$  to derive the equation of the parabola as follows:  $(x - 0)^2 = 4(1)(y - 3)$

$$x^2 = 4y - 12$$

$$x^2 + 12 = 4y$$

$$\frac{x^2}{4} + 3 = y$$

or A point  $(x,y)$  on the parabola must be the same distance from the focus as it is from the directrix. For any such point  $(x,y)$ , the distance to the focus is  $\sqrt{(x-0)^2 + (y-4)^2}$  and the distance to the directrix is  $y - 2$ . Setting this equal leads to:  $x^2 + y^2 - 8y + 16 = y^2 - 4y + 4$

$$x^2 + 16 = 4y + 4$$

$$\frac{x^2}{4} + 3 = y$$

REF: spr1502aii NAT: G.GPE.A.2 TOP: Graphing Quadratic Functions

217 ANS: 4 REF: 061601aii NAT: N.RN.A.2 TOP: Radicals and Rational Exponents

KEY: variables

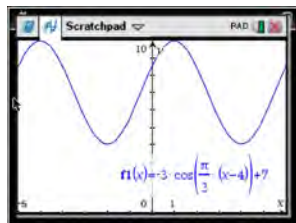
218 ANS: 2

$$6xi^3(-4xi + 5) = -24x^2i^4 + 30xi^3 = -24x^2(1) + 30x(-1) = -24x^2 - 30xi$$

REF: 061704aii NAT: N.CN.A.2 TOP: Operations with Complex Numbers

219 ANS: 1 REF: 011704aii NAT: F.TF.C.8 TOP: Simplifying Trigonometric Expressions

220 ANS: 4



As the range is  $[4,10]$ , the midline is  $y = \frac{4 + 10}{2} = 7$ .

REF: fall1506aii NAT: F.IF.C.7 TOP: Graphing Trigonometric Functions

KEY: mixed

221 ANS: 3 REF: 061602aii NAT: A.CED.A.1 TOP: Modeling Rationals

222 ANS: 2

$$\begin{array}{r}
 2x^2 - 3x + 7 \\
 2x + 3 \overline{) 4x^3 + 0x^2 + 5x + 10} \\
 \underline{4x^3 + 6x^2} \phantom{+ 5x + 10} \\
 -6x^2 + 5x \phantom{+ 10} \\
 \underline{-6x^2 - 9x} \phantom{+ 10} \\
 14x + 10 \\
 \underline{14x + 21} \\
 -11
 \end{array}$$

REF: 061614aai NAT: A.APR.D.6 TOP: Rational Expressions

KEY: division

223 ANS: 4

$$(1) \frac{B(60) - B(10)}{60 - 10} \approx 28\% \quad (2) \frac{B(69) - B(19)}{69 - 19} \approx 33\% \quad (3) \frac{B(72) - B(36)}{72 - 36} \approx 38\% \quad (4) \frac{B(73) - B(60)}{73 - 60} \approx 46\%$$

REF: 011721aai NAT: F.IF.B.6 TOP: Rate of Change

224 ANS: 2

$$\frac{212}{1334} \approx .16 \quad ME = \left( z \sqrt{\frac{p(1-p)}{n}} \right) = \left( 1.96 \sqrt{\frac{(0.16)(0.84)}{1334}} \right) \approx 0.02 \quad \text{or} \quad \frac{1}{\sqrt{1334}} \approx .027$$

REF: 081716aai NAT: S.IC.B.4 TOP: Analysis of Data

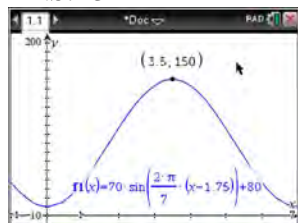
225 ANS: 1 REF: 061708aai NAT: F.TF.B.5 TOP: Modeling Trigonometric Functions

226 ANS: 3

The pattern suggests an exponential pattern, not linear or sinusoidal. A 4% growth rate is accurate, while a 43% growth rate is not.

REF: 011713aai NAT: S.ID.B.6 TOP: Regression KEY: choose model

227 ANS: 3



$H(t)$  is at a minimum at  $70(-1) + 80 = 10$

REF: 061613aai NAT: F.IF.B.4 TOP: Graphing Trigonometric Functions

KEY: maximum/minimum

228 ANS: 3

REF: 011706aai NAT: S.IC.B.3 TOP: Analysis of Data

KEY: type

229 ANS: 3

$f(x) = -f(x)$ , so  $f(x)$  is odd.  $g(-x) \neq g(x)$ , so  $g(x)$  is not even.  $g(-x) \neq -g(x)$ , so  $g(x)$  is not odd.  $h(-x) = h(x)$ , so  $h(x)$  is even.

REF: fall1502aii NAT: F.BF.B.3 TOP: Even and Odd Functions

230 ANS: 1

$$\frac{157}{25 + 47 + 157}$$

REF: 081607aii NAT: S.CP.A.4 TOP: Conditional Probability

231 ANS: 4 REF: 081622aii NAT: F.BF.A.1 TOP: Modeling Exponential Functions

232 ANS: 1

$$\frac{A}{P} = e^{rt}$$

$$0.42 = e^{rt}$$

$$\ln 0.42 = \ln e^{rt}$$

$$-0.87 \approx rt$$

REF: 011723aii NAT: F.BF.A.1 TOP: Modeling Exponential Functions

233 ANS: 4

$$(x+y)^3 = x^3 + 3x^2y + 3xy^2 + y^3 \neq x^3 + 3xy + y^3$$

REF: 081620aii NAT: A.APR.C.4 TOP: Polynomial Identities

234 ANS: 2 REF: 061724aii NAT: A.SSE.B.4 TOP: Series

235 ANS: 1

$$\frac{2(x-4)}{(x+3)(x-4)} + \frac{3(x+3)}{(x-4)(x+3)} = \frac{2x-2}{x^2-x-12}$$

$$2x - 8 + 3x + 9 = 2x - 2$$

$$3x = -3$$

$$x = -1$$

REF: 011717aii NAT: A.REI.A.2 TOP: Solving Rationals

KEY: rational solutions

236 ANS: 1 REF: 081722aii NAT: S.IC.B.6 TOP: Analysis of Data

237 ANS: 2

The events are independent because  $P(A \text{ and } B) = P(A) \cdot P(B)$ .

$$0.125 = 0.5 \cdot 0.25$$

If  $P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B) = 0.25 + 0.5 - .125 = 0.625$ , then the events are not mutually exclusive because  $P(A \text{ or } B) \neq P(A) + P(B)$

$$0.625 \neq 0.5 + 0.25$$

REF: 061714aii NAT: S.CP.B.7 TOP: Theoretical Probability

238 ANS: 3

$$0.75^{\frac{1}{10}} \approx .9716$$

REF: 061713aii NAT: A.SSE.B.3 TOP: Modeling Exponential Functions

239 ANS: 4 REF: 081624aii NAT: F.BF.A.2 TOP: Sequences

240 ANS: 2

Combining (1) and (3):  $-6c = -18$  Combining (1) and (2):  $5a + 3c = -1$  Using (3):  $-(-2) - 5b - 5(3) = 2$ 

$$c = 3$$

$$5a + 3(3) = -1$$

$$2 - 5b - 15 = 2$$

$$5a = -10$$

$$b = -3$$

$$a = -2$$

REF: 081623aii NAT: A.REI.C.6 TOP: Solving Linear Systems

KEY: three variables

241 ANS: 3

$$\sqrt{56-x} = x \quad -8 \text{ is extraneous.}$$

$$56 - x = x^2$$

$$0 = x^2 + x - 56$$

$$0 = (x + 8)(x - 7)$$

$$x = 7$$

REF: 061605aii NAT: A.REI.A.2 TOP: Solving Radicals

KEY: extraneous solutions

242 ANS: 2

$$B(t) = 750 \left( 1.16^{\frac{1}{12}} \right)^{12t} \approx 750(1.012)^{12t} \quad B(t) = 750 \left( 1 + \frac{0.16}{12} \right)^{12t} \text{ is wrong, because the growth is an annual rate}$$

that is not compounded monthly.

REF: spr1504aii NAT: A.SSE.B.3 TOP: Modeling Exponential Functions

243 ANS: 3 REF: 011708aii NAT: F.BF.B.4 TOP: Inverse of Functions

KEY: other

244 ANS: 1  
 $8(2^{x+3}) = 48$

$$2^{x+3} = 6$$

$$(x+3)\ln 2 = \ln 6$$

$$x+3 = \frac{\ln 6}{\ln 2}$$

$$x = \frac{\ln 6}{\ln 2} - 3$$

REF: 061702aia NAT: F.LE.A.4 TOP: Exponential Equations

KEY: without common base

245 ANS: 1  
 The graph of  $y = \sin x$  is unchanged when rotated  $180^\circ$  about the origin.

REF: 081614aia NAT: F.BF.B.3 TOP: Even and Odd Functions

246 ANS: 3  
 $1.0525^{\frac{1}{12}} \approx 1.00427$

REF: 061621aia NAT: F.BF.A.1 TOP: Modeling Exponential Functions

247 ANS: 1 REF: 081609aia NAT: F.BF.B.6 TOP: Sigma Notation

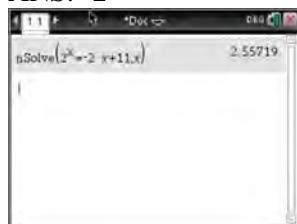
KEY: represent

248 ANS: 2 REF: 011709aia NAT: S.IC.B.5 TOP: Analysis of Data

249 ANS: 3 REF: 061720aia NAT: F.LE.A.2 TOP: Sequences

KEY: explicit

250 ANS: 2



REF: 081603aia NAT: A.REI.D.11 TOP: Other Systems

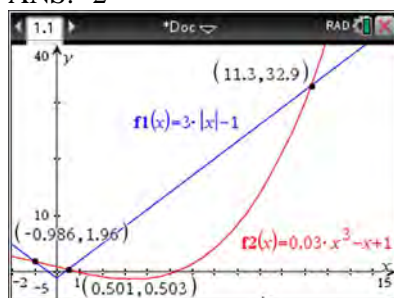
251 ANS: 4  

$$x = \frac{8 \pm \sqrt{(-8)^2 - 4(6)(29)}}{2(6)} = \frac{8 \pm \sqrt{-632}}{12} = \frac{8 \pm i\sqrt{4}\sqrt{158}}{12} = \frac{2}{3} \pm \frac{1}{6}i\sqrt{158}$$

REF: 011711aia NAT: A.REI.B.4 TOP: Solving Quadratics

KEY: complex solutions | quadratic formula

252 ANS: 2



REF: 061705aai NAT: A.REI.D.11 TOP: Other Systems

253 ANS: 2

$$\begin{array}{r}
 x^2 + 0x + 1 \\
 x + 2 \overline{) x^3 + 2x^2 + x + 6} \\
 \underline{x^3 + 2x^2} \phantom{+ x + 6} \\
 0x^2 + x \phantom{+ 6} \\
 \underline{0x^2 + 0x} \phantom{+ 6} \\
 x + 6 \\
 \underline{x + 2} \\
 4
 \end{array}$$

REF: 081611aai NAT: A.APR.D.6 TOP: Rational Expressions

KEY: division

254 ANS: 3

$$\frac{f(7) - f(-7)}{7 - (-7)} = \frac{2^{-0.25(7)} \cdot \sin\left(\frac{\pi}{2}(7)\right) - 2^{-0.25(-7)} \cdot \sin\left(\frac{\pi}{2}(-7)\right)}{14} \approx -0.26$$

REF: 061721aai NAT: F.IF.B.6 TOP: Rate of Change

255 ANS: 4

$$496 \pm 2(115)$$

REF: 011718aai NAT: S.ID.A.4 TOP: Normal Distributions

KEY: interval



256 ANS: 3



REF: 081604aai NAT: S.ID.A.4 TOP: Normal Distributions

KEY: probability

257 ANS: 4

$$x(x+7) \left[ \frac{3x+25}{x+7} - 5 = \frac{3}{x} \right]$$

$$x(3x+25) - 5x(x+7) = 3(x+7)$$

$$3x^2 + 25x - 5x^2 - 35x = 3x + 21$$

$$2x^2 + 13x + 21 = 0$$

$$(2x+7)(x+3) = 0$$

$$x = -\frac{7}{2}, -3$$

REF: fall1501aai NAT: A.REI.A.2 TOP: Solving Rationals

KEY: rational solutions

258 ANS: 4

$$d = 32(.8)^{b-1} \quad S_n = \frac{32 - 32(.8)^{12}}{1 - .8} \approx 149$$

REF: 081721aai NAT: A.SSE.B.4 TOP: Series

259 ANS: 3

$$d = 10 \log \frac{6.3 \times 10^{-3}}{1.0 \times 10^{-12}} \approx 98$$

REF: 011715aai NAT: F.IF.B.4 TOP: Evaluating Logarithmic Expressions

260 ANS: 2

$$(2-yi)(2-yi) = 4 - 4yi + y^2 i^2 = -y^2 - 4yi + 4$$

REF: 061603aai NAT: N.CN.A.2 TOP: Operations with Complex Numbers

261 ANS: 1

$$\begin{array}{r}
 3x^2 + 4x - 1 \\
 2x + 3 \overline{) 6x^3 + 17x^2 + 10x + 2} \\
 \underline{6x^3 + 9x^2} \phantom{+ 10x + 2} \\
 8x^2 + 10x \phantom{+ 2} \\
 \underline{8x^2 + 12x} \phantom{+ 2} \\
 -2x + 2 \\
 \underline{-2x - 3} \\
 5
 \end{array}$$

