Letter from Thomas Jefferson to William G. Munford, Monticello, June 18, 1799.
1. The size of a certain type of molecule is 0.00009078 inch. If this number is expressed as $9.078 \times 10^n$, what is the value of $n$?


2. Sterling silver is made of an alloy of silver and copper in the ratio of 37:3. If the mass of a sterling silver ingot is 600 grams, how much silver does it contain?

[A] 200 g  [B] 450 g  
[C] 555 g  [D] 48.65 g

3. Which property of real numbers is illustrated by the equation $-\sqrt{3} + \sqrt{3} = 0$?

[A] associative property of addition  
[B] additive inverse  
[C] additive identity  
[D] commutative property of addition

4. The expression $(x^2z^3)(xy^2z)$ is equivalent to

[A] $x^3y^2z^4$  
[B] $x^3y^3z^4$  
[C] $x^4y^2z^5$  
[D] $x^2y^2z^3$

5. If rain is falling at the rate of 2 inches per hour, how many inches of rain will fall in $x$ minutes?

[A] $2x$  
[B] $\frac{60}{x}$  
[C] $\frac{x}{30}$  
[D] $\frac{30}{x}$

6. The graph of the equation $x^2 + y^2 = r^2$ forms

[A] two intersecting lines  
[B] a circle  
[C] a straight line  
[D] a parabola

7. Simplify: $\sqrt{50r^2s^4}$

8. Vertex angle $A$ of isosceles triangle $ABC$ measures 20° more than three times $m\angle B$. Find $m\angle C$.

9. The area of the rectangular playground enclosure at South School is 500 square meters. The length of the playground is 5 meters longer than the width. Find the dimensions of the playground, in meters. [Only an algebraic solution will be accepted.]

10. On the accompanying set of axes, draw the reflection of $ABCD$ in the $y$-axis. Label and state the coordinates of the reflected figure.
11. Ramón said that the set of integers is *not* closed for one of the basic operations (addition, subtraction, multiplication, or division). You want to show Ramón that his statement is correct. For the operation for which the set of integers is *not* closed, write an example using:
- o a positive even integer and a zero
- o a positive and a negative even integer
- o two negative even integers
Be sure to explain why each of your examples illustrates that the set of integers is *not* closed for that operation.

12. There are 461 students and 20 teachers taking buses on a trip to a museum. Each bus can seat a maximum of 52. What is the least number of buses needed for the trip?


13. The accompanying diagram shows two parallel streets, Main Street and Brooks Road, intersected by Jay Street. The obtuse angle that Jay Street forms with Brooks Road is three times the measure of the acute angle that Jay Street forms with Main Street.

What is the measure of the acute angle formed by Jay Street and Main Street?


14. Tanisha and Rachel had lunch at the mall. Tanisha ordered three slices of pizza and two colas. Rachel ordered two slices of pizza and three colas. Tanisha's bill was $6.00, and Rachel's bill was $5.25. What was the price of one slice of pizza? What was the price of one cola?

15. Which statement is *not* always true about a parallelogram?

[A] The diagonals are congruent.
[B] The opposite sides are congruent.
[C] The opposite angles are congruent.
[D] The opposite sides are parallel.

16. Which is an equation of the parabola shown in the accompanying diagram?

![Parabola Diagram]

[A] \( y = -x^2 - 2x + 3 \)  [B] \( y = -x^2 + 2x + 3 \)
[C] \( y = x^2 - 2x + 3 \)  [D] \( y = x^2 + 2x + 3 \)
Math A Regents Exam Questions at Random

17. The following set of data represents the scores on a mathematics quiz:
   58, 79, 81, 99, 68, 92, 76, 84, 53, 57, 81, 91, 77, 50, 65, 57, 51, 72, 84, 89
   Complete the frequency table below and, on the accompanying grid, draw and label a frequency histogram of these scores.

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<thead>
<tr>
<th>Interval</th>
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18. Seth bought a used car that had been driven 20,000 miles. After he owned the car for 2 years, the total mileage of the car was 49,400. Find the average number of miles he drove each month during those 2 years.

19. An equation of the line that has a slope of 3 and a y-intercept of -2 is
   [A] \( x = 3y - 2 \)  \hspace{1cm} [B] \( y = -x \)
   [C] \( y = -2x + 3 \)  \hspace{1cm} [D] \( y = 3x - 2 \)

20. What is the slope of the line whose equation is \( 2y = 5x + 4 \)?
   \( \frac{5}{2} \)

21. Written in simplest factored form, the binomial \( 2x^2 - 50 \) can be expressed as
   [A] \( 2(x - 5)(x + 5) \)  \hspace{1cm} [B] \( 2(x - 5)(x - 5) \)
   [C] \( 2x(x - 50) \)  \hspace{1cm} [D] \( (x - 5)(x + 5) \)

22. What is the total number of points of intersection in the graphs of the equations \( x^2 + y^2 = 16 \) and \( y = 4 \)?
   [A] 1  \hspace{1cm} [B] 3  \hspace{1cm} [C] 0  \hspace{1cm} [D] 2

23. Which is an irrational number?
   \( \frac{3}{4} \)  \hspace{1cm} \( \sqrt{9} \)  \hspace{1cm} 3.14  \hspace{1cm} \( \sqrt{3} \)

24. Tina's preschool has a set of cardboard building blocks, each of which measures 9 inches by 9 inches by 4 inches. How many of these blocks will Tina need to build a wall 4 inches thick, 3 feet high, and 12 feet long?
25. A bicyclist leaves Bay Shore traveling at an average speed of 12 miles per hour. Three hours later, a car leaves Bay Shore, on the same route, traveling at an average speed of 30 miles per hour. How many hours after the car leaves Bay Shore will the car catch up to the cyclist?


26. On the accompanying grid, graph a circle whose center is at (0,0) and whose radius is 5. Determine if the point (5,-2) lies on the circle.

27. The expression \( \frac{y}{x} - \frac{1}{2} \) is equivalent to

[A] \( \frac{1 - y}{2x} \)  
[B] \( \frac{2y - x}{2x} \)
[C] \( \frac{y - 1}{x - 2} \)  
[D] \( \frac{x - 2y}{2x} \)

28. For which value of \( x \) will the fraction \( \frac{3}{2x + 4} \) be undefined?


29. In a class of 450 students, 300 are taking a mathematics course and 260 are taking a science course. If 140 of these students are taking both courses, how many students are not taking either of these courses?


30. Which graph is symmetric with respect to the \( y \)-axis?

[A]  
[B]  
[C]  
[D]  

31. When \( -2x^2 + 4x + 2 \) is subtracted from \( x^2 + 6x - 4 \), the result is

[A] \( 3x^2 + 2x - 6 \)  
[B] \( -3x^2 - 2x + 6 \)  
[C] \( 2x^2 - 2x - 6 \)  
[D] \( -x^2 + 10x - 2 \)
32. The accompanying graph represents the yearly cost of playing 0 to 5 games of golf at the Shadybrook Golf Course. What is the total cost of joining the club and playing 10 games during the year?

![Yearly Total Cost Graph]

33. If \(a\) is an odd number, \(b\) an even number, and \(c\) an odd number, which expression will always be equivalent to an odd number?

[A] \(ac(b)^0\)  
[B] \(ac(b)^2\)  
[C] \(ac(b)^1\)  
[D] \(a(bc)\)

