INTEGRATED ALGEBRA

The University of the State of New York REGENTS HIGH SCHOOL EXAMINATION

INTEGRATED ALGEBRA

Tuesday, January 27, 2015 — 1:15 to 4:15 p.m., only

Student Name: <u>Steve Watson</u> School Name: <u>www.jmap.org</u>

The possession or use of any communications device is strictly prohibited when taking this examination. If you have or use any communications device, no matter how briefly, your examination will be invalidated and no score will be calculated for you.

Print your name and the name of your school on the lines above.

A separate answer sheet for Part I has been provided to you. Follow the instructions from the proctor for completing the student information on your answer sheet.

This examination has four parts, with a total of 39 questions. You must answer all questions in this examination. Record your answers to the Part I multiple-choice questions on the separate answer sheet. Write your answers to the questions in Parts II, III, and IV directly in this booklet. All work should be written in pen, except graphs and drawings, which should be done in pencil. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. The formulas that you may need to answer some questions in this examination are found at the end of the examination. This sheet is perforated so you may remove it from this booklet.

Scrap paper is not permitted for any part of this examination, but you may use the blank spaces in this booklet as scrap paper. A perforated sheet of scrap graph paper is provided at the end of this booklet for any question for which graphing may be helpful but is not required. You may remove this sheet from this booklet. Any work done on this sheet of scrap graph paper will *not* be scored.

When you have completed the examination, you must sign the statement printed at the end of the answer sheet, indicating that you had no unlawful knowledge of the questions or answers prior to the examination and that you have neither given nor received assistance in answering any of the questions during the examination. Your answer sheet cannot be accepted if you fail to sign this declaration.

Notice...

A graphing calculator and a straightedge (ruler) must be available for you to use while taking this examination.

DO NOT OPEN THIS EXAMINATION BOOKLET UNTIL THE SIGNAL IS GIVEN.

ΑΑΑΞΘΙΑ ΟΞΤΑΑΘΞΤΝΙ

Part I

Answer all 30 questions in this part. Each correct answer will receive 2 credits. No partial credit will be allowed. For each question, write on the separate answer sheet the numeral preceding the word or expression that best completes the statement or answers the question. [60]

Use this space for **1** If $A = \{1, (2), 3, (3), 5, (6), 7, (8), and B = (2, (4), (6), (8), 12\}, the$ intersection includes elements common to both sets. intersection of sets A and B is $(1) \{10, 12\}$ (3) {1, 3, 5, 7} $\{2, 4, 6, 8\}$ (4) {1, 2, 3, 4, 5, 6, 7, 8, 10, 12} **2** What is the value of *n* in the equation 0.2(n - 6) = 2.8? 0.2(n-6) = 2.820(1) 8= 2.8 ·2n - 1.2 (2) 2(4) 44 1.2 +1.2 = 40 .21 4.0 3 **3** The expression $\frac{24x^6y^3}{-6x^3y}$ is equivalent to = 20 5 2 (1) $-4x^2y^3$ (3) $-4x^9y^4$ (2) $-4x^3y^3$ $-4x^3u^2$ **4** Which situation is represented by bivariate data? (1) A student lists her algebra quiz grades for one month. Uariable (2) A wrestler records his weight before each match. User is le (3) A musician writes down how many minutes she practices her 10 arichle instrument each day. Zvariables An ice cream vendor tracks the daily high temperature and how many ice cream bars he sells each day. meens [2]

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- 7 Jose wants to ride his bike a total of 50 miles this weekend. If he rides m miles on Saturday, which expression represents the number of miles he must ride on Sunday?
 - (1) m 50

(2) m + 50

(4) 50 - m

[3]

8 Four students are playing a math game at home. One of the math game questions asked them to write an algebraic equation.



9 A student spent 15 minutes painting a 2-foot by 3-foot bulletin board. To the nearest tenth of a minute, how long did it take the student to A 2x3 foot bulletin board has area of 6 ft2 paint 1 square foot? (1) 0.42.5 (4) 3.5 (2) 1.5 $\frac{15\min}{12L^2} = \frac{X\min}{12L^2}$ 10 What is an equation of the line that passes through the points (2,1)11 What is $\frac{10}{7x} - \frac{3}{5x}$ expressed in simplest form? (4) $\frac{55}{35x}$ (2) $\frac{29}{2r}$ $\frac{50}{35X} - \frac{21}{35X}$

[4]

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13 The length of a rectangle is three feet less than twice its width. If x represents the width of the rectangle, in feet, which inequality represents the area of the rectangle that is *at most* 30 square feet?

