## 0609ia

1 It takes Tammy 45 minutes to ride her bike 5 miles. At this rate, how long will it take her to ride 8 miles?

1) 0.89 hour
2) 1.125 hours
3) 48 minutes
4) 72 minutes

2 What are the roots of the equation $x^{2}-7 x+6=0$ ?

1) 1 and 7
2)     - 1 and 7
3) -1 and -6
4) 1 and 6

3 Which expression represents $\frac{27 x^{18} y^{5}}{9 x^{6} y}$ in simplest form?

1) $3 x^{12} y^{4}$
2) $3 x^{3} y^{5}$
3) $18 x^{12} y^{4}$
4) $18 x^{3} y^{5}$

4 Marie currently has a collection of 58 stamps. If she buys $s$ stamps each week for $w$ weeks, which expression represents the total number of stamps she will have?

1) 58 sw
2) $58+s w$
3) $58 s+w$
4) $58+s+w$

5 Which data set describes a situation that could be classified as qualitative?

1) the ages of the students in Ms. Marshall's Spanish class
2) the test scores of the students in Ms. Fitzgerald's class
3) the favorite ice cream flavor of each of Mr. Hayden's students
4) the heights of the players on the East High School basketball team

6 The sign shown below is posted in front of a roller coaster ride at the Wadsworth County Fairgrounds.


If $h$ represents the height of a rider in inches, what is a correct translation of the statement on this sign?

1) $h<48$
2) $h>48$
3) $h \leq 48$
4) $h \geq 48$

7 Which value of $x$ is the solution of the equation $\frac{2 x}{3}+\frac{x}{6}=5$ ?

1) 6
2) 10
3) 15
4) 30

8 Students in Ms. Nazzeer's mathematics class tossed a six-sided number cube whose faces are numbered 1 to 6 . The results are recorded in the table below.

| Result | Frequency |
| :---: | :---: |
| 1 | 3 |
| 2 | 6 |
| 3 | 4 |
| 4 | 6 |
| 5 | 4 |
| 6 | 7 |

Based on these data, what is the empirical probability of tossing a 4 ?

1) $\frac{8}{30}$
2) $\frac{6}{30}$
3) $\frac{5}{30}$
4) $\frac{1}{30}$

9 What is the value of $x$, in inches, in the right triangle below?


1) $\sqrt{15}$
2) 8
3) $\sqrt{34}$
4) 4

10 What is $\sqrt{32}$ expressed in simplest radical form?

1) $16 \sqrt{2}$
2) $4 \sqrt{2}$
3) $4 \sqrt{8}$
4) $2 \sqrt{8}$

11 If the speed of sound is 344 meters per second, what is the approximate speed of sound, in meters per hour?

> 60 seconds $=1$ minute
> 60 minutes $=1$ hour

1) 20,640
2) 41,280
3) 123,840
4) $1,238,400$

12 The sum of two numbers is 47 , and their difference is 15 . What is the larger number?

1) 16
2) 31
3) 32
4) 36

13 If $a+a r=b+r$, the value of $a$ in terms of $b$ and $r$ can be expressed as

1) $\frac{b}{r}+1$
2) $\frac{1+b}{r}$
3) $\frac{b+r}{1+r}$
4) $\frac{1+b}{r+b}$

14 Which value of $x$ is in the solution set of $\frac{4}{3} x+5<17$ ?

1) 8
2) 9
3) 12
4) 16

15 The box-and-whisker plot below represents students' scores on a recent English test.


What is the value of the upper quartile?

1) 68
2) 76
3) 84
4) 94

16 Which value of $n$ makes the expression $\frac{5 n}{2 n-1}$ undefined?

1) 1
2) 0
3) $-\frac{1}{2}$
4) $\frac{1}{2}$

17 At Genesee High School, the sophomore class has 60 more students than the freshman class. The junior class has 50 fewer students than twice the students in the freshman class. The senior class is three times as large as the freshman class. If there are a total of 1,424 students at Genesee High School, how many students are in the freshman class?

1) 202
2) 205
3) 235
4) 236

18 What are the vertex and axis of symmetry of the parabola $y=x^{2}-16 x+63$ ?

1) vertex: $(8,-1)$; axis of symmetry: $x=8$
2) vertex: $(8,1)$; axis of symmetry: $x=8$
3) vertex: $(-8,-1)$; axis of symmetry: $x=-8$
4) vertex: $(-8,1)$; axis of symmetry: $x=-8$

19 Which statement is true about the relation shown on the graph below?


1) It is a function because there exists one $x$-coordinate for each $y$-coordinate.
2) It is a function because there exists one $y$-coordinate for each $x$-coordinate.
3) It is not a function because there are multiple $y$-values for a given $x$-value.
4) It is not a function because there are multiple $x$-values for a given $y$-value.

