INTEGRATED ALGEBRA

The University of the State of New York REGENTS HIGH SCHOOL EXAMINATION

INTEGRATED ALGEBRA

Tuesday, January 22, 2013 — 9:15 a.m. to 12:15 p.m., only

Steve Watson

Student Name:_____

School Name: WWW. JMAP. ORG

The possession or use of any communications device is strictly prohibited when taking this examination. If you have or use any communications device, no matter how briefly, your examination will be invalidated and no score will be calculated for you.

Print your name and the name of your school on the lines above.

A separate answer sheet for Part I has been provided to you. Follow the instructions from the proctor for completing the student information on your answer sheet.

This examination has four parts, with a total of 39 questions. You must answer all questions in this examination. Record your answers to the Part I multiple-choice questions on the separate answer sheet. Write your answers to the questions in Parts II, III, and IV directly in this booklet. All work should be written in pen, except graphs and drawings, which should be done in pencil. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. The formulas that you may need to answer some questions in this examination are found at the end of the examination. This sheet is perforated so you may remove it from this booklet.

Scrap paper is not permitted for any part of this examination, but you may use the blank spaces in this booklet as scrap paper. A perforated sheet of scrap graph paper is provided at the end of this booklet for any question for which graphing may be helpful but is not required. You may remove this sheet from this booklet. Any work done on this sheet of scrap graph paper will *not* be scored.

When you have completed the examination, you must sign the statement printed at the end of the answer sheet, indicating that you had no unlawful knowledge of the questions or answers prior to the examination and that you have neither given nor received assistance in answering any of the questions during the examination. Your answer sheet cannot be accepted if you fail to sign this declaration.

Notice...

A graphing calculator and a straightedge (ruler) must be available for you to use while taking this examination.

DO NOT OPEN THIS EXAMINATION BOOKLET UNTIL THE SICNAL IS CIVEN.

ΑΑΒΕΙΑΤΕΡ ΑΓΕΕΡΑΙΟ

Part I

Answer all 30 questions in this part. Each correct answer will receive 2 credits. No partial credit will be allowed. Record your answers on your separate answer sheet. [60]

1 The number of hours spent on math homework during one week and the math exam grades for eleven students in Ms. Smith's algebra class are plotted below.

> Ms. Smith's Class positive 100 90 Exam Grade (percent) 80 70 60 -50 40 30 20 correla 10 0 3 8 9 10 5 6 Time Spent on Math Homework (hours)

Use this space for

computations.

Based on the plotted data, what is the correlation between the time spent on homework and the exam grade?

positive

(3) no correlation

(2) negative

- (4) cannot be determined
- **2** A car uses one gallon of gasoline for every 20 miles it travels. If a gallon of gasoline costs \$3.98, how much will the gas cost, to the *nearest dollar*, to travel 180 miles?

3 If Angelina's weekly allowance is d dollars, which expression represents her allowance, in dollars, for x weeks?

Use this space for computations.

- 4 What is the solution of the system of equations shown in the graph below?



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[3]

[OVER]

= - 2 X

 $\frac{12}{-2}$ = $\frac{-2x}{-2}$

-6 = X

12



8 A bag contains five green gumdrops and six red gumdrops. If Kim pulls a green gumdrop out of the bag and eats it, what is the probability that the next gumdrop she pulls out will be red?

 $(3)\frac{6}{11}$

 $\frac{6}{10}$

 $(1)\frac{5}{11}$

 $(2) \frac{5}{10}$

P(red) = 6 10

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[4]

5green - Igreen = 4green 6 red - Ored = 6 red 11 total - 1 total = 10 total



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[OVER]

Use this space for computations.

- 11 Which verbal expression is represented by 2(x + 4)?
 - twice the sum of a number and four)
 - (2) the sum of two times a number and four
 - (3) two times the difference of a number and four
 - (4) twice the product of a number and four

12 How many cubes with 5-inch sides will completely fill a cube that is 10 inches on a side?

- (1) 50 (2) 25 (4) 4 10 10 10 10 1000 1000 125 = 8 125 cmbic in ches
- 13 A school newspaper will survey students about the quality of the school's lunch program. Which method will create the *least* biased results?
 - (1) Twenty-five vegetarians are randomly surveyed.

Twenty-five students are randomly chosen from each grade level.

- (3) Students who dislike the school's lunch program are chosen to complete the survey.
- (4) A booth is set up in the cafeteria for the students to voluntarily complete the survey.





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rant Groen 2×8+×10

Use this space for computations.





