## 0809ge

1 Based on the diagram below, which statement is true?


1) $a \| b$
2) $a \| c$
3) $b \| c$
4) $d \| e$

2 The diagram below shows the construction of the bisector of $\angle A B C$.


Which statement is not true?

1) $\mathrm{m} \angle E B F=\frac{1}{2} \mathrm{~m} \angle A B C$
2) $\mathrm{m} \angle D B F=\frac{1}{2} \mathrm{~m} \angle A B C$
3) $\mathrm{m} \angle E B F=\mathrm{m} \angle A B C$
4) $\mathrm{m} \angle D B F=\mathrm{m} \angle E B F$

3 In the diagram of $\triangle A B C$ below, $\overline{A B} \cong \overline{A C}$. The measure of $\angle B$ is $40^{\circ}$.


What is the measure of $\angle A$ ?

1) $40^{\circ}$
2) $50^{\circ}$
3) $70^{\circ}$
4) $100^{\circ}$

4 In the diagram of circle $O$ below, chord $\overline{C D}$ is parallel to diameter $\overline{A O B}$ and $\mathrm{m} \overparen{A C}=30$.


What is $\mathrm{m} \overparen{C D}$ ?

1) 150
2) 120
3) 100
4) 60

5 In the diagram of trapezoid $A B C D$ below, diagonals $\overline{A C}$ and $\overline{B D}$ intersect at $E$ and $\triangle A B C \cong \triangle D C B$.


Which statement is true based on the given information?

1) $\overline{A C} \cong \overline{B C}$
2) $\overline{C D} \cong \overline{A D}$
3) $\angle C D E \cong \angle B A D$
4) $\angle C D B \cong \angle B A C$

6 Which transformation produces a figure similar but not congruent to the original figure?

1) $T_{1,3}$
2) $D \frac{1}{2}$
3) $R_{90^{\circ}}$
4) $r_{y=x}$

7 In the diagram below of parallelogram $A B C D$ with diagonals $\overline{A C}$ and $\overline{B D}, \mathrm{~m} \angle 1=45$ and $\mathrm{m} \angle D C B=120$.


What is the measure of $\angle 2$ ?

1) $15^{\circ}$
2) $30^{\circ}$
3) $45^{\circ}$
4) $60^{\circ}$

8 On the set of axes below, Geoff drew rectangle $A B C D$. He will transform the rectangle by using the translation $(x, y) \rightarrow(x+2, y+1)$ and then will reflect the translated rectangle over the $x$-axis.


What will be the area of the rectangle after these transformations?

1) exactly 28 square units
2) less than 28 square units
3) greater than 28 square units
4) It cannot be determined from the information given.

9 What is the equation of a line that is parallel to the line whose equation is $y=x+2$ ?

1) $x+y=5$
2) $2 x+y=-2$
3) $y-x=-1$
4) $y-2 x=3$

10 The endpoints of $\overline{C D}$ are $C(-2,-4)$ and $D(6,2)$.
What are the coordinates of the midpoint of $\overline{C D}$ ?

1) $(2,3)$
2) $(2,-1)$
3) $(4,-2)$
4) $(4,3)$

11 What are the center and the radius of the circle
whose equation is $(x-3)^{2}+(y+3)^{2}=36$

1) center $=(3,-3)$; radius $=6$
2) center $=(-3,3)$; radius $=6$
3) center $=(3,-3)$; radius $=36$
4) center $=(-3,3)$; radius $=36$

12 Given the equations: $y=x^{2}-6 x+10$

$$
y+x=4
$$

What is the solution to the given system of equations?

1) $(2,3)$
2) $(3,2)$
3) $(2,2)$ and $(1,3)$
4) $(2,2)$ and $(3,1)$

13 The diagonal $\overline{A C}$ is drawn in parallelogram $A B C D$.
Which method can not be used to prove that
$\triangle A B C \cong \triangle C D A$ ?

1) SSS
2) SAS
3) SSA
4) ASA

14 In the diagram below, line $k$ is perpendicular to plane $P$ at point $T$.


Which statement is true?

1) Any point in plane $\mathscr{P}$ also will be on line $k$.
2) Only one line in plane $\mathscr{P}$ will intersect line $k$.
3) All planes that intersect plane $\mathscr{P}$ will pass through $T$.
4) Any plane containing line $k$ is perpendicular to plane $\mathscr{P}$.

15 In the diagram below, which transformation was used to map $\triangle A B C$ to $\triangle A^{\prime} B^{\prime} C^{\prime}$ ?