REF: fall1503aii NAT: A.APR.D.6 TOP: Rational Expressions

KEY: division

262 ANS: 3

$$-33t^2 + 360t = 700 + 5t$$

$$-33t^2 + 355t - 700 = 0$$

$$t = \frac{-355 \pm \sqrt{355^2 - 4(-33)(-700)}}{2(-33)} \approx 3,8$$

REF: 081606aii NAT: A.REI.D.11 TOP: Quadratic-Linear Systems

263 ANS: 1

1) let  $y = x + 2$ , then  $y^2 + 2y - 8$ 

$$(y + 4)(y - 2)$$

$$(x + 2 + 4)(x + 2 - 2)$$

$$(x + 6)x$$

REF: 081715aii NAT: A.SSE.A.2 TOP: Factoring Polynomials

KEY: multivariable

264 ANS: 2 REF: 061620aii NAT: F.IF.B.4 TOP: Graphing Polynomial Functions

265 ANS: 2 REF: 011720aii NAT: A.APR.B.2 TOP: Remainder Theorem

266 ANS: 4

$$m^5 + m^3 - 6m = m(m^4 + m^2 - 6) = m(m^2 + 3)(m^2 - 2)$$

REF: 011703aii NAT: A.SSE.A.2 TOP: Factoring Polynomials

KEY: higher power

267 ANS: 1

$$d = 18; r = \pm \frac{5}{4}$$

REF: 011714aii NAT: F.IF.A.3 TOP: Sequences KEY: explicit

268 ANS: 2

$$\begin{aligned}
 x(30 - 0.01x) - (0.15x^3 + 0.01x^2 + 2x + 120) &= 30x - 0.01x^2 - 0.15x^3 - 0.01x^2 - 2x - 120 \\
 &= -0.15x^3 - 0.02x^2 + 28x - 120
 \end{aligned}$$

REF: 061709aii NAT: F.BF.A.1 TOP: Operations with Functions

269 ANS: 1

$$\frac{2x}{x-2} \left( \frac{x}{x} \right) - \frac{11}{x} \left( \frac{x-2}{x-2} \right) = \frac{8}{x^2 - 2x}$$

$$2x^2 - 11x + 22 = 8$$

$$2x^2 - 11x + 14 = 0$$

$$(2x - 7)(x - 2) = 0$$

$$x = \frac{7}{2}, 2$$

REF: 061719aai NAT: A.REI.A.2 TOP: Solving Rationals

270 ANS: 1 REF: 061701aai NAT: A.APR.B.3 TOP: Graphing Polynomial Functions

271 ANS: 3 REF: 081724aai NAT: F.BF.A.2 TOP: Sequences

272 ANS: 2 REF: 081610aai NAT: F.IF.B.4 TOP: Graphing Trigonometric Functions

KEY: increasing/decreasing

273 ANS: 3 REF: 081705aai NAT: F.IF.B.4 TOP: Graphing Trigonometric Functions

KEY: increasing/decreasing

274 ANS: 4

The scenario represents a decreasing geometric sequence with a common ratio of 0.80.

REF: 061610aai NAT: F.BF.A.2 TOP: Sequences

275 ANS: 2

$$x = \frac{y+1}{y-2}$$

$$xy - 2x = y + 1$$

$$xy - y = 2x + 1$$

$$y(x - 1) = 2x + 1$$

$$y = \frac{2x+1}{x-1}$$

REF: 081714aai NAT: F.BF.B.4 TOP: Inverse of Functions

KEY: other

276 ANS: 4

$$y = g(x) = (x-2)^2 \quad (x-2)^2 = 3x-2 \quad y = 3(6)-2 = 16$$

$$x^2 - 4x + 4 = 3x - 2 \quad y = 3(1) - 2 = 1$$

$$x^2 - 7x + 6 = 0$$

$$(x-6)(x-1) = 0$$

$$x = 6, 1$$

REF: 011705aai NAT: A.REI.C.7 TOP: Quadratic-Linear Systems

277 ANS: 2

$$\begin{array}{r|rrrr} -4 & 1 & -11 & 16 & 84 \\ & & -4 & 60 & -304 \\ \hline & 1 & -15 & 76 & \end{array}$$

Since there is a remainder when the cubic is divided by  $x + 4$ , this binomial is not a factor.

REF: 081720aai NAT: A.APR.B.2 TOP: Remainder Theorem

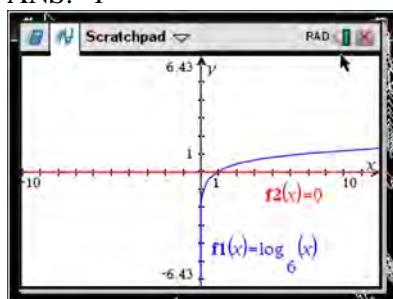
278 ANS: 1

$$\begin{array}{r} 2x^2 + x + 5 \\ 2x - 1 \overline{) 4x^3 + 0x^2 + 9x - 5} \\ \underline{4x^3 - 2x^2} \phantom{- 5} \\ 2x^2 + 9x \phantom{- 5} \\ \underline{2x^2 - x} \phantom{- 5} \\ 10x - 5 \\ \underline{10x - 5} \\ 0 \end{array}$$

REF: 081713aai NAT: A.APR.D.6 TOP: Rational Expressions

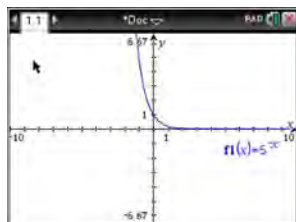
KEY: division

279 ANS: 1



REF: 061618aai NAT: F.IF.C.7 TOP: Graphing Logarithmic Functions

280 ANS: 4



$$y = 5^{-x} = \left(\frac{1}{5}\right)^x$$

REF: 061615aai NAT: F.IF.C.7 TOP: Graphing Exponential Functions

281 ANS: 3

$$-2\left(-\frac{1}{2}x^2 = -6x + 20\right)$$

$$x^2 - 12x = -40$$

$$x^2 - 12x + 36 = -40 + 36$$

$$(x - 6)^2 = -4$$

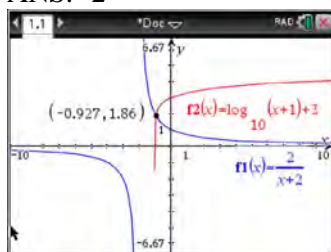
$$x - 6 = \pm 2i$$

$$x = 6 \pm 2i$$

REF: fall1504aii NAT: A.REI.B.4 TOP: Solving Quadratics

KEY: complex solutions | completing the square

282 ANS: 2



REF: 011712aii NAT: A.REI.D.11 TOP: Other Systems

283 ANS: 4

$$\frac{-3x^2 - 5x + 2}{x^3 + 2x^2} = \frac{(-3x + 1)(x + 2)}{x^2(x + 2)} = \frac{-3x}{x^2} + \frac{1}{x^2} = -3x^{-1} + x^{-2}$$

REF: 061723aii NAT: A.APR.D.6 TOP: Expressions with Negative Exponents

KEY: variables

284 ANS: 4

$$k^4 - 4k^2 + 8k^3 - 32k + 12k^2 - 48$$

$$k^2(k^2 - 4) + 8k(k^2 - 4) + 12(k^2 - 4)$$

$$(k^2 - 4)(k^2 + 8k + 12)$$

$$(k + 2)(k - 2)(k + 6)(k + 2)$$

REF: fall1505aii NAT: A.SSE.A.2 TOP: Factoring Polynomials

KEY: factoring by grouping

285 ANS: 1

$$x^2 + 2x - 8 = 0$$

$$(x + 4)(x - 2) = 0$$

$$x = -4, 2$$

REF: 081701aii NAT: A.APR.D.6 TOP: Undefined Rationals

286 ANS: 3 REF: 061623aii NAT: F.BF.A.2 TOP: Sequences

287 ANS: 3

$$\left(\frac{1}{2}\right)^{\frac{1}{73.83}} \approx 0.990656$$

REF: 081710aii NAT: A.SSE.B.3 TOP: Modeling Exponential Functions

288 ANS: 3 REF: 061607aii NAT: S.IC.A.2 TOP: Analysis of Data

289 ANS: 4

The maximum volume of  $p(x) = -(x+2)(x-10)(x-14)$  is about 56, at  $x = 12.1$

REF: 081712aii NAT: F.IF.B.4 TOP: Graphing Polynomial Functions

290 ANS: 1

II. Ninth graders drive to school less often; III. Students know little about adults; IV. Calculus students love math!

REF: 081602aii NAT: S.IC.B.3 TOP: Analysis of Data

KEY: bias

291 ANS: 1

(2) is not recursive

REF: 081608aii NAT: F.LE.A.2 TOP: Sequences KEY: recursive

292 ANS: 4 REF: 081718aii NAT: F.IF.C.7 TOP: Graphing Trigonometric Functions

KEY: amplitude

293 ANS: 2

$$\left(m^{\frac{5}{3}}\right)^{-\frac{1}{2}} = m^{-\frac{5}{6}} = \frac{1}{\sqrt[6]{m^5}}$$

REF: 011707aii NAT: N.RN.A.2 TOP: Radicals and Rational Exponents

KEY: variables

294 ANS: 4 REF: 061706aii NAT: F.IF.B.4 TOP: Graphing Trigonometric Functions

295 ANS: 3

$$\log_{0.8}\left(\frac{V}{17000}\right) = t \quad \frac{17,000(0.8)^3 - 17,000(0.8)^1}{3-1} \approx -2450$$

$$0.8^t = \frac{V}{17000}$$

$$V = 17000(0.8)^t$$

REF: 081709aii NAT: F.IF.B.6 TOP: Rate of Change

296 ANS: 2

The 2010 population is 110 million.

REF: 061718aii NAT: F.LE.B.5 TOP: Modeling Exponential Functions

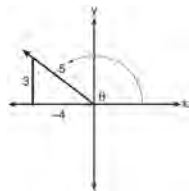
297 ANS: 4

The vertex is  $(2, -1)$  and  $p = 2$ .  $y = -\frac{1}{4(2)}(x - 2)^2 - 1$

REF: 081619aia NAT: G.GPE.A.2 TOP: Graphing Quadratic Functions

298 ANS: 1

A reference triangle can be sketched using the coordinates  $(-4, 3)$  in the second quadrant to find the value of  $\sin \theta$ .



REF: spr1503aia NAT: F.TF.A.2 TOP: Determining Trigonometric Functions

KEY: extension to reals

## Algebra II 2 Point Regents Exam Questions

### Answer Section

299 ANS:

Based on these data, the two events do not appear to be independent.  $P(F) = \frac{106}{200} = 0.53$ , while

$P(F|T) = \frac{54}{90} = 0.6$ ,  $P(F|R) = \frac{25}{65} = 0.39$ , and  $P(F|C) = \frac{27}{45} = 0.6$ . The probability of being female are not the same as the conditional probabilities. This suggests that the events are not independent.

REF: fall1508aai NAT: S.CP.A.4 TOP: Conditional Probability

300 ANS:

sample: pails of oranges; population: truckload of oranges. It is likely that about 5% of all the oranges are unsatisfactory.

REF: 011726aai NAT: S.IC.A.2 TOP: Analysis of Data

301 ANS:

$$P(W/D) = \frac{P(W \cap D)}{P(D)} = \frac{.4}{.5} = .8$$

REF: 081726aai NAT: S.CP.B.6 TOP: Conditional Probability

302 ANS:

Amplitude, because the height of the graph shows the volume of the air.

REF: 081625aai NAT: F.IF.C.7 TOP: Graphing Trigonometric Functions

KEY: mixed

303 ANS:

$$x^2(4x - 1) + 4(4x - 1) = (x^2 + 4)(4x - 1)$$

REF: 061727aai NAT: A.SSE.A.2 TOP: Factoring Polynomials

KEY: factoring by grouping

304 ANS:

$$(1 - i)(1 - i)(1 - i) = (1 - 2i + i^2)(1 - i) = -2i(1 - i) = -2i + 2i^2 = -2 - 2i$$

REF: 011725aai NAT: N.CN.A.2 TOP: Operations with Complex Numbers

305 ANS:

The expression is of the form  $y^2 - 5y - 6$  or  $(y - 6)(y + 1)$ . Let  $y = 4x^2 + 5x$ :

$$(4x^2 + 5x - 6)(4x^2 + 5x + 1)$$

$$(4x - 3)(x + 2)(4x + 1)(x + 1)$$

REF: fall1512aai NAT: A.SSE.A.2 TOP: Factoring Polynomials

KEY:  $a > 1$



306 ANS:

$$a_1 = 4$$

$$a_n = 3a_{n-1}$$

REF: 081931aii NAT: F.LE.A.2 TOP: Sequences KEY: recursive

307 ANS:

Light wave C. The periods for A, B, and C are 280, 220 and 320.