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[OVER]



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25 A cube with faces numbered 1 through 6 is rolled 75 times, and the results are given in the table below.

		0 7+14+20 - 41
Number	Frequency	620 = 75 - 75
1	7	
2	22	$P(.) = \frac{22+6+6}{34} = \frac{34}{34}$
3	14	(even) 73 13
4	6	$P(20(4)) = \frac{22+6}{2} = \frac{28}{2}$
5	20	75 (3
6	6	$P(g_{22} p_{55}) = \frac{7+22+19}{7+22+19} = \frac{93}{75}$
		7.5 15

Based on these results, which statement is true? 23/75(1) P(odd) < P(even)(2) P(3 or less) < P(odd) 43/75(3) P(2 or 4) < P(3 or less) 28/75 23/75(4) P(2 or 4) < P(3 or less) 28/75 23/7523/75

910 8 3 4 5 6 7 Ζ x2 16 y 9 25 36 49 64 81 100 **26** Given: 4, 9, 16, 25, 36, 44, 64, 81, 100 3A = {perfect square integers from 4 to 100, inclusive} $B = \{\hat{1}, 6, 36, 48, 64\}$

The complement of set *B* in the universal set *A* is

(1) $\{9, 25, 81\}$ (3) $\{1, 4, 9, 25, 81, 100\}$ (4) $\{4, 9, 25, 81, 100\}$ (4) $\{4, 16, 36, 49, 64, 100\}$

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[9]

[OVER]

Use this space for computations.



Part II

Answer all 3 questions in this part. Each correct answer will receive 2 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. For all questions in this part, a correct numerical answer with no work shown will receive only 1 credit. All answers should be written in pen, except for graphs and drawings, which should be done in pencil. [6]

31 Express $4\sqrt{75}$ in simplest radical form. 4 575 4 JZ5 J3 $(4)(5)J_{3}$ $[20J_{3}]$

32 Factor completely: $5x^3 - 20x^2 - 60x$

$$5x^{3}-20x^{2}-60x$$

$$5(x^{3}-4x^{2}-12x)$$

$$(5)(x)(x^{2}-4x-12)$$

$$(5x)(x+2)(x-6)$$

X2-4X-12 |z|1 12 (+2-6)(x+z)(x-6)



Part III

Answer all 3 questions in this part. Each correct answer will receive 3 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. For all questions in this part, a correct numerical answer with no work shown will receive only 1 credit. All answers should be written in pen, except for graphs and drawings, which should be done in pencil. [9]



8.50 SN 40 35 The cost of three notebooks and four pencils is \$8.50. The cost of five notebooks and eight 3N pencils is \$14.50. Determine the cost of one notebook and the cost of one pencil = 14.50 [Only an algebraic solution can receive full credit.] Eq. #3 = (E2. $6N + 8P = \frac{1}{17.00}$ $3N + 4P = \frac{1}{8.50}$ $5N + 8P = \frac{1}{14.50}$ E9.#3 后世 Eq.#2 -#2.50 \ Notebook N Substitute N=250 into Eq. # 2 5(2.50) + 8P = 414.5012.50 + 8P = 414.50 8P =# 2.00 = 25¢ Pencil $E_{2,\pm}$ 3(2.50) + 4(.25) = 8.507.50 + 1.00 = 0 7.50 + 1.00 = 8.50 8.50 = 8.50 True V 5(2.50) + 8(,25) = 14,50 Ey.#Z 12.50 + 2.00 = 14.50 14.50 = 14,50 True 1

[OVER]

36 Wendy measures the floor in her rectangular bedroom for new carpeting. Her measurements are 24 feet by 14 feet. The actual measurements are 24.2 feet by 14.1 feet.

Determine the relative error in calculating the area of her bedroom. Express your answer as a decimal to the *nearest thousandth*.

$$Error = \left(\frac{Actual - Measured}{Actual}\right)$$

$$Actual Area = (24, 2)(14, 1) = 341, 22$$

$$Measured Area = (24)(14) = 336$$

$$Error = \frac{341, 22 - 336}{341, 22} = \frac{5, 22}{341, 22} = .015298$$

$$Har 500$$

$$Relative Error = .015$$

Part IV

Answer all 3 questions in this part. Each correct answer will receive 4 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. For all questions in this part, a correct numerical answer with no work shown will receive only 1 credit. All answers should be written in pen, except for graphs and drawings, which should be done in pencil. [12]



38 A metal pipe is used to hold up a 9-foot fence, as shown in the diagram below. The pipe makes an angle of 48° with the ground.



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