20 Which graph represents the solution of $3 y-9 \leq 6 x$ ?
1)
2)




21 Which expression represents $\frac{x^{2}-2 x-15}{x^{2}+3 x}$ in simplest form?

1) -5
2) $\frac{x-5}{x}$
3) $\frac{-2 x-5}{x}$
4) $\frac{-2 x-15}{3 x}$

22 What is an equation of the line that passes through the point $(4,-6)$ and has a slope of -3 ?

1) $y=-3 x+6$
2) $y=-3 x-6$
3) $y=-3 x+10$
4) $y=-3 x+14$

23 When $4 x^{2}+7 x-5$ is subtracted from $9 x^{2}-2 x+3$, the result is

1) $5 x^{2}+5 x-2$
2) $5 x^{2}-9 x+8$
3) $-5 x^{2}+5 x-2$
4) $-5 x^{2}+9 x-8$

24 The equation $y=x^{2}+3 x-18$ is graphed on the set of axes below.


Based on this graph, what are the roots of the equation $x^{2}+3 x-18=0$ ?

1) -3 and 6
2) 0 and -18
3) 3 and -6
4) 3 and - 18

25 What is the value of the $y$-coordinate of the solution to the system of equations $x+2 y=9$ and $x-y=3$ ?

1) 6
2) 2
3) 3
4) 5

26 What is the additive inverse of the expression $a-b$ ?

1) $a+b$
2) $a-b$
3) $-a+b$
4) $-a-b$

27 What is the product of 12 and $4.2 \times 10^{6}$ expressed in scientific notation?

1) $50.4 \times 10^{6}$
2) $50.4 \times 10^{7}$
3) $5.04 \times 10^{6}$
4) $5.04 \times 10^{7}$

28 To calculate the volume of a small wooden cube, Ezra measured an edge of the cube as 2 cm . The actual length of the edge of Ezra's cube is 2.1 cm . What is the relative error in his volume calculation to the nearest hundredth?

1) 0.13
2) 0.14
3) 0.15
4) 0.16

29 What is $\frac{6}{4 a}-\frac{2}{3 a}$ expressed in simplest form?

1) $\frac{4}{a}$
2) $\frac{5}{6 a}$
3) $\frac{8}{7 a}$
4) $\frac{10}{12 a}$

30 The set $\{11,12\}$ is equivalent to

1) $\{x \mid 11<x<12$, where $x$ is an integer $\}$
2) $\{x \mid 11<x \leq 12$, where $x$ is an integer $\}$
3) $\{x \mid 10 \leq x<12$, where $x$ is an integer $\}$
4) $\{x \mid 10<x \leq 12$, where $x$ is an integer $\}$

31 Determine how many three-letter arrangements are possible with the letters $A, N, G, L$, and $E$ if no letter may be repeated.

32 Factor completely: $4 x^{3}-36 x$

33 Some books are laid on a desk. Two are English, three are mathematics, one is French, and four are social studies. Theresa selects an English book and Isabelle then selects a social studies book. Both girls take their selections to the library to read. If Truman then selects a book at random, what is the probability that he selects an English book?

34 In the diagram below, the circumference of circle $O$ is $16 \pi$ inches. The length of $\overline{B C}$ is three-quarters of the length of diameter $\overline{A D}$ and $C E=4$ inches. Calculate the area, in square inches, of trapezoid $A B C D$.


35 A bank is advertising that new customers can open a savings account with a $3 \frac{3}{4} \%$ interest rate compounded annually. Robert invests $\$ 5,000$ in an account at this rate. If he makes no additional deposits or withdrawals on his account, find the amount of money he will have, to the nearest cent, after three years.

36 The table below shows the number of prom tickets sold over a ten-day period.

Prom Ticket Sales

| Day $(x)$ | 1 | 2 | 5 | 7 | 10 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Number of <br> Prom Tickets <br> Sold $(y)$ | 30 | 35 | 55 | 60 | 70 |

Plot these data points on the coordinate grid below. Use a consistent and appropriate scale. Draw a reasonable line of best fit and write its equation.


Day

37 A stake is to be driven into the ground away from the base of a 50 -foot pole, as shown in the diagram below. A wire from the stake on the ground to the top of the pole is to be installed at an angle of elevation of $52^{\circ}$.


How far away from the base of the pole should the stake be driven in, to the nearest foot? What will be the length of the wire from the stake to the top of the pole, to the nearest foot?