20-3

$x(2x-3) \le 30$	(3) $x(3-2x) \le 30$
(2) $x(2x-3) \ge 30$	$(4) \ x(3-2x) \ge 30$







15 The weights of 40 students were recorded. If the 75th percentile of their weights was 140 pounds, what is the total number of students who weighed *more than* 140 pounds?

 $-\frac{4}{3}$

(2) $\frac{7}{3}$

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[5]

 $\begin{array}{r} y = ... \\ 4x + 3y = 7 \\ -4x \\ -4x \\ 3y = -4x + 7 \\ y = \frac{-4}{3}x + 7 \\ y = \frac{-4}{3}x + 7 \\ OVER \end{array}$

17 What is $\sqrt{150} + \sqrt{24}$ expressed in simplest radical form?

 \bigcirc $7\sqrt{6}$ (3) $\sqrt{87}$ (2) $7\sqrt{12}$ (4) $\sqrt{174}$



18 In $\triangle ABC$ below, the measure of $\angle A = 90^{\circ}$, AB = 6, AC = 8, and BC = 10.





Which ratio represents the sine of $\angle B$?

(1)	$\frac{10}{8}$	(3)	$\frac{6}{10}$
-----	----------------	-----	----------------

(2)
$$\frac{8}{6}$$
 $\bigcirc \frac{8}{10}$

 $E_{y} = 300 \text{ and } 3x + 7y = 285 \text{ represent the}$ However, If x represents the cost for each chocolate gift basket, what is the cost y represents the cost for each chocolate gift basket, what is the cost (1) \$20 19 The equations 6x + 5y = 300 and 3x + 7y = 285 represent the

(4) \$54

- (2) \$25

$$6\chi + 14\gamma = 570$$

$$6\chi + 14\gamma = 300$$

$$6\chi + 5\gamma = 300$$

$$9\gamma = 270$$

$$\gamma = \frac{270}{9}$$

$$\gamma = 30$$

20 Which equation represents the axis of symmetry of the graph of the equation $y = x^2 + 4x - 5?$

 $X = \frac{-5}{20}$ (3) y = -2x = -2X = - Z (4) y = 4(2) x = 4X = . [6]Integrated Algebra - Jan. '15

21 For which value of x is the expression $\frac{x+2}{2x-1}$ undefined? undefined means the denominator = 0

- $(3) -\frac{1}{2}$ (1) 0
- (2) -2
- 2x = 1 $x = \frac{1}{2}$ 22 Last year, Nick rode his bicycle a total of 8000 miles. To the

 $\frac{1}{2}$

nearest yard, Nick rode an average of how many yards per day?



2X - 1 = 0

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[OVER]

25 The diagram below shows the path a bird flies from the top of a 9.5-foot-tall sunflower to a point on the ground 5 feet from the base of the sunflower.

Summover. $fan = \frac{opposite}{odjocent}$ $fan X = \frac{5}{9.5}$ djocent $arctan \frac{5}{9.5} = 27.75854$ $\boxed{27.8^{\circ}}$

To the *nearest tenth of a degree*, what is the measure of angle *x*?

	27.8	(3)	58.2
(2)	31.8	(4)	62.2

26 Which set of numbers represents the lengths of the sides of a right triangle?

- (7, 24, 25)
 (2) {9, 16, 23}



27 How many different seven-letter arrangements of the letters in the word *HEXAGON* can be made if each letter is used only once?



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28 Three students each rolled a wooden cube with faces painted red, white, and blue. The color of the top face is recorded each time the cube is rolled. The table below shows the results.

Student	Number of Rolls	Red	White	Blue
1	30	11	7	12
2	50	19	11	20
3	20	8	4	8
	100			40

The probability of blue is 40 out of 100 P(blue) = 40 100

If a fourth student rolled the cube 75 times, based on these experimental data, approximately how many times can the cube be expected to land with blue on top?

(4) 40

- (3) 35 (1) 25

30

 $\frac{40}{100} = \frac{x}{75}$ 100 X = 40(75) 100X = 3000x = 30

- **29** Dominick graphs the equation y = a|x| where a is a positive Use graphing calculator $U_{se} = \frac{1}{2} |x|$ $V_{s} = \frac{1}{2} |x|$ $V_{s} = -30 |x|$ integer. If Gina multiplies a by -3, the new graph will become
 - *i* narrower and open downward
 - (2) narrower and open upward
 - (3) wider and open downward
 - (4) wider and open upward

- Use this space for
- 30 Mr. Suppe recorded the height, in inches, of each student in his class. The results are recorded in the table below.

computations.

