

August 18, 1981

## Part I

Answer all questions in this part. Each correct answer will receive 2 credits. No partial credit will be allowed. Write your answers in the spaces provided.

1. Solve for  $y$ :  $5y - 17 = 4 + 2y$  1\_\_\_\_\_
2. If 19 is subtracted from three times a number, the result is 110. Find the number. 2\_\_\_\_\_
3. Solve for  $x$ :  $5(x + 1) = 6$  3\_\_\_\_\_
4. Solve for  $x$ :  $0.9x + 0.4 = 7.6$  4\_\_\_\_\_
5. Find the value of  $(6a)^2$  when  $a = \frac{1}{2}$ . 5\_\_\_\_\_
6. Express as a monomial in radical form:  $3\sqrt{7} - \sqrt{7} + 4\sqrt{7}$  6\_\_\_\_\_
7. What is the additive inverse of 3? 7\_\_\_\_\_
8. Express  $\frac{x}{2} + \frac{x}{3}$  as a single fraction. 8\_\_\_\_\_
9. If one acute angle of a right triangle measures  $37^\circ$ , what is the number of degrees in the other acute angle? 9\_\_\_\_\_
10. The lengths of the sides of a triangle are represented by  $(5x + 2)$ ,  $(2x - 7)$ , and  $(6x - 4)$ . Express the perimeter of the triangle as a binomial in terms of  $x$ . 10\_\_\_\_\_
11. Carol can mow a lawn in 45 minutes. What part of the lawn can she mow in 15 minutes? 11\_\_\_\_\_
12. Express the product of  $(x + 14)$  and  $(x - 3)$  as a trinomial. 12\_\_\_\_\_
13. Factor:  $x^2 - a^2$  13\_\_\_\_\_
14. If  $\cos A = 0.4796$ , find the measure of angle  $A$  to the nearest degree. 14\_\_\_\_\_
15. Solve for  $x$ :  $\frac{10}{3x} = \frac{2}{3}$  15\_\_\_\_\_
16. Solve for  $x$  in terms of  $a$  and  $b$ :  $2x + b = a$  16\_\_\_\_\_
17. Two numbers are in the ratio 3:2 and their sum is 10. Find the smaller number. 17\_\_\_\_\_
18. Solve the following system of equations for  $a$ :  

$$\begin{array}{r} 2a + 5b = 19 \\ -3a + 5b = 9 \end{array}$$
18\_\_\_\_\_

*Directions (19-30):* Write in the space provided on the answer sheet the numeral preceding the expression that best completes each statement or answers each question.

19. Rounded to the nearest hundredth, 87.4566 is (1) 87.00  
(2) 87.45 (3) 87.457 (4) 87.46 19\_\_\_\_\_

20. The product of  $2x^3$  and  $6x^2$  is (1)  $12x^6$   $12x^5$   
(3)  $8x^6$  (4)  $8x^5$  20\_\_\_\_\_

21. If  $2a + 5b$  is subtracted from  $3a - 4b$ , the difference is  
(1)  $a + b$  (2)  $5a + b$  (3)  $a + 9b$  (4)  $a - 9b$  21\_\_\_\_\_

22. What is the y-intercept of the line whose equation is  
 $y - 2x = 5$ ? (1)  $-2$  (2)  $2$  (3)  $-5$  (4)  $5$  22\_\_\_\_\_

23. The sum of two numbers is 24. If the larger number is represented by  $x$ , then the smaller number may be represented by (1)  $x - 24$   
(2)  $x + 24$  (3)  $24 - x$  (4)  $24x$  23\_\_\_\_\_

24. The value of  $|-7| - |3|$  is (1)  $-10$  (2)  $10$   
(3)  $-4$  (4)  $4$  24\_\_\_\_\_

25. Which is true of the graph of  $x = 3$ ? (1) It has a slope of 3.  
(2) It is parallel to the y-axis. (3) It has a negative slope.  
(4) It is parallel to the x-axis. 25\_\_\_\_\_

26. If the lengths of the legs of a right triangle are 8 and 3, what is the length of the hypotenuse? (1)  $\sqrt{73}$  (2)  $\sqrt{55}$  (3)  $\sqrt{11}$  (4)  $\sqrt{5}$  26\_\_\_\_\_

27. Which is the solution set of  $1 < x \leq 3$ , if the replacement set is the set of integers? (1)  $\{1\}$  (2)  $\{1,2\}$  (3)  $\{1,2,3\}$  (4)  $\{2,3\}$  27\_\_\_\_\_

28. The solution set of  $x^2 - 2x = 15$  is (1)  $\{3,5\}$  (2)  $\{3,-5\}$   
(3)  $\{-3,5\}$  (4)  $\{-3,-5\}$  28\_\_\_\_\_

29. Which value of  $b$  will make the expression  $\frac{(b-1)(b+1)}{b-3}$   
undefined or meaningless? (1) 1 (2)  $-1$  (3) 3 (4)  $-3$  29\_\_\_\_\_

30. Last season, a soccer team won 8 games and lost 2. What percent of the games played did they lose? (1) 20% (2) 25%  
(3) 80% (4) 400% 30\_\_\_\_\_

## Part II

Answer four questions from this part. Show all work unless otherwise directed.

31. Solve graphically and check:  $y = 2x - 1$   
 $3x + 2y = 12$  [8, 2]

32. Answer both a and b.

a Multiply and express the answer in simplest form:

$$\frac{x^2 - 3x - 40}{x^2 - 25} \cdot \frac{2x - 10}{x - 8} \quad [5]$$

b Express as a single fraction in simplest form:

$$\frac{x + y}{3} - \frac{x}{4} \quad [5]$$

33. Write an equation or system of equations that can be used to solve each of the following problems. In each case state what the variable or variables represent. [Solution of the equations is not required.]

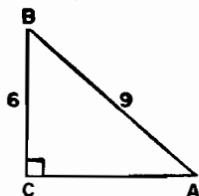
a Two cars pass each other going in opposite directions on the interstate highway. One is traveling at 55 miles per hour and the other at 45 miles per hour. If they continue at the same average speeds, in how many hours will they be 250 miles apart? [5]

b A merchant wishes to mix peanuts selling for \$2.00 a pound with raisins selling for \$1.50 a pound. How many pounds of each should she mix to obtain a mixture of 120 pounds to sell for \$1.75 a pound? [5]

34. The length of a rectangle is 14 meters longer than the width. Find the dimensions of the rectangle if the area is 51 square meters. [Only an algebraic solution will be accepted.] [5, 5]

35. A man invests \$10,000, part of it at 10% and the rest at 5%. The annual income from the two investments is \$700. Find the amount invested at each rate. [Only an algebraic solution will be accepted.] [5, 5]

36. As shown in the accompanying diagram,  $ABC$  is a right triangle,  $C$  is a right angle,  $BC = 6$ , and  $AB = 9$ .



a Find the measure of angle  $A$  to the nearest degree. [5]

b Find the length of  $AC$  to the nearest integer. [5]

37. The questions below refer to set  $A = \{-1, 0, 1, 2\}$ . On your answer paper, write the letters  $a$  through  $e$  and next to each write the set of elements which answers the question. [Each answer must be a member of set  $A$ .] [10]

a What is the additive identity element for the set of real numbers?

b What is the multiplicative identity element for the set of real numbers?

c What is the additive inverse of  $-1$ ?

d What is the multiplicative inverse of  $-1$ ?

e Which element of the replacement set is a prime number?