

SOLID GEOMETRY

Thursday, June 9, 1910—9.15 a. m. to 12.15 p. m., only

Write at the top of the first page of your answer paper (a) the name of the school where you have studied, (b) the number of weeks and recitations a week that you have had in solid geometry.

Two recitations a week for a school year (or four recitations a week for half a school year), in a recognized academic school, is the regular requirement, and any statement showing less or other than this should be accompanied by a satisfactory claim or explanation made by the candidate and certified by the principal; otherwise such paper will be returned.

Answer eight questions, selecting two from each group.

Group I 1 Prove that all the perpendiculars to a given straight line at a given point lie in a plane perpendicular to that line.

2 Prove that the volume of a triangular pyramid is equal to one third the volume of a prism having the same base and the same altitude.

3 Find the total surface and the volume of a regular tetrahedron whose edge is 8 centimeters.

Group II 4 Prove that sections, of a prism made by parallel planes cutting all the lateral edges are equal polygons.

5 Prove that the acute angle which a straight line makes with its projection on a plane is the least angle which it makes with any line of the plane.

6 Prove that if from any point in a dihedral angle perpendiculars are drawn to the faces, the plane determined by these perpendiculars is perpendicular to the edge of the dihedral angle.

Group III 7 The edge of a cube is 5 inches; find the altitude of a right circular cylinder of equal volume whose base is inscribed in the base of the cube.

8 Regarding the earth as a sphere, show that $\frac{1}{8}$ of its volume is included between the planes of the small circles of 30° north latitude and 30° south latitude.

9 A lune whose angle is 36° is equivalent to a zone on the same sphere; find the ratio of the altitude of the zone to the radius of the sphere.

Group IV 10 The four sides of a certain spheric quadrilateral are equal; prove that its diagonals are perpendicular to each other.

11 Find the locus of a point whose distance from a fixed straight line is always equal to its distance from a fixed plane perpendicular to that line.

12 Find a point at equal distances from four points not all in the same plane.