REF: 012030aii NAT: F.IF.C.7 TOP: Graphing Trigonometric Functions

KEY: period

308 ANS:

Self selection is a cause of bias because people with more free time are more likely to respond.

REF: 061828aii NAT: S.IC.B.3 TOP: Analysis of Data

KEY: bias

309 ANS:

$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$
 A and B are independent since  $P(A \cap B) = P(A) \cdot P(B)$ 

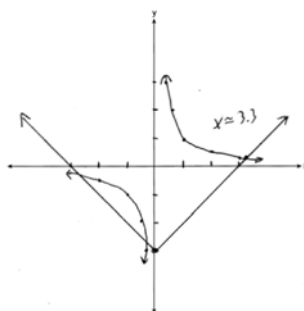
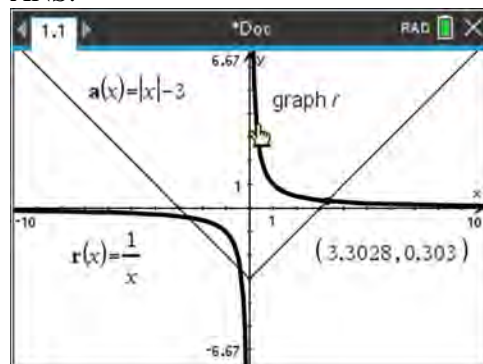
$$0.8 = 0.6 + 0.5 - P(A \cap B) \qquad 0.3 = 0.6 \cdot 0.5$$

$$P(A \cap B) = 0.3 \qquad 0.3 = 0.3$$

REF: 081632aii NAT: S.CP.A.2 TOP: Probability of Compound Events

KEY: independence

310 ANS:



REF: 081932aii NAT: A.REI.D.11 TOP: Other Systems

311 ANS:

period is  $\frac{2}{3}$ . The wheel rotates once every  $\frac{2}{3}$  second.

REF: 061728aii NAT: F.IF.C.7 TOP: Graphing Trigonometric Functions

KEY: period

312 ANS:

$\csc \theta = \frac{1}{\sin \theta}$ , and  $\sin \theta$  on a unit circle represents the  $y$  value of a point on the unit circle. Since  $y = \sin \theta$ ,

$$\csc \theta = \frac{1}{y}.$$

REF: 011727aii NAT: F.TF.A.2 TOP: Reciprocal Trigonometric Relationships

313 ANS:

$$4\% \quad 8.75 = 1.25(1+r)^{49} \quad \text{or} \quad 8.75 = 1.25e^{49r}$$

$$7 = (1+r)^{49} \quad \ln 7 = \ln e^{49r}$$

$$r+1 = \sqrt[49]{7} \quad \ln 7 = 49r$$

$$r \approx .04 \quad r = \frac{\ln 7}{49}$$

$$r \approx .04$$

REF: 081730aii NAT: F.LE.A.4 TOP: Exponential Growth

314 ANS:

$j(-x) = (-x)^4 - 3(-x)^2 - 4 = x^2 - 3x^2 - 4$  Since  $j(x) = j(-x)$ , the function is even.

REF: 081731aii NAT: F.BF.B.3 TOP: Even and Odd Functions

315 ANS:

$$P(A+B) = P(A) \cdot P(B|A) = 0.8 \cdot 0.85 = 0.68$$

REF: 011928aii NAT: S.CP.A.3 TOP: Conditional Probability

316 ANS:

$$\frac{x^3+9}{x^3+8} = \frac{x^3+8}{x^3+8} + \frac{1}{x^3+8}$$

$$\frac{x^3+9}{x^3+8} = \frac{x^3+9}{x^3+8}$$

REF: 061631aii NAT: A.APR.C.4 TOP: Polynomial Identities

317 ANS:

$$\left( \frac{\frac{5}{3}}{x^{\frac{5}{3}}} \right)^{\frac{6}{5}} = \left( \frac{\frac{5}{6}}{y^{\frac{5}{6}}} \right)^{\frac{6}{5}}$$

$$x^2 = y$$

REF: 011730aii NAT: N.RN.A.2 TOP: Radicals and Rational Exponents  
KEY: variables

318 ANS:

A student is more likely to jog if both siblings jog. 1 jogs:  $\frac{416}{2239} \approx 0.19$ . both jog:  $\frac{400}{1780} \approx 0.22$

REF: 061732aii NAT: S.CP.A.4 TOP: Conditional Probability

319 ANS:

$q$  has the smaller minimum value for the domain  $[-2, 2]$ .  $h$ 's minimum is  $-1(2(-1) + 1)$  and  $q$ 's minimum is  $-8$ .

REF: 011830aii NAT: F.IF.C.9 TOP: Comparing Functions

320 ANS:

Rewrite  $\frac{4}{3}$  as  $\frac{1}{3} \cdot \frac{4}{1}$ , using the power of a power rule.

REF: 081725aii NAT: N.RN.A.1 TOP: Radicals and Rational Exponents

321 ANS:

$$A = Pe^{rt}$$

$$135000 = 100000e^{5r}$$

$$1.35 = e^{5r}$$

$$\ln 1.35 = \ln e^{5r}$$

$$\ln 1.35 = 5r$$

$$.06 \approx r \text{ or } 6\%$$

REF: 061632aii NAT: F.LE.A.4 TOP: Exponential Growth

322 ANS:

$$(x^2 - 6)(x^2 + 2)$$

REF: 081825aii NAT: A.SSE.A.2 TOP: Factoring Polynomials

KEY: higher power

323 ANS:

$$\sin^2 \theta + (-0.7)^2 = 1 \quad \text{Since } \theta \text{ is in Quadrant II, } \sin \theta = \sqrt{.51} \text{ and } \tan \theta = \frac{\sin \theta}{\cos \theta} = \frac{\sqrt{.51}}{-0.7} \approx -1.02$$

$$\sin^2 \theta = .51$$

$$\sin \theta = \pm \sqrt{.51}$$

REF: 081628aii NAT: F.TF.C.8 TOP: Determining Trigonometric Functions

324 ANS:

$$\frac{9}{6} = 1.5 \quad a_1 = 6$$

$$a_n = 1.5 \cdot a_{n-1}$$

REF: 061931aii NAT: F.LE.A.2 TOP: Sequences KEY: recursive

325 ANS:  
 $1200 \cdot 0.784 \approx 941$

REF: 081828aai NAT: S.ID.A.4 TOP: Normal Distributions  
 KEY: predict

326 ANS:  
 No.  $0.499 \pm 2(0.049) \rightarrow 0.401 - 0.597$ . Since 0.43 falls within this interval, Robin's coin is likely not unfair.

REF: 061932aai NAT: S.IC.A.2 TOP: Analysis of Data

327 ANS:  
 $\sqrt{x-4} = -x+6$        $\sqrt{x-4} = -8+6 = -2$  is extraneous.

$$x-4 = x^2 - 12x + 36$$

$$0 = x^2 - 13x + 40$$

$$0 = (x-8)(x-5)$$

$$x = 5, 8$$

REF: 061730aai NAT: A.REI.A.2 TOP: Solving Radicals  
 KEY: extraneous solutions

328 ANS:  
 $20e^{.05t} = 30e^{.03t}$

$$\frac{\frac{2}{3}e^{.05t}}{e^{.05t}} = \frac{e^{.03t}}{e^{.05t}}$$

$$\ln \frac{2}{3} = \ln e^{-.02t}$$

$$\ln \frac{2}{3} = -.02t \ln e$$

$$\frac{\ln \frac{2}{3}}{-.02} = t$$

$$20.3 \approx t$$

REF: 011829aai NAT: A.REI.D.11 TOP: Other Systems

329 ANS:

$$\begin{array}{r}
 2a^2 + 5a + 2 \\
 3a - 2 \overline{) 6a^3 + 11a^2 - 4a - 9} \quad 2a^2 + 5a + 2 - \frac{5}{3a - 2} \\
 \underline{6a^3 - 4a^2} \\
 15a^2 - 4a \\
 \underline{15a^2 - 10a} \\
 6a - 9 \\
 \underline{6a - 4} \\
 -5
 \end{array}$$

REF: 061829aai NAT: A.APR.D.6 TOP: Rational Expressions

KEY: division

330 ANS:

$$\sqrt[3]{x} \cdot \sqrt{x} = x^{\frac{1}{3}} \cdot x^{\frac{1}{2}} = x^{\frac{3}{6}} \cdot x^{\frac{3}{6}} = x^{\frac{5}{6}}$$

REF: 061731aai NAT: N.RN.A.2 TOP: Operations with Radicals

KEY: with variables, index &gt; 2

331 ANS:

Let  $x$  equal the first integer and  $x + 1$  equal the next.  $(x + 1)^2 - x^2 = x^2 + 2x + 1 - x^2 = 2x + 1$ .  $2x + 1$  is an odd integer.

REF: fall1511aai NAT: A.APR.C.4 TOP: Polynomial Identities

332 ANS:

Using a 95% level of confidence,  $x \pm 2$  standard deviations sets the usual wait time as 150-302 seconds. 360 seconds is unusual.

REF: 081629aai NAT: S.IC.B.6 TOP: Analysis of Data

333 ANS:

$$\tan \theta = \frac{\sin \theta}{\cos \theta} = \frac{-7/25}{-24/25} \quad \cos \theta = \frac{-24}{25}$$

REF: 061928aai NAT: F.TF.C.8 TOP: Determining Trigonometric Functions

334 ANS:

$P(-2) = 60$   $Q(-2) = 0$   $(x + 2)$  is a factor of  $Q(x)$  since  $Q(-2) = 0$ .

REF: 081929aai NAT: A.APR.B.2 TOP: Remainder Theorem

335 ANS:

$$\frac{7}{2x} - \frac{2}{x+1} = \frac{1}{4}$$

$$\frac{7x+7-4x}{2x^2+2x} = \frac{1}{4}$$

$$2x^2 + 2x = 12x + 28$$

$$x^2 - 5x - 14 = 0$$

$$(x-7)(x+2) = 0$$

$$x = 7, -2$$

REF: 061926aii NAT: A.REI.A.2 TOP: Solving Rationals

KEY: rational solutions

336 ANS:

No, because  $P(M/R) \neq P(M)$ 

$$\frac{70}{180} \neq \frac{230}{490}$$

$$0.38 \neq 0.47$$

REF: 011731aii NAT: S.CP.A.4 TOP: Conditional Probability

337 ANS:

$$\frac{x^{\frac{8}{3}}}{x^{\frac{4}{3}}} = x^y$$

$$x^{\frac{4}{3}} = x^y$$

$$\frac{4}{3} = y$$

REF: spr1505aii NAT: N.RN.A.2 TOP: Radicals and Rational Exponents

KEY: numbers

338 ANS:

$$M = \frac{(152500 - 15250) \left( \frac{.036}{12} \right) \left( 1 + \frac{.036}{12} \right)^{360}}{\left( 1 + \frac{.036}{12} \right)^{360} - 1} \approx 624$$

REF: 061831aii NAT: A.SSE.B.4 TOP: Series

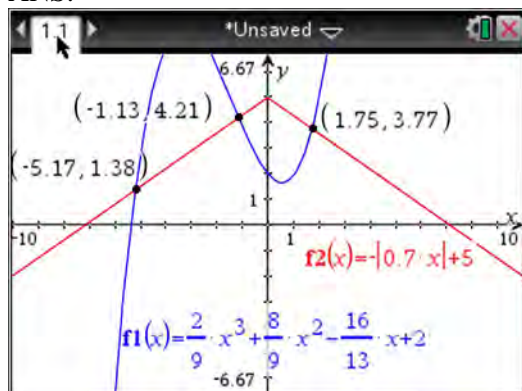
339 ANS:

Randomly assign participants to two groups. One group uses the toothpaste with ingredient  $X$  and the other group uses the toothpaste without ingredient  $X$ .

REF: 061626aai NAT: S.IC.B.3 TOP: Analysis of Data

KEY: type

340 ANS:



REF: fall1510aai NAT: A.REI.D.11 TOP: Other Systems

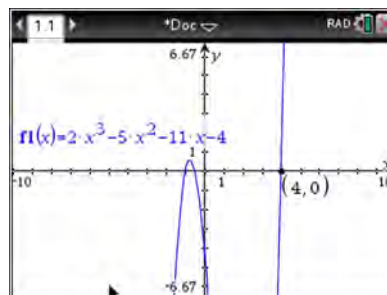
341 ANS:

$$S_{10} = \frac{15 - 15(1.03)^{10}}{1 - 1.03} \approx 171.958$$

REF: 011929aai NAT: A.SSE.B.4 TOP: Series

342 ANS:

$f(4) = 2(4)^3 - 5(4)^2 - 11(4) - 4 = 128 - 80 - 44 - 4 = 0$  Any method that demonstrates 4 is a zero of  $f(x)$  confirms



that  $x - 4$  is a factor, as suggested by the Remainder Theorem.