1) dilation
2) rotation
3) reflection
4) glide reflection

16 Which set of numbers represents the lengths of the sides of a triangle?

1) $\{5,18,13\}$
2) $\{6,17,22\}$
3) $\{16,24,7\}$
4) $\{26,8,15\}$

17 What is the slope of a line perpendicular to the line whose equation is $y=-\frac{2}{3} x-5$ ?

1) $-\frac{3}{2}$
2) $-\frac{2}{3}$
3) $\frac{2}{3}$
4) $\frac{3}{2}$

18 A quadrilateral whose diagonals bisect each other and are perpendicular is a

1) rhombus
2) rectangle
3) trapezoid
4) parallelogram

19 If the endpoints of $\overline{A B}$ are $A(-4,5)$ and $B(2,-5)$, what is the length of $\overline{A B}$ ?

1) $2 \sqrt{34}$
2) 2
3) $\sqrt{61}$
4) 8

20 In the diagram below of $\triangle A C T, D$ is the midpoint of $\overline{A C}, O$ is the midpoint of $\overline{A T}$, and $G$ is the midpoint of $\overline{C T}$.


If $A C=10, A T=18$, and $C T=22$, what is the perimeter of parallelogram $C D O G$ ?

1) 21
2) 25
3) 32
4) 40

21 Which equation represents circle $K$ shown in the graph below?


1) $(x+5)^{2}+(y-1)^{2}=3$
2) $(x+5)^{2}+(y-1)^{2}=9$
3) $(x-5)^{2}+(y+1)^{2}=3$
4) $(x-5)^{2}+(y+1)^{2}=9$

22 In the diagram below of right triangle $A C B$, altitude $\overline{C D}$ is drawn to hypotenuse $\overline{A B}$.


If $A B=36$ and $A C=12$, what is the length of $\overline{A D}$ ?

1) 32
2) 6
3) 3
4) 4

23 In the diagram of circle $O$ below, chord $\overline{A B}$ intersects chord $\overline{C D}$ at $E, D E=2 x+8, E C=3$, $A E=4 x-3$, and $E B=4$.


What is the value of $x$ ?

1) 1
2) 3.6
3) 5
4) 10.25

24 What is the negation of the statement "Squares are parallelograms"?

1) Parallelograms are squares.
2) Parallelograms are not squares.
3) It is not the case that squares are parallelograms.
4) It is not the case that parallelograms are squares.

25 The diagram below shows the construction of the center of the circle circumscribed about $\triangle A B C$.


This construction represents how to find the intersection of

1) the angle bisectors of $\triangle A B C$
2) the medians to the sides of $\triangle A B C$
3) the altitudes to the sides of $\triangle A B C$
4) the perpendicular bisectors of the sides of $\triangle A B C$

26 A right circular cylinder has a volume of 1,000 cubic inches and a height of 8 inches. What is the radius of the cylinder to the nearest tenth of an inch?

1) 6.3
2) 11.2
3) 19.8
4) 39.8

27 If two different lines are perpendicular to the same plane, they are

1) collinear
2) coplanar
3) congruent
4) consecutive

28 How many common tangent lines can be drawn to the two externally tangent circles shown below?


1) 1
2) 2
3) 3
4) 4

29 In the diagram below of isosceles trapezoid $D E F G$, $\overline{D E} \| \overline{G F}, D E=4 x-2, E F=3 x+2, F G=5 x-3$, and $G D=2 x+5$. Find the value of $x$.


30 A regular pyramid with a square base is shown in the diagram below.


A side, $s$, of the base of the pyramid is 12 meters, and the height, $h$, is 42 meters. What is the volume of the pyramid in cubic meters?

31 Write an equation of the line that passes through the point $(6,-5)$ and is parallel to the line whose equation is $2 x-3 y=11$.

32 Using a compass and straightedge, construct the angle bisector of $\angle A B C$ shown below. [Leave all construction marks.]


33 The degree measures of the angles of $\triangle A B C$ are represented by $x, 3 x$, and $5 x-54$. Find the value of $x$.

34 In the diagram below of $\triangle A B C$ with side $\overline{A C}$ extended through $D, \mathrm{~m} \angle A=37$ and $\mathrm{m} \angle B C D=117$. Which side of $\triangle A B C$ is the longest side? Justify your answer.

(Not drawn to scale)

35 Write an equation of the perpendicular bisector of the line segment whose endpoints are $(-1,1)$ and $(7,-5)$. [The use of the grid below is optional]


36 On the set of axes below, sketch the points that are 5 units from the origin and sketch the points that are 2 units from the line $y=3$. Label with an $\mathbf{X}$ all points that satisfy both conditions.


37 Triangle $D E G$ has the coordinates $D(1,1), E(5,1)$, and $G(5,4)$. Triangle $D E G$ is rotated $90^{\circ}$ about the origin to form $\triangle D^{\prime} E^{\prime} G^{\prime}$. On the grid below, graph and label $\triangle D E G$ and $\triangle D^{\prime} E^{\prime} G^{\prime}$. State the coordinates of the vertices $D^{\prime}, E^{\prime}$, and $G^{\prime}$. Justify that this transformation preserves distance.


