

SOLID GEOMETRY

Monday, June 18, 1917—9.15 a. m. to 12.15 p. m., only

Write at top of first page of answer paper (a) name of school where you have studied, (b) number of weeks and recitations a week in solid geometry. The minimum time requirement is two recitations a week for a school year or four recitations a week for half a school year.

Name the author of the textbook you have used in your study of solid geometry.

Answer eight questions, including four from group I and four from group II.

Group I

Answer four questions from this group.

1 Prove that if two angles, not in the same plane, have their sides respectively parallel and lying in the same direction, they are equal.

2 Prove that if a pyramid is cut by a plane parallel to its base, the edges and the altitude are divided proportionally and the section is a polygon similar to the base.

3 Prove that the lateral area of a regular pyramid is equal to the product of the perimeter of its base and half its slant height. ($S = \frac{1}{2} pl$.)

4 Write the formulas for the surface and the volume of a sphere and prove *one* of them.

5 If two planes are perpendicular to each other, a straight line drawn in one of them, perpendicular to their intersection, is perpendicular to the other.

6 A point is at a given distance from a fixed point P and is also equidistant from two other fixed points Q and R . What is the locus of the point? Prove one of the locus propositions on which your answer depends.

Group II

Answer four questions from this group.

7 The edge of a cube is e , its total surface is s and its volume is v .

a Find s and v in terms of e .

b Find e in terms of v .

8 The dimensions of a rectangular block are to be consecutive integers and the total surface is to be 94 square units; find the dimensions.

9 A cylindrical tank having an internal diameter of 14 feet is filled with water to a height of 10 feet; what is the length of a six inch pipe which this water will exactly fill?

10 On the base of a right circular cone a hemisphere is constructed so that it lies outside the cone. The surface of the hemisphere is equal to the lateral surface of the cone. The radius of the hemisphere is r . Find (a) the slant height of the cone, (b) the volume of the entire solid.

11 On the six faces of a cube as bases regular pyramids are constructed, all lying without the cube. The height of each pyramid is one half the edge e of the cube. Find (a) the surface of the entire solid, (b) the volume of the entire solid.

12 A solid has the form of a regular hexagonal prism of base edge e and of height h , through which a circular, cylindrical hole of diameter e has been cut perpendicularly from base to base. Find (a) the total surface of the resulting solid, (b) the volume of the resulting solid.

13 What fraction of the surface of a sphere is covered by a spheric triangle whose angles are 90 degrees, 100 degrees and 110 degrees? What is the area of the triangle if the radius of the sphere is 10 inches?