REF: spr1507aai NAT: A.APR.B.2 TOP: Remainder Theorem

343 ANS:

$$r = \frac{360}{300} = 1.2 \quad S_n = \frac{300 - 300(1.2)^n}{1 - 1.2} \quad S_{10} = \frac{300 - 300(1.2)^{10}}{1 - 1.2} \approx 7787.6$$

REF: 012029aai NAT: A.SSE.B.4 TOP: Series

344 ANS:

$0 = \log_{10}(x-4)$  The  $x$ -intercept of  $h$  is  $(2,0)$ .  $f$  has the larger value.

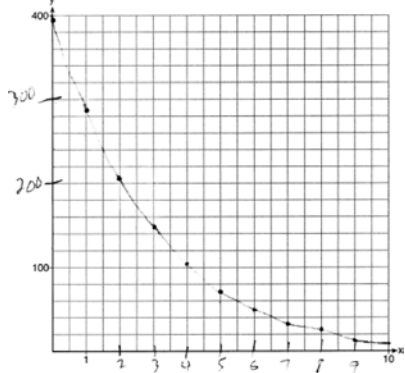
$$10^0 = x - 4$$

$$1 = x - 4$$

$$x = 5$$

REF: 081630aai NAT: F.IF.C.9 TOP: Comparing Functions

345 ANS:



REF: 061729aai NAT: F.IF.C.7 TOP: Graphing Exponential Functions

346 ANS:

$a_1 = 3$   $a_2 = 7$   $a_3 = 15$   $a_4 = 31$ ; No, because there is no common ratio:  $\frac{7}{3} \neq \frac{15}{7}$

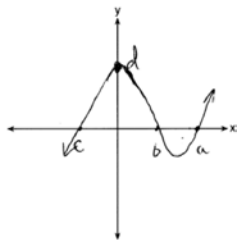
REF: 061830aai NAT: F.IF.A.3 TOP: Sequences KEY: recursive

347 ANS:

The denominator of the rational exponent represents the index of a root, and the 4th root of 81 is 3 and  $3^3$  is 27.

REF: 011832aai NAT: N.RN.A.1 TOP: Radicals and Rational Exponents

348 ANS:



REF: 081732aai NAT: F.IF.C.7 TOP: Graphing Polynomial Functions

349 ANS:

$$B(t) = 100(2)^{\frac{t}{30}}$$

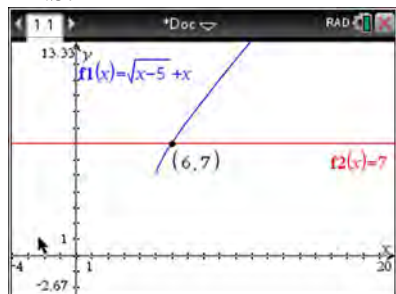
REF: 012031aai NAT: F.LE.A.2 TOP: Modeling Exponential Functions



350 ANS:  
 $250(1) + 2450 = 2700$  The maximum lung capacity of a person is 2700 mL.

REF: 081928aai NAT: F.IF.B.4 TOP: Graphing Trigonometric Functions

351 ANS:



$$\sqrt{x-5} = -x+7 \quad \sqrt{x-5} = -9+7 = -2 \text{ is extraneous.}$$

$$x-5 = x^2 - 14x + 49$$

$$0 = x^2 - 15x + 54$$

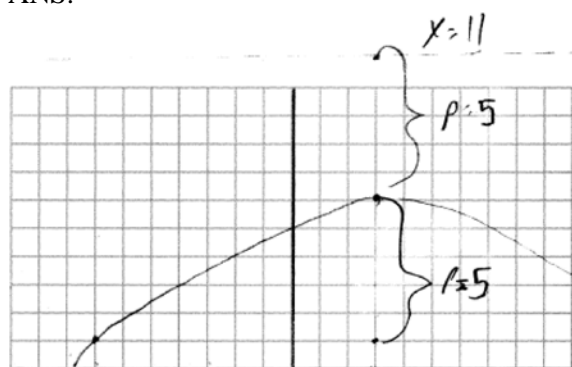
$$0 = (x-6)(x-9)$$

$$x = 6, 9$$

REF: spr1508aai NAT: A.REI.A.2 TOP: Solving Radicals

KEY: extraneous solutions

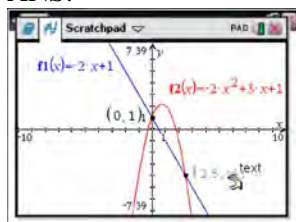
352 ANS:



vertex (3, 6), focus (3, 1),  $p = 5$ , directrix  $y = 6 + 5 = 11$

REF: 012028aai NAT: G.GPE.A.2 TOP: Graphing Quadratic Functions

353 ANS:



$$-2x + 1 = -2x^2 + 3x + 1$$

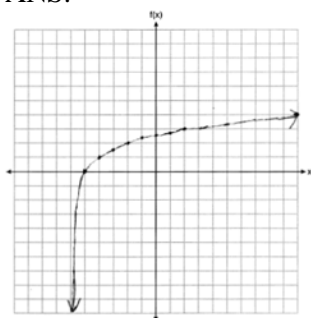
$$2x^2 - 5x = 0$$

$$x(2x - 5) = 0$$

$$x = 0, \frac{5}{2}$$

REF: fall1507aai NAT: A.REI.C.7 TOP: Quadratic-Linear Systems

354 ANS:



REF: 061927aai NAT: F.IF.C.7 TOP: Graphing Logarithmic Functions

355 ANS:

$$(a + b)^3 = a^3 + b^3 \quad \text{No. Erin's shortcut only works if } a = 0, b = 0 \text{ or } a = -b.$$

$$a^3 + 3a^2b + 3ab^2 + b^3 = a^3 + b^3$$

$$3ab^2 + 3a^2b = 0$$

$$3ab(b + a) = 0$$

$$a = 0, b = 0, a = -b$$

REF: 011927aai NAT: A.APR.C.4 TOP: Polynomial Identities

356 ANS:

$$\frac{10.1 - -2}{2} - \frac{2.5 - -0.1}{2} = 6.05 - 1.3 = 4.75$$

REF: 081930aai NAT: F.IF.C.7 TOP: Graphing Trigonometric Functions

KEY: amplitude

357 ANS:

$$\frac{13.9 - 9.4}{4 - 1} = 1.5 \quad \text{The average rate of change in the number of hours of daylight from January 1-April 1 is 1.5.}$$

REF: 061925aai NAT: F.IF.B.6 TOP: Rate of Change

358 ANS:

The denominator of the rational exponent represents the index of a root, and the numerator of the rational exponent represents the power of the base.  $(\sqrt{9})^5 = 243$

REF: 081926aii NAT: N.RN.A.1 TOP: Radicals and Rational Exponents

359 ANS:

$$x^2 + (x - 28)^2 = 400 \quad y = 12 - 28 = -16 \quad y = 16 - 28 = -12$$

$$x^2 + x^2 - 56x + 784 = 400$$

$$2x^2 - 56x + 384 = 0$$

$$x^2 - 28x + 192 = 0$$

$$(x - 16)(x - 12) = 0$$

$$x = 12, 16$$

REF: 081831aii NAT: A.REI.C.7 TOP: Quadratic-Linear Systems

360 ANS:

$$\frac{\sqrt[3]{x^2 y^5}}{\sqrt[4]{x^3 y^4}} = \frac{x^{\frac{2}{3}} y^{\frac{5}{3}}}{x^{\frac{3}{4}} y^1} = \frac{x^{\frac{8}{12}} y^{\frac{20}{12}}}{x^{\frac{9}{12}} y^{\frac{12}{12}}} = x^{-\frac{1}{12}} y^{\frac{2}{3}}$$

REF: 011925aii NAT: N.RN.A.2 TOP: Radicals and Rational Exponents

KEY: variables

361 ANS:

$$x = (y - 3)^3 + 1$$

$$x - 1 = (y - 3)^3$$

$$\sqrt[3]{x - 1} = y - 3$$

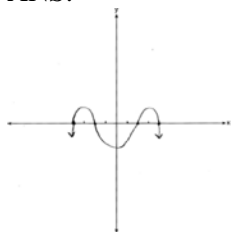
$$\sqrt[3]{x - 1} + 3 = y$$

$$f^{-1}(x) = \sqrt[3]{x - 1} + 3$$

REF: fall1509aii NAT: F.BF.B.4 TOP: Inverse of Functions

KEY: other

362 ANS:



REF: 011926aii NAT: F.IF.C.7 TOP: Graphing Polynomial Functions

363 ANS:

$$D = 1.223(2.652)^A$$

REF: 011826aii NAT: S.ID.B.6 TOP: Regression KEY: exponential

364 ANS:

$$-6(x+3)\left(\frac{-3}{x+3} - \frac{x}{6} + 1 = 0\right)$$

$$18 + x(x+3) - 6(x+3) = 0$$

$$18 + x^2 + 3x - 6x - 18 = 0$$

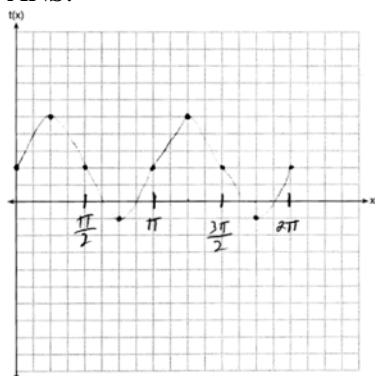
$$x^2 - 3x = 0$$

$$x(x-3) = 0$$

$$x = 0, 3$$

REF: 081829aii NAT: A.REI.A.2 TOP: Solving Rationals  
KEY: rational solutions

365 ANS:

REF: 081830aii NAT: F.IF.C.7 TOP: Graphing Trigonometric Functions  
KEY: graph

366 ANS:

$$\text{No. } \left(\sqrt[7]{x^2}\right)\left(\sqrt[5]{x^3}\right) = x^{\frac{2}{7}} \cdot x^{\frac{3}{5}} = x^{\frac{31}{35}} = \sqrt[35]{x^{31}}$$

REF: 061929aia NAT: N.RN.A.2 TOP: Radicals and Rational Exponents

KEY: variables

367 ANS:



69

REF: 061726aia NAT: S.ID.A.4 TOP: Normal Distributions

KEY: percent

368 ANS:

$$\frac{165 + 66 - 33}{825} = \frac{198}{825}$$

REF: 081925aia NAT: S.CP.B.6 TOP: Conditional Probability

369 ANS:

$$xi(-6i)^2 = xi(36i^2) = 36xi^3 = -36xi$$

REF: 081627aia NAT: N.CN.A.2 TOP: Operations with Complex Numbers

370 ANS:

$$P(S \cap M) = P(S) + P(M) - P(S \cup M) = \frac{649}{1376} + \frac{433}{1376} - \frac{974}{1376} = \frac{108}{1376}$$

REF: 061629aia NAT: S.CP.B.7 TOP: Theoretical Probability

371 ANS:

Since there are six flavors, each flavor can be assigned a number, 1-6. Use the simulation to see the number of times the same number is rolled 4 times in a row.

REF: 081728aia NAT: S.IC.A.2 TOP: Analysis of Data

372 ANS:

$$\frac{1}{x} - \frac{1}{3} = -\frac{1}{3x}$$

$$\frac{3-x}{3x} = -\frac{1}{3x}$$

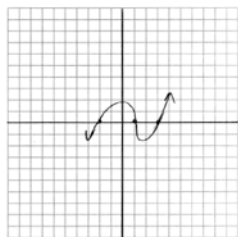
$$3-x = -1$$

$$x = 4$$

REF: 061625aia NAT: A.REI.A.2 TOP: Solving Rationals

KEY: rational solutions

373 ANS:



REF: 011729aai NAT: F.IF.C.7 TOP: Graphing Polynomial Functions

374 ANS:

$$t^2 + \left(\frac{4}{7}\right)^2 = 1 \quad -\frac{\sqrt{33}}{7}$$

$$t^2 + \frac{16}{49} = \frac{49}{49}$$

$$t^2 = \frac{33}{49}$$

$$t = \frac{\pm\sqrt{33}}{7}$$

REF: 011931aai NAT: F.TF.A.2 TOP: Unit Circle

375 ANS:

$$\begin{array}{r} 3x + 13 \\ x - 2 \overline{) 3x^2 + 7x - 20} \quad 3x + 13 + \frac{6}{x - 2} \\ \underline{3x^2 - 6x} \phantom{- 20} \\ 13x - 20 \\ \underline{13x - 26} \\ 6 \end{array}$$

REF: 011732aai NAT: A.APR.D.6 TOP: Rational Expressions

KEY: division

376 ANS:

$$x = \frac{-5 \pm \sqrt{5^2 + 4(2)(8)}}{2(2)} = -\frac{5}{4} \pm \frac{i\sqrt{39}}{4}$$

REF: 061827aai NAT: A.REI.B.4 TOP: Solving Quadratics

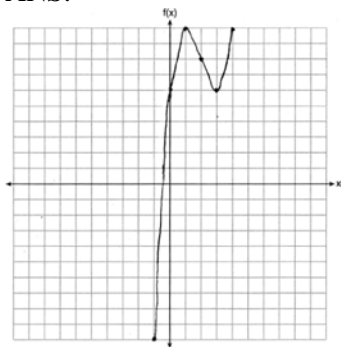
KEY: complex solutions | quadratic formula

377 ANS:

$m(3) = 3^3 - 3^2 - 5(3) - 3 = 27 - 9 - 15 - 3 = 0$  Since  $m(3) = 0$ , there is no remainder when  $m(x)$  is divided by  $x - 3$ , and so  $x - 3$  is a factor.