38 The Fahrenheit temperature readings on 30 April mornings in Stormville, New York, are shown below.

$$
\begin{aligned}
& 41^{\circ}, 58^{\circ}, 61^{\circ}, 54^{\circ}, 49^{\circ}, 46^{\circ}, 52^{\circ}, 58^{\circ}, 67^{\circ}, 43^{\circ}, \\
& 47^{\circ}, 60^{\circ}, 52^{\circ}, 58^{\circ}, 48^{\circ}, 44^{\circ}, 59^{\circ}, 66^{\circ}, 62^{\circ}, 55^{\circ}, \\
& 44^{\circ}, 49^{\circ}, 62^{\circ}, 61^{\circ}, 59^{\circ}, 54^{\circ}, 57^{\circ}, 58^{\circ}, 63^{\circ}, 60^{\circ}
\end{aligned}
$$

Using the data, complete the frequency table below.

| Interval | Tally | Frequency |
| :---: | :---: | :---: |
| $40-44$ |  |  |
| $45-49$ |  |  |
| $50-54$ |  |  |
| $55-59$ |  |  |
| $60-64$ |  |  |
| $65-69$ |  |  |

On the grid below, construct and label a frequency histogram based on the table.


39 On the set of axes below, solve the following system of equations graphically for all values of $x$ and $y$.

$$
\begin{gathered}
y=x^{2}-6 x+1 \\
y+2 x=6
\end{gathered}
$$



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Answer Section

1 ANS: 4
$\frac{5}{45}=\frac{8}{x}$
$5 x=360$
$x=72$
PTS: 2
REF: 060901ia
STA: A.M. 1
TOP: Speed
2 ANS: 4
$x^{2}-7 x+6=0$
$(x-6)(x-1)=0$
$x=6 \quad x=1$
PTS: 2 REF: 060902
3 ANS: 1
PTS: 2
STA: A.A. 28
REF: 060903ia
TOP: Roots of Quadratics
TOP: Division of Powers
4 ANS: 2
PTS: 2
REF: 060904ia
STA: A.A. 1
TOP: Expressions
5 ANS: 3
The other situations are quantitative.

PTS: 2
6 ANS: 4
REF: 060905ia
PTS: 2
TOP: Modeling Inequalities
7 ANS: 1

PTS: 2
REF: 060907ia
STA: A.A. 25
TOP: Solving Equations with Fractional Expressions
8 ANS: 2
PTS: 2
REF: 060908ia
STA: A.S. 21
TOP: Empirical Probability

STA: A.S. 1
REF: 060906ia

$$
\begin{aligned}
\frac{(2 x \times 6)+(3 \times x)}{3 \times 6} & =5 \\
\frac{12 x+3 x}{18} & =5 \\
15 x & =90 \\
x & =6
\end{aligned}
$$



TOP: Analysis of Data
STA: A.A. 4

9 ANS: 3

$$
\begin{aligned}
3^{2}+5^{2} & =x^{2} \\
34 & =x^{2} \\
\sqrt{34} & =x
\end{aligned}
$$

PTS: 2 REF: 060909ia STA: A.A. 45 TOP: Pythagorean Theorem
10 ANS: 2
$\sqrt{32}=\sqrt{16} \sqrt{2}=4 \sqrt{2}$
PTS: 2
REF: 060910ia
STA: A.N. 2
TOP: Simplifying Radicals
11 ANS: 4
$\frac{344 \mathrm{~m}}{\mathrm{sec}} \times \frac{60 \mathrm{sec}}{1 \mathrm{~min}} \times \frac{60 \mathrm{~min}}{1 \mathrm{hr}}=1,238,400 \frac{\mathrm{~m}}{\mathrm{hr}}$

PTS: 2
REF: 060911ia
STA: A.M. 2
TOP: Conversions
12 ANS: 2
$L+S=47$
$L-S=15$
$2 L=62$
$L=31$
PTS: 2
REF: 060912ia
STA: A.A. 7
TOP: Writing Linear Systems
13 ANS: 3

$$
\begin{aligned}
a+a r & =b+r \\
a(1+r) & =b+r \\
a & =\frac{b+r}{1+r}
\end{aligned}
$$

PTS: 2
REF: 060913ia
STA: A.A. 23
TOP: Transforming Formulas
14 ANS: 1
$\frac{4}{3} x+5<17$
$\frac{4}{3} x<12$
$4 x<36$
$x<9$
PTS: 2
REF: 060914ia
STA: A.A. 21
TOP: Interpreting Solutions
15 ANS: 3
The value of the upper quartile is the last vertical line of the box.
PTS: 2 REF: 060915ia STA: A.S. 6 TOP: Box-and-Whisker Plots
16 ANS: 4
PTS: 2
TOP: Undefined Rationals

