The University of the State of New York REGENTS HIGH SCHOOL EXAMINATION

INTEGRATED ALGEBRA

Wednesday, June 1, 2016 — 1:15 to 4:15 p.m., only

Steve Watson

JMAP. ORG

Student Name:_____

School Name:

The possession or use of any communications device is strictly prohibited when taking this examination. If you have or use any communications device, no matter how briefly, your examination will be invalidated and no score will be calculated for you.

Print your name and the name of your school on the lines above.

A separate answer sheet for Part I has been provided to you. Follow the instructions from the proctor for completing the student information on your answer sheet.

This examination has four parts, with a total of 39 questions. You must answer all questions in this examination. Record your answers to the Part I multiple-choice questions on the separate answer sheet. Write your answers to the questions in Parts II, III, and IV directly in this booklet. All work should be written in pen, except graphs and drawings, which should be done in pencil. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. The formulas that you may need to answer some questions in this examination are found at the end of the examination. This sheet is perforated so you may remove it from this booklet.

Scrap paper is not permitted for any part of this examination, but you may use the blank spaces in this booklet as scrap paper. A perforated sheet of scrap graph paper is provided at the end of this booklet for any question for which graphing may be helpful but is not required. You may remove this sheet from this booklet. Any work done on this sheet of scrap graph paper will *not* be scored.

When you have completed the examination, you must sign the statement printed at the end of the answer sheet, indicating that you had no unlawful knowledge of the questions or answers prior to the examination and that you have neither given nor received assistance in answering any of the questions during the examination. Your answer sheet cannot be accepted if you fail to sign this declaration.

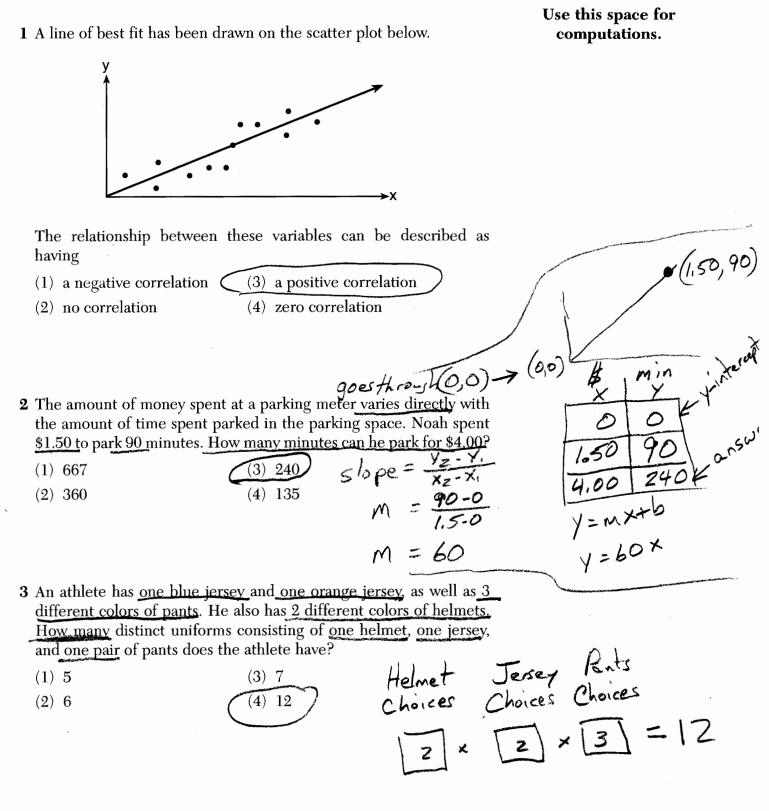
Notice...

A graphing calculator and a straightedge (ruler) must be available for you to use while taking this examination.

DO NOT OPEN THIS EXAMINATION BOOKLET UNTIL THE SIGNAL IS GIVEN.

