## 0611ge

1 Line segment $A B$ is shown in the diagram below.


Which two sets of construction marks, labeled I, II, III, and IV, are part of the construction of the perpendicular bisector of line segment $A B$ ?

1) I and II
2) I and III
3) II and III
4) II and IV

2 If $\triangle J K L \cong \triangle M N O$, which statement is always true?

1) $\angle K L J \cong \angle N M O$
2) $\angle K J L \cong \angle M O N$
3) $\overline{J L} \cong \overline{M O}$
4) $\overline{J K} \cong \overline{O N}$

3 In the diagram below, $\Delta A^{\prime} B^{\prime} C^{\prime}$ is a transformation of $\triangle A B C$, and $\Delta A^{\prime \prime} B^{\prime \prime} C^{\prime \prime}$ is a transformation of $\Delta A^{\prime} B^{\prime} C^{\prime}$.


The composite transformation of $\triangle A B C$ to $\Delta A^{\prime \prime} B^{\prime \prime} C^{\prime \prime}$ is an example of a

1) reflection followed by a rotation
2) reflection followed by a translation
3) translation followed by a rotation
4) translation followed by a reflection

4 In the diagram below of $\triangle A C E$, medians $\overline{A D}, \overline{E B}$, and $\overline{C F}$ intersect at $G$. The length of $\overline{F G}$ is 12 cm .


What is the length, in centimeters, of $\overline{G C}$ ?

1) 24
2) 12
3) 6
4) 4

5 In the diagram below of circle $O$, chord $\overline{A B}$ is parallel to chord $\overline{C D}$.


Which statement must be true?

1) $\overparen{A C} \cong \overparen{B D}$
2) $\overparen{A B} \cong \overparen{C D}$
3) $\overline{A B} \cong \overline{C D}$
4) $\widehat{A B D} \cong \overparen{C D B}$

6 In the diagram below, line $p$ intersects line $m$ and line $n$.


If $\mathrm{m} \angle 1=7 x$ and $\mathrm{m} \angle 2=5 x+30$, lines $m$ and $n$ are parallel when $x$ equals

1) 12.5
2) 15
3) 87.5
4) 105

7 In the diagram of $\triangle K L M$ below, $\mathrm{m} \angle L=70$, $\mathrm{m} \angle M=50$, and $\overline{M K}$ is extended through $N$.


What is the measure of $\angle L K N$ ?

1) $60^{\circ}$
2) $120^{\circ}$
3) $180^{\circ}$
4) $300^{\circ}$

8 If two distinct planes, $\mathcal{A}$ and $\mathcal{B}$, are perpendicular to line $c$, then which statement is true?

1) Planes $\mathcal{A}$ and $\mathscr{B}$ are parallel to each other.
2) Planes $\mathcal{A}$ and $\mathscr{B}$ are perpendicular to each other.
3) The intersection of planes $\mathcal{A}$ and $\mathcal{B}$ is a line parallel to line $c$.
4) The intersection of planes $\mathcal{A}$ and $\mathscr{B}$ is a line perpendicular to line $c$.

9 What is the length of the line segment whose endpoints are $A(-1,9)$ and $B(7,4)$ ?

1) $\sqrt{61}$
2) $\sqrt{89}$
3) $\sqrt{205}$
4) $\sqrt{233}$

10 What is an equation of circle $O$ shown in the graph below?


1) $(x+1)^{2}+(y-3)^{2}=25$
2) $(x-1)^{2}+(y+3)^{2}=25$
3) $(x-5)^{2}+(y+6)^{2}=25$
4) $(x+5)^{2}+(y-6)^{2}=25$

11 In the diagram below, parallelogram $A B C D$ has diagonals $\overline{A C}$ and $\overline{B D}$ that intersect at point $E$.


Which expression is not always true?