60	59	70	65	64
61	58	72	75	66
65	67	63	62	68
68	69	74	61	70

4×5 = 20 students

Which cumulative frequency histogram represents the data?



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[10]

Part II

Answer all 3 questions in this part. Each correct answer will receive 2 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. For all questions in this part, a correct numerical answer with no work shown will receive only 1 credit. All answers should be written in pen, except for graphs and drawings, which should be done in pencil. [6]

31 As shown in the diagram below, a ladder 12 feet long leans against a wall and makes an angle of 72° with the ground.



Find, to the nearest tenth of a foot, the distance from the wall to the base of the ladder.

$$\cos 72^{\circ} = \frac{adj}{hyp}$$

$$\cos 72^{\circ} = \frac{adj}{12}$$

$$12(\cos 72^{\circ}) = adjacent$$

$$3.708 = adjacent$$

$$3.77feet$$

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[OVER]

32 Carla bought a dress at a sale for 20% off the original price. The sale price of the dress was \$28.80. Find the original price of the dress, in dollars.

Original cost (1007.-20%) = #28.80Original cost (80%) = #28.80Original cost (.80) = \$28,80 $Original cost = \frac{428:80}{.80}$ Original cost = #36.00

 $\begin{array}{rcl} \# & 36.00 \times 80\% = \frac{\#}{28.80} \\ \# & 36.00 \times 8 & = \frac{\#}{28.80} \\ \# & 28.80 & = \frac{\#}{28.80} \end{array}$ heck

[12]

33 The probability that a student owns a dog is $\frac{1}{3}$. The probability that the same student owns a dog and a cat is $\frac{2}{15}$. Determine the probability that the student owns a cat.

(robability (event A and event B) = F(A) * F(B) Let PA represent the probability of owning a dog. $P_{(A)} = \frac{1}{3}$ Let $P_{(B)}$ represent the probability of owning a <u>cat</u>. $P_{(B)} = \frac{2}{3}$ Let P(And 3) represent the probability of owning a dog and cat $P(Aond B) = \frac{2}{15}$ Mand B) = MA) · MB)

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[OVER]

Part III

Answer all 3 questions in this part. Each correct answer will receive 3 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. For all questions in this part, a correct numerical answer with no work shown will receive only 1 credit. All answers should be written in pen, except for graphs and drawings, which should be done in pencil. [9]

34 A DVD costs twice as much as a music CD. Jack buys 2 DVD sund 2 CDs and spends 845.
Determine how much one CD costs, in dollars. [Only an algebraic solution can receive full credit.]
Let D regressent the cost of a DVD
Let C represent the cost of a DVD
Let C represent the cost of a CD

$$D = 2C$$

 $2(D) + 2C = 45$
 $2(2C) + 2C = 45$
 $4C + 2C = 45$
 $6C = 45$
 $C = 15$
 $D = 2(7.50)$
 $15 = 15$ V
 $2(15) + 2(7.5) = 45$
 $15 = 45$ V
 $45 = 45$ V

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[14]

35 Noj has the following test scores:

76, 84, 69, 74, 91

His teacher will allow him to retake the test on which he scored lowest. Noj wants an average of at least 82. Determine the least number of additional points Noj must score on the retest.



36 Graph y < x and x > 5 on the axes below. y h ►X (10, -10)State the coordinates of a point in the solution set. A point in the solution set is (10,-10) Check X>5 10>5/ Y < X -10 < 10

Part IV

Answer all 3 questions in this part. Each correct answer will receive 4 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. For all questions in this part, a correct numerical answer with no work shown will receive only 1 credit. All answers should be written in pen, except for graphs and drawings, which should be done in pencil. [12]

37 The Rock Solid Concrete Company has been asked to pave a rectangular area surrounding a circular fountain with a diameter of 8 feet, as shown in the diagram.



Find the cost, *in dollars*, of paving the area if the Rock Solid Concrete Company charges \$8.95 per square foot.

490 square Feet times \$895/52.1 490 (8.95) = \$4,385.50

38 Solve the following system of equations algebraically:

$$\begin{array}{c}
E_{2}, \#_{2} \\
F_{2}, \#_{2}$$

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39 Perform the indicated operations and express the result in simplest form: $\left(\frac{10x^2y}{x^2+xy}\right)$ $\left(x+y\right)^2$ ÷ 2xChange keep ' P $10 x^2$ $X^{z} + X$ ZX Facto Cancel 5 5 Y X - Y3

State Contraction