34. The student scores on Mrs. Frederick’s mathematics test are shown on the stem-and-leaf plot below.

```
4 | 3
6 | 0 5 5 7 9
7 | 2 5 6 8 9 9 9
9 | 0 1 2 5 9
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Key: 4 | 3 = 43 points

Find the median of these scores.

35. Construct a triangle with sides of lengths \(a\), \(b\), and \(c\), as shown below. Be sure the longest side of your triangle lies on \(\overline{PQ}\) and that point \(P\) is one of the triangle's vertices. [Show all arcs necessary for a valid construction.]

![Construction Diagram]

36. Which statement is the converse of "If the sum of two angles is 180°, then the angles are supplementary"?

[A] If two angles are supplementary, then their sum is 180°.  
[B] If the sum of two angles is not 180°, then the angles are supplementary.  
[C] If the sum of two angles is not 180°, then the angles are not supplementary.  
[D] If two angles are not supplementary, then their sum is not 180°.

37. The accompanying figure represents a section of bathroom floor tiles shaped like regular hexagons.

![Hexagon Diagram]

What is the measure of angle \(ABC\)?

[A] 120°  
[B] 60°  
[C] 150°  
[D] 90°
38. John uses the equation \( x^2 + y^2 = 9 \) to represent the shape of a garden on graph paper.
   a. Graph \( x^2 + y^2 = 9 \) on the accompanying grid.
   b. What is the area of the garden to the nearest square unit?

39. Factor completely: \( 3x^2 - 27 \)
   [A] \( 3(x + 3)(x - 3) \) 
   [B] \( 3(x + 3)(x - 9) \) 
   [C] \( 3(x - 3)^2 \) 
   [D] \( 3(x^2 - 27) \)

40. The coordinates of point \( R \) are (-3,2) and the coordinates of point \( T \) are (4,1). What is the length of \( \overline{RT} \)?
   [A] \( \sqrt{10} \) 
   [B] \( 5\sqrt{2} \) 
   [C] \( 2\sqrt{2} \) 
   [D] \( 4\sqrt{3} \)

41. The expression \( (3x^2 + 2xy + 7) - (6x^2 - 4xy + 3) \) is equivalent to
   [A] \( -3x^2 - 2xy + 4 \) 
   [B] \( -3x^2 + 6xy + 4 \) 
   [C] \( 3x^2 - 6xy - 4 \) 
   [D] \( 3x^2 - 2xy + 4 \)

42. If \( x \) and \( y \) are defined as indicated by the accompanying table, which equation correctly represents the relationship between \( x \) and \( y \)?

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<td>5</td>
<td>7</td>
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<td>7</td>
<td>11</td>
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</tbody>
</table>

   [A] \( y = 2x - 3 \) 
   [B] \( y = 2x + 3 \) 
   [C] \( y = 2x + 2 \) 
   [D] \( y = x + 2 \)

43. What is the sum of \( 5\sqrt{7} \) and \( 3\sqrt{28} \)?
   [A] \( 8\sqrt{35} \) 
   [B] \( 9\sqrt{7} \) 
   [C] \( 60\sqrt{7} \) 
   [D] \( 11\sqrt{7} \)

44. Melissa's test scores are 75, 83, and 75. Which statement is true about this set of data?
   [A] mode < median 
   [B] mean = median 
   [C] mean < mode 
   [D] mode = median

45. Determine the area, in square feet, of the smallest square that can contain a circle with a radius of 8 feet.
46. An image of a building in a photograph is 6 centimeters wide and 11 centimeters tall. If the image is similar to the actual building and the actual building is 174 meters wide, how tall is the actual building, in meters?

47. The solution set for the equation 
\[ x^2 - 2x - 15 = 0 \] 
is
[A] \{5,3\}  [B] \{-5,-3\}  
[C] \{-5,3\}  [D] \{5,-3\}

48. Expressed in simplest radical form, the product of \( \sqrt{6} \cdot \sqrt{15} \) is
[A] \( 9\sqrt{10} \)  [B] \( \sqrt{90} \)  
[C] \( 3\sqrt{15} \)  [D] \( 3\sqrt{10} \)

49. Which set is closed under division?
[A] integers  [B] whole numbers 
[C] counting numbers  [D] \{1\}

50. If 0.0347 is written by a scientist in the form \(3.47 \times 10^n\), the value of \(n\) is

52. In the accompanying diagram of \(\triangle BCD\), \(\triangle ABC\) is an equilateral triangle and \(AD = AB\). What is the value of \(x\), in degrees?

53. If \(a\) and \(b\) are both odd integers, which expression must always equal an odd integer?
[A] \(a - b\)  [B] \(\frac{a}{b}\)  
[C] \(a + b\)  [D] \(a \cdot b\)

54. If the lengths of two sides of a triangle are 4 and 10, what could be the length of the third side?

55. On the accompanying diagram of \(\triangle ABC\), use a compass and a straightedge to construct a median from \(A\) to \(\overline{BC}\).
56. What is the inverse of the statement "If Mike did his homework, then he will pass this test"?

[A] If Mike does not pass this test, then he only did half his homework.

[B] If Mike does not pass this test, then he did not do his homework.

[C] If Mike passes this test, then he did his homework.

[D] If Mike did not do his homework, then he will not pass this test.

57. The multiplicative inverse of $-\frac{1}{3}$ is

[A] $-\frac{1}{3}$  
[B] 3 
[C] $\frac{1}{3}$ 
[D] -3

58. Which line is perpendicular to the line whose equation is $5y + 6 = -3x$?

[A] $y = \frac{3}{5}x + 7$ 
[B] $y = -\frac{3}{5}x + 7$

[C] $y = \frac{5}{3}x + 7$ 
[D] $y = \frac{5}{3}x + 7$

59. The midpoint of $AB$ is $(-1,5)$ and the coordinates of point $A$ are $(-3,2)$. What are the coordinates of point $B$?

[A] (-5,8) 
[B] (0,7)

[C] (1,8) 
[D] (1,10)

60. Determine the distance between point $A(-1,-3)$ and point $B(5,5)$. Write an equation of the perpendicular bisector of $AB$. [The use of the accompanying grid is optional.]

61. A farmer has a rectangular field that measures 100 feet by 150 feet. He plans to increase the area of the field by 20%. He will do this by increasing the length and width by the same amount, $x$. Which equation represents the area of the new field?

[A] $2(100+x) + 2(150+x) = 15,000$

[B] $(100 + 2x)(150 + x) = 18,000$

[C] $(100 + x)(150 + x) = 18,000$

[D] $(100 + x)(150 + x) = 15,000$

62. A cake recipe calls for 1.5 cups of milk and 3 cups of flour. Seth made a mistake and used 5 cups of flour. How many cups of milk should he use to keep the proportions correct?

[A] 1.75 
[B] 2.5 
[C] 2 
[D] 2.25
63. Sal has a small bag of candy containing three green candies and two red candies. While waiting for the bus, he ate two candies out of the bag, one after another, without looking. What is the probability that both candies were the same color?

64. If \( a + b \) is less than \( c + d \), and \( d + e \) is less than \( a + b \), then \( e \) is

[A] less than \( d \)  [B] less than \( c \)
[C] equal to \( c \)  [D] greater than \( d \)

65. If \( x = 4 \) and \( y = -2 \), the value of \( \frac{1}{2} x y^2 \) is


66. On the accompanying set of axes, graph \( \triangle ABC \) with coordinates \( A(-1,2) \), \( B(0,6) \), and \( C(5,4) \). Then graph \( \triangle ABC' \), the image of \( \triangle ABC \) after a dilation of 2.

67. If \( -2x + 3 = 7 \) and \( 3x + 1 = 5 + y \), the value of \( y \) is

[A] -10  [B] 1  [C] 10  [D] 0

68. The angle of elevation from a point 25 feet from the base of a tree on level ground to the top of the tree is 30°. Which equation can be used to find the height of the tree?

[A] \( \tan 30^\circ = \frac{x}{25} \)  [B] \( 30^2 + 25^2 = x^2 \)
[C] \( \cos 30^\circ = \frac{x}{25} \)  [D] \( \sin 30^\circ = \frac{x}{25} \)

69. What is the slope of line \( \ell \) shown in the accompanying diagram?

[A] -\( \frac{4}{3} \)  [B] \( \frac{3}{4} \)  [C] -\( \frac{3}{4} \)  [D] \( \frac{4}{3} \)

70. The graphs of the equations \( y = x^2 + 4x - 1 \) and \( y + 3 = x \) are drawn on the same set of axes. At which point do the graphs intersect?

[A] (1, 4)  [B] (1, -2)
[C] (-2, -5)  [D] (-2, 1)
71. A rocket car on the Bonneville Salt Flats is traveling at a rate of 640 miles per hour. How much time would it take for the car to travel 384 miles at this rate?  
[A] 245 minutes  [B] 36 minutes  
[C] 256 minutes  [D] 1.7 hours

72. The following data consists of the weights, in pounds, of 30 adults:  
Using the data, complete the accompanying cumulative frequency table and construct a cumulative frequency histogram on the grid below.

<table>
<thead>
<tr>
<th>Interval</th>
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<tr>
<td>51–100</td>
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<td>101–150</td>
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<td>151–200</td>
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<td>201–250</td>
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73. A company manufactures bicycles and skateboards. The company's daily production of bicycles cannot exceed 10, and its daily production of skateboards must be less than or equal to 12. The combined number of bicycles and skateboards cannot be more than 16. If \( x \) is the number of bicycles and \( y \) is the number of skateboards, graph on the accompanying set of axes the region that contains the number of bicycles and skateboards the company can manufacture daily.

74. In Ms. Wright's English class, 16 students are in band, 7 students play sports, 3 students participate in both activities, and 9 students are not in band and do not play sports. How many students are in Ms. Wright's English class?  

75. The profits in a business are to be shared by the three partners in the ratio of 3 to 2 to 5. The profit for the year was $176,500. Determine the number of dollars each partner is to receive.
76. What is the sum, in degrees, of the measures of the interior angles of a pentagon?


77. In the accompanying diagram, triangle \(A\) is similar to triangle \(B\). Find the value of \(n\).

78. Which expression represents the product of two consecutive odd integers, where \(n\) is an odd integer?

[A] \(n(n + 2)\)  [B] \(n(n + 3)\)  
[C] \(n(n + 1)\)  [D] \(2n + 1\)

79. Manuel plans to install a fence around the perimeter of his yard. His yard is shaped like a square and has an area of 40,000 square feet. The company that he hires charges $2.50 per foot for the fencing and $50.00 for the installation fee. What will be the cost of the fence, in dollars?

80. Tamika has a hard rubber ball whose circumference measures 13 inches. She wants to box it for a gift but can only find cube-shaped boxes of sides 3 inches, 4 inches, 5 inches, or 6 inches. What is the smallest box that the ball will fit into with the top on?

81. Triangle \(ABC\) has coordinates \(A(2,0), B(1,7),\) and \(C(5,1)\). On the accompanying set of axes, graph, label, and state the coordinates of \(\triangle A'B'C'\), the reflection of \(\triangle ABC\) in the \(y\)-axis.

82. A deli has five types of meat, two types of cheese, and three types of bread. How many different sandwiches, consisting of one type of meat, one type of cheese, and one type of bread, does the deli serve?


83. Which graph represents the solution set for \(2x - 4 \leq 8\) and \(x + 5 \geq 7\)?

[A]  
[B]  
[C]  
[D]  
84. Which set could not represent the lengths of the sides of a triangle?

[A] \{3,4,5\} \quad [B] \{5,10,12\}  
[C] \{7,9,11\} \quad [D] \{2,5,9\}

85. Bob and Ray are describing the same number. Bob says, "The number is a positive even integer less than or equal to 20." Ray says, "The number is divisible by 4." If Bob's statement is true and Ray's statement is false, what are all the possible numbers?

86. Which is an irrational number?

[A] \sqrt{49} \quad [B] \frac{3}{8} \quad [C] 0.\overline{3} \quad [D] \pi

87. What is the image of \((x, y)\) after a translation of 3 units right and 7 units down?

[A] \((x - 3, y + 7)\) \quad [B] \((x + 3, y + 7)\)  
[C] \((x + 3, y - 7)\) \quad [D] \((x - 3, y - 7)\)

88. A box in the shape of a cube has a volume of 64 cubic inches. What is the length of a side of the box?

[A] 8 \text{ in} \quad [B] 4 \text{ in}  
[C] 16 \text{ in} \quad [D] 21.3 \text{ in}

89. A student council has seven officers, of which five are girls and two are boys. If two officers are chosen at random to attend a meeting with the principal, what is the probability that the first officer chosen is a girl and the second is a boy?

[A] \frac{2}{7} \quad [B] \frac{7}{14} \quad [C] \frac{7}{13} \quad [D] \frac{10}{42}

90. Expressed in factored form, the binomial \(4a^2 - 9b^2\) is equivalent to

[A] \((2a + 3b)(2a - 3b)\) \quad [B] \((4a - 3b)(a + 3b)\)  
[C] \((2a - 3b)(2a - 3b)\) \quad [D] \((2a - 9b)(2a + b)\)

91. Maria's backyard has two trees that are 40 feet apart, as shown in the accompanying diagram. She wants to place lampposts so that the posts are 30 feet from both of the trees. Draw a sketch to show where the lampposts could be placed in relation to the trees. How many locations for the lampposts are possible?

92. A boy got 50% of the questions on a test correct. If he had 10 questions correct out of the first 12, and \(\frac{1}{4}\) of the remaining questions correct, how many questions were on the test?

[A] 28 \quad [B] 26 \quad [C] 16 \quad [D] 24
93. The second side of a triangle is two more than the first side, and the third side is three less than the first side. Which expression represents the perimeter of the triangle?