Part I

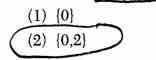
Answer all 30 questions in this part. Each correct answer will receive 2 credits. No partial credit will be allowed. For each question, write on the separate answer sheet the numeral preceding the word or expression that best completes the statement or answers the question. [60]



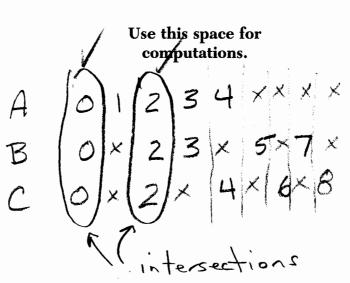
4 Given:

 $A = \{0, 1, 2, 3, 4\}$ $B = \{0, 2, 3, 5, 7\}$ $C = \{0, 2, 4, 6, 8\}$

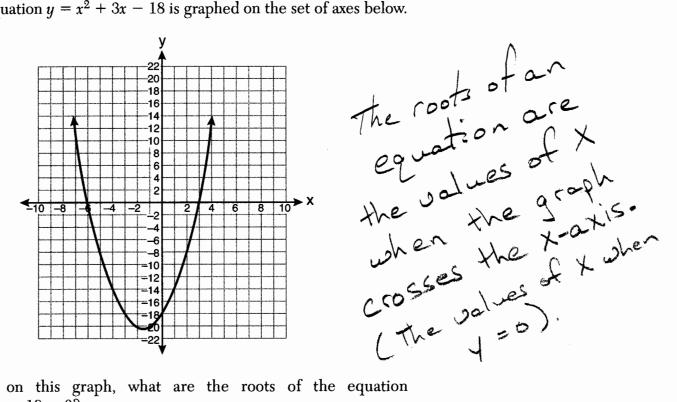
What is the intersection of sets A, B, and C?



 $(3) \{0,2,3,4\}$ $(4) \{0,1,2,3,4,5,6,7,8\}$



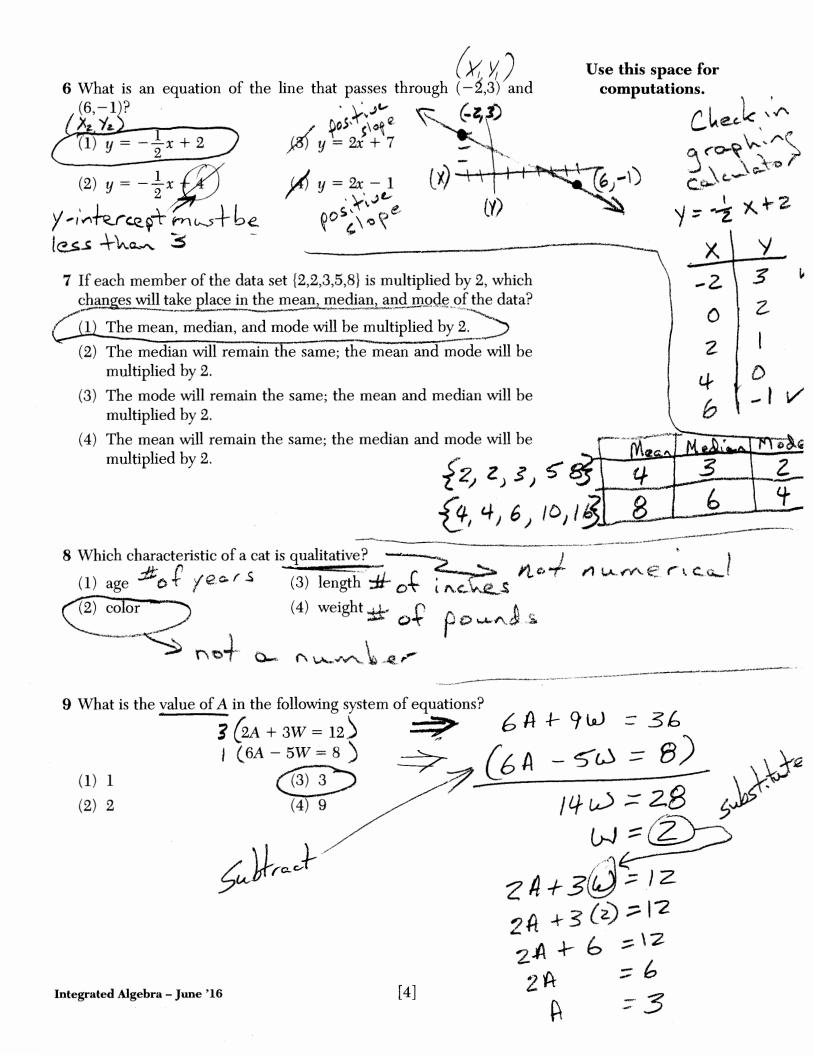
5 The equation $y = x^2 + 3x - 18$ is graphed on the set of axes below.