REF: 012026aai NAT: A.APR.B.2 TOP: Remainder Theorem

378 ANS:



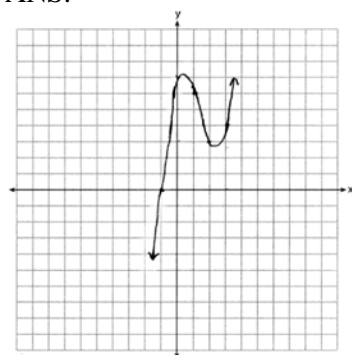
REF: 061826aia NAT: F.IF.C.7 TOP: Graphing Polynomial Functions

379 ANS:

$$\frac{103}{110+103} = \frac{103}{213}$$

REF: 061825aia NAT: S.CP.A.4 TOP: Conditional Probability

380 ANS:



REF: 012032aia NAT: F.IF.C.7 TOP: Graphing Polynomial Functions

381 ANS:

$$\frac{p(x)}{x-1} = x^2 + 7 + \frac{5}{x-1}$$

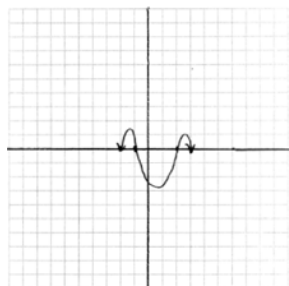
$$p(x) = x^3 - x^2 + 7x - 7 + 5$$

$$p(x) = x^3 - x^2 + 7x - 2$$

REF: 061930aia NAT: A.APR.D.6 TOP: Rational Expressions

KEY: division

382 ANS:



REF: 011831aii NAT: F.IF.C.7 TOP: Graphing Polynomial Functions

383 ANS:

Translation 3 units right and 4 units up

REF: 012027aii NAT: F.IF.C.7 TOP: Graphing Exponential Functions

384 ANS:

 $2(0.042) = 0.084 \approx 0.08$  The percent of users making in-app purchases will be within 8% of 35%.

REF: 081832aii NAT: S.IC.B.4 TOP: Analysis of Data

385 ANS:

 $\frac{306.25 - 156.25}{70 - 50} = \frac{150}{20} = 7.5$  Between 50-70 mph, each additional mph in speed requires 7.5 more feet to stop.

REF: 081631aii NAT: F.IF.B.6 TOP: Rate of Change

386 ANS:

$$\frac{2x^{\frac{3}{2}}}{2x^{\frac{2}{2}}} = x^{\frac{1}{2}} = \sqrt{x}$$

REF: 081826aii NAT: N.RN.A.2 TOP: Radicals and Rational Exponents

KEY: variables

387 ANS:

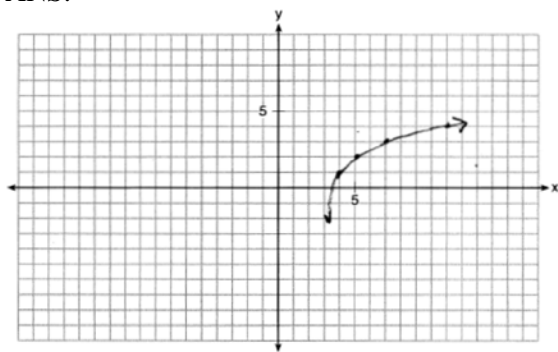
$$3x^3 + x^2 + 3xy + y = x^2(3x + 1) + y(3x + 1) = (x^2 + y)(3x + 1)$$

REF: 011828aii NAT: A.SSE.A.2 TOP: Factoring Polynomials

KEY: factoring by grouping

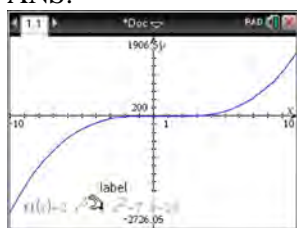


388 ANS:



REF: 011932aia NAT: F.IF.C.7 TOP: Graphing Logarithmic Functions

389 ANS:



$$x - 5 \overline{) 2x^3 - 4x^2 - 7x - 10} \quad \text{Since there is a remainder, } x - 5 \text{ is not a factor.}$$

$$\underline{2x^3 - 10x^2}$$

$$6x^2 - 7x$$

$$\underline{6x^2 - 30x}$$

$$23x - 10$$

$$\underline{23x - 115}$$

$$105$$

REF: 061627aia NAT: A.APR.B.2 TOP: Remainder Theorem

390 ANS:

$$\frac{-1}{\sqrt{2^2 + (-1)^2}} = -\frac{1}{\sqrt{5}}$$

REF: 061832aia NAT: F.TF.A.2 TOP: Determining Trigonometric Functions

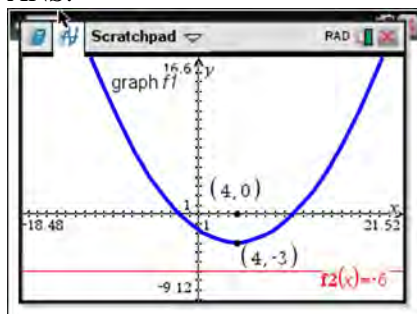
KEY: extension to reals

391 ANS:

$$-\frac{1}{2}i^3(3i-4) - 3i^2 = -\frac{3}{2}i^4 + 2i^3 - 3i^2 = -\frac{3}{2} - 2i + 3 = \frac{3}{2} - 2i$$

REF: 081927aia NAT: N.CN.A.2 TOP: Operations with Complex Numbers

392 ANS:



The vertex of the parabola is  $(4, -3)$ . The  $x$ -coordinate of the focus and the vertex is the same. Since the distance from the vertex to the directrix is 3, the distance from the vertex to the focus is 3, so the  $y$ -coordinate of the focus is 0. The coordinates of the focus are  $(4, 0)$ .

REF: 061630aai NAT: G.GPE.A.2 TOP: Graphing Quadratic Functions

393 ANS:

$$i^2 = -1, \text{ and not } 1; 10 + 10i$$

REF: 011825aai NAT: N.CN.A.2 TOP: Operations with Complex Numbers

394 ANS:

$$(4 - 3i)(5 + 2yi - 5 + 2yi)$$

$$(4 - 3i)(4yi)$$

$$16yi - 12yi^2$$

$$12y + 16yi$$

REF: spr1506aai NAT: N.CN.A.2 TOP: Operations with Complex Numbers

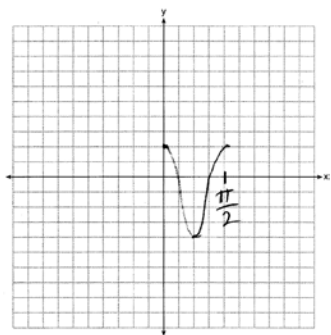
395 ANS:

Applying the commutative property,  $\left(3^{\frac{1}{5}}\right)^2$  can be rewritten as  $\left(3^2\right)^{\frac{1}{5}}$  or  $9^{\frac{1}{5}}$ . A fractional exponent can be

rewritten as a radical with the denominator as the index, or  $9^{\frac{1}{5}} = \sqrt[5]{9}$ .

REF: 081626aai NAT: N.RN.A.1 TOP: Radicals and Rational Exponents

396 ANS:



REF: 061628aii NAT: F.IF.C.7 TOP: Graphing Trigonometric Functions

KEY: graph

397 ANS:

$$\left(p^2 n^{\frac{1}{2}}\right)^8 \sqrt{p^5 n^4} = (p^{16} n^4) p^2 n^2 \sqrt{p} = p^{18} n^6 \sqrt{p}$$

REF: 012025aii NAT: N.RN.A.2 TOP: Radicals and Rational Exponents

398 ANS:

$$(x^2 + y^2)^2 = (x^2 - y^2)^2 + (2xy)^2$$

$$x^4 + 2x^2y^2 + y^4 = x^4 - 2x^2y^2 + y^4 + 4x^2y^2$$

$$x^4 + 2x^2y^2 + y^4 = x^4 + 2x^2y^2 + y^4$$

REF: 081727aii NAT: A.APR.C.4 TOP: Polynomial Identities

399 ANS:

$$a_1 = 4 \quad a_8 = 639$$

$$a_n = 2a_{n-1} + 1$$

REF: 081729aii NAT: F.LE.A.2 TOP: Sequences KEY: recursive

400 ANS:

$\left(\ln \frac{1}{2}\right)$   
 1590 is negative, so  $M(t)$  represents decay.

REF: 011728aii NAT: F.IF.C.7 TOP: Graphing Exponential Functions

401 ANS:

$$\frac{1}{8} + \frac{1}{6} = \frac{1}{t_b}; \quad \frac{24t_b}{8} + \frac{24t_b}{6} = \frac{24t_b}{t_b}$$

$$3t_b + 4t_b = 24$$

$$t_b = \frac{24}{7} \approx 3.4$$

REF: 011827aai NAT: A.CED.A.1 TOP: Modeling Rationals

402 ANS:

$r(2) = -6$ . Since there is a remainder when the cubic is divided by  $x - 2$ , this binomial is not a factor.

$$\begin{array}{r|rrrr} 2 & 1 & -4 & 4 & 6 \\ & & 2 & -4 & 0 \\ \hline & 1 & -2 & 0 & -6 \end{array}$$

REF: 061725aai NAT: A.APR.B.2 TOP: Remainder Theorem

403 ANS:

$\frac{B(11) - B(8)}{11 - 8} \approx -10.1$  The average monthly high temperature decreases  $10.1^\circ$  each month from August to November.

REF: 011930aai NAT: F.IF.B.6 TOP: Rate of Change

404 ANS:

$$\frac{p(8) - p(4)}{8 - 4} \approx 48.78$$

REF: 081827aai NAT: F.IF.B.6 TOP: Rate of Change

## Algebra II 4 Point Regents Exam Questions

## Answer Section

405 ANS:

$29.101 \pm 2 \cdot 0.934 = 27.23 - 30.97$ . Yes, since 30 falls within the 95% interval.

REF: 011935aai NAT: S.IC.A.2 TOP: Analysis of Data

406 ANS:

$$M = 172600 \cdot \frac{0.00305(1 + 0.00305)^{12 \cdot 15}}{(1 + 0.00305)^{12 \cdot 15} - 1} \approx 1247 \quad 1100 = (172600 - x) \cdot \frac{0.00305(1 + 0.00305)^{12 \cdot 15}}{(1 + 0.00305)^{12 \cdot 15} - 1}$$

$$1100 \approx (172600 - x) \cdot (0.007228)$$

$$152193 \approx 172600 - x$$

$$20407 \approx x$$

REF: 061734aai NAT: A.SSE.B.4 TOP: Series

407 ANS:

$$C(t) = 63000 \left(1 + \frac{0.0255}{12}\right)^{12t} \quad 63000 \left(1 + \frac{0.0255}{12}\right)^{12t} = 100000$$

$$12t \log(1.002125) = \log \frac{100}{63}$$

$$t \approx 18.14$$

REF: 061835aai NAT: A.CED.A.1 TOP: Exponential Growth

408 ANS:

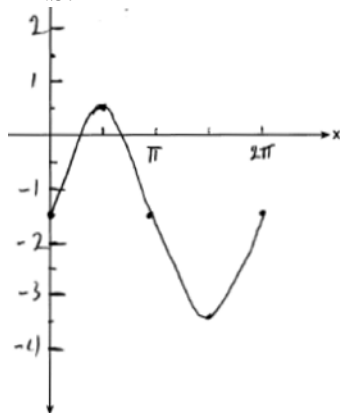
$$\text{normcdf}(510, 540, 480, 24) = 0.0994 \quad z = \frac{510 - 480}{24} = 1.25 \quad 1.25 = \frac{x - 510}{20} \quad 2.5 = \frac{x - 510}{20} \quad 535 - 560$$

$$z = \frac{540 - 480}{24} = 2.5 \quad x = 535 \quad x = 560$$

REF: fall1516aai NAT: S.ID.A.4 TOP: Normal Distributions

KEY: probability

409 ANS:

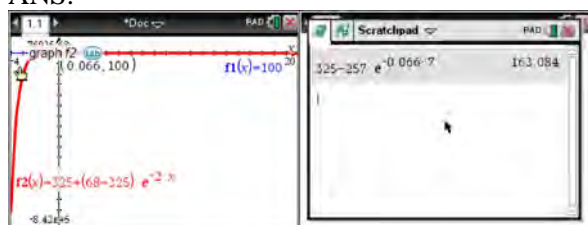


Part a sketch is shifted  $\frac{\pi}{3}$  units right.