[A] $x^2 - x - 6$  
[B] $3x - 1$  
[C] $x + 5$  
[D] $2x - 1$

94. If one-half of a number is 8 less than two-thirds of the number, what is the number?

[A] 48  
[B] 24  
[C] 54  
[D] 32

95. If the measure of an angle is represented by $2x$, which expression represents the measure of its complement?

[A] $180 - 2x$  
[B] $90 + 2x$  
[C] $90 - 2x$  
[D] $88x$

96. For five algebra examinations, Maria has an average of 88. What must she score on the sixth test to bring her average up to exactly 90?

[A] 94  
[B] 100  
[C] 98  
[D] 92

97. In order to be admitted for a certain ride at an amusement park, a child must be greater than or equal to 36 inches tall and less than 48 inches tall. Which graph represents these conditions?

[A]  
[B]  
[C]  
[D]  

98. A candy store sells 8-pound bags of mixed hazelnuts and cashews. If $c$ pounds of cashews are in a bag, the price $p$ of the bag can be found using the formula $p = 2.59c + 1.72(8 - c)$. If one bag is priced at $18.11, how many pounds of cashews does it contain?

99. In the next Olympics, the United States can enter four athletes in the diving competition. How many different teams of four divers can be selected from a group of nine divers?

[A] 126  
[B] 6,561  
[C] 3,024  
[D] 36

100. A group of 148 people is spending five days at a summer camp. The cook ordered 12 pounds of food for each adult and 9 pounds of food for each child. A total of 1,410 pounds of food was ordered.

a) Write an equation or a system of equations that describes the above situation and define your variables.

b) Using your work from part a), find:
   (1) the total number of adults in the group
   (2) the total number of children in the group

101. The sum of $\frac{3}{x} + \frac{2}{5}$, $x \neq 0$, is

[A] $\frac{5}{x+5}$  
[B] $\frac{1}{x}$  
[C] $\frac{2x+15}{5x}$  
[D] $\frac{2x+15}{x+5}$

102. If $x + y = 9x + y$, then $x$ is equal to

[A] $y$  
[B] $\frac{1}{5}y$  
[C] 0  
[D] 8
103. The coordinates of the endpoints of $\overline{AB}$ are $A(0,2)$ and $B(4,6)$. Graph and state the coordinates of $A'$ and $B'$, the images of $A$ and $B$ after $\overline{AB}$ is reflected in the $x$-axis.

104. If $2m + 2p = 16$, $p$ equals

[A] $8 - m$  
[B] $16 + 2m$  
[C] $16 - m$  
[D] $9m$

105. A committee of five members is to be randomly selected from a group of nine freshmen and seven sophomores. Which expression represents the number of different committees of three freshmen and two sophomores that can be chosen?

[A] $_9C_3 \cdot _7C_2$  
[B] $_9C_3 + _7C_2$  
[C] $_9C_3 \cdot _7C_2$  
[D] $_9P_3 \cdot _7P_2$

106. Tina wants to sew a piece of fabric into a scarf in the shape of an isosceles triangle, as shown in the accompanying diagram.

What are the values of $x$ and $y$?

[A] $x = 69$ and $y = 69$  
[B] $x = 96$ and $y = 42$  
[C] $x = 42$ and $y = 96$  
[D] $x = 90$ and $y = 48$

107. The value of $\frac{7!}{3!}$ is

[A] 24  
[B] 4  
[C] 840  
[D] 7

108. What is the value of $p$ in the equation $2(3p - 4) = 10$?

[A] $\frac{1}{3}$  
[B] $2 \frac{1}{3}$  
[C] 3  
[D] 1

109. Which expression must be added to $3x - 7$ to equal 0?

[A] $-3x - 7$  
[B] $-3x + 7$  
[C] 0  
[D] $3x + 7$

110. If $t = -3$, then $3t^2 + 5t + 6$ equals

[A] -36  
[B] -6  
[C] 6  
[D] 18
111. Which value is equivalent to $_3P_3$?

112. Alexandra purchases two doughnuts and three cookies at a doughnut shop and is charged $3.30. Briana purchases five doughnuts and two cookies at the same shop for $4.95. All the doughnuts have the same price and all the cookies have the same price. Find the cost of one doughnut and find the cost of one cookie.

113. In the accompanying diagram, the base of a 15-foot ladder rests on the ground 4 feet from a 6-foot fence.

   a If the ladder touches the top of the fence and the side of a building, what angle, to the nearest degree, does the ladder make with the ground?
   b Using the angle found in part a, determine how far the top of the ladder reaches up the side of the building, to the nearest foot.

114. The expression $(x - 6)^2$ is equivalent to
   [A] $x^2 + 12x + 36$    [B] $x^2 - 12x + 36$
   [C] $x^2 + 36$    [D] $x^2 - 36$

115. If the midpoints of the sides of a triangle are connected, the area of the triangle formed is what part of the area of the original triangle?
   [A] $\frac{1}{4}$    [B] $\frac{3}{8}$    [C] $\frac{1}{3}$    [D] $\frac{1}{2}$

116. The party registration of the voters in Jonesville is shown in the table below.

<table>
<thead>
<tr>
<th>Party Registration</th>
<th>Number of Voters Registered</th>
</tr>
</thead>
<tbody>
<tr>
<td>Democrat</td>
<td>6,000</td>
</tr>
<tr>
<td>Republican</td>
<td>5,300</td>
</tr>
<tr>
<td>Independent</td>
<td>3,700</td>
</tr>
</tbody>
</table>

   If one of the registered Jonesville voters is selected at random, what is the probability that the person selected is not a Democrat?
   [A] 0.400    [B] 0.333    [C] 0.667    [D] 0.600

117. Which statement is the inverse of "If the waves are small, I do not go surfing"?
   [A] If the waves are not small, I do not go surfing.
   [B] If I go surfing, the waves are not small.
   [C] If the waves are not small, I go surfing.
   [D] If I do not go surfing, the waves are small.
118. Which equation could represent the relationship between the $x$ and $y$ values shown in the accompanying table?

<table>
<thead>
<tr>
<th>$x$</th>
<th>$y$</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>2</td>
</tr>
<tr>
<td>1</td>
<td>3</td>
</tr>
<tr>
<td>2</td>
<td>6</td>
</tr>
<tr>
<td>3</td>
<td>11</td>
</tr>
<tr>
<td>4</td>
<td>18</td>
</tr>
</tbody>
</table>

[A] $y = x^2$  [B] $y = x^2 + 2$
[C] $y = x + 2$  [D] $y = 2^x$

119. In the accompanying diagram of right triangle $ABC$, $AB = 8$, $BC = 15$, $AC = 17$, and $m \angle ABC = 90$. What is $\tan \angle C$?

[A] $\frac{8}{15}$  [B] $\frac{17}{15}$  [C] $\frac{8}{17}$  [D] $\frac{15}{17}$

120. Sara's telephone service costs $21 per month plus $0.25 for each local call, and long-distance calls are extra. Last month, Sara's bill was $36.64, and it included $6.14 in long-distance charges. How many local calls did she make?

121. Construct a stem-and-leaf plot listing the scores below in order from lowest to highest. 15, 25, 28, 32, 39, 40, 43, 26, 50, 75, 65, 19, 55, 72, 50

122. Which properties best describe the coordinate graph of two distinct parallel lines?

[A] same slopes and different intercepts  [B] different slopes and different intercepts
[C] different slopes and same intercepts  [D] same slopes and same intercepts

123. Which is a rational number?

[A] $6\sqrt{2}$  [B] $\pi$  [C] $\sqrt{8}$  [D] $5\sqrt{9}$
124. If Laquisha can enter school by any one of three doors and the school has two staircases to the second floor, in how many different ways can Laquisha reach a room on the second floor? Justify your answer by drawing a tree diagram or listing a sample space.

125. Katrina hikes 5 miles north, 7 miles east, and then 3 miles north again. To the nearest tenth of a mile, how far, in a straight line, is Katrina from her starting point?

126. In the accompanying diagram, lines $a$ and $b$ are parallel, and lines $c$ and $d$ are transversals.

Which angle is congruent to angle 8?
[A] 6  [B] 5  [C] 3  [D] 4

127. Robin has 8 blouses, 6 skirts, and 5 scarves. Which expression can be used to calculate the number of different outfits she can choose, if an outfit consists of a blouse, a skirt, and a scarf?
[A] $8 \cdot 6 \cdot 5$  [B] $8 + 6 + 5$
[C] $8!6!5!$  [D] $\binom{19}{3}$

128. In the accompanying diagram of equilateral triangle $ABC$, $DE = 5$ and $\overline{DE} \parallel \overline{AB}$.

If $AB$ is three times as long as $DE$, what is the perimeter of quadrilateral $ABED$?

129. A translation moves $P(3,5)$ to $P'(6,1)$. What are the coordinates of the image of point $(-3,-5)$ under the same translation?
[A] (0,-9)  [B] (-6,-1)  [C] (-5,-3)  [D] (-6,-9)

130. The set of integers $\{3,4,5\}$ is a Pythagorean triple. Another such set is
[A] $\{6,7,8\}$  [B] $\{6,8,12\}$
[C] $\{8,15,17\}$  [D] $\{6,12,13\}$

131. How many different three-member teams can be formed from six students?
132. There are 28 students in a mathematics class. If \( \frac{1}{4} \) of the students are called to the guidance office, \( \frac{1}{3} \) of the remaining students are called to the nurse, and, finally, \( \frac{1}{2} \) of those left go to the library, how many students remain in the classroom?

133. Which piece of paper can be folded into a pyramid?

[A]  
[B]  
[C]  
[D]  

134. The perimeter of an equilateral triangle varies directly as the length of a side. When the length of a side is doubled, the perimeter of the triangle is

[A] doubled  
[B] multiplied by 3  
[C] divided by 3  
[D] halved

135. If the number represented by \( n-3 \) is an odd integer, which expression represents the next greater odd integer?

[A] \( n - 2 \)  
[B] \( n + 1 \)  
[C] \( n - 1 \)  
[D] \( n - 5 \)

136. Amy tossed a ball in the air in such a way that the path of the ball was modeled by the equation \( y = -x^2 + 6x \). In the equation, \( y \) represents the height of the ball in feet and \( x \) is the time in seconds.

a) Graph \( y = -x^2 + 6x \) for \( 0 \leq x \leq 6 \) on the grid provided below.

b) At what time, \( x \), is the ball at its highest point?

137. Given: \( \frac{\sqrt{99}}{11}, \sqrt{164}, \sqrt{196} \)

Identify the expression that is a rational number and explain why it is rational.

138. What is the product of \( \frac{1}{3}x^2y \) and \( \frac{1}{6}xy^3 \)?

[A] \( \frac{1}{9}x^3y^4 \)  
[B] \( \frac{1}{18}x^3y^4 \)  
[C] \( \frac{1}{18}x^2y^3 \)  
[D] \( \frac{1}{2}x^2y^3 \)
139. Jerry and Jean Jogger start at the same time from point A shown on the accompanying set of axes. Jerry jogs at a rate of 5 miles per hour traveling from point A to point R to point S and then to point C. Jean jogs directly from point A to point C on $\overline{AC}$ at the rate of 3 miles per hour. Which jogger reaches point C first? Explain or show your reasoning.

140. The accompanying diagram shows two similar triangles.

Which proportion could be used to solve for $x$?

[A] $\frac{32}{12} = \frac{15}{x}$  
[B] $\frac{32}{x} = \frac{12}{15}$  
[C] $\frac{24}{9} = \frac{15}{x}$  
[D] $\frac{x}{24} = \frac{9}{15}$

141. The coordinates of $A$ are (-9, 2) and the coordinates of $G$ are (3, 14). What are the coordinates of the midpoint of $\overline{AG}$?

[A] (-3, 8)  
[B] (-21, -10)  
[C] (-6, 16)  
[D] (-6, 6)

142. The mass of an orchid seed is approximately 0.0000035 gram. Written in scientific notation, that mass is equivalent to $3.5 \times 10^n$. What is the value of $n$?

[A] -5  
[B] -7  
[C] -8  
[D] -6

143. Which equation illustrates the associative property of addition?

[A] $3 + x = 0$  
[B] $x + y = y + x$  
[C] $(3 + x) + y = 3 + (x + y)$  
[D] $3(x + 2) = 3x + 6$

144. The accompanying diagram shows a transformation.

Which transformation performed on figure 1 resulted in figure 2?

[A] dilation  
[B] reflection  
[C] rotation  
[D] translation
145. In the accompanying diagram, line $m$ is parallel to line $p$, line $t$ is a transversal, $m \angle a = 3x + 12$, and $m \angle b = 2x + 13$. Find the value of $x$.

![Diagram](image)

146. Deborah built a box by cutting 3-inch squares from the corners of a rectangular sheet of cardboard, as shown in the accompanying diagram, and then folding the sides up. The volume of the box is 150 cubic inches, and the longer side of the box is 5 inches more than the shorter side. Find the number of inches in the shorter side of the original sheet of cardboard.

![Diagram](image)

147. If a girl 1.2 meters tall casts a shadow 2 meters long, how many meters tall is a tree that casts a shadow 75 meters long at the same time?

148. The expression $\frac{5x}{6} + \frac{x}{4}$ is equivalent to

[A] $\frac{13x}{12}$  
[B] $\frac{5x}{24}$  
[C] $\frac{5x^2}{10}$  
[D] $\frac{3x}{5}$

149. On an English examination, two students received scores of 90, five students received 85, seven students received 75, and one student received 55. The average score on this examination was

[A] 77  
[B] 76  
[C] 79  
[D] 75

150. The accompanying diagram is an example of which type of graph?

[A] histogram  
[B] box-and-whisker plot  
[C] stem-and-leaf plot  
[D] bar graph

151. The expression $\frac{5x^6 y^2}{x^8 y}$ is equivalent to

[A] $\frac{5y}{x^2}$  
[B] $\frac{5y^3}{x^{14}}$  
[C] $5x^{14} y^3$  
[D] $5x^2 y$
152. Sean knows the length of the base, $b$, and the area, $A$, of a triangular window in his bedroom. Which formula could he use to find the height, $h$, of this window?

$\text{[A]} \ h = (2A)(b) \quad \text{[B]} \ h = \frac{A}{2b} \quad \text{[C]} \ h = 2A - b \quad \text{[D]} \ h = \frac{2A}{b}$