Based on this graph, what are the roots of the equation $x^2 + 3x - 18 = 0$?

- (1) -3 and 6
- (2) 0 and -18

(3) 3 and -6(4) 3 and -18



Use this space for computations.

- **10** A cell phone company is conducting a survey to determine the cell phone features that its customers use. Which survey is *least* biased?
 - (1) The company conducts the survey on teenagers.
 - (2) The company conducts the survey on all age groups.
 - (3) The company conducts the survey on retired females.
 - (4) The company conducts the survey on middle-aged males.

11 Which pair of linear equations represents parallel lines?

(1) The company conducts the survey on teenagers.
(2) The company conducts the survey on all age groups.
(3) The company conducts the survey on middle-aged males.
(4) The company conducts the survey on middle-aged males.
(4) The company conducts the survey on middle-aged males.
(4) The company conducts the survey on middle-aged males.
(5)
$$y = -\frac{1}{2}x + 4$$
 (6) $y = 5x + 1$
 $y = 2x + 4$ (7) $y = -5x + 7$
(7) $x + y = 5 \Rightarrow \sqrt{z - x} + 5$ (4) $2x + y = 4$ $\sqrt{z - 2x + 4}$ (hoices 1) z , and z have
 $-x + y = 4$ $y = x + 4$ $y + 2x = 8$ $\sqrt{z - 2x + 6}$ different to be percented.
2 Which set of points does not represent a function?
(1) $\{(-3, -2), (-1, -2), (0, -1), (1, 0)\}$

12 Which set of points does not represent a function

$$(1) \{(-3,-2),(-1,-2),(0,-1),(1,0)\}$$

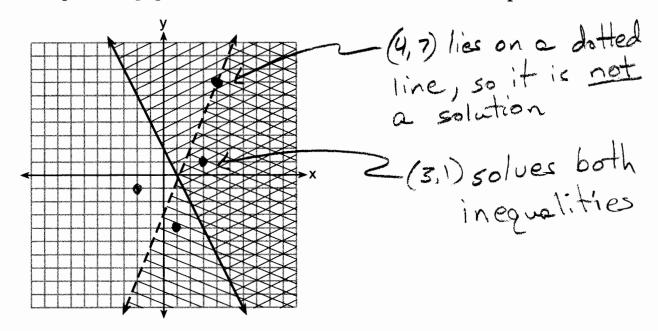
$$(2) \{(-2,3),(0,4),(3,-2),(4,2)\}$$

$$(3) \{(2,-2),(1,4),(2,5),(3,6)\}$$

$$(4) \{(-2,4),(1,1),(2,4),(3,9)\}$$

13 A system of inequalities is graphed on the set of axes below.

Use this space for computations.



The coordinates of a point in the solution of this system of inequalities are

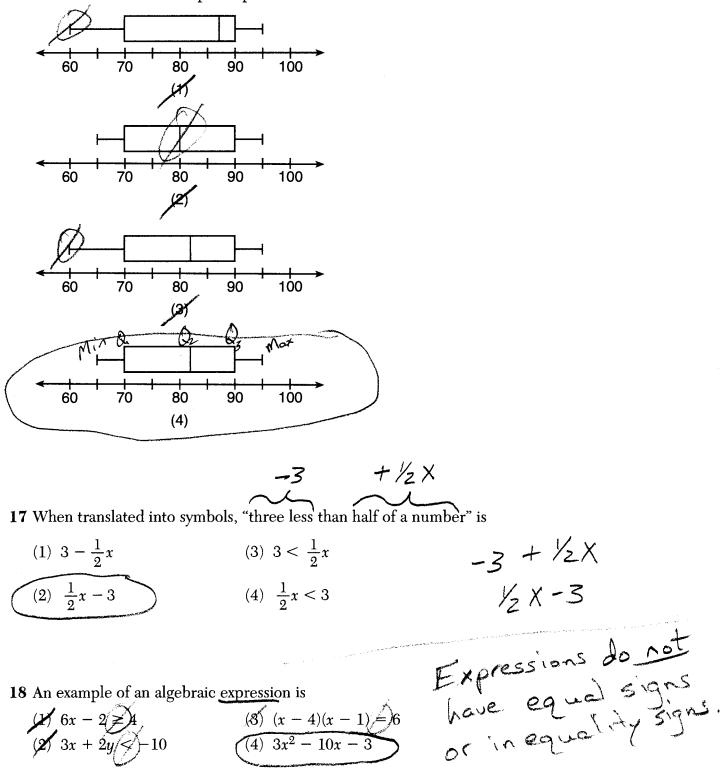
14 The axis of symmetry and the vertex of $y = x^2 - 4x + 10$ are $\underbrace{(1) \ x = 2 \text{ and } (2,6)}_{(2) \ y = 2 \text{ and } (2,6)} (3) \ y = -2 \text{ and } (-2,6) \qquad \text{Cris of symmetry } \mathbb{C} \times \mathbb{C} = \mathbb{C}$ $\underbrace{(1) \ x = 2 \text{ and } (2,6)}_{(2) \ y = 2 \text{ and } (2,6)} (3) \ y = -2 \text{ and } (-2,6) \qquad \text{Cris of symmetry } \mathbb{C} \times \mathbb{C} = \mathbb{C}$ X_ 10 \mathcal{O} 7 ١ 6 $(3) -\frac{4}{3} \qquad \mathcal{U}\chi = 3(\gamma + \vartheta)$ 3 $(1) \frac{4}{3}$ 10 (4) $-\frac{3}{4}$ $4\chi = 3\gamma + 24$ (2) $\frac{3}{4}$ 4x - 24 = 3yY=mx+b N slope '븢x-:븢=Y Y= ⅓ X-8 [6] Integrated Algebra - June '16 sbpe