REF: 081735aia NAT: F.IF.C.7 TOP: Graphing Trigonometric Functions

KEY: graph

410 ANS:



$$100 = 325 + (68 - 325)e^{-2k} \quad T = 325 - 257e^{-0.066t}$$

$$-225 = -257e^{-2k}$$

$$T = 325 - 257e^{-0.066(7)} \approx 163$$

$$k = \frac{\ln\left(\frac{-225}{-257}\right)}{-2}$$

$$k \approx 0.066$$

REF: fall1513aia NAT: F.LE.A.4 TOP: Exponential Growth

411 ANS:

$$\frac{47}{108} = \frac{1}{4} + \frac{116}{459} - P(M \text{ and } J); \text{ No, because } \frac{31}{459} \neq \frac{1}{4} \cdot \frac{116}{459}$$

$$P(M \text{ and } J) = \frac{31}{459}$$

REF: 011834aia NAT: S.CP.A.3 TOP: Conditional Probability

412 ANS:

$0.301 \pm 2(0.058) \rightarrow 0.185 - 0.417 \frac{14}{60} \approx 0.23$ . It is not unusual because 0.23 falls within this interval.

REF: 081935aia NAT: S.IC.B.5 TOP: Analysis of Data

413 ANS:

$$20000 = PMT \left( \frac{1 - (1 + 0.00625)^{-60}}{0.00625} \right) \quad 21000 - x = 300 \left( \frac{1 - (1 + 0.00625)^{-60}}{0.00625} \right)$$

$$PMT \approx 400.76$$

$$x \approx 6028$$

REF: 011736aii NAT: A.SSE.B.4 TOP: Series

414 ANS:

$$\begin{array}{ccccccc} x + y + z = 1 & x + y + z = 1 & x + y + z = 1 & -2z - z = 3 & y - (-1) = 3 & x + 2 - 1 = 1 \\ x + 2y + 3z = 1 & \underline{x + 2y + 3z = 1} & \underline{-x + 3y - 5z = 11} & -3z = 3 & y = 2 & x = 0 \\ -x + 3y - 5z = 11 & y + 2z = 0 & 4y - 4z = 12 & z = -1 & & & \\ & y = -2z & y - z = 3 & & & & \end{array}$$

REF: 061733aii NAT: A.REI.C.6 TOP: Solving Linear Systems

KEY: three variables

415 ANS:

$$a_n = 100(.8)^{n-1} \quad S_{20} = \frac{100 - 100(.8)^{20}}{1 - .8} \approx 494 \text{ No, because } 494 > 40 \times 12.$$

REF: 012033aii NAT: A.SSE.B.4 TOP: Series

416 ANS:

$$P(F|L) = \frac{12}{27} \quad P(F) = \frac{22}{45} \quad \text{Since } P(F|L) \neq P(F), \text{ the events are not independent.}$$

REF: 061936aii NAT: S.CP.A.4 TOP: Conditional Probability

417 ANS:

$$\begin{aligned} s(t) &= 200(0.5)^{\frac{t}{15}} & \frac{1}{10} &= (0.5)^{\frac{t}{15}} \\ \log \frac{1}{10} &= \log(0.5)^{\frac{t}{15}} \\ -1 &= \frac{t \cdot \log(0.5)}{15} \\ t &= \frac{-15}{\log(0.5)} \approx 50 \end{aligned}$$

REF: 061934aii NAT: F.LE.A.4 TOP: Exponential Decay

418 ANS:

$$7 = 20(0.5)^{\frac{t}{8.02}}$$

$$\log 0.35 = \log 0.5^{\frac{t}{8.02}}$$

$$\log 0.35 = \frac{t \log 0.5}{8.02}$$

$$\frac{8.02 \log 0.35}{\log 0.5} = t$$

$$t \approx 12$$

REF: 081634aai NAT: F.LE.A.4 TOP: Exponential Decay

419 ANS:

$$a_n = x^{n-1}(x+1) \quad x^{n-1} = 0 \quad x+1 = 0$$

$$x = 0 \quad x = -1$$

REF: spr1511aai NAT: F.LE.A.2 TOP: Sequences KEY: recursive

420 ANS:

$$6x - 3y + 2z = -10 \quad x + 3y + 5z = 45 \quad 4x + 10z = 62 \quad 4x + 4(7) = 20 \quad 6(-2) - 3y + 2(7) = -10$$

$$-2x + 3y + 8z = 72 \quad 6x - 3y + 2z = -10 \quad 4x + 4z = 20 \quad 4x = -8 \quad -3y = -12$$

$$4x + 10z = 62 \quad 7x + 7z = 35 \quad 6z = 42 \quad x = -2 \quad y = 4$$

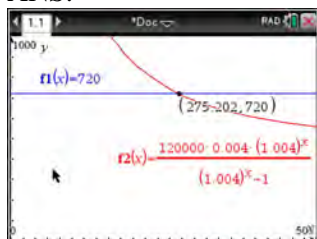
$$4x + 4z = 20 \quad z = 7$$

REF: spr1510aai NAT: A.REI.C.6 TOP: Solving Linear Systems

KEY: three variables



421 ANS:



$$720 = \frac{120000 \left( \frac{.048}{12} \right) \left( 1 + \frac{.048}{12} \right)^n}{\left( 1 + \frac{.048}{12} \right)^n - 1} \frac{275.2}{12} \approx 23 \text{ years}$$

$$720(1.004)^n - 720 = 480(1.004)^n$$

$$240(1.004)^n = 720$$

$$1.004^n = 3$$

$$n \log 1.004 = \log 3$$

$$n \approx 275.2 \text{ months}$$

REF: spr1509aii NAT: A.CED.A.1 TOP: Exponential Growth

422 ANS:

Yes. The margin of error from this simulation indicates that 95% of the observations fall within  $\pm 0.12$  of the simulated proportion, 0.25. The margin of error can be estimated by multiplying the standard deviation, shown to

be 0.06 in the dotplot, by 2, or applying the estimated standard error formula,  $\left( \sqrt{\frac{p(1-p)}{n}} \right)$  or  $\left( \sqrt{\frac{(0.25)(0.75)}{50}} \right)$

and multiplying by 2. The interval  $0.25 \pm 0.12$  includes plausible values for the true proportion of people who prefer Stephen's new product. The company has evidence that the population proportion could be at least 25%. As seen in the dotplot, it can be expected to obtain a sample proportion of 0.18 (9 out of 50) or less several times, even when the population proportion is 0.25, due to sampling variability. Given this information, the results of the survey do not provide enough evidence to suggest that the true proportion is not at least 0.25, so the development of the product should continue at this time.

REF: spr1512aii NAT: S.IC.B.4 TOP: Analysis of Data

423 ANS:

$N(t) = 950e^{0.0475t}$  The base is  $e$  because growth is continuous.  $N\left(\frac{36}{24}\right) \approx 1020$

REF: 081933aii NAT: F.LE.A.2 TOP: Modeling Exponential Functions

424 ANS:

$$0 = 6(-5)^3 + b(-5)^2 - 52(-5) + 15 \quad z(x) = 6x^3 + 19x^2 - 52x + 15$$

$$0 = -750 + 25b + 260 + 15$$

$$475 = 25b$$

$$19 = b$$

$$\begin{array}{r|rrrr} -5 & 6 & 19 & -52 & 15 \\ & & -30 & 55 & 15 \\ \hline & 6 & -11 & 3 & 0 \end{array}$$

$$6x^2 - 11x + 3 = 0$$

$$(2x - 3)(3x - 1) = 0$$

$$x = \frac{3}{2}, \frac{1}{3}, -5$$

REF: fall1515aii NAT: A.APR.B.2 TOP: Remainder Theorem

425 ANS:

$0.602 \pm 2 \cdot 0.066 = 0.47 - 0.73$ . Since 0.50 falls within the 95% interval, this supports the concern there may be an even split.

REF: 061635aii NAT: S.IC.B.5 TOP: Analysis of Data

426 ANS:

$$3\sqrt{x} - 2x = -5 \quad 1 \text{ is extraneous.}$$

$$3\sqrt{x} = 2x - 5$$

$$9x = 4x^2 - 20x + 25$$

$$4x^2 - 29x + 25 = 0$$

$$(4x - 25)(x - 1) = 0$$

$$x = \frac{25}{4}, 1$$

REF: 011936aii NAT: A.REI.A.2 TOP: Solving Radicals

KEY: extraneous solutions

427 ANS:

$$y = 101.523(.883)^x \quad 29 = 101.523(.883)^x$$

$$\frac{29}{101.523} = (.883)^x$$

$$\log \frac{29}{101.523} = x \log(.883)$$

$$\frac{\log \frac{29}{101.523}}{\log(.883)} = x$$

$$x \approx 10.07$$

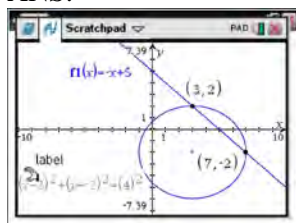
REF: 012036aai NAT: S.ID.B.6 TOP: Regression KEY: exponential

428 ANS:

$0.506 \pm 2 \cdot 0.078 = 0.35 - 0.66$ . The 32.5% value falls below the 95% confidence level.

REF: 061736aai NAT: S.IC.B.5 TOP: Analysis of Data

429 ANS:



$$y = -x + 5 \quad y = -7 + 5 = -2$$

$$(x-3)^2 + (-x+5+2)^2 = 16 \quad y = -3 + 5 = 2$$

$$x^2 - 6x + 9 + x^2 - 14x + 49 = 16$$

$$2x^2 - 20x + 42 = 0$$

$$x^2 - 10x + 21 = 0$$

$$(x-7)(x-3) = 0$$

$$x = 7, 3$$

REF: 061633aai NAT: A.REI.C.7 TOP: Quadratic-Linear Systems

430 ANS:

$$4x + 6y - 8z = -2 \quad 4x + 6y - 8z = -2 \quad 4x - 8y + 20z = 12 \quad z + 2 = 3z - 4 \quad y = 3 + 2 \quad -4x + 5 + 3 = 16$$

$$4x - 8y + 20z = 12 \quad \underline{-4x + y + z = 16} \quad \underline{-4x + y + z = 16} \quad 6 = 2z \quad = 5 \quad -4x = 8$$

$$-4x + y + z = 16 \quad 7y - 7z = 14 \quad -7y + 21z = 28 \quad z = 3 \quad x = -2$$

$$y - z = 2 \quad y - 3z = -4$$

$$y = z + 2 \quad y = 3z - 4$$

REF: 081833aai NAT: A.REI.C.6 TOP: Solving Linear Systems

KEY: three variables

431 ANS:

$$y = 4.168(3.981)^x \quad 100 = 4.168(3.981)^x$$

$$\log \frac{100}{4.168} = \log(3.981)^x$$

$$\log \frac{100}{4.168} = x \log(3.981)$$

$$\frac{\log \frac{100}{4.168}}{\log(3.981)} = x$$

$$x \approx 2.25$$

REF: 081736aai NAT: S.ID.B.6 TOP: Regression KEY: exponential

432 ANS:

$$16x^4 - 81 = (4x^2 + 9)(4x^2 - 9) = (4x^2 + 9)(2x + 3)(2x - 3). \text{ No, because } \pm \frac{3i}{2} \text{ are roots.}$$

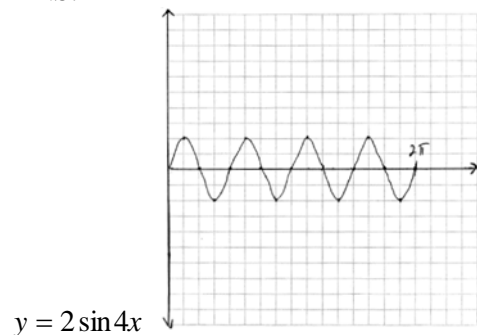
REF: 061933aai NAT: F.IF.B.4 TOP: Graphing Polynomial Functions

433 ANS:

$$\frac{6.25 - 2.25}{21 - 5} = \frac{4}{16} = \$0.25 \text{ fine per day. } 2.25 - 5(.25) = \$1 \text{ replacement fee. } a_n = 1.25 + (n - 1)(.25). a_{60} = \$16$$

REF: 081734aai NAT: F.BF.A.2 TOP: Sequences

434 ANS:

REF: 081934aai NAT: F.IF.C.7 TOP: Graphing Trigonometric Functions  
KEY: graph

435 ANS:

John found the means of the scores of the two rooms and subtracted the means. The mean score for the classical room was 7 higher than the rap room (82-75). Yes, there is less than a 5% chance this difference occurring due to random chance. It is likely the difference was due to the music.