153. Which statement is logically equivalent to "If I eat, then I live"?

$\text{[A]}$ I live if and only if I eat.

$\text{[B]}$ If I eat, then I do not live.

$\text{[C]}$ If I live, then I eat.

$\text{[D]}$ If I do not live, then I do not eat.

154. The sum of Scott's age and Greg's age is 33 years. If Greg's age is represented by $g$, Scott's age is represented by

$\text{[A]} \ g + 33 \quad \text{[B]} \ 33g \quad \text{[C]} \ g - 33 \quad \text{[D]} \ 33 - g$

155. The telephone company has run out of seven-digit telephone numbers for an area code. To fix this problem, the telephone company will introduce a new area code. Find the number of new seven-digit telephone numbers that will be generated for the new area code if both of the following conditions must be met:

- The first digit cannot be a zero or a one.
- The first three digits cannot be the emergency number (911) or the number used for information (411).

156. The accompanying diagram shows a square dartboard. The side of the dartboard measures 30 inches. The square shaded region at the center has a side that measures 10 inches. If darts thrown at the board are equally likely to land anywhere on the board, what is the theoretical probability that a dart does not land in the shaded region?

157. The transformation of $\triangle ABC$ to $\triangle AB'C'$ is shown in the accompanying diagram.

$\text{[A]}$ translation  \quad \text{[B]}$ dilation

$\text{[C]}$ line reflection in line $\ell$  \quad \text{[D]}$ rotation about point $A$

158. The product of $3x^2y$ and $-4xy^3$ is

$\text{[A]} \ -12x^2y^3 \quad \text{[B]} \ 12x^2y^3$

$\text{[C]} \ 12x^3y^4 \quad \text{[D]} \ -12x^3y^4$
159. Which statement is expressed as a biconditional?

[A] If two angles are both right angles, then they are congruent.

[B] Two angles are congruent if they have the same measure.

[C] Two angles are congruent if and only if they have the same measure.

[D] If two angles are congruent, then they are both right angles.

160. Jorge made the accompanying stem-and-leaf plot of the weights, in pounds, of each member of the wrestling team he was coaching.

<table>
<thead>
<tr>
<th>Stem</th>
<th>Leaf</th>
</tr>
</thead>
<tbody>
<tr>
<td>10</td>
<td>9</td>
</tr>
<tr>
<td>11</td>
<td></td>
</tr>
<tr>
<td>12</td>
<td>3 8</td>
</tr>
<tr>
<td>13</td>
<td>2 4 4 6 8</td>
</tr>
<tr>
<td>14</td>
<td>1 3 5 5 9</td>
</tr>
<tr>
<td>15</td>
<td>2 3 7 7 9</td>
</tr>
<tr>
<td>16</td>
<td>1 3 7 8 8 8 9</td>
</tr>
<tr>
<td>17</td>
<td>8 8</td>
</tr>
</tbody>
</table>

[Key: 16 1 = 161]

What is the mode of the weights?


161. Linda paid $48 for a jacket that was on sale for 25% of the original price. What was the original price of the jacket?


162. Point \((k, -3)\) lies on the line whose equation is \(x - 2y = -2\). What is the value of \(k\)?

[A] 6  [B] -6  [C] 8  [D] -8

163. Which list is in order from smallest value to largest value?

[A] \(\sqrt{10}, \frac{22}{7}, \pi, 3.1\)  [B] \(\pi, \frac{22}{7}, 3.1, \sqrt{10}\)

[C] \(3.1, \pi, \frac{22}{7}, \sqrt{10}\)  [D] \(3.1, \frac{22}{7}, \pi, \sqrt{10}\)

164. If \(2x^2 - x + 6\) is subtracted from \(x^2 + 3x - 2\), the result is

[A] \(x^2 - 4x + 8\)  [B] \(-x^2 + 4x - 8\)

[C] \(-x^2 + 2x - 8\)  [D] \(x^2 + 2x - 8\)

165. The test scores for 10 students in Ms. Sampson's homeroom were 61, 67, 81, 83, 87, 88, 89, 90, 98, and 100. Which frequency table is accurate for this set of data?

[A]  

<table>
<thead>
<tr>
<th>Interval</th>
<th>Frequency</th>
</tr>
</thead>
<tbody>
<tr>
<td>61–70</td>
<td>2</td>
</tr>
<tr>
<td>71–80</td>
<td>2</td>
</tr>
<tr>
<td>81–90</td>
<td>7</td>
</tr>
<tr>
<td>91–100</td>
<td>10</td>
</tr>
</tbody>
</table>

[B]  

<table>
<thead>
<tr>
<th>Interval</th>
<th>Frequency</th>
</tr>
</thead>
<tbody>
<tr>
<td>61–70</td>
<td>2</td>
</tr>
<tr>
<td>71–80</td>
<td>0</td>
</tr>
<tr>
<td>81–90</td>
<td>8</td>
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<td>91–100</td>
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</table>

[C]  

<table>
<thead>
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<th>Interval</th>
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<td>71–80</td>
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[D]  

<table>
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<tr>
<td>71–80</td>
<td>0</td>
</tr>
<tr>
<td>81–90</td>
<td>6</td>
</tr>
<tr>
<td>91–100</td>
<td>2</td>
</tr>
</tbody>
</table>
166. Which graph best represents the solution set for the inequality \( x > \sqrt{2} \)?

[A] 

[B] 

[C] 

[D] 

167. The accompanying diagram shows a square with side \( y \) inside a square with side \( x \).

Which expression represents the area of the shaded region?

[A] \( y^2 - x^2 \) 

[B] \( x^2 - y^2 \) 

[C] \( x^2 \) 

[D] \( y^2 \) 

168. Solve for \( m \): \( 0.6m + 3 = 2m + 0.2 \) 

169. If \( bx - 2 = K \), then \( x \) equals

[A] \( \frac{K+2}{b} \) 

[B] \( \frac{K-2}{b} \) 

[C] \( \frac{K}{b} + 2 \) 

[D] \( \frac{2-K}{b} \) 

170. How many different three-member teams can be selected from a group of seven students?

[A] 210  

[B] 35  

[C] 5,040  

[D] 1 

171. Which ordered pair is in the solution set of the system of inequalities shown in the accompanying graph?

[A] (3,2)  

[B] (0,1)  

[C] (0,0)  

[D] (1,5) 

172. What is the sum, in degrees, of the measures of the interior angles of a stop sign, which is in the shape of an octagon?

[A] 1,440  

[B] 1,080  

[C] 1,880  

[D] 360
173. Which expression represents "5 less than the product of 7 and \(x\)?"

[A] \(7x - 5\) 
[B] \(5 - 7x\) 
[C] \(7 + x - 5\) 
[D] \(7(x - 5)\)

174. A triangular park is formed by the intersection of three streets, Bridge Street, Harbor Place, and College Avenue, as shown in the accompanying diagram. A walkway parallel to Harbor Place goes through the park. A time capsule has been buried in the park in a location that is equidistant from Bridge Street and College Avenue and 5 yards from the walkway. Indicate on the diagram with an \(\times\) each possible location where the time capsule could be buried.

175. Juan has a cellular phone that costs $12.95 per month plus 25¢ per minute for each call. Tiffany has a cellular phone that costs $14.95 per month plus 15¢ per minute for each call. For what number of minutes do the two plans cost the same?

176. On a map, 1 centimeter represents 40 kilometers. How many kilometers are represented by 8 centimeters?

[A] 5 
[B] 48 
[C] 280 
[D] 320

177. Tamika could not remember her scores from five mathematics tests. She did remember that the mean (average) was exactly 80, the median was 81, and the mode was 88. If all her scores were integers with 100 the highest score possible and 0 the lowest score possible, what was the lowest score she could have received on any one test?

178. What is the solution of the equation \(3y - 5y + 10 = 36\)?

[A] 13 
[B] 4.5 
[C] 2 
[D] -13

179. When Kimberly bought her new car, she found that there were 72 different ways her car could be equipped. Her choices included four choices of engine and three choices of transmission. If her only other choice was color, how many choices of color did she have?

[A] 65 
[B] 60 
[C] 12 
[D] 6

180. A hockey team played \(n\) games, losing four of them and winning the rest. The ratio of games won to games lost is

[A] \(\frac{n}{4}\) 
[B] \(\frac{4}{n}\) 
[C] \(\frac{n-4}{4}\) 
[D] \(\frac{4}{n-4}\)

181. Rosario and Enrique are in the same mathematics class. On the first five tests, Rosario received scores of 78, 77, 64, 86, and 70. Enrique received scores of 90, 61, 79, 73, and 87. How much higher was Enrique's average than Rosario's average?

[A] 2 points 
[B] 15 points 
[C] 3 points 
[D] 4 points
182. Dan is sketching a map of the location of his house and his friend Matthew's house on a set of coordinate axes. Dan locates his house at point $D(0,0)$ and locates Matthew's house, which is 6 miles east of Dan's house, at point $M(6,0)$. On the accompanying set of coordinate axes, graph the locus of points equidistant from the two houses. Then write the equation of the locus.

183. What is the value of $y$ in the following system of equations?

\[
\begin{align*}
2x + 3y &= 6 \\
2x + y &= -2
\end{align*}
\]

[A] 4 [B] 2 [C] -3 [D] 1

184. The tickets for a dance recital cost $5.00 for adults and $2.00 for children. If the total number of tickets sold was 295 and the total amount collected was $1,220, how many adult tickets were sold? [Only an algebraic solution can receive full credit.]

185. Given the statement: "If $x$ is a rational number, then $\sqrt{x}$ is irrational." Which value of $x$ makes the statement false?

[A] 3 [B] 2 [C] $\frac{3}{2}$ [D] 4

186. The accompanying diagram shows the roof of a house that is in the shape of an isosceles triangle. The vertex angle formed at the peak of the roof is $84^\circ$.

What is the measure of $x$?

[A] $48^\circ$ [B] $138^\circ$ [C] $96^\circ$ [D] $84^\circ$

187. What is the converse of the statement "If Alicia goes to Albany, then Ben goes to Buffalo"?

[A] Alicia goes to Albany if and only if Ben goes to Buffalo.
[B] If Alicia does not go to Albany, then Ben does not go to Buffalo.
[C] If Ben goes to Buffalo, then Alicia goes to Albany.
[D] If Ben does not go to Buffalo, then Alicia does not go to Albany.
188. Mr. Petri has a rectangular plot of land with length = 20 feet and width = 10 feet. He wants to design a flower garden in the shape of a circle with two semicircles at each end of the center circle, as shown in the accompanying diagram. He will fill in the shaded area with wood chips. If one bag of wood chips covers 5 square feet, how many bags must he buy?

189. Sarah's mathematics grades for one marking period were 85, 72, 97, 81, 77, 93, 100, 75, 86, 70, 96, and 80.
   a Complete the tally sheet and frequency table below, and construct and label a frequency histogram for Sarah's grades using the accompanying grid.
   b Which interval contains the 75th percentile (upper quartile)?

<table>
<thead>
<tr>
<th>Interval (grades)</th>
<th>Tally</th>
<th>Frequency</th>
</tr>
</thead>
<tbody>
<tr>
<td>61–70</td>
<td></td>
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<td>71–80</td>
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<td></td>
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<tr>
<td>91–100</td>
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<td></td>
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</tbody>
</table>

190. On the set of axes provided below, sketch a circle with a radius of 3 and center at (2,1) and also sketch the graph of the line $2x + y = 8$.

191. Five people have volunteered to work on an awards dinner at Madison High School. How many different committees of four can be formed from the five people?
   [A] 10   [B] 5   [C] 20   [D] 1

192. A person measures the angle of depression from the top of a wall to a point on the ground. The point is located on level ground 62 feet from the base of the wall and the angle of depression is $52^\circ$. How high is the wall, to the nearest tenth of a foot?
193. How many different five-member teams can be made from a group of eight students, if each student has an equal chance of being chosen?


194. In a school building, there are 10 doors that can be used to enter the building and 8 stairways to the second floor. How many different routes are there from outside the building to a class on the second floor?


195. What is the \(y\)-intercept of the graph of the line whose equation is \(y = -\frac{2}{5}x + 4\)?

[A] \(-\frac{2}{5}\)  [B] 0  [C] \(-\frac{5}{2}\)  [D] 4

196. The Excel Cable Company has a monthly fee of $32.00 and an additional charge of $8.00 for each premium channel. The Best Cable Company has a monthly fee of $26.00 and additional charge of $10.00 for each premium channel. The Horton family is deciding which of these two cable companies to subscribe to.

a. For what number of premium channels will the total monthly subscription fee for the Excel and Best Cable companies be the same?
b. The Horton family decides to subscribe to 2 premium channels for a period of one year.
   1) Which cable company should they subscribe to in order to spend less money?
   2) How much money will the Hortons save in one year by using the less expensive company?

197. The base of an isosceles triangle is 5 and its perimeter is 11. The base of a similar isosceles triangle is 10. What is the perimeter of the larger triangle?


198. Shanaya graphed the line represented by the equation \(y = x - 6\).

Write an equation for a line that is parallel to the given line.
Write an equation for a line that is perpendicular to the given line.
Write an equation for a line that is identical to the given line but has different coefficients.