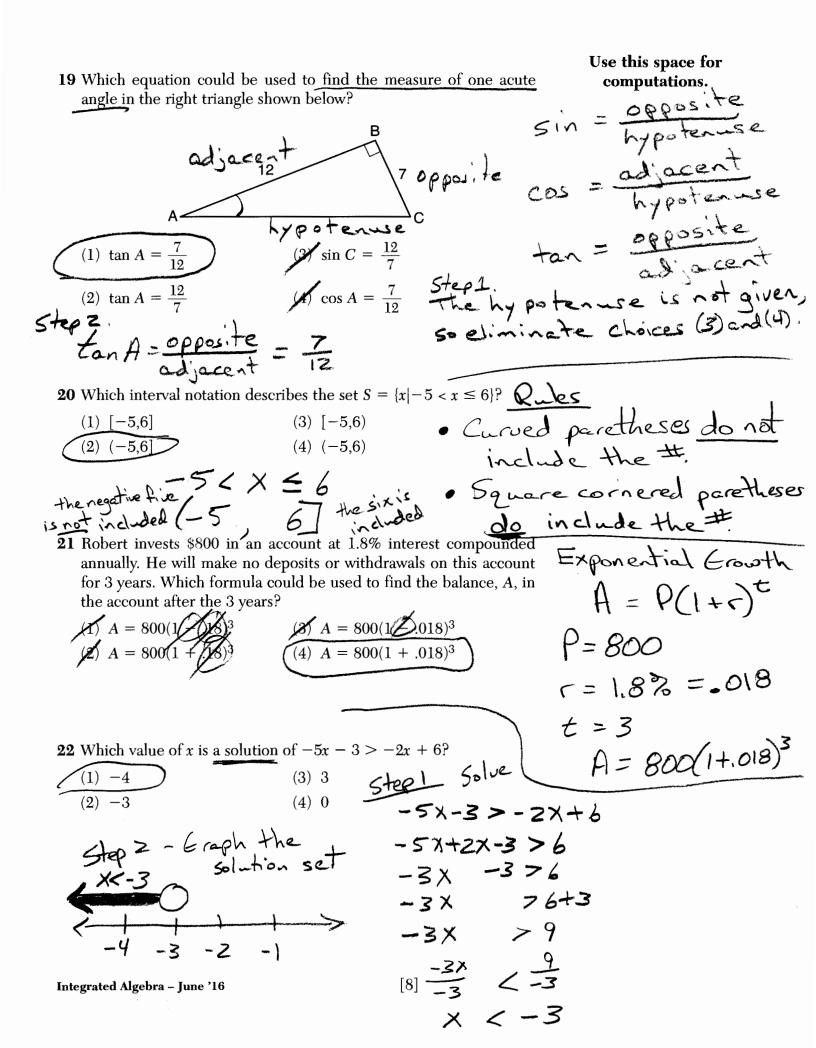
16 The students in Ms. Glenn's math class earned the grades shown

Use this space for computations.