REF: 081836aai NAT: S.IC.B.5 TOP: Analysis of Data

436 ANS:

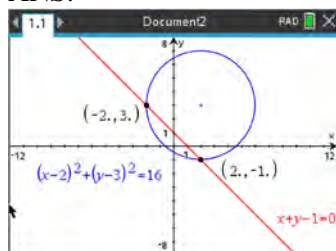
$$x+2 \overline{) \begin{array}{r} x^3 + 4 \\ x^4 + 2x^3 + 4x - 10 \end{array}} \quad x^3 + 4 - \frac{18}{x+2}. \text{ No, because there is a remainder.}$$

$$\begin{array}{r} x^4 + 2x^3 \\ \underline{x^4 + 2x^3} \\ 4x - 10 \\ \underline{4x + 8} \\ -18 \end{array}$$

REF: 011934aia NAT: A.APR.D.6 TOP: Rational Expressions

KEY: division

437 ANS:



$$y = -x + 1 \quad y = -2 + 1 = -1 \quad (2, -1)$$

$$(x-2)^2 + (-x+1-3)^2 = 16 \quad y = 2+1 = 3 \quad (-2, 3)$$

$$x^2 - 4x + 4 + x^2 + 4x + 4 = 16$$

$$2x^2 = 8$$

$$x = -2, 2$$

REF: 012035aia NAT: A.REI.C.7 TOP: Quadratic-Linear Systems

438 ANS:

$23 - 18 = 5$ ,  $\bar{x} \pm 2\sigma = -3.07 - 3.13$ , Yes, a difference of 5 or more occurred three times out of a thousand, which is statistically significant.

REF: 061834aia NAT: S.IC.B.5 TOP: Analysis of Data

439 ANS:

$$\frac{3p}{p-5} = \frac{p+2}{p+3}$$

$$3p^2 + 9p = p^2 - 3p - 10$$

$$2p^2 + 12p + 10 = 0$$

$$p^2 + 6p + 5 = 0$$

$$(p+5)(p+1) = 0$$

$$p = -5, -1$$

REF: 081733aii NAT: A.REI.A.2 TOP: Solving Rationals

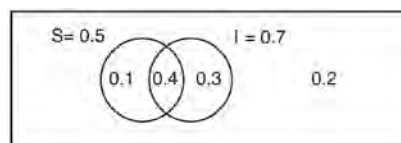
KEY: rational solutions

440 ANS:

$$f(x) = x^2(x+4)(x-3); g(x) = (x+2)^2(x+6)(x-1)$$

REF: 011836aii NAT: A.APR.B.3 TOP: Graphing Polynomial Functions

441 ANS:



This scenario can be modeled with a Venn Diagram:

Since  $P(S \cup I) = 0.2$ ,  $P(S \cup I) = 0.8$ . Then,  $P(S \cap I) = P(S) + P(I) - P(S \cup I)$  If  $S$  and  $I$  are independent, then the

$$= 0.5 + 0.7 - 0.8$$

$$= 0.4$$

Product Rule must be satisfied. However,  $(0.5)(0.7) \neq 0.4$ . Therefore, salary and insurance have not been treated independently.

REF: spr1513aii NAT: S.CP.A.2 TOP: Probability of Compound Events

KEY: independence

442 ANS:

$$a + 4b + 6c = 23 \quad a + 2b + c = 2 \quad 8b + 3c = 16 \quad 2b + 5(4) = 21 \quad a + 4\left(\frac{1}{2}\right) + 6(4) = 23$$

$$\underline{a + 2b + c = 2} \quad \underline{-a + 6b + 2c = 14} \quad \underline{8b + 20c = 84} \quad 2b = 1 \quad a + 2 + 24 = 23$$

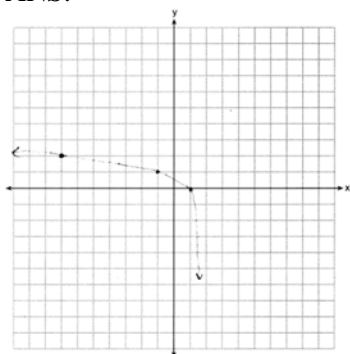
$$2b + 5c = 21 \quad 8b + 3c = 16 \quad 17c = 68 \quad b = \frac{1}{2} \quad a = -3$$

$$c = 4$$

REF: 011933aii NAT: A.REI.C.6 TOP: Solving Linear Systems

KEY: three variables

443 ANS:

Domain:  $x < 2$ , Asymptote  $x = 2$ 

REF: 012034aai NAT: F.IF.C.7 TOP: Graphing Logarithmic Functions

444 ANS:

$$S_n = \frac{33000 - 33000(1.04)^n}{1 - 1.04} \quad S_{15} = \frac{33000 - 33000(1.04)^{15}}{1 - 1.04} \approx 660778.39$$

REF: 061634aai NAT: A.SSE.B.4 TOP: Series

445 ANS:

Some of the students who did not drink energy drinks read faster than those who did drink energy drinks.

$17.7 - 19.1 = -1.4$  Differences of  $-1.4$  and less occur  $\frac{25}{232}$  or about 10% of the time, so the difference is not unusual.

REF: 081636aai NAT: S.IC.B.5 TOP: Analysis of Data

446 ANS:

Jillian's plan, because distance increases by one mile each week.  $a_1 = 10$        $a_n = n + 12$ 

$$a_n = a_{n-1} + 1$$

REF: 011734aai NAT: F.LE.A.2 TOP: Sequences KEY: recursive

447 ANS:

$$2x^3 - 10x^2 + 11x - 7 = 2x^3 + hx^2 + 3x - 8x^2 - 4hx - 12 + k \quad h = -2$$

$$-2x^2 + 8x + 5 = hx^2 - 4hx + k \quad k = 5$$

REF: 011733aai NAT: A.APR.C.4 TOP: Polynomial Identities

448 ANS:

$$(2x^2 + x - 3) \cdot (x - 1) - \left[ (2x^2 + x - 3) + (x - 1) \right]$$

$$(2x^3 - 2x^2 + x^2 - x - 3x + 3) - (2x^2 + 2x - 4)$$

$$2x^3 - 3x^2 - 6x + 7$$

REF: 011833aai NAT: F.BF.A.1 TOP: Operations with Functions

449 ANS:

$$\begin{aligned} (\sqrt{2x-7})^2 &= (5-x)^2 & \sqrt{2(4)-7}+4=5 & \sqrt{2(8)-7}+8=5 \\ 2x-7 &= 25-10x+x^2 & \sqrt{1} &= 1 & \sqrt{9} &\neq -3 \\ 0 &= x^2-12x+32 \\ 0 &= (x-8)(x-4) \\ x &= 4,8 \end{aligned}$$

REF: 081635aai NAT: A.REI.A.2 TOP: Solving Radicals  
KEY: extraneous solutions

450 ANS:

$$\begin{aligned} j(-1) &= 2(-1)^4 - (-1)^3 - 35(-1)^2 + 16(-1) + 48 = 2 + 1 - 35 - 16 + 48 = 0; \quad x+1 \text{ is a factor of } j(x); \\ 2x^3 - 3x^2 - 32x + 48 &= 0 \\ x^2(2x-3) - 16(2x-3) &= 0 \\ (x^2-16)(2x-3) &= 0 \\ x &= \pm 4, \frac{3}{2} \end{aligned}$$

REF: 081834aai NAT: A.APR.B.2 TOP: Remainder Theorem

451 ANS:

$$\begin{aligned} \frac{f(4)-f(-2)}{4-(-2)} &= \frac{80-1.25}{6} = 13.125 \quad g(x) \text{ has a greater rate of change} \\ \frac{g(4)-g(-2)}{4-(-2)} &= \frac{179-(-49)}{6} = 38 \end{aligned}$$

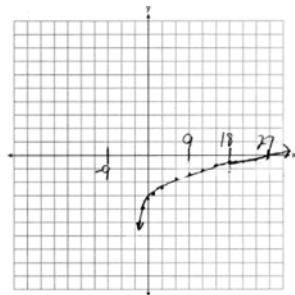
REF: 061636aai NAT: F.IF.C.9 TOP: Comparing Functions

452 ANS:

$138.905 \pm 2 \cdot 7.95 = 123 - 155$ . No, since 125 (50% of 250) falls within the 95% interval.

REF: 011835aai NAT: S.IC.A.2 TOP: Analysis of Data

453 ANS:



As  $x \rightarrow -3, y \rightarrow -\infty$ . As  $x \rightarrow \infty, y \rightarrow \infty$ .

REF: 061735aai NAT: F.IF.C.7 TOP: Graphing Logarithmic Functions

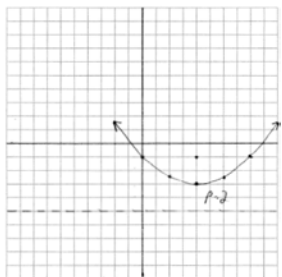


454 ANS:

$$P(P/K) = \frac{P(P \wedge K)}{P(K)} = \frac{1.9}{2.3} \approx 82.6\% \quad \text{A key club member has an 82.6\% probability of being enrolled in AP Physics.}$$

REF: 011735aia NAT: S.CP.B.6 TOP: Conditional Probability

455 ANS:



$$y = \frac{1}{4(2)}(x-4)^2 - 3 \quad y = \frac{-1 + -5}{2} = -3. \quad \text{The vertex is } (4, -3) \text{ and } p = 2.$$

REF: 061935aia NAT: G.GPE.A.2 TOP: Graphing Quadratic Functions

456 ANS:

$$\frac{h(2) - h(1)}{2 - 1} = -12, \quad h(t) = 0 \text{ at } t \approx 2.2, 3.8, \text{ using a graphing calculator to find where } h(t) = 0.$$

REF: 061836aia NAT: F.IF.B.4 TOP: Graphing Trigonometric Functions

457 ANS:

$$\sqrt{6-2x} + x = 2x + 30 - 9 \quad \sqrt{6-2(-29)} \neq -29 + 21, \text{ so } -29 \text{ is extraneous.}$$

$$\sqrt{6-2x} = x + 21 \quad \sqrt{64} \neq -8$$

$$6 - 2x = x^2 + 42x + 441$$

$$x^2 + 44x + 435 = 0$$

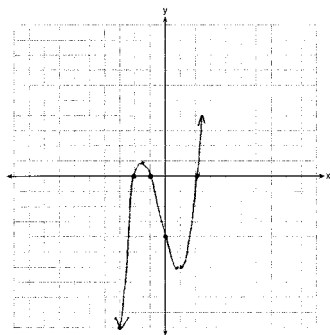
$$(x + 29)(x + 15) = 0$$

$$x = -29, -15$$

REF: 061833aia NAT: A.REI.A.2 TOP: Solving Radicals

KEY: extraneous solutions

458 ANS:



$$0 = x^2(x + 1) - 4(x + 1)$$

$$0 = (x^2 - 4)(x + 1)$$

$$0 = (x + 2)(x - 2)(x + 1)$$

$$x = -2, -1, 2$$

REF: 081633aai NAT: F.IF.C.7 TOP: Graphing Polynomial Functions

459 ANS:

$$x^2 - 6x = -17 \quad \text{The solution is imaginary because the parabola and line do not intersect.}$$

$$x^2 - 6x + 9 = -17 + 9$$

$$(x - 3)^2 = -8$$

$$x - 3 = \pm 2i\sqrt{2}$$

$$x = 3 \pm 2i\sqrt{2}$$

REF: 081936aai NAT: A.REI.B.4 TOP: Solving Quadratics

KEY: complex solutions | completing the square

460 ANS:

The mean difference between the students' final grades in group 1 and group 2 is  $-3.64$ . This value indicates that students who met with a tutor had a mean final grade of 3.64 points less than students who used an on-line subscription. One can infer whether this difference is due to the differences in intervention or due to which students were assigned to each group by using a simulation to rerandomize the students' final grades many (500) times. If the observed difference  $-3.64$  is the result of the assignment of students to groups alone, then a difference of  $-3.64$  or less should be observed fairly regularly in the simulation output. However, a difference of  $-3$  or less occurs in only about 2% of the rerandomizations. Therefore, it is quite unlikely that the assignment to groups alone accounts for the difference; rather, it is likely that the difference between the interventions themselves accounts for the difference between the two groups' mean final grades.