1) $\angle D A E \cong \angle B C E$
2) $\angle D E C \cong \angle B E A$
3) $\overline{A C} \cong \overline{D B}$
4) $\overline{D E} \cong \overline{E B}$

12 The volume, in cubic centimeters, of a sphere whose diameter is 6 centimeters is

1) $12 \pi$
2) $36 \pi$
3) $48 \pi$
4) $288 \pi$

13 The equation of line $k$ is $y=\frac{1}{3} x-2$. The equation of line $m$ is $-2 x+6 y=18$. Lines $k$ and $m$ are

1) parallel
2) perpendicular
3) the same line
4) neither parallel nor perpendicular

14 What are the center and the radius of the circle whose equation is $(x-5)^{2}+(y+3)^{2}=16$ ?

1) $(-5,3)$ and 16
2) $(5,-3)$ and 16
3) $(-5,3)$ and 4
4) $(5,-3)$ and 4

15 Triangle $A B C$ has vertices $A(0,0), B(3,2)$, and $C(0,4)$. The triangle may be classified as

1) equilateral
2) isosceles
3) right
4) scalene

16 In rhombus $A B C D$, the diagonals $\overline{A C}$ and $\overline{B D}$ intersect at $E$. If $A E=5$ and $B E=12$, what is the length of $\overline{A B}$ ?

1) 7
2) 10
3) 13
4) 17

17 In the diagram below of circle $O, \overline{P A}$ is tangent to circle $O$ at $A$, and $\overline{P B C}$ is a secant with points $B$ and $C$ on the circle.


If $P A=8$ and $P B=4$, what is the length of $\overline{B C}$ ?

1) 20
2) 16
3) 15
4) 12

18 Lines $m$ and $n$ intersect at point $A$. Line $k$ is perpendicular to both lines $m$ and $n$ at point $A$. Which statement must be true?

1) Lines $m, n$, and $k$ are in the same plane.
2) Lines $m$ and $n$ are in two different planes.
3) Lines $m$ and $n$ are perpendicular to each other.
4) Line $k$ is perpendicular to the plane containing lines $m$ and $n$.

19 In $\triangle D E F, \mathrm{~m} \angle D=3 x+5, \mathrm{~m} \angle E=4 x-15$, and $\mathrm{m} \angle F=2 x+10$. Which statement is true?

1) $D F=F E$
2) $D E=F E$
3) $\mathrm{m} \angle E=\mathrm{m} \angle F$
4) $\mathrm{m} \angle D=\mathrm{m} \angle F$

20 As shown in the diagram below, $\triangle A B C \sim \triangle D E F$, $A B=7 x, B C=4, D E=7$, and $E F=x$.


What is the length of $\overline{A B}$ ?

1) 28
2) 2
3) 14
4) 4

21 A man wants to place a new bird bath in his yard so that it is 30 feet from a fence, $f$, and also 10 feet from a light pole, $P$. As shown in the diagram below, the light pole is 35 feet away from the fence.


How many locations are possible for the bird bath?

1) 1
2) 2
3) 3
4) 0

22 As shown on the graph below, $\Delta R^{\prime} S^{\prime} T^{\prime}$ is the image of $\triangle R S T$ under a single transformation.


Which transformation does this graph represent?

1) glide reflection
2) line reflection
3) rotation
4) translation

23 Which line is parallel to the line whose equation is $4 x+3 y=7$ and also passes through the point $(-5,2)$ ?

1) $4 x+3 y=-26$
2) $4 x+3 y=-14$
3) $3 x+4 y=-7$
4) $3 x+4 y=14$

24 If the vertex angles of two isosceles triangles are congruent, then the triangles must be

1) acute
2) congruent
3) right
4) similar

25 Which quadrilateral has diagonals that always bisect its angles and also bisect each other?

1) rhombus
2) rectangle
3) parallelogram
4) isosceles trapezoid

26 When $\triangle A B C$ is dilated by a scale factor of 2 , its image is $\Delta A^{\prime} B^{\prime} C^{\prime}$. Which statement is true?

1) $\overline{A C} \cong \overline{A^{\prime} C^{\prime}}$
2) $\angle A \cong \angle A^{\prime}$
3) perimeter of $\triangle A B C=$ perimeter of $\triangle A^{\prime} B^{\prime} C^{\prime}$
4) $2($ area of $\Delta A B C)=$ area of $\Delta A^{\prime} B^{\prime} C^{\prime}$

27 What is the slope of a line that is perpendicular to the line whose equation is $3 x+5 y=4$ ?

1) $-\frac{3}{5}$
2) $\frac{3}{5}$
3) $-\frac{5}{3}$
4) $\frac{5}{3}$

28 In the diagram below of right triangle $A B C$, altitude $\overline{B D}$ is drawn to hypotenuse $\overline{A C}, A C=16$, and $C D=7$.


What is the length of $\overline{B D}$ ?

1) $3 \sqrt{7}$
2) $4 \sqrt{7}$
3) $7 \sqrt{3}$
4) 12

29 Given the true statement, "The medians of a triangle are concurrent," write the negation of the statement and give the truth value for the negation.

