

## INTERMEDIATE ALGEBRA

Monday, January 20, 1913 — 9.15 a. m. to 12.15 p. m., only

Write at top of first page of answer paper (a) name of school where you have studied, (b) number of weeks and recitations a week in algebra. The minimum time requirement is two recitations a week for a school year or four recitations a week for half a school year, after the completion of elementary algebra.

Answer eight questions, including the questions in group I and two questions in each of the other groups. Credit will not be granted unless all operations (except mental ones) necessary to find results are given; simply indicating the operations is not sufficient. Each answer should be reduced to its simplest form.

## Group I

1 Simplify  $(x^2 - y^2 + \frac{4xy(y+x)}{x-y}) \div (\frac{x^2 + y(y+2x)}{4x^2 - 6xy + 2y^2})$

[Credit will not be granted for the answer to this question if there is any error in the work.]

2 Solve  $x^{-4} - 4x^{-2} - 21 = 0$

## Group II

3 Find two numbers in the ratio of 3:2 such that their sum shall be to the difference of their squares as 1:5.

4 Write, with integral coefficients, the quadratic equation whose roots are  $\frac{1}{2}(3 + \sqrt{-7})$  and  $\frac{1}{2}(3 - \sqrt{-7})$

5 Find the sum of the series  $4, -\frac{8}{3}, \frac{16}{9}, \dots$  to infinity.

## Group III

6 Solve  $x^2 + px + q = 0$  and state the relation between the roots and the coefficients.

7 Solve  $3\sqrt{x+8} - \sqrt{x-8} = 2\sqrt{2x+2}$

8 The sum of the cubes of two numbers is 756; the sum of the squares of these numbers diminished by their product is equal to 63. Find the numbers.

## Group IV

9 A merchant bought some pieces of silk for \$900; had he bought 3 pieces more for the same money, he would have paid \$15 less for each piece. Find the number of pieces purchased.

10 Solve graphically the following, estimating the roots to the nearest tenth:

$$\begin{cases} y = 8 - x^2 \\ 2x - 6y = -9 \end{cases}$$

11 Divide  $\frac{1}{x-1} - \frac{1}{y-1}$  by  $\sqrt[3]{x} - \sqrt[3]{y}$

[Credit will not be granted for the answer to this question if there is any error in the work.]