≥65, 70, 70, 80, 80, 82, 88, 88, 90, 90, 95 Max (2) below. Min

Which box-and-whisker plot represents these data?





Use this space for 23 Given $W = \frac{V^2 t}{R}$, which expression can be used to represent t in computations. terms of W, R, and V? $\omega = \frac{V^2 + E}{P}$ (1) \underline{WR} (3) $\frac{W}{R} - V^2$ V^2 $RW = V^2 t$ (2) $\frac{W}{RV^2}$ (4) $WB - V^2$ RW = t hypotenuse 24 The longest side of a right triangle is 25. If one of the other sides is $a^2+b^2=c^2$ 5, which measure is the length of the missing side? 25 $a^2 + 5^2 = 25^2$ (1) $5\sqrt{26}$ (3) 30 (2) $10\sqrt{6}$ $2^{2}+25=625$ (4) 60 =600 $\sigma = 2000$ 25 Which statement is correct? (1) $(2b^3c^5)(-3b^2c) = -6b^5c^{(5)}$ a = J100 J6 $(2) \quad \frac{6m^3t^8}{-2m^5t^3} = \frac{-3t^5}{m^2}$ a = 10 56 $(2) (-5n^4q)^2 = 25n^2q^2$ $(4) \frac{t^{3}}{v^{5}} \div \frac{v}{t} = \frac{t^{2}}{v^{2}} \qquad \frac{t^{3}}{t^{5}} \times \frac{t}{v} = \frac{t^{4}}{v^{6}}$ 26 What value of x would make the expression $\frac{x}{2x+1}$ undefined? Is undefined when the (1) 0 (3) -1 denominator = zero. $(2) -\frac{1}{1}$ (4) $\frac{1}{2}$ 2X+1=02X = -1X = -1Difference of Perfect Square 27 Written in factored form, the binomial $a^2 - 16b^2$ is equivalent to $a^{2}-b^{2}=(a+b)(a-b)$ $\underbrace{(1) \ (a-4b)(a+4b)}_{(2) \ (a-4b)(a-4b)}$ (3) (a - 8b)(a + 8b) $a = 16b^2 = (a + 4b)(a - 4b)$ (4) (a - 8b)(a - 8b)

Use this space for 28 A spinner is divided into three equal regions, as shown in the computations. (Outcomes) diagram below. Ray spun the spinner six times and recorded his results: red, blue, blue, green, red, red. Emperica Theorot Probab. Red Green Red Blue Blue Free Which statement is true about the outcomes of blue in Ray's experiment? (A) The empirical probability was less than the theoretical probability. (2) The empirical probability was greater than the theoretical probability. (3) The empirical and theoretical probabilities were equal. Inches Feet (4) The empirical and theoretical probabilities were unrelated 2 Liem 9 Eli Faith 0 29 Liem is 6 feet 2 inches, Eli is 5 feet 9 inches, Faith is 6 feet, and 4 Simon is 5 feet 4 inches. In yards, what is the total of their heights? Simon 22ft. 15in. (3) $22\frac{15}{36}$ (1) $7\frac{3}{4}$ Total 2244. 15 in. 23 ft 3 in. 7 yds 2 ft 3 in. 7 yds 0 ft 27 in 7 $\frac{32}{36}$ yds 0 ft 0 in 7 $\frac{37}{36}$ yds 5 implify (2) $7\frac{16}{36}$ (4) $23\frac{1}{4}$ **30** The sum of $\frac{x}{2a}$ and $\frac{2x}{3a}$ is $\frac{7x}{6a}$ (1) $\frac{3x}{5a}$ (3)(2) $\frac{3x}{6a}$