199. The senior class is sponsoring a dance. The cost of a student disk jockey is $40, and tickets sell for $2 each. Write a linear equation and, on the accompanying grid, graph the equation to represent the relationship between the number of tickets sold and the profit from the dance. Then find how many tickets must be sold to break even.

200. The expression \(2^3 \cdot 4^2\) is equivalent to

[A] 8^6  [B] 2^{12}  [C] 2^7  [D] 8^5
201. A total of 600 tickets were sold for a concert. Twice as many tickets were sold in advance than were sold at the door. If the tickets sold in advance cost $25 each and the tickets sold at the door cost $32 each, how much money was collected for the concert?

202. The formula \( C = \frac{5}{9}(F - 32) \) is used to convert Fahrenheit temperature, \( F \), to Celsius temperature, \( C \). What temperature, in degrees Fahrenheit, is equivalent to a temperature of 10° Celsius?

203. Simplify: \( \frac{9x^2 - 15xy}{9x^2 - 25y^2} \)

204. A certain state is considering changing the arrangement of letters and numbers on its license plates. The two options the state is considering are:
Option 1: three letters followed by a four-digit number with repetition of both letters and digits allowed
Option 2: four letters followed by a three-digit number without repetition of either letters or digits
[Zero may be chosen as the first digit of the number in either option.]
Which option will enable the state to issue more license plates? How many more different license plates will that option yield?

205. Which letter has point symmetry, but not line symmetry?

206. Which ratio represents \( \cos A \) in the accompanying diagram of \( \triangle ABC \)?

207. Shoe sizes and foot length are related by the formula \( S = 3F - 24 \), where \( S \) represents the shoe size and \( F \) represents the length of the foot, in inches.
\( a \) Solve the formula for \( F \).
\( b \) To the nearest tenth of an inch, how long is the foot of a person who wears a size 10 \( \frac{1}{2} \) shoe?

208. The expression \( 8^{-4} \cdot 8^{6} \) is equivalent to
[A] \( 8^{10} \)  [B] \( 8^{2} \)  [C] \( 8^{-2} \)  [D] \( 8^{-24} \)

209. In the accompanying diagram of parallelogram \( ABCD \), \( m\angle A = (2x + 10) \) and \( m\angle B = 3x \). Find the number of degrees in \( m\angle B \).
210. Which number below is irrational?
\[ \sqrt{4}, \sqrt{20}, \sqrt{121} \]
Why is the number you chose an irrational number?

211. Triangle ABC, with side AC extended to D, is shown in the accompanying diagram. If \( m\angle ABC = 63 \) and \( m\angle BCD = 92 \), what is \( m\angle BAC \)?

![Diagram of Triangle ABC with extended side AC to D]

212. Which graph represents the equation \( x = 2 \)?

[A] [B] [C] [D]

213. The expression \( (a^2 + b^2)^2 \) is equivalent to

[A] \( a^4 + 2a^2b^2 + b^4 \)  [B] \( a^4 + b^4 \)  
[C] \( a^4 + a^2b^2 + b^4 \)  [D] \( a^4 + 4a^2b^2 + b^4 \)

214. The Eye Surgery Institute just purchased a new laser machine for $500,000 to use during eye surgery. The Institute must pay the inventor $550 each time the machine is used. If the Institute charges $2,000 for each laser surgery, what is the minimum number of surgeries that must be performed in order for the Institute to make a profit?

215. Paloma has 3 jackets, 6 scarves, and 4 hats. Determine the number of different outfits consisting of a jacket, a scarf, and a hat that Paloma can wear.

216. Solve for \( x \): \( x^2 + 3x - 28 = 0 \)

217. In the graph of \( y \leq -x \), which quadrant is completely shaded?


218. A line segment on the coordinate plane has endpoints (2,4) and (4,y). The midpoint of the segment is point (3,7). What is the value of \( y \)?


219. A certain car comes in three body styles with a choice of two engines, a choice of two transmissions, and a choice of six colors. What is the minimum number of cars a dealer must stock to have one car of every possible combination?

220. On the banks of a river, surveyors marked locations \(A, B,\) and \(C.\) The measure of \(\angle ACB = 70^\circ\) and the measure of \(\angle ABC = 65^\circ.\)

Which expression shows the relationship between the lengths of the sides of this triangle?

[A] \(AB < BC < AC\)  
[B] \(BC < AB < AC\)  
[C] \(AC < AB < BC\)  
[D] \(BC < AC < AB\)

221. A car dealer has 22 vehicles on his lot. If 8 of the vehicles are vans and 6 of the vehicles are red, and 10 vehicles are neither vans nor red, how many red vans does he have on his lot?

222. What is the greatest possible number of points of intersection of a triangle and a circle?

[A] 3  
[B] 4  
[C] 6  
[D] 2

223. Expressed in decimal notation, \(4.726 \times 10^{-3}\) is

[A] 4.726  
[B] 0.004726  
[C] 0.04726  
[D] 472.6

224. In the accompanying diagram, \(AB\) and \(CD\) intersect at \(E.\) If \(m\angle AEC = 4x - 40\) and \(m\angle BED = x + 50,\) find the number of degrees in \(\angle AEC.\)

225. What was the median high temperature in Middletown during the 7-day period shown in the table below?

<table>
<thead>
<tr>
<th>Day</th>
<th>Temperature (°F)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Sunday</td>
<td>66</td>
</tr>
<tr>
<td>Monday</td>
<td>73</td>
</tr>
<tr>
<td>Tuesday</td>
<td>73</td>
</tr>
<tr>
<td>Wednesday</td>
<td>75</td>
</tr>
<tr>
<td>Thursday</td>
<td>69</td>
</tr>
<tr>
<td>Friday</td>
<td>67</td>
</tr>
<tr>
<td>Saturday</td>
<td>63</td>
</tr>
</tbody>
</table>

[A] 70  
[B] 69  
[C] 75  
[D] 73

226. In the equation \(A = p + prt,\) \(t\) is equivalent to

[A] \(\frac{A - pr}{p}\)  
[B] \(\frac{A - pr}{p}\)  
[C] \(\frac{A - p}{pr}\)  
[D] \(\frac{A - p}{pr}\)
227. Write the equation for the line shown in the accompanying graph. Explain your answer.

![Graph of a line](image)

228. Kyoko's mathematics teacher gave her the accompanying cards and asked her to arrange the cards in order from least to greatest. In what order should Kyoko arrange the cards?

\[ \pi, \sqrt{8}, 3.1, 2\sqrt{3}, 2\frac{4}{5} \]

229. Which equation represents a line parallel to the line \( y = 2x - 5 \)?

[A] \( y = -2x - 5 \)  
[B] \( y = 5x - 2 \)  
[C] \( y = -\frac{1}{2}x - 5 \)  
[D] \( y = 2x + 5 \)

230. Perform the indicated operation and express the result in simplest terms:

\[
\frac{x}{x+3} \div \frac{3x}{x^2 - 9}
\]

231. The accompanying table shows the weights, in pounds, for the students in an algebra class. Using the data, complete the cumulative frequency table and construct a cumulative frequency histogram on the grid below.

<table>
<thead>
<tr>
<th>Interval</th>
<th>Frequency</th>
</tr>
</thead>
<tbody>
<tr>
<td>91–100</td>
<td>6</td>
</tr>
<tr>
<td>101–110</td>
<td>3</td>
</tr>
<tr>
<td>111–120</td>
<td>0</td>
</tr>
<tr>
<td>121–130</td>
<td>3</td>
</tr>
<tr>
<td>131–140</td>
<td>0</td>
</tr>
<tr>
<td>141–150</td>
<td>2</td>
</tr>
<tr>
<td>151–160</td>
<td>2</td>
</tr>
</tbody>
</table>

232. The graph of the equation \( x + 3y = 6 \) intersects the \( y \)-axis at the point whose coordinates are

[A] (0,18)  
[B] (0,6)  
[C] (6,0)  
[D] (0,2)
233. Which inequality is true if \( x = \frac{3.04}{1.48} \), 
\( y = 1.99 + 0.33 \), and \( z = (1.3)^3 \) ?

[A] \( y < x < z \)    [B] \( y < z < x \)

[C] \( x < z < y \)    [D] \( x < y < z \)

234. Julia has four different flags that she wants to hang on the wall of her room. How many different ways can the flags be arranged in a row?


235. A doughnut shop charges \$0.70 for each doughnut and \$0.30 for a carryout box. Shirley has \$5.00 to spend. At most, how many doughnuts can she buy if she also wants them in one carryout box?

236. The operation \(*\) for the set \( \{p,r,s,v\} \) is defined in the accompanying table. What is the inverse element of \( r \) under the operation \(*\) ?

<table>
<thead>
<tr>
<th></th>
<th>( p )</th>
<th>( r )</th>
<th>( s )</th>
<th>( v )</th>
</tr>
</thead>
<tbody>
<tr>
<td>( p )</td>
<td>( s )</td>
<td>( v )</td>
<td>( p )</td>
<td>( r )</td>
</tr>
<tr>
<td>( r )</td>
<td>( v )</td>
<td>( p )</td>
<td>( r )</td>
<td>( s )</td>
</tr>
<tr>
<td>( s )</td>
<td>( p )</td>
<td>( r )</td>
<td>( s )</td>
<td>( v )</td>
</tr>
<tr>
<td>( v )</td>
<td>( r )</td>
<td>( s )</td>
<td>( v )</td>
<td>( p )</td>
</tr>
</tbody>
</table>

[A] \( v \)    [B] \( s \)    [C] \( p \)    [D] \( r \)

237. Factor completely: \( 3x^2 + 15x - 42 \)

238. Which statement is logically equivalent to "If I did not eat, then I am hungry"?

[A] If I am not hungry, then I did not eat.

[B] If I did not eat, then I am not hungry.

[C] If I am hungry, then I did eat.

[D] If I am not hungry, then I did eat.

239. An algebra class of 21 students must send 5 students to meet with the principal. How many different groups of 5 students could be formed from this class?

240. The measures of two consecutive angles of a parallelogram are in the ratio 5:4. What is the measure of an obtuse angle of the parallelogram?


241. Triangle \( ABC \) represents a metal flag on pole \( AD \), as shown in the accompanying diagram. On a windy day the triangle spins around the pole so fast that it looks like a three-dimensional shape.

Which shape would the spinning flag create?

[A] pyramid    [B] sphere

[C] cone    [D] right circular cylinder
242. On the accompanying grid, draw and label quadrilateral $ABCD$ with points $A(1,2)$, $B(6,1)$, $C(7,6)$, and $D(3,7)$. On the same set of axes, plot and label quadrilateral $A'B'C'D'$, the reflection of quadrilateral $ABCD$ in the y-axis. Determine the area, in square units, of quadrilateral $A'B'C'D'$.

243. Frank, George, and Hernando are a plumber, a cabinet maker, and an electrician, though not necessarily in that order. Each can do all work appropriate to his own field, but no work in other fields. Frank was not able to install a new electric line in his home. Hernando was not able to make cabinets. George is also a building contractor who hired one of the other people to do his electrical work. Which statement must be true?

[A] George is a cabinet maker.
[B] Frank is a plumber.
[C] Frank is an electrician.
[D] Hernando is an electrician.

244. Mr. Yee has 10 boys and 15 girls in his mathematics class. If he chooses two students at random to work on the blackboard, what is the probability that both students chosen are girls?

245. In the time trials for the 400-meter run at the state sectionals, the 15 runners recorded the times shown in the table below.

<table>
<thead>
<tr>
<th>Time (sec)</th>
<th>Frequency</th>
</tr>
</thead>
<tbody>
<tr>
<td>50.0–50.9</td>
<td></td>
</tr>
<tr>
<td>51.0–51.9</td>
<td>11</td>
</tr>
<tr>
<td>52.0–52.9</td>
<td>14</td>
</tr>
<tr>
<td>53.0–53.9</td>
<td>13</td>
</tr>
<tr>
<td>54.0–54.9</td>
<td>14</td>
</tr>
</tbody>
</table>

a) Using the data from the frequency column, draw a frequency histogram on the grid provided below.

b) What percent of the runners completed the time trial between 52.0 and 53.9 seconds?
246. In the accompanying diagram, parallel lines $\overline{AB}$ and $\overline{CD}$ are intersected by transversal $\overline{EF}$ at points $X$ and $Y$, and $m\angle FYD = 123^\circ$. Find $m\angle AXY$.

![Diagram](image)

247. The inequality $\frac{1}{2}x + 3 < 2x - 6$ is equivalent to

[A] $x < 6$  
[B] $x < -\frac{5}{6}$  
[C] $x > -\frac{5}{6}$  
[D] $x > 6$

248. The expression $2x^2 - x^2$ is equivalent to

[A] $2$  
[B] $-2x^4$  
[C] $x^2$  
[D] $x^0$

249. In a class of 50 students, 18 take music, 26 take art, and 2 take both art and music. How many students in the class are not enrolled in either music or art?

[A] 24  
[B] 8  
[C] 16  
[D] 6

250. $\overline{AB}$ and $\overline{CD}$ intersect at $E$. If $m\angle AEC = 5x - 20$ and $m\angle BED = x + 50$, find, in degrees, $m\angle CEB$.

251. A square dartboard is represented in the accompanying diagram. The entire dartboard is the first quadrant from $x = 0$ to 6 and from $y = 0$ to 6. A triangular region on the dartboard is enclosed by the graphs of the equations $y = 2$, $x = 6$, and $y = x$. Find the probability that a dart that randomly hits the dartboard will land in the triangular region formed by the three lines.

![Graph](image)

252. Hersch says if a triangle is an obtuse triangle, then it cannot also be an isosceles triangle. Using a diagram, show that Hersch is incorrect, and indicate the measures of all the angles and sides to justify your answer.

253. Julio's wages vary directly as the number of hours that he works. If his wages for 5 hours are $29.75, how much will he earn for 30 hours?

254. Which number has the greatest value?

[A] $\frac{\pi}{2}$  
[B] $\sqrt{2}$  
[C] 1.5  
[D] $1\frac{2}{3}$
255. Which statement is logically equivalent to "If it is Saturday, then I am not in school"?

[A] If it is not Saturday, then I am in school.
[B] If it is Saturday, then I am in school.
[C] If I am not in school, then it is Saturday.
[D] If I am in school, then it is not Saturday.