38 Given: Quadrilateral $A B C D$, diagonal $\overline{A F E C}$, $\overline{A E} \cong \overline{F C}, \overline{B F} \perp \overline{A C}, \overline{D E} \perp \overline{A C}, \angle 1 \cong \angle 2$
Prove: $A B C D$ is a parallelogram.


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## Answer Section

1 ANS: 4
The marked $60^{\circ}$ angle and the angle above it are on the same straight line and supplementary. This unmarked supplementary angle is $120^{\circ}$. Because the unmarked $120^{\circ}$ angle and the marked $120^{\circ}$ angle are alternate exterior angles and congruent, $d \| e$.

|  | PTS: 2 | REF: 080901ge | STA: G.G. 35 | TOP: Parallel Lines and Transversals |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 2 | ANS: 3 | PTS: 2 | REF: 080902ge | STA: G.G. 17 |  |
| TOP: Constructions |  |  |  |  |  |
| 3 | ANS: 4 |  |  |  |  |
|  | $180-(40+40)=100$ |  |  |  |  |

PTS: 2 REF: 080903ge STA: G.G. 31 TOP: Isosceles Triangle Theorem
4 ANS: 2
Parallel chords intercept congruent arcs. $\mathrm{m} \overparen{A C}=\mathrm{m} \overparen{B D}=30.180-30-30=120$.
PTS: 2 REF: 080904ge STA: G.G. 52 TOP: Chords
5 ANS: 4 PTS: 2 REF: 080905ge STA: G.G. 29
TOP: Triangle Congruency
6 ANS: 2
A dilation affects distance, not angle measure.
PTS: 2 REF: 080906ge STA: G.G. 60 TOP: Identifying Transformations
7 ANS: 1
$\angle D C B$ and $\angle A D C$ are supplementary adjacent angles of a parallelogram. $180-120=60 . \angle 2=60-45=15$.
PTS: 2 REF: 080907ge STA: G.G. 38 TOP: Parallelograms
8 ANS: 1
Translations and reflections do not affect distance.
PTS: 2 REF: 080908ge STA: G.G. 59 TOP: Properties of Transformations
9 ANS: 3
The slope of $y=x+2$ is 1 . The slope of $y-x=-1$ is $\frac{-A}{B}=\frac{-(-1)}{1}=1$.
PTS: 2 REF: 080909ge STA: G.G. 63 TOP: Parallel and Perpendicular Lines
10 ANS: 2
$M_{x}=\frac{-2+6}{2}=2 . M_{y}=\frac{-4+2}{2}=-1$
PTS: 2 REF: 080910ge STA: G.G. 66 TOP: Midpoint
11 ANS: 1 PTS: 2 REF: 080911ge STA: G.G. 73
TOP: Equations of Circles

12 ANS: 4
$y+x=4 . x^{2}-6 x+10=-x+4 . y+x=4 . y+2=4$

$y=-x+4 \quad x^{2}-5 x+6=0 \quad y+3=4 \quad y=2$

$$
(x-3)(x-2)=0 \quad y=1
$$

$$
x=3 \text { or } 2
$$

PTS: 2 REF: 080912ge

STA: G.G. 70
REF: 080913ge
REF: 080914ge
REF: 080915ge STA: G.G. 56

15 ANS: 4 PTS: 2
TOP: Identifying Transformations
16 ANS: 2
$6+17>22$
PTS: 2 REF: 080916ge STA: G.G. 33 TOP: Triangle Inequality Theorem
17 ANS: 4
The slope of $y=-\frac{2}{3} x-5$ is $-\frac{2}{3}$. Perpendicular lines have slope that are opposite reciprocals.
PTS: 2 REF: 080917ge STA: G.G. 62 TOP: Parallel and Perpendicular Lines
18 ANS: 1
PTS: 2
REF: 080918ge
STA: G.G. 41
TOP: Special Quadrilaterals
19 ANS: 1
$d=\sqrt{(-4-2)^{2}+(5-(-5))^{2}}=\sqrt{36+100}=\sqrt{136}=\sqrt{4} \cdot \sqrt{34}=2 \sqrt{34}$.
PTS: 2 REF: 080919ge STA: G.G. 67 TOP: Distance
20 ANS: 3

$\begin{array}{lllll}\text { PTS: } 2 & \text { REF: } 080920 \mathrm{ge} & \text { STA: G.G. } 42 & \text { TOP: Midsegments } \\ \text { ANS: } 2 & \text { PTS: } 2 & \text { REF: } 080921 \mathrm{ge} & \text { STA: } & \text { G.G. } 72 \\ \text { TOP: } & \text { Equations of Circles } & & & \end{array}$