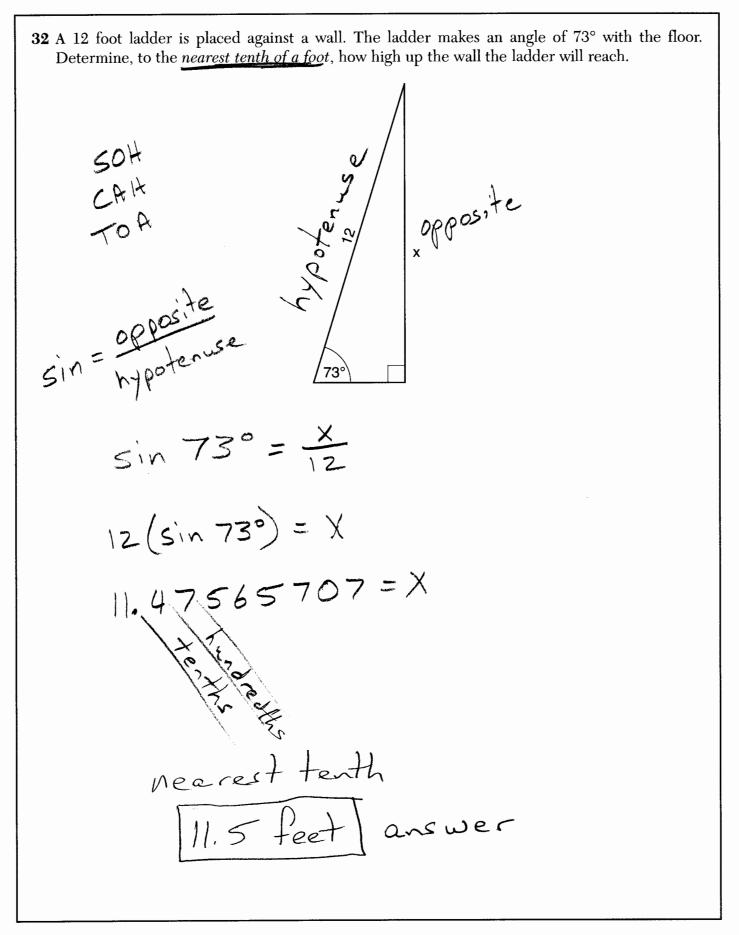
Part II

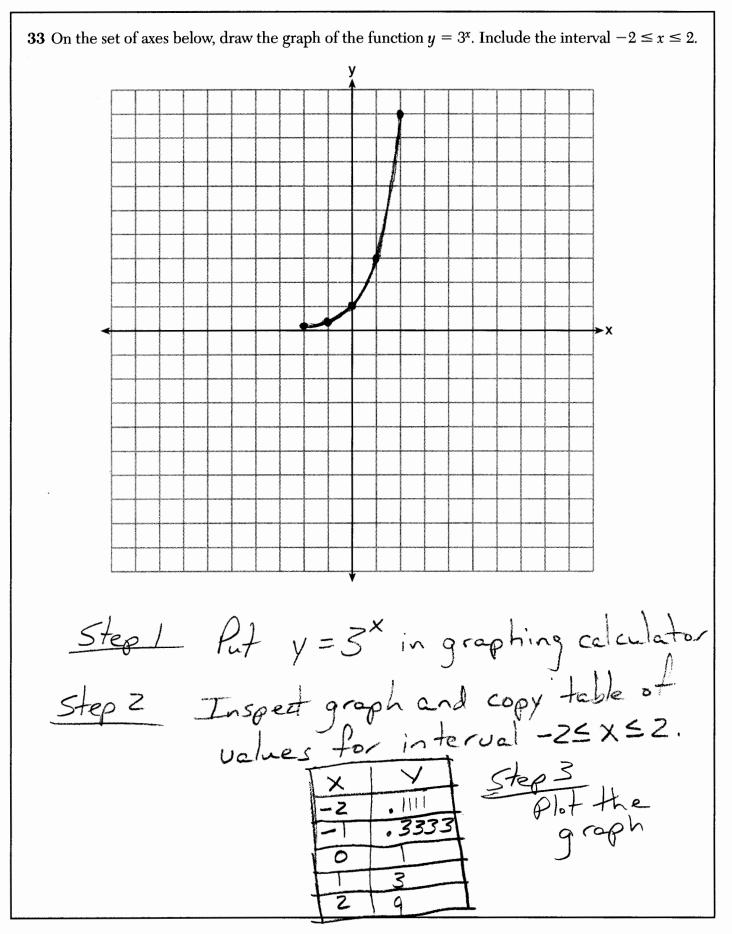
Answer all 3 questions in this part. Each correct answer will receive 2 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. For all questions in this part, a correct numerical answer with no work shown will receive only 1 credit. All answers should be written in pen, except for graphs and drawings, which should be done in pencil. [6]

31 Jim calculated the area of a triangle to be 51.75 cm². The actual area of the triangle is 53.24 cm²
Find the relative error in Jim's calculation of the area to the nearest thousandth.