30 Using a compass and straightedge, on the diagram below of $\overleftrightarrow{R S}$, construct an equilateral triangle with $\overline{R S}$ as one side. [Leave all construction marks.]


31 The Parkside Packing Company needs a rectangular shipping box. The box must have a length of 11 inches and a width of 8 inches. Find, to the nearest tenth of an inch, the minimum height of the box such that the volume is at least 800 cubic inches.

32 A pentagon is drawn on the set of axes below. If the pentagon is reflected over the $y$-axis, determine if this transformation is an isometry. Justify your answer. [The use of the set of axes is optional.]


33 In the diagram below of $\triangle A B C, D$ is a point on $\overline{A B}$, $E$ is a point on $\overline{B C}, \overline{A C} \| \overline{D E}, C E=25$ inches, $A D=18$ inches, and $D B=12$ inches. Find, to the nearest tenth of an inch, the length of $\overline{E B}$.


34 In circle $O$, diameter $\overline{R S}$ has endpoints $R(3 a, 2 b-1)$ and $S(a-6,4 b+5)$. Find the coordinates of point $O$, in terms of $a$ and $b$. Express your answer in simplest form.

35 On the set of coordinate axes below, graph the locus of points that are equidistant from the lines $y=6$ and $y=2$ and also graph the locus of points that are 3 units from the $y$-axis. State the coordinates of all points that satisfy both conditions.


36 In the diagram below, tangent $\overline{M L}$ and secant $\overline{M N K}$ are drawn to circle $O$. The ratio $\mathrm{m} \overparen{L N}: \mathrm{m} \overparen{N K}: \mathrm{m} \overparen{K L}$ is $3: 4: 5$. Find $\mathrm{m} \angle L M K$.


37 Solve the following system of equations graphically.

$$
\begin{gathered}
2 x^{2}-4 x=y+1 \\
x+y=1
\end{gathered}
$$



38 In the diagram below, $\overline{P A}$ and $\overline{P B}$ are tangent to circle $O, \overline{O A}$ and $\overline{O B}$ are radii, and $\overline{O P}$ intersects the circle at $C$. Prove: $\angle A O P \cong \angle B O P$


## 0611ge

## Answer Section



PTS: 2
REF: 061105ge
STA: G.G. 52
TOP: Chords
6 ANS: 2
$7 x=5 x+30$
$2 x=30$
$x=15$

PTS: 2
7 ANS: 2
TOP
8 ANS: 1
8 ANS: 1
TOP: Planes
9 ANS: 2
$d=\sqrt{(-1-7)^{2}+(9-4)^{2}}=\sqrt{64+25}=\sqrt{89}$
PTS: 2
KEY: general
10 ANS: 1
PTS: 2
TOP: Equations of Circles
11 ANS: $3 \quad$ PTS: 2
TOP: Parallelograms
12 ANS: 2
$V=\frac{4}{3} \pi r^{3}=\frac{4}{3} \pi \cdot 3^{3}=36 \pi$
PTS: 2 REF: 061112ge
13 ANS: 1
PTS: 2
TOP: Parallel and Perpendicular Lines
14 ANS: 4 PTS: 2
TOP: Equations of Circles
15 ANS: $2 \quad$ PTS: 2
TOP: Triangles in the Coordinate Plane

STA: G.G. 16
REF: 061113ge
REF: 061114ge
REF: 061115ge STA: G.G. 69

TOP: Volume and Surface Area
STA: G.G. 63
STA: G.G. 73

16 ANS: 3
$\sqrt{5^{2}+12^{2}}=13$
PTS: 2 REF: 061116ge STA: G.G. 39 TOP: Special Parallelograms
17 ANS: 4
$4(x+4)=8^{2}$
$4 x+16=64$
$4 x=48$
$x=12$
PTS: 2
REF: 061117ge
STA: G.G. 53
TOP: Segments Intercepted by Circle
KEY: tangent and secant
18 ANS: 4
PTS: 2
REF: 061118ge
STA: G.G. 1
TOP: Planes
19 ANS: 1
$3 x+5+4 x-15+2 x+10=180 . \mathrm{m} \angle D=3(20)+5=65 . \mathrm{m} \angle E=4(20)-15=65$.