256. What is the first step in simplifying the expression \((2 - 3 \times 4 + 5)^2\)?

[A] subtract 3 from 2  
[B] square 5  
[C] multiply 3 by 4  
[D] add 4 and 5

257. The measures of two complementary angles are represented by \((3x + 15)\) and \((2x - 10)\). What is the value of \(x\)?

[A] 35  
[B] 19  
[C] 37  
[D] 17

258. If \(x \neq 0\), the expression \(\frac{x^2 + 2x}{x}\) is equivalent to

[A] 2  
[B] 4  
[C] \(x + 2\)  
[D] 3x

259. A fish tank with a rectangular base has a volume of 3,360 cubic inches. The length and width of the tank are 14 inches and 12 inches, respectively. Find the height, in inches, of the tank.

260. Sue bought a picnic table on sale for 50% off the original price. The store charged her 10% tax and her final cost was $22.00. What was the original price of the picnic table?

261. What is the solution set of the equation \(3x^2 = 48\)?

[A] \(\{4,4\}\)  
[B] \(-2,-8\)  
[C] \(\{2,8\}\)  
[D] \(\{4,-4\}\)

262. Graph the following systems of inequalities on the accompanying set of axes and label the solution set \(S\):

\[y > x - 4\]
\[y + x \geq 2\]

[Only a graphic solution can receive full credit.]

263. When solved graphically, which system of equations will have exactly one point of intersection?

[A] \(y = -x + 15\)  
\(y = -x + 25\)

[B] \(y = \frac{3}{5}x + 12\)  
\(y = 0.6x - 19\)

[C] \(y = 0.5x + 30\)  
\(y = 0.5x - 30\)

[D] \(y = -x - 20\)  
\(y = x + 17\)
264. In the accompanying diagram, the perimeter of \( \triangle MNO \) is equal to the perimeter of square \( ABCD \). If the sides of the triangle are represented by \( 4x + 4, 5x - 3, \) and 17, and one side of the square is represented by \( 3x \), find the length of a side of the square.

265. What is true about the statement "If two angles are right angles, the angles have equal measure" and its converse "If two angles have equal measure then the two angles are right angles"?

[A] Both the statement and its converse are true.
[B] The statement is false but its converse is true.
[C] Both the statement and its converse are false.
[D] The statement is true but its converse is false.

266. Which expression is a factor of \( n^2 + 3n - 54 \)?

[A] \( n^2 + 9 \)       [B] \( n - 9 \)
[C] \( n + 6 \)       [D] \( n + 9 \)

267. What is the inverse of the statement "If it is sunny, I will play baseball"?

[A] If I do not play baseball, then it is not sunny.
[B] If I play baseball, then it is sunny.
[C] I will play baseball if and only if it is sunny.
[D] If it is not sunny, I will not play baseball.

268. The accompanying graph shows the high temperatures in Elmira, New York, for a 5-day period in January.

Which statement describes the data?

[A] mean < mode       [B] mean = mode
[C] median = mode       [D] median = mean

269. What is the image of point \((-3, -1)\) under a reflection in the origin?

[A] (-3, 1)       [B] (-1, -3)
[C] (3, 1)       [D] (1, 3)
270. A fair coin is thrown in the air four times. If the coin lands with the head up on the first three tosses, what is the probability that the coin will land with the head up on the fourth toss?

[A] $\frac{1}{8}$  [B] $\frac{1}{2}$  [C] 0  [D] $\frac{1}{16}$

271. The locus of points equidistant from two sides of an acute scalene triangle is

[A] an angle bisector  [B] a median  
[C] an altitude  [D] the third side

272. When $-9x^5$ is divided by $-3x^3$, $x \neq 0$, the quotient is

[A] $-3x^2$  [B] $-27x^{15}$  
[C] $27x^8$  [D] $3x^2$

273. Two trains leave the same station at the same time and travel in opposite directions. One train travels at 80 kilometers per hour and the other at 100 kilometers per hour. In how many hours will they be 900 kilometers apart?

274. In a survey of 400 teenage shoppers at a large mall, 240 said they shopped at Abernathy’s, 210 said they shopped at Bongo Republic, and 90 said they shopped at both stores. How many of the teenage shoppers surveyed did not shop at either store?

275. What is the value of $3^0 + 3^{-2}$ ?

[A] 0  [B] $\frac{1}{9}$  [C] 6  [D] $1\frac{1}{9}$

276. If $2ax - 5x = 2$, then $x$ is equivalent to

[A] $\frac{2 + 5a}{2a}$  [B] $\frac{1}{a - 5}$  
[C] $7 - 2a$  [D] $\frac{2}{2a - 5}$

277. For which value of $x$ is the expression $\frac{3}{x - 2}$ undefined?

[A] 3  [B] -2  [C] 0  [D] 2

278. A surveyor needs to determine the distance across the pond shown in the accompanying diagram. She determines that the distance from her position to point $P$ on the south shore of the pond is 175 meters and the angle from her position to point $X$ on the north shore is $32^\circ$. Determine the distance, $PX$, across the pond, rounded to the nearest meter.

279. What is the slope of the line whose equation is $3x - 4y - 16 = 0$?

[A] -4  [B] $\frac{4}{3}$  [C] $\frac{3}{4}$  [D] 3
280. If \(2x^2 - 4x + 6\) is subtracted from \(5x^2 + 8x - 2\), the difference is

[A] \(-3x^2 - 12x + 8\)  
[B] \(3x^2 + 12x - 8\)  
[C] \(-3x^2 + 4x + 4\)  
[D] \(3x^2 + 4x + 4\)

281. Ashanti and Maria went to the store to buy snacks for their back-to-school party. They bought bags of chips, pretzels, and nachos. They bought three times as many bags of pretzels as bags of chips, and two fewer bags of nachos than bags of pretzels. If \(x\) represents the number of bags of chips they bought, express, in terms of \(x\), how many bags of snacks they bought in all.

282. The lengths of the sides of home plate in a baseball field are represented by the expressions in the accompanying figure.

Which expression represents the perimeter of the figure?

[A] \(2x + 3yz\)  
[B] \(2x + 2y + yz\)  
[C] \(x^2 + y^3z\)  
[D] \(5xyz\)

283. The expression \(15 - 3[2 + 6(-3)]\) simplifies to

[A] 63  
[B] 192  
[C] -33  
[D] -45

284. What is the least common denominator of \(\frac{1}{2}\), \(\frac{2}{7x}\), and \(\frac{5}{x}\)?

[A] \(14x^2\)  
[B] \(9x\)  
[C] \(14x\)  
[D] \(2x\)

285. What is the product of \(10x^4y^2\) and \(3xy^3\)?

[A] \(30x^4y^6\)  
[B] \(30x^5y^5\)  
[C] \(30x^4y^5\)  
[D] \(30x^5y^6\)

286. The accompanying diagram shows two parallel roads, Hope Street and Grand Street, crossed by a transversal road, Broadway.

If \(m \angle 1 = 110\), what is the measure of \(\angle 7\)?

[A] 70°  
[B] 110°  
[C] 40°  
[D] 180°

287. What is the inverse of the statement "If Bob gets hurt, then the team loses the game"? 

[A] If the team loses the game, then Bob gets hurt.  
[B] If Bob does not get hurt, then the team does not lose the game.  
[C] If the team does not lose the game, then Bob does not get hurt.  
[D] Bob gets hurt if the team loses the game.
288. The accompanying diagram shows a football player crossing the 20-yard line at an angle of 30° and continuing along the same path.

What is the measure of angle B, where the player crosses into the end zone?

289. Solve for $x$: \[
\frac{1}{16}x + \frac{1}{4} = \frac{1}{2}
\]

290. Delroy's sailboat has two sails that are similar triangles. The larger sail has sides of 10 feet, 24 feet, and 26 feet. If the shortest side of the smaller sail measures 6 feet, what is the perimeter of the smaller sail?
[A] 36 ft  [B] 60 ft  [C] 100 ft  [D] 15 ft

291. The expression $\sqrt{50} + \sqrt{32}$ is equivalent to
[A] $9\sqrt{2}$  [B] $8\sqrt{2}$  [C] 6  [D] 18

292. The expression $\sqrt{27} + \sqrt{12}$ is equivalent to
[A] $13\sqrt{3}$  [B] $5\sqrt{3}$  [C] $5\sqrt{6}$  [D] $\sqrt{39}$

293. The accompanying diagram shows a kite that has been secured to a stake in the ground with a 20-foot string. The kite is located 12 feet from the ground, directly over point $X$. What is the distance, in feet, between the stake and point $X$?

What is $m\angle CAD$?

294. In the accompanying diagram of rectangle $ABCD$, $m\angle BAC = 3x + 4$ and $m\angle ACD = x + 28$.

295. If a line is horizontal, its slope is
[A] 1  [B] 0  [C] undefined  [D] negative
296. The accompanying box-and-whisker plot represents the scores earned on a science test.

What is the median score?

297. The sum of the measures of the interior angles of an octagon is
[A] 1,080°  [B] 540°
[C] 360°  [D] 180°

298. In the accompanying diagram, \( x \) represents the length of a ladder that is leaning against a wall of a building, and \( y \) represents the distance from the foot of the ladder to the base of the wall. The ladder makes a 60° angle with the ground and reaches a point on the wall 17 feet above the ground. Find the number of feet in \( x \) and \( y \).

299. What is the approximate circumference of a circle with radius 3?
[C] 7.07  [D] 18.85

300. In the accompanying figure, two lines intersect, \( m\angle 3 = 6t + 30 \), and \( m\angle 2 = 8t - 60 \). Find the number of degrees in \( m\angle 4 \).

301. The faces of a cube are numbered from 1 to 6. What is the probability of not rolling a 5 on a single toss of this cube?
[A] \( \frac{4}{5} \)  [B] \( \frac{1}{5} \)  [C] \( \frac{5}{6} \)  [D] \( \frac{1}{6} \)

302. Which equation represents the locus of points 4 units from the origin?
[A] \( x^2 + y^2 = 4 \)  [B] \( x^2 + y^2 = 16 \)
[C] \( x + y = 16 \)  [D] \( x = 4 \)

303. What are the coordinates of \( P' \), the image of \( P(-4, 0) \) under the translation \( (x - 3, y + 6) \)?
[A] (-7,6)  [B] (2,-3)
[C] (7,-6)  [D] (1,6)
304. Kimberly has three pair of pants: one black, one red, and one tan. She also has four shirts: one pink, one white, one yellow, and one green. Draw a tree diagram or list the sample space showing all possible outfits that she could wear, if an outfit consists of one pair of pants and one shirt. How many different outfits can Kimberly wear?

305. In a class of 24 students, 10 have brown hair, 8 have black hair, 4 have blond hair, and 2 have red hair. On the accompanying diagram, construct a circle graph to show the students’ hair color.

306. The expression \( (x^2 - 5x - 2) - (-6x^2 - 7x - 3) \) is equivalent to

\[ \text{[A]} \quad 7x^2 + 2x + 1 \quad \text{[B]} \quad 7x^2 - 2x + 1 \]
\[ \text{[C]} \quad 7x^2 + 2x - 5 \quad \text{[D]} \quad 7x^2 - 12x - 5 \]

307. Solve the following system of equations algebraically.
\[ y = x^2 + 4x - 2 \]
\[ y = 2x + 1 \]

308. Steve has a treasure map, represented in the accompanying diagram, that shows two trees 8 feet apart and a straight fence connecting them. The map states that treasure is buried 3 feet from the fence and equidistant from the two trees.

\( a \) Sketch a diagram to show all the places where the treasure could be buried. Clearly indicate in your diagram where the treasure could be buried.

\( b \) What is the distance between the treasure and one of the trees?

309. Helen is using a capital \( H \) in an art design. The \( H \) has

\[ \text{[A]} \quad \text{two lines of symmetry and two points of symmetry} \]
\[ \text{[B]} \quad \text{only two points of symmetry} \]
\[ \text{[C]} \quad \text{two lines of symmetry and only one point of symmetry} \]
\[ \text{[D]} \quad \text{only one line of symmetry} \]

310. Which equation represents a line that is perpendicular to the line whose equation is \( -2y = 3x + 7 \)?

\[ \text{[A]} \quad y = \frac{3}{2}x - 3 \quad \text{[B]} \quad y = \frac{2}{3}x - 3 \]
\[ \text{[C]} \quad 2y = 3x - 3 \quad \text{[D]} \quad y = x + 7 \]
311. For which value of $x$ is the expression $\frac{3x - 6}{x - 4}$ undefined?

[A] 0  [B] -4  [C] 4  [D] 2

312. Given the true statements: "Jason goes shopping or he goes to the movies" and "Jason does not go to the movies." Which statement must also be true?

[A] Jason does not go shopping and he does not go to the movies.
[C] Jason goes shopping.
[D] Jason does not go shopping.

313. On February 18, from 9 a.m. until 2 p.m., the temperature rose from -14°F to 36°F. What was the total increase in temperature during this time period?


314. Brett was given the problem: "Evaluate $2x^2 + 5$ when $x = 3.$" Brett wrote that the answer was 41. Was Brett correct? Explain your answer.

315. All seven-digit telephone numbers in a town begin with 245. How many telephone numbers may be assigned in the town if the last four digits do not begin or end in a zero?

316. What is the measure of the largest angle in the accompanying triangle?


317. An arch is built so that it is 6 feet wide at the base. Its shape can be represented by a parabola with the equation $y = -2x^2 + 12x$, where $y$ is the height of the arch.

a) Graph the parabola from $x = 0$ to $x = 6$ on the grid below.

b) Determine the maximum height, $y$, of the arch.

318. If $a > 0$, then $\sqrt{9a^2 + 16a^2}$ equals

[A] $\sqrt{7a}$  [B] $5a$  [C] $5\sqrt{a}$  [D] $7a$
319. Joe is holding his kite string 3 feet above the ground, as shown in the accompanying diagram. The distance between his hand and a point directly under the kite is 95 feet. If the angle of elevation to the kite is 50°, find the height, \( h \), of his kite, to the nearest foot.