$$Relative Free = \left| \frac{actual - measured}{actual} \right|$$

$$= \left| \frac{-1.49}{53.24} \right|$$





Part III

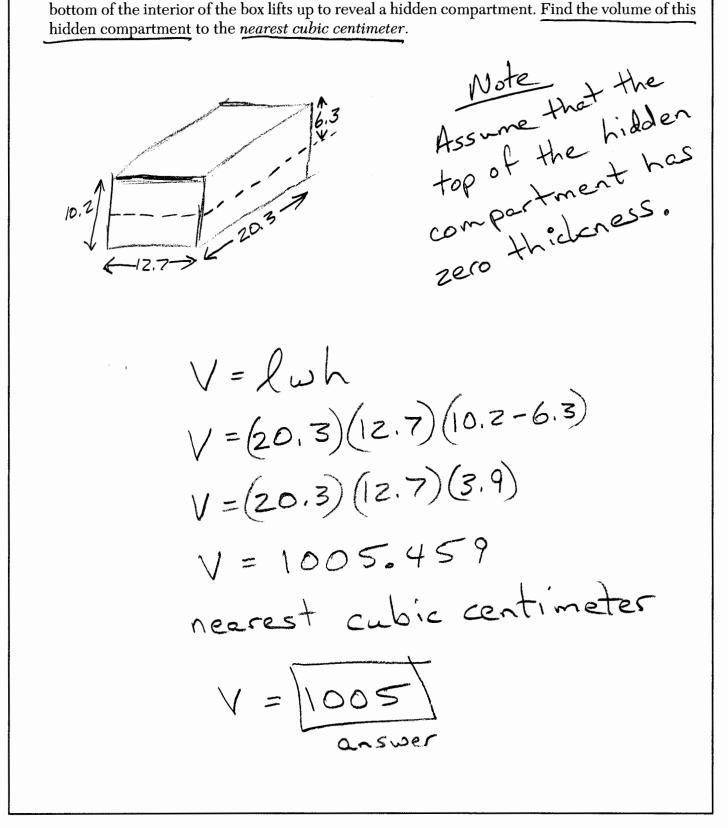
Answer all 3 questions in this part. Each correct answer will receive 3 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. For all questions in this part, a correct numerical answer with no work shown will receive only 1 credit. All answers should be written in pen, except for graphs and drawings, which should be done in pencil. [9]

34 Ryan bought three bags of mixed tulip bulbs at a local garden store. The first bag contained 7 yellow bulbs, 8 red bulbs, and 5 white bulbs. The second bag contained 3 yellow bulbs, 11 red bulbs, and 6 white bulbs. The third bag contained 13 yellow bulbs, 2 red bulbs, and 5 white bulbs. Ryan combined the contents of these three bags into a single container. He randomly selected one bulb, planted it, and then randomly selected another and planted that one. Determine if it is more likely that Ryan planted a red bulb and then another red bulb, or planted a yellow bulb and then a white bulb. Justify your answer.

-					
f	~	Yellow	Red	white	Totals
	Bag 1	~	8	5	20
	Bag 2	3		6	20
	Bag 3	13	2	5	20
	Totals	23	21	16	60

Marb) = Par (b) $(red+red) = \left(\frac{21}{60}\right)$ 23 Answer followed by red is more

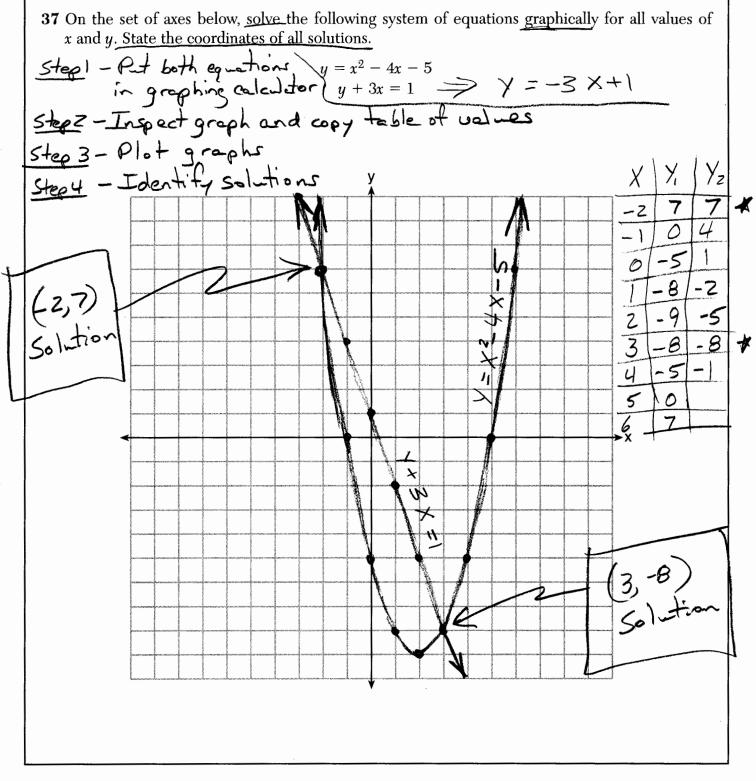
35 A particular jewelry box is in the shape of a rectangular prism. The box is advertised as having an interior length of 20.3 centimeters, an interior width of 12.7 centimeters, and an interior height of 10.2 centimeters. However, when a customer measures the interior of the box, she finds that the interior height is actually 6.3 centimeters. Upon further examination, she discovers that the bottom of the interior of the box lifts up to reveal a hidden compartment. Find the volume of this hidden compartment to the *nearest cubic centimeter*.