$$
\begin{aligned}
9 x & =180 \\
x & =20
\end{aligned}
$$

PTS: 2 REF: 061119ge STA: G.G. 30 TOP: Interior and Exterior Angles of Triangles
20 ANS: 3
$\frac{7 x}{4}=\frac{7}{x} .7(2)=14$
$7 x^{2}=28$
$x=2$
PTS: 2
REF: 061120ge
STA: G.G. 45 TOP: Similarity
KEY: basic
21 ANS: 2
PTS: 2
REF: 061121ge
STA: G.G. 22
TOP: Locus
22 ANS: 3
PTS: 2
REF: 061122ge STA: G.G. 56
TOP: Identifying Transformations
23 ANS: 2
The slope of a line in standard form is $\frac{-A}{B}$, so the slope of this line is $\frac{-4}{3}$. A parallel line would also have a slope of $\frac{-4}{3}$. Since the answers are in standard form, use the point-slope formula. $y-2=-\frac{4}{3}(x+5)$

$$
\begin{aligned}
3 y-6 & =-4 x-20 \\
4 x+3 y & =-14
\end{aligned}
$$

PTS: 2
24 ANS: 4
REF: 061123ge
STA: G.G. 65
TOP: Isosceles Triangle Theorem

25 ANS: $1 \quad$ PTS: 2
REF: 061125ge STA: G.G. 39
TOP: Special Parallelograms
26 ANS: $2 \quad$ PTS: 2
TOP: Properties of Transformations
27 ANS: 4
The slope of $3 x+5 y=4$ is $m=\frac{-A}{B}=\frac{-3}{5} . m_{\perp}=\frac{5}{3}$.
PTS: 2
REF: 061127ge
STA: G.G. 62
TOP: Parallel and Perpendicular Lines
28 ANS: 1
$x^{2}=7(16-7)$
$x^{2}=63$
$x=\sqrt{9} \sqrt{7}$
$x=3 \sqrt{7}$
PTS: 2
REF: 061128ge
STA: G.G. 47
TOP: Similarity
KEY: altitude
29 ANS:
The medians of a triangle are not concurrent. False.
PTS: 2
REF: 061129 ge
STA: G.G. 24
ANS:


PTS: 2
REF: 061130ge
STA: G.G. 20
31 ANS:
9.1. (11)(8) $h=800$

$$
h \approx 9.1
$$

PTS: 2
REF: 061131ge
STA: G.G. 12
TOP: Constructions

TOP: Volume

32 ANS:
Yes. A reflection is an isometry.
PTS: 2 REF: 061132ge STA: G.G. 55 TOP: Properties of Transformations
33 ANS:
16.7. $\frac{x}{25}=\frac{12}{18}$

$$
\begin{aligned}
18 x & =300 \\
x & \approx 16.7
\end{aligned}
$$

PTS: 2 REF: 061133ge STA: G.G. 46 TOP: Side Splitter Theorem
34
ANS:
$(2 a-3,3 b+2) .\left(\frac{3 a+a-6}{2}, \frac{2 b-1+4 b+5}{2}\right)=\left(\frac{4 a-6}{2}, \frac{6 b+4}{2}\right)=(2 a-3,3 b+2)$
PTS: 2 REF: 061134ge STA: G.G. 66 TOP: Midpoint
35 ANS:


PTS: 4 REF: 061135ge STA: G.G. 23 TOP: Locus
36 ANS:
30. $3 x+4 x+5 x=360 . \mathrm{m} \overparen{L N}: \mathrm{m} \overparen{N K}: \mathrm{m} \overparen{K L}=90: 120: 150 . \frac{150-90}{2}=30$

$$
x=20
$$

PTS: 4 REF: 061136ge STA: G.G.51 TOP: Arcs Determined by Angles
KEY: outside circle

37 ANS:


PTS: 4
REF: 061137ge
STA: G.G. 70
TOP: Quadratic-Linear Systems
38 ANS:
$\overline{O A} \cong \overline{O B}$ because all radii are equal. $\overline{O P} \cong \overline{O P}$ because of the reflexive property. $\overline{O A} \perp \overline{P A}$ and $\overline{O B} \perp \overline{P B}$ because tangents to a circle are perpendicular to a radius at a point on a circle. $\angle P A O$ and $\angle P B O$ are right angles because of the definition of perpendicular. $\angle P A O \cong \angle P B O$ because all right angles are congruent. $\triangle A O P \cong \triangle B O P$ because of HL. $\angle A O P \cong \angle B O P$ because of CPCTC.

PTS: 6
REF: 061138ge
STA: G.G. 27
TOP: Circle Proofs