17 ANS: 1
so $=f+60 j=2 f-50$ se $=3 f . f+(f+60)+(2 f-50)+3 f=1424$

$$
\begin{gathered}
7 f+10=1424 \\
f=202
\end{gathered}
$$

PTS: 2 REF: 060917ia STA: A.A. 7 TOP: Writing Linear Systems
18 ANS: 1
$x=\frac{-b}{2 a}=\frac{-(-16)}{2(1)}=8 . y=(8)^{2}-16(8)+63=-1$
PTS: 2 REF: 060918ia STA: A.A. 41
TOP: Identifying the Vertex of a Quadratic Given Equation
19 ANS: 3 PTS: 2
TOP: Defining Functions
20 ANS: $1 \quad$ PTS: $2 \quad$ REF: 060920ia STA: A.G. 6
TOP: Linear Inequalities
21 ANS: 2
$\frac{x^{2}-2 x-15}{x^{2}+3 x}=\frac{(x-5)(x+3)}{x(x+3)}=\frac{x-5}{x}$
PTS: 2 REF: 060921ia STA: A.A. 16 TOP: Rational Expressions
KEY: a > 0
22 ANS: 1
$y=m x+b$
$-6=(-3)(4)+b$
$b=6$
PTS: 2 REF: 060922ia STA: A.A. 34
23 ANS: 2
PTS: 2
REF: 060923ia
TOP: Addition and Subtraction of Polynomials
24 ANS: 3
PTS: 2
REF: 060924ia
TOP: Solving Quadratics by Graphing
25 ANS: 2
$x+2 y=9$
$x-y=3$
$3 y=6$

$$
y=2
$$

PTS: 2
REF: 060925ia
26 ANS: 3
PTS: 2
STA: A.A. 10
TOP: Properties of Reals
27 ANS: 4
PTS: 2
REF: 060926ia

TOP: Operations with Scientific Notation

28 ANS: 2
The volume of the cube using Ezra's measurements is $8\left(2^{3}\right)$. The actual volume is $9.261\left(2.1^{3}\right)$. The relative error is $\left|\frac{9.261-8}{9.261}\right| \approx 0.14$.

PTS: 2 REF: 060928ia STA: A.M. 3 TOP: Error
29 ANS: 2
$\frac{6}{4 a}-\frac{2}{3 a}=\frac{18 a-8 a}{12 a^{2}}=\frac{10 a}{12 a^{2}}=\frac{5}{6 a}$
PTS: 2 REF: 060929ia STA: A.A. 17 TOP: Addition and Subtraction of Rationals
30 ANS: 4
PTS: 2
REF: 060930ia
STA: A.A. 29
TOP: Set Theory
31 ANS:
60. ${ }_{5} P_{3}=60$

PTS: 2
REF: 060931ia
STA: A.N. 8
TOP: Permutations
32 ANS:
$4 x(x+3)(x-3) .4 x^{3}-36 x=4 x\left(x^{2}-9\right)=4 x(x+3)(x-3)$
PTS: 2
REF: 060932ia STA: A.A. 19
TOP: Factoring the Difference of Perfect Squares
33 ANS:
$\frac{1}{8}$. After the English and social studies books are taken, 8 books are left and 1 is an English book.
PTS: 2 REF: 060933ia STA: A.S. 18 TOP: Conditional Probability
34 ANS:
56. If the circumference of circle $O$ is 16 inches, the diameter, $\overline{A D}$, is 16 inches and the length of $\overline{B C}$ is 12 inches $\frac{3}{4} \times 16$. The area of trapezoid $A B C D$ is $\frac{1}{2} \times 4(12+16)=56$.

PTS: 3 REF: 060934ia STA: A.G. 1 TOP: Compositions of Polygons and Circles
35 ANS:
5,583.86. $A=P(1+R)^{t}=5000(1+0.0375)^{3} \approx 5583.86$
PTS: 3
REF: 060935ia
STA: A.A. 9
TOP: Exponential Functions

36
ANS:


PTS: 3
REF: 060936ia
STA: A.S. 8
TOP: Scatter Plots
37 ANS:
39, 63. $\tan 52=\frac{50}{x} \cdot \sin 52=\frac{50}{x}$

$$
x \approx 39 \quad x \approx 63
$$

PTS: 4
38 ANS:
REF: 060937ia STA: A.A. 44

| Interval | Tally | Frequency |
| :---: | :--- | :---: |
| $40-44$ | $\\|$ II | 4 |
| $45-49$ | UH | 5 |
| $50-54$ | II II | 4 |
| $55-59$ | HI II | 8 |
| $60-64$ | HI II | 7 |
| $65-69$ | $\\|\\|$ | 2 |



PTS: 4
REF: 060938ia
STA: A.S. 5
TOP: Frequency Histograms, Bar Graphs and Tables
ANS:


PTS: 4
REF: 060939ia STA: A.G. 9
TOP: Quadratic-Linear Systems