36 Solve algebraically for all values of x that satisfy the equation: $\frac{x}{x+4} = \frac{3}{x+2}$ 3 God Mit ett. 3 in left ett. 4 Simplify $X^2 + 2X - 3X - 12 = 0$ 5 Foctor $X^2 - X - 12 = 0$ (X-4) (X+3) = 0 6 multiplication reperty of X-4 = 0 X+3 = 0 7 answers [X=4] [X=-3] Check X=4 4 = 3 4+4 = 4+2 $\begin{array}{c} X = -3 \\ -3 \\ -3 + 4 \end{array} = \frac{3}{-3 + 2}$ $\frac{-3}{-1} = \frac{3}{-1}$ -3=-3/

Part IV

Answer all 3 questions in this part. Each correct answer will receive 4 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. For all questions in this part, a correct numerical answer with no work shown will receive only 1 credit. All answers should be written in pen, except for graphs and drawings, which should be done in pencil. [12]



Adivision $\frac{\chi^{2} + 5\chi + 6}{\chi^{2} - \chi - 20} \propto \frac{2\chi - 10}{\chi^{2} + \chi - 16}$ inverted **38** Express in simplest form: $\frac{x^2 + 5x + 6}{x^2 - x - 20} \bigoplus_{x=1}^{\infty} \frac{x^2 + x - 6}{2x - 10}$ or (X+3)(X+2 (2)concel 1 [x+3)(x-2)] (x + 4)(X+2)(2)(X+4) (X-2) swer 2X+4 $x^{2}+2x-8$

39 The length of a rectangle is $(3\sqrt{8} + 2)$ and the width is $(2\sqrt{2} + 1)$.

Express the perimeter of the rectangle in simplest radical form.

$$P = 2 (l+\omega)$$

$$P = 2(3J\overline{3} + 2 + 2J\overline{2} + 1)$$

$$P = 2(3J\overline{3}\overline{2} + 2 + 2J\overline{2} + 1)$$

$$P = 2(3 \cdot 2J\overline{2} + 2 + 2J\overline{2} + 1)$$

$$P = 2(6J\overline{2} + 2J\overline{2} + 2 + 1)$$

$$P = 2(8J\overline{2} + 3)$$

$$P = 16J\overline{2} + 6 \quad \text{answer}$$
ress the area of the rectangle in simplest radical form.

$$A = 1\omega$$

$$A = (3J\overline{3} + 2)(2J\overline{2} + 1)$$

$$A = (3J\overline{3} \cdot 2J\overline{2}) + (3J\overline{3} \cdot 1) + (2\cdot 2J\overline{2})$$

Exp

$$A = 24 + 65z + 2 = 25z + 1$$

$$A = (3 J = +2)(2 J = +1)$$

$$A = (3 J = 2 J = 2)(2 J = +1) + (2 \cdot 2 J = 2) + (2 \cdot 1)$$

$$A = (6 J = -1) + (3 J = -1) + (2 J = -1) + (2 - 1)$$

$$A = (6 \cdot 4) + (3 J = J = -1) + (4 J = -1) + (2 - 1)$$

$$A = 24 + (3 \cdot 2 J = -1) + (4 J = -1) + (2 - 1)$$

$$A = 24 + (3 \cdot 2 J = -1) + (4 J = -1) + (2 - 1)$$

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