22 ANS: 4
Let $\overline{A D}=x .36 x=12^{2}$

$$
x=4
$$

PTS: 2 REF: 080922ge STA: G.G. 47 TOP: Similarity
KEY: leg
23 ANS: 2
$4(4 x-3)=3(2 x+8)$
$16 x-12=6 x+24$
$10 x=36$

$$
x=3.6
$$

PTS: 2 REF: 080923ge STA: G.G. 53 TOP: Segments Intercepted by Circle
KEY: two chords
24 ANS: 3 PTS: 2 REF: 080924ge STA: G.G. 24
TOP: Negations
25 ANS: $4 \quad$ PTS: 2
REF: 080925ge STA: G.G. 21
TOP: Centroid, Orthocenter, Incenter and Circumcenter
26 ANS: 1

$$
\begin{aligned}
V & =\pi r^{2} h \\
1000 & =\pi r^{2} \cdot 8 \\
r^{2} & =\frac{1000}{8 \pi} \\
r & \approx 6.3
\end{aligned}
$$

PTS: 2
27 ANS: 2
TOP: Planes
28 ANS: 3
TOP: Tangents

REF: 080926ge STA: G.G. 14
PTS: 2
PTS: 2
KEY: common tangency

29 ANS:
3. The non-parallel sides of an isosceles trapezoid are congruent. $2 x+5=3 x+2$

$$
x=3
$$

PTS: 2
REF: 080929ge STA: G.G. 40
TOP: Trapezoids
30 ANS:
2016. $V=\frac{1}{3} B h=\frac{1}{3} s^{2} h=\frac{1}{3} 12^{2} \cdot 42=2016$

PTS: 2
REF: 080930ge
STA: G.G. 13
TOP: Volume

31 ANS:
$y=\frac{2}{3} x-9$. The slope of $2 x-3 y=11$ is $-\frac{A}{B}=\frac{-2}{-3}=\frac{2}{3} .-5=\left(\frac{2}{3}\right)(6)+b$

$$
\begin{aligned}
-5 & =4+b \\
b & =-9
\end{aligned}
$$

PTS: 2
REF: 080931ge STA: G.G. 65
TOP: Parallel and Perpendicular Lines
32
ANS:


PTS: 2
REF: 080932ge
STA: G.G. 17
TOP: Constructions
33 ANS:
26. $x+3 x+5 x-54=180$

$$
\begin{aligned}
9 x & =234 \\
x & =26
\end{aligned}
$$

PTS: 2
REF: 080933ge
STA: G.G. 30
TOP: Interior and Exterior Angles of Triangles
34 ANS:
$\overline{A C} \cdot \mathrm{~m} \angle B C A=63$ and $\mathrm{m} \angle A B C=80 . \overline{A C}$ is the longest side as it is opposite the largest angle.
PTS: 2
REF: 080934ge
STA: G.G. 34
TOP: Angle Side Relationship

35 ANS:
$y=\frac{4}{3} x-6 . M_{x}=\frac{-1+7}{2}=3 \quad$ The perpendicular bisector goes through $(3,-2)$ and has a slope of $\frac{4}{3}$.

$$
\begin{aligned}
& M_{y}=\frac{1+(-5)}{2}=-2 \\
& m=\frac{1-(-5)}{-1-7}=-\frac{3}{4}
\end{aligned}
$$

$y-y_{M}=m\left(x-x_{M}\right)$.

$y+2=\frac{4}{3}(x-3)$
PTS: 4
REF: 080935ge
STA: G.G. 68
TOP: Perpendicular Bisector
36 ANS:


PTS: 4
REF: 080936ge
STA: G.G. 23
TOP: Locus
37 ANS:


PTS: 4
REF: 080937ge STA: G.G. 55
TOP: Properties of Transformations

ANS:

$\overline{F E} \cong \overline{F E}$ (Reflexive Property); $\overline{A E}-\overline{F E} \cong \overline{F C}-\overline{E F}$ (Line Segment Subtraction Theorem) $\overline{A F} \cong \overline{C E}$ (Substitution); $\angle B F A \cong \angle D E C$ (All right angles are congruent); $\triangle B F A \cong \triangle D E C$ (ANS); $\overline{A B} \cong \overline{C D}$ and $\overline{B F} \cong \overline{D E}$ (CPCTC); $\angle B F C \cong \angle D E A$ (All right angles are congruent); $\triangle B F C \cong \triangle D E A$ (SASs); $\overline{A D} \cong \overline{C B}(\mathrm{CPCTC}) ; A B C D$ is a parallelogram (opposite sides of quadrilateral $A B C D$ are congruent)

PTS: 6
REF: 080938ge STA: G.G. 27
TOP: Quadrilateral Proofs