\[
3 \text{ ft} \\
\hline
95 \text{ ft} \\
\hline
\hline
\hline
\hline
\text{(Not drawn to scale)}
\]

320. In the accompanying figure, \( ACDH \) and \( BCEF \) are rectangles, \( AH = 2 \), \( GH = 3 \), \( GF = 4 \), and \( FE = 5 \).

321. When \( 3a^2 - 2a + 5 \) is subtracted from \( a^2 + a - 1 \), the result is

\[
\begin{align*}
[A] & \quad 2a^2 - 3a - 6 \\
[B] & \quad -2a^2 + 3a - 6 \\
[C] & \quad -2a^2 + 3a + 6 \\
[D] & \quad 2a^2 - 3a + 6
\end{align*}
\]

322. If 6 and \( x \) have the same mean (average) as 2, 4, and 24, what is the value of \( x \)?

\[
[A] 14 \quad [B] 36 \quad [C] 10 \quad [D] 5
\]

323. The accompanying circle graph shows the favorite colors of the 300 students in the ninth grade. How many students chose red as their favorite color?

324. During each marking period, there are five tests. If Vanita needs a 65 average to pass this marking period and her first four grades are 60, 72, 55, and 80, what is the lowest score she can earn on the last test to have a passing average?

\[
[A] 65 \quad [B] 58 \quad [C] 100 \quad [D] 80
\]
325. The expression $\sqrt{93}$ is a number between
[A] 3 and 9  [B] 46 and 47
[C] 8 and 9  [D] 9 and 10

326. The scores on a mathematics test were 70, 55, 61, 80, 85, 72, 65, 40, 74, 68, and 84.
Complete the accompanying table, and use the table to construct a frequency histogram for these scores.

<table>
<thead>
<tr>
<th>Score</th>
<th>Tally</th>
<th>Frequency</th>
</tr>
</thead>
<tbody>
<tr>
<td>40–49</td>
<td></td>
<td></td>
</tr>
<tr>
<td>50–59</td>
<td></td>
<td></td>
</tr>
<tr>
<td>60–69</td>
<td></td>
<td></td>
</tr>
<tr>
<td>70–79</td>
<td></td>
<td></td>
</tr>
<tr>
<td>80–89</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

327. A 14-gram serving of mayonnaise contains 11 grams of fat. What percent of the mayonnaise, to the nearest tenth of a percent, is fat?

328. Which equation illustrates the distributive property of multiplication over addition?
[A] $6(3a + 4b) = (3a + 4b)6$
[B] $6(3a + 4b) = 18a + 4b$
[C] $6(3a + 4b) = 6(4b + 3a)$
[D] $6(3a + 4b) = 18a + 24b$

329. At a school costume party, seven girls wore masks and nine boys did not. If there were 15 boys at the party and 20 students did not wear masks, what was the total number of students at the party?

330. When Albert flips open his mathematics textbook, he notices that the product of the page numbers of the two facing pages that he sees is 156. Which equation could be used to find the page numbers that Albert is looking at?
[A] $(x+1) + (x+2) = 156$
[B] $x(x+1) = 156$  [C] $x + (x + 1) = 156$
[D] $(x+1)(x+3) = 156$

331. What is the solution set of the equation $x^2 - 5x - 24 = 0$?
[A] {-3,-8}  [B] {-3,8}
[C] {3,8}  [D] {3,-8}

332. How many different 4-letter arrangements can be formed using the letters of the word "JUMP," if each letter is used only once?
333. A triangle has sides whose lengths are 5, 12, and 13. A similar triangle could have sides with lengths of

[A] 3, 4, and 15 [B] 6, 8, and 10
[C] 10, 24, and 26 [D] 7, 24, and 25

334. An architect is designing a museum entranceway in the shape of a parabolic arch represented by the equation \( y = -x^2 + 20x \), where \( 0 \leq x \leq 20 \) and all dimensions are expressed in feet. On the accompanying set of axes, sketch a graph of the arch and determine its maximum height, in feet.

335. In the accompanying diagram, line \( a \) intersects line \( b \).

What is the value of \( x \)?


336. An engineer measured the dimensions for a rectangular site by using a wooden pole of unknown length \( x \). The length of the rectangular site is 2 pole measures increased by 3 feet, while the width is 1 pole measure decreased by 4 feet. Write an algebraic representation, in terms of \( x \), for the perimeter of the site.

337. The number \( 8.375 \times 10^{-3} \) is equivalent to

[A] 0.008375 [B] 0.0008375 [C] 0.08375 [D] 8.375

338. Which statement is logically equivalent to "If a triangle is an isosceles triangle, then it has two congruent sides"?

[A] If a triangle does not have two congruent sides, then it is not an isosceles triangle.
[B] If a triangle is not an isosceles triangle, then it has two congruent sides.
[C] If a triangle is an isosceles triangle, then it does not have two congruent sides.
[D] If a triangle does not have two congruent sides, then it is an isosceles triangle.

339. Simplify: \( \frac{x^2 + 6x + 5}{x^2 - 25} \)

340. If two lines are parallel and the slope of one of the lines is \( m \), what is the product of their slopes?

[A] 0 [B] \( m^2 \) [C] 2\( m \) [D] 1
341. On a science quiz, 20 students received the following scores: 100, 95, 95, 90, 85, 85, 85, 80, 80, 80, 80, 75, 75, 75, 70, 70, 65, 65, 60, 55. Construct a statistical graph, such as a histogram or a stem-and-leaf plot, to display this data. [Be sure to title the graph and label all axes or parts used.]

If your type of plot requires a grid, show your work here. If no grid is necessary, show your work here.

342. Which equation represents a circle whose center is (3, -2)?

[A] \((x - 2)^2 + (y + 3)^2 = 4\)
[B] \((x + 3)^2 + (y - 2)^2 = 4\)
[C] \((x + 2)^2 + (y - 3)^2 = 4\)
[D] \((x - 3)^2 + (y + 2)^2 = 4\)

344. Which expression is a factor of \(x^2 + 2x - 15\)

[A] \((x - 5)\) \quad [B] \((x - 3)\)
[C] \((x + 3)\) \quad [D] \((x + 15)\)

345. John left his home and walked 3 blocks to his school, as shown in the accompanying graph.

What is one possible interpretation of the section of the graph from point B to point C?

[A] John arrived at school and stayed throughout the day.
[C] John reached the top of a hill and began walking on level ground.
[D] John returned home to get his mathematics homework.

346. The exact average of a set of six test scores is 92. Five of these scores are 90, 98, 96, 94, and 85. What is the other test score?

[A] 89 \quad [B] 91 \quad [C] 92 \quad [D] 86

347. What is the multiplicative inverse of \(\frac{3}{4}\)?

[A] \(\frac{4}{3}\) \quad [B] \(-\frac{4}{3}\) \quad [C] \(-\frac{3}{4}\) \quad [D] -1
348. The expression \((6x^3y^6)^2\) is equivalent to

[A] \(12x^6y^{12}\)  [B] \(36x^5y^8\)
[C] \(36x^6y^{12}\)  [D] \(6x^6y^{12}\)

349. Mary chooses an integer at random from 1 to 6. What is the probability that the integer she chooses is a prime number?

[A] \(\frac{2}{6}\)  [B] \(\frac{5}{6}\)  [C] \(\frac{4}{6}\)  [D] \(\frac{3}{6}\)

350. If point \(P\) lies on line \(\ell\), which diagram represents the locus of points 3 centimeters from point \(P\)?

[A]  
[B]  
[C]  
[D]  

352. To get from his high school to his home, Jamal travels 5.0 miles east and then 4.0 miles north. When Sheila goes to her home from the same high school, she travels 8.0 miles east and 2.0 miles south. What is the measure of the shortest distance, to the nearest tenth of a mile, between Jamal's home and Sheila's home? [The use of the accompanying grid is optional.]

353. Given the statement: "If two sides of a triangle are congruent, then the angles opposite these sides are congruent." Given the converse of the statement: "If two angles of a triangle are congruent, then the sides opposite these angles are congruent." What is true about this statement and its converse?

[A] The statement is false but its converse is true.
[B] Both the statement and its converse are true.
[C] Neither the statement nor its converse is true.
[D] The statement is true but its converse is false.

351. If one factor of \(56x^4y^3 - 42x^2y^6\) is \(14x^2y^3\), what is the other factor?

[A] \(4x^2 - 3y^2\)  [B] \(4x^2y - 3xy^2\)
[C] \(4x^2 - 3y^3\)  [D] \(4x^2y - 3xy^3\)
354. Sharu has $2.35 in nickels and dimes. If he has a total of thirty-two coins, how many of each coin does he have?

355. One root of the equation $2x^2 - x - 15 = 0$ is

[A] 3  [B] -3  [C] $\frac{5}{2}$  [D] $\frac{3}{2}$

356. The statement "x is divisible by 5 or x is divisible by 4" is false when x equals


357. Melissa is walking around the outside of a building that is in the shape of a regular polygon. She determines that the measure of one exterior angle of the building is 60°. How many sides does the building have?


358. Which linear equation represents the data in the accompanying table?

<table>
<thead>
<tr>
<th>c</th>
<th>d</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>20.00</td>
</tr>
<tr>
<td>1</td>
<td>21.50</td>
</tr>
<tr>
<td>2</td>
<td>23.00</td>
</tr>
<tr>
<td>3</td>
<td>24.50</td>
</tr>
</tbody>
</table>

[A] $d = 21.50c$  [B] $d = 20.00c + 1.50$  
[C] $d = 1.50c + 20.00$  [D] $d = 1.50c$

359. How many points are equidistant from two parallel lines and also equidistant from two points on one of the lines?


360. The accompanying diagram shows a box-and-whisker plot of student test scores on last year's Mathematics A midterm examination.

What is the median score?


361. Which statement is logically equivalent to "If the team has a good pitcher, then the team has a good season"?

[A] If the team does not have a good season, then the team does not have a good pitcher.

[B] If the team has a good season, then the team has a good pitcher.

[C] If the team does not have a good pitcher, then the team does not have a good season.

[D] The team has a good pitcher and the team does not have a good season.

362. Juan has three blue shirts, two green shirts, seven red shirts, five pairs of denim pants, and two pairs of khaki pants. How many different outfits consisting of one shirt and one pair of pants are possible?

363. A target shown in the accompanying diagram consists of three circles with the same center. The radii of the circles have lengths of 3 inches, 7 inches, and 9 inches.

\[
\text{a} \quad \text{What is the area of the shaded region to the nearest tenth of a square inch?}
\]
\[
\text{b} \quad \text{To the nearest percent, what percent of the target is shaded?}
\]

364. If the probability that it will rain on Thursday is \(\frac{5}{6}\), what is the probability that it will not rain on Thursday?

[A] \(\frac{5}{6}\)  [B] 1  [C] 0  [D] \(\frac{1}{6}\)

365. A wall is supported by a brace 10 feet long, as shown in the diagram below. If one end of the brace is placed 6 feet from the base of the wall, how many feet up the wall does the brace reach?

366. If \(n\) represents an odd number, which computation results in an answer that is an even number?

[A] \(3 \times n - 2\)  [B] \(2 \times n - 1\)  [C] \(2 \times n + 1\)  [D] \(3 \times n + 1\)

367. Running at a constant speed, Andrea covers 15 miles in \(2\frac{1}{2}\) hours. At this speed, how many minutes will it take her to run 2 miles?

368. TOP Electronics is a small business with five employees. The mean (average) weekly salary for the five employees is $360. If the weekly salaries of four of the employees are $340, $340, $345, and $425, what is the salary of the fifth employee?

369. There were seven students running in a race. How many different arrangements of first, second, and third place are possible?

370. Ramón rented a sprayer and a generator. On his first job, he used each piece of equipment for 6 hours at a total cost of $90. On his second job, he used the sprayer for 4 hours and the generator for 8 hours at a total cost of $100. What was the hourly cost of each piece of equipment?

371. The expression \(9\choose 2\) is equivalent to

[A] \(9P_2\)  [B] \(9C_7\)  [C] \(\frac{9!}{2!}\)  [D] \(9P_7\)
372. The NuFone Communications Company must run a telephone line between two poles at opposite ends of a lake, as shown in the accompanying diagram. The length and width of the lake are 75 feet and 30 feet, respectively.

What is the distance between the two poles, to the nearest foot?


373. Which inequality represents the probability, \(x\), of any event happening?

[A] \(0 \leq x \leq 1\)  [B] \(x < 1\)
[C] \(0 < x < 1\)  [D] \(x \geq 0\)

374. Which type of transformation is illustrated in the accompanying diagram?

[A] dilation  [B] translation
[C] rotation  [D] reflection

375. The quotient of \(-\frac{15x^8}{5x^3}\), \(x \neq 0\), is

[A] \(-10x^6\)  [B] \(-3x^4\)
[C] \(-3x^6\)  [D] \(-10x^4\)

376. There are four students, all of different heights, who are to be randomly arranged in a line. What is the probability that the tallest student will be first in line and the shortest student will be last in line?

377. Alan, Becky, Jesus, and Mariah are four students in the chess club. If two of these students will be selected to represent the school at a national convention, how many combinations of two students are possible?

378. The number of people on the school board is represented by \(x\). Two subcommittees with an equal number of members are formed, one with \(\frac{2}{3}x - 5\) members and the other with \(\frac{x}{4}\) members. How many people are on the school board?