REF: fall1514aai NAT: S.IC.B.5 TOP: Analysis of Data

461 ANS:

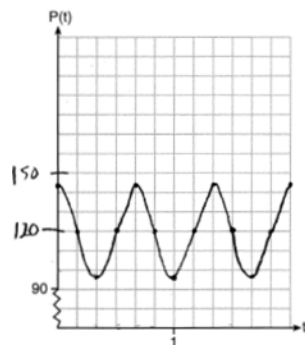
$$2 = e^{0.0375t}$$

$$t \approx 18.5$$

REF: 081835aai NAT: F.LE.A.4 TOP: Exponential Growth

## Algebra II 6 Point Regents Exam Questions Answer Section

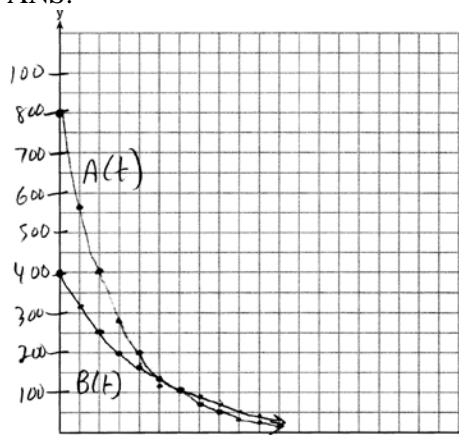
462 ANS:



The period of  $P$  is  $\frac{2}{3}$ , which means the patient's blood pressure reaches a high every  $\frac{2}{3}$  second and a low every  $\frac{2}{3}$  second. The patient's blood pressure is high because  $144$  over  $96$  is greater than  $120$  over  $80$ .

REF: 011837aii    NAT: F.IF.C.7    TOP: Graphing Trigonometric Functions  
KEY: graph

463 ANS:



$$A(t) = 800e^{-0.347t}$$

$$800e^{-0.347t} = 400e^{-0.231t} \quad 0.15 = e^{-0.347t}$$

$$B(t) = 400e^{-0.231t}$$

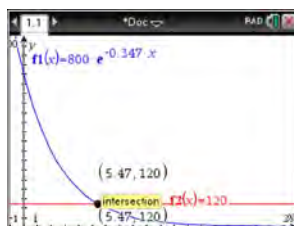
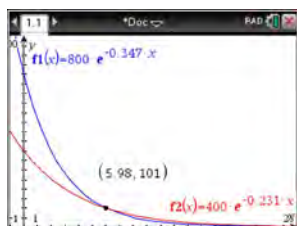
$$\ln 2e^{-0.347t} = \ln e^{-0.231t} \quad \ln 0.15 = \ln e^{-0.347t}$$

$$\ln 2 + \ln e^{-0.347t} = \ln e^{-0.231t} \quad \ln 0.15 = -0.347t \cdot \ln e$$

$$\ln 2 - 0.347t = -0.231t \quad 5.5 \approx t$$

$$\ln 2 = 0.116t$$

$$6 \approx t$$



REF: 061637aII NAT: A.REI.D.11 TOP: Other Systems

464 ANS:

$$100 = 140 \left( \frac{1}{2} \right)^{\frac{5}{h}} \quad \log \frac{100}{140} = \log \left( \frac{1}{2} \right)^{\frac{5}{h}} \quad 40 = 140 \left( \frac{1}{2} \right)^{\frac{t}{10.3002}}$$

$$\log \frac{5}{7} = \frac{5}{h} \log \frac{1}{2}$$

$$\log \frac{2}{7} = \log \left( \frac{1}{2} \right)^{\frac{t}{10.3002}}$$

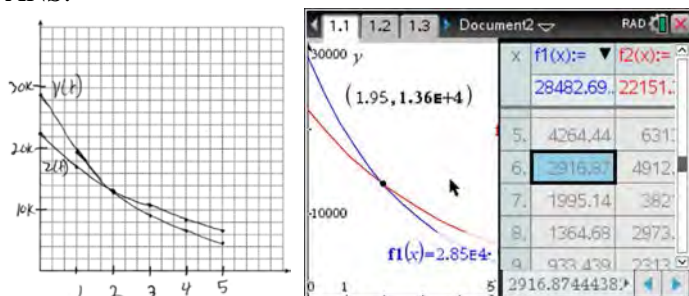
$$h = \frac{5 \log \frac{1}{2}}{\log \frac{5}{7}} \approx 10.3002$$

$$\log \frac{2}{7} = \frac{t \log \left( \frac{1}{2} \right)}{10.3002}$$

$$t = \frac{10.3002 \log \frac{2}{7}}{\log \frac{1}{2}} \approx 18.6$$

REF: 061737aII NAT: F.LE.A.4 TOP: Exponential Decay

465 ANS:



At 1.95 years, the value of the car equals the loan balance. Zach can cancel the policy after 6 years.

REF: 081737aii NAT: A.REI.D.11 TOP: Other Systems

466 ANS:

$$A = 5000(1.045)^n \quad 5000\left(1 + \frac{.046}{4}\right)^{4(6)} - 5000(1.045)^6 \approx 6578.87 - 6511.30 \approx 67.57 \quad 10000 = 5000\left(1 + \frac{.046}{4}\right)^{4n}$$

$$B = 5000\left(1 + \frac{.046}{4}\right)^{4n}$$

$$2 = 1.0115^{4n}$$

$$\log 2 = 4n \cdot \log 1.0115$$

$$n = \frac{\log 2}{4 \log 1.0115}$$

$$n \approx 15.2$$

REF: 081637aii NAT: A.CED.A.1 TOP: Exponential Growth

467 ANS:

$$0 = \sqrt{t} - 2t + 6 \quad 2\left(\frac{9}{4}\right) - 6 < 0, \text{ so } \frac{9}{4} \text{ is extraneous.}$$

$$2t - 6 = \sqrt{t}$$

$$4t^2 - 24t + 36 = t$$

$$4t^2 - 25t + 36 = 0$$

$$(4t - 9)(t - 4) = 0$$

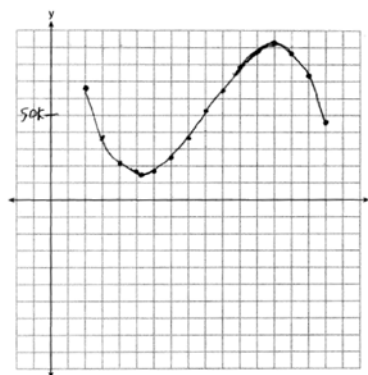
$$t = \frac{9}{4}, 4$$

$$(\sqrt{1} - 2(1) + 6) - (\sqrt{3} - 2(3) + 6) = 5 - \sqrt{3} \approx 3.268 \quad 327 \text{ mph}$$

REF: 011737aii NAT: A.REI.A.2 TOP: Solving Radicals

KEY: context

468 ANS:



$$P(x) = R(x) - C(x) = -330x^3 + 9000x^2 - 67000x + 167000$$

Least profitable at year 5 because there is a minimum in  $P(x)$ . Most profitable at year 13 because there is a maximum in  $P(x)$ .

REF: 081837aii NAT: F.IF.C.7 TOP: Graphing Polynomial Functions

469 ANS:

$$B = 1.69\sqrt{30 + 4.45} - 3.49 \approx 6, \text{ which is a steady breeze.}$$

$$15 = 1.69\sqrt{s + 4.45} - 3.49$$

$$18.49 = 1.69\sqrt{s + 4.45}$$

$$\frac{18.49}{1.69} = \sqrt{s + 4.45}$$

$$\left(\frac{18.49}{1.69}\right)^2 = s + 4.45$$

$$s = \left(\frac{18.49}{1.69}\right)^2 - 4.45$$

$$s \approx 115$$

$$9.5 = 1.69\sqrt{s + 4.45} - 3.49 \quad 10.49 = 1.69\sqrt{s + 4.45} - 3.49 \quad 55-64$$

$$12.99 = 1.69\sqrt{s + 4.45} \quad 13.98 = 1.69\sqrt{s + 4.45}$$

$$\frac{12.99}{1.69} = \sqrt{s + 4.45} \quad \frac{13.98}{1.69} = \sqrt{s + 4.45}$$

$$\left(\frac{12.99}{1.69}\right)^2 = s + 4.45 \quad \left(\frac{13.98}{1.69}\right)^2 = s + 4.45$$

$$s = \left(\frac{12.99}{1.69}\right)^2 - 4.45 \quad s = \left(\frac{13.98}{1.69}\right)^2 - 4.45$$

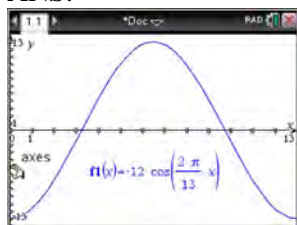
$$s \approx 55$$

$$s \approx 64$$

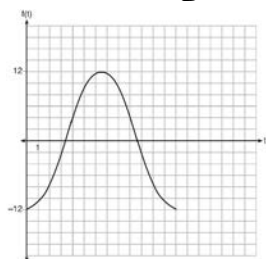
REF: 081937aii NAT: A.REI.A.2 TOP: Solving Radicals

KEY: context

470 ANS:



The amplitude, 12, can be interpreted from the situation, since the water level has a minimum of  $-12$  and a maximum of  $12$ . The value of  $A$  is  $-12$  since at  $8:30$  it is low tide. The period of the function is 13 hours, and is expressed in the function through the parameter  $B$ . By experimentation with technology or using the relation  $P = \frac{2\pi}{B}$  (where  $P$  is the period), it is determined that  $B = \frac{2\pi}{13}$ .



$$f(t) = -12 \cos\left(\frac{2\pi}{13} t\right)$$

In order to answer the question about when to fish, the student must interpret the function and determine which choice,  $7:30$  pm or  $10:30$  pm, is on an increasing interval. Since the function is increasing from  $t = 13$  to  $t = 19.5$  (which corresponds to  $9:30$  pm to  $4:00$  am),  $10:30$  is the appropriate choice.

REF: spr1514aii NAT: F.IF.C.7 TOP: Graphing Trigonometric Functions

KEY: graph

471 ANS:

$$\text{antibiotic } n(0) = \frac{0+1}{0+5} + \frac{18}{0^2 + 8(0) + 15} = \frac{3}{15} + \frac{18}{15} = \frac{21}{15}$$

$$\frac{t+1}{t+5} + \frac{18}{t^2 + 8t + 15} = \frac{9}{t+3}$$

$$a(0) = \frac{9}{0+3} = 3$$

$$\frac{(t+1)(t+3)}{(t+5)(t+3)} + \frac{18}{(t+3)(t+5)} = \frac{9(t+5)}{(t+3)(t+5)}$$

$$t^2 + 4t + 3 + 18 = 9t + 45$$

$$t^2 - 5t - 24 = 0$$

$$(t-8)(t+3) = 0$$

$$t = 8$$

REF: 012037aii NAT: A.REI.A.2 TOP: Solving Rationals

KEY: rational solutions

472 ANS:

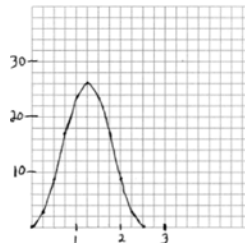
$A(t) = 100(0.5)^{\frac{t}{63}}$ , where  $t$  is time in years, and  $A(t)$  is the amount of titanium-44 left after  $t$  years.

$\frac{A(10) - A(0)}{10 - 0} = \frac{89.58132 - 100}{10} = -1.041868$  The estimated mass at  $t = 40$  is  $100 - 40(-1.041868) \approx 58.3$ . The

actual mass is  $A(40) = 100(0.5)^{\frac{40}{63}} \approx 64.3976$ . The estimated mass is less than the actual mass.

REF: fall1517aai NAT: F.LE.A.2 TOP: Modeling Exponential Functions

473 ANS:



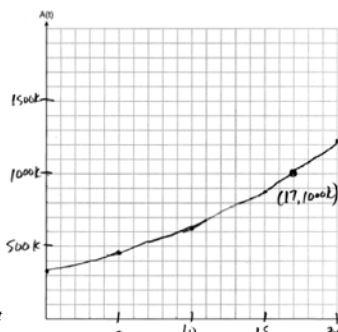
period =  $\frac{2\pi}{0.8\pi} = 2.5$ . The wheel rotates once every 2.5 seconds.  
of  $f(t) = 26$ .

No, because the maximum

REF: 061937aai NAT: F.IF.C.7 TOP: Graphing Trigonometric Functions

KEY: graph

474 ANS:



$A(t) = 318000(1.07)^t$   $318000(1.07)^t = 1000000$  The graph of  $A(t)$  nearly intersects

$$1.07^t = \frac{1000}{318}$$

$$t \log 1.07 = \log \frac{1000}{318}$$

$$t = \frac{\log \frac{1000}{318}}{\log 1.07}$$

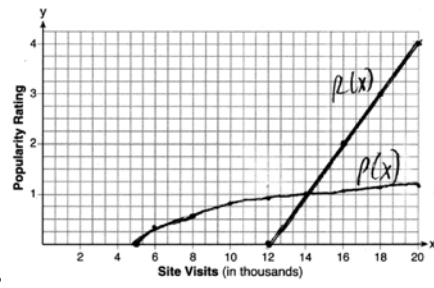
$$t \approx 17$$

the point (17, 1000000).

REF: 011937aai NAT: A.CED.A.1 TOP: Exponential Growth



475 ANS:



$P(16) = \log(16 - 4) \approx 1.1$ , 14000

REF: 061837aii NAT: A.REI.D.11 TOP: Other Systems