379. Which quadrilateral must have diagonals that are congruent and perpendicular?

[A] rhombus  [B] trapezoid
[C] parallelogram  [D] square
380. Connor wants to compare Celsius and Fahrenheit temperatures by drawing a conversion graph. He knows that \(-40^\circ C = -40^\circ F\) and that \(20^\circ C = 68^\circ F\). On the accompanying grid, construct the conversion graph and, using the graph, determine the Celsius equivalent of 25\(^\circ\)F.

381. If the measures of the angles of a triangle are represented by \(2x\), \(3x-15\), and \(7x+15\), the triangle is

[A] an acute triangle
[B] an equiangular triangle
[C] a right triangle
[D] an isosceles triangle

382. What is a common factor of \(x^2 - 9\) and \(x^2 - 5x + 6\)?

[A] \(x^2\)  
[B] \(x - 2\)  
[C] \(x + 3\)  
[D] \(x - 3\)

383. The graph of the equation \(x^2 + y^2 = 4\) can be described as a

[A] circle with its center at the origin and a radius of 4
[B] parabola with its vertex at (0,2)
[C] circle with its center at the origin and a radius of 2
[D] line passing through points (0,2) and (2,0)

384. Write an irrational number and explain why it is irrational.

385. The lengths of the sides of two similar rectangular billboards are in the ratio 5:4. If 250 square feet of material is needed to cover the larger billboard, how much material, in square feet, is needed to cover the smaller billboard?

386. Which statement is the converse of "If it is a 300 ZX, then it is a car"?

[A] If it is not a 300 ZX, then it is not a car.
[B] If it is a car, then it is not a 300 ZX.
[C] If it is a car, then it is a 300 ZX.
[D] If it is not a car, then it is not a 300 ZX.

387. How many different outfits consisting of a hat, a pair of slacks, and a sweater can be made from two hats, three pairs of slacks, and four sweaters?

[A] 29  
[B] 24  
[C] 12  
[D] 9
388. If point (-1,0) is on the line whose equation is \( y = 2x + b \), what is the value of \( b \)?

[A] 2    [B] 0    [C] 1    [D] 3

389. In a telephone survey of 100 households, 32 households purchased Brand A cereal and 45 purchased Brand B cereal. If 10 households purchased both items, how many of the households surveyed did not purchase either Brand A or Brand B cereal?

390. \( \overline{AB} \) and \( \overline{CD} \) intersect at point \( E \), \( \angle AEC = 6x + 20 \), and \( \angle DEB = 10x \). What is the value of \( x \)?

[A] \( \frac{3}{8} \)    [B] \( \frac{21}{4} \)    [C] 10    [D] 5

391. The coordinates of the midpoint of \( \overline{AB} \) are (2,4), and the coordinates of point \( B \) are (3,7). What are the coordinates of point \( A \)? [The use of the accompanying grid is optional.]

392. A swimmer plans to swim at least 100 laps during a 6-day period. During this period, the swimmer will increase the number of laps completed each day by one lap. What is the least number of laps the swimmer must complete on the first day?

393. Ninety percent of the ninth grade students at Richbartville High School take algebra. If 180 ninth grade students take algebra, how many ninth grade students do not take algebra?

394. The graph of a quadratic equation is shown in the accompanying diagram. The scale on the axes is a unit scale. Write an equation of this graph in standard form.

395. Kerry is planning a rectangular garden that has dimensions of 4 feet by 6 feet. Kerry wants one-half of the garden to have roses, and she says that the rose plot will have dimensions of 2 feet by 3 feet. Is she correct? Explain.
396. Solve the following system of equations:
\[ y = x^2 + 4x + 1 \]
\[ y = 5x + 3 \]
[The use of the grid is optional.]

397. In the accompanying diagram of \( \triangle ABC \), \( AB \) is extended through \( D \), \( m \angle CBD = 30 \), and \( AB \cong BC \).

What is the measure of \( \angle A \)?

398. Which expression has the smallest value?
[A] \(-\sqrt{10}\)  [B] \(-3.02\)  
[C] \(-\pi\)  [D] \(-\frac{16}{5}\)

399. Selena and Tracey play on a softball team. Selena has 8 hits out of 20 times at bat, and Tracey has 6 hits out of 16 times at bat. Based on their past performance, what is the probability that both girls will get a hit next time at bat?
[A] \(\frac{14}{36}\)  [B] 1  [C] \(\frac{48}{320}\)  [D] \(\frac{31}{40}\)

400. The sum of \(\sqrt{75}\) and \(\sqrt{3}\) is
[A] 18  [B] \(6\sqrt{3}\)  [C] \(\sqrt{78}\)  [D] 15

401. Which is an irrational number?
[A] \(\pi\)  [B] \(\sqrt{9}\)  [C] \(-\frac{1}{3}\)  [D] 0

402. Two parallel roads, Elm Street and Oak Street, are crossed by a third, Walnut Street, as shown in the accompanying diagram. Find the number of degrees in the acute angle formed by the intersection of Walnut Street and Elm Street.

403. If the circumference of a circle is doubled, the diameter of the circle
[A] increases by 2  [B] remains the same  
[C] is doubled  [D] is multiplied by 4
404. The image of point (3,-5) under the translation that shifts \((x,y)\) to \((x-1,y-3)\) is

[A] (-3,15)  [B] (2,-8)
[C] (2,8)     [D] (-4,8)

405. Find, to the nearest tenth of a foot, the height of the tree represented in the accompanying diagram.

![Diagram of a tree with measurements](image)

406. At the Phoenix Surfboard Company, $306,000 in profits was made last year. This profit was shared by the four partners in the ratio 3:3:5:7. How much more money did the partner with the largest share make than one of the partners with the smallest share?

407. The image of point (-2,3) under translation \(T\) is (3,-1). What is the image of point (4,2) under the same translation?

[A] (9,-2)  [B] (5,4)
[C] (-1,6)   [D] (0,7)

408. On June 17, the temperature in New York City ranged from 90° to 99°, while the temperature in Niagara Falls ranged from 60° to 69°. The difference in the temperatures in these two cities must be between

[A] 30° and 40°  [B] 20° and 30°
[C] 25° and 35°  [D] 20° and 40°

409. In the accompanying diagram, parallel lines \(\overline{AB}\) and \(\overline{CD}\) are intersected by transversal \(\overline{EF}\) at points \(G\) and \(H\), respectively, \(m\angle AGH = x + 15\), and \(m\angle GHD = 2x\).

![Diagram with angle measurements](image)

Which equation can be used to find the value of \(x\)?

[A] \(2x = x + 15\)  [B] \(2x + x + 15 = 180\)
[C] \(2x(x + 15) = 0\)  [D] \(2x + x + 15 = 90\)

410. A truck travels 40 miles from point \(A\) to point \(B\) in exactly 1 hour. When the truck is halfway between point \(A\) and point \(B\), a car starts from point \(A\) and travels at 50 miles per hour. How many miles has the car traveled when the truck reaches point \(B\)?

411. Which equation illustrates the multiplicative inverse property?

[A] \(-1 \cdot x = -x\)  
[B] \(1 \cdot 0 = 0\)  
[C] \(1 \cdot x = x\)  
[D] \(\frac{x \cdot 1}{x} = 1\)

412. How many different 6-letter arrangements can be formed using the letters in the word “ABSENT,” if each letter is used only once?

[A] 36  
[B] 46,656  
[C] 720  
[D] 6

413. One of the roots of the equation \(x^2 + 3x - 18 = 0\) is 3. What is the other root?

[A] -21  
[B] 15  
[C] 6  
[D] -6

414. The ages of five children in a family are 3, 3, 5, 8, and 18. Which statement is true for this group of data?

[A] mode > mean  
[B] median > mean  
[C] median = mode  
[D] mean > median

415. The Edison Lightbulb Company tests 5% of their daily production of lightbulbs. If 500 bulbs were tested on Tuesday, what was the total number of bulbs produced that day?

[A] 1,000  
[B] 100,000  
[C] 25  
[D] 10,000

416. If \((x - 4)\) is a factor of \(x^2 - x - w = 0\), then the value of \(w\) is

[A] -3  
[B] 3  
[C] -12  
[D] 12

417. As shown in the accompanying diagram, a ladder is leaning against a vertical wall, making an angle of 70° with the ground and reaching a height of 10.39 feet on the wall. Find, to the nearest foot, the length of the ladder. Find, to the nearest foot, the distance from the base of the ladder to the wall.

418. The accompanying Venn diagram shows the number of students who take various courses. All students in circle A take mathematics. All in circle B take science. All in circle C take technology. What percentage of the students take mathematics or technology?

419. What is the perimeter of an equilateral triangle whose height is \(2\sqrt{3}\)?

[A] 12  
[B] 6  
[C] \(6\sqrt{3}\)  
[D] \(12\sqrt{3}\)
420. At a school fair, the spinner represented in the accompanying diagram is spun twice.

![Spinner Diagram]

What is the probability that it will land in section $G$ the first time and then in section $B$ the second time?

- [A] $\frac{1}{16}$
- [B] $\frac{1}{8}$
- [C] $\frac{1}{4}$
- [D] $\frac{1}{2}$

421. On the accompanying square, draw all the lines of symmetry.

![Square Diagram]

422. If $a < b$, $c < d$, and $a$, $b$, $c$, and $d$ are all greater than 0, which expression is always true?

- [A] $a + c > b + d$
- [B] $ac < bd$
- [C] $\frac{a}{d} > \frac{b}{c}$
- [D] $a - c + b - d = 0$

423. If $x = 2a - b^2$, then $a$ equals

- [A] $\frac{x + b^2}{2}$
- [B] $\frac{b^2 - x}{2}$
- [C] $\frac{x - b^2}{2}$
- [D] $x + b^2$

424. Which expression is equivalent to $x^{-1} \cdot y^2$?

- [A] $\frac{x}{y^2}$
- [B] $\frac{y^2}{x}$
- [C] $xy^2$
- [D] $x y^{-2}$

425. Two health clubs offer different membership plans. The graph below represents the total cost of belonging to Club $A$ and Club $B$ for one year.

![Health Club Fees Graph]

a. If the yearly cost includes a membership fee plus a monthly charge, what is the membership fee for Club $A$?

b. (1) What is the number of the month when the total cost is the same for both clubs?
   (2) What is the total cost for Club $A$ when both plans are the same?

c. What is the monthly charge for Club $B$?
426. The accompanying diagram shows the results of a survey asking which sports the members of the Key Club watch on television.

Which statement or statements are true?
I  The most watched sport is tennis.
II  The least watched sport is baseball.
III  More Key Club members watch tennis than football.

[A] II, only  [B] I, only
[C] I and II, only  [D] II and III, only

427. In the accompanying diagram, line $\ell_1$ is parallel to line $\ell_2$.

Which term describes the locus of all points that are equidistant from line $\ell_1$ and $\ell_2$?

[A] line  [B] circle
[C] rectangle  [D] point

428. In the accompanying figure, what is one pair of alternate interior angles?

[A] $\angle 1$ and $\angle 2$  [B] $\angle 6$ and $\angle 8$
[C] $\angle 4$ and $\angle 6$  [D] $\angle 4$ and $\angle 5$

429. Solve for $x$: $15x - 3(3x + 4) = 6$

[A] $-\frac{1}{2}$  [B] $\frac{1}{3}$  [C] 3  [D] 1

430. A box contains six black balls and four white balls. What is the probability of selecting a black ball at random from the box?

[A] $\frac{6}{4}$  [B] $\frac{6}{10}$  [C] $\frac{1}{10}$  [D] $\frac{4}{6}$

431. A stop sign in the shape of a regular octagon is resting on a brick wall, as shown in the accompanying diagram.

What is the measure of angle $x$?

[A] $60^\circ$  [B] $45^\circ$  [C] $120^\circ$  [D] $135^\circ$
432. The ratio of two supplementary angles is 2:7. What is the measure of the smaller angle?


433. The volume of a rectangular pool is 1,080 cubic meters. Its length, width, and depth are in the ratio 10:4:1. Find the number of meters in each of the three dimensions of the pool.

434. The equation \( P = 2L + 2W \) is equivalent to

[A] \( 2L = \frac{P}{2W} \)  [B] \( L = P - W \)

[C] \( L = \frac{P + 2W}{2} \)  [D] \( L = \frac{P - 2W}{2} \)

435. Solve for \( x \): \( x^2 + 2x - 24 = 0 \)

436. A bookshelf contains six mysteries and three biographies. Two books are selected at random without replacement.

a What is the probability that both books are mysteries?

b What is the probability that one book is a mystery and the other is a biography?

437. Which statement best illustrates the additive identity property?

[A] \( 6 + (-6) = 0 \)  [B] \( 6 + 2 = 2 + 6 \)

[C] \( 6 + 0 = 6 \)  [D] \( 6(2) = 2(6) \)

438. What is the solution set of the equation \( \frac{x}{5} + \frac{x}{2} = 14 \) ?

[A] \{10\}  [B] \{20\}  [C] \{4\}  [D] \{49\}

439. A rocket is launched from the ground and follows a parabolic path represented by the equation \( y = -x^2 + 10x \). At the same time, a flare is launched from a height of 10 feet and follows a straight path represented by the equation \( y = -x + 10 \). Using the accompanying set of axes, graph the equations that represent the paths of the rocket and the flare, and find the coordinates of the point or points where the paths intersect.

440. Mario paid $44.25 in taxi fare from the hotel to the airport. The cab charged $2.25 for the first mile plus $3.50 for each additional mile. How many miles was it from the hotel to the airport?

441. Rashawn bought a CD that cost $18.99 and paid $20.51, including sales tax. What was the rate of the sales tax?
   [A] 8%  [B] 2%  [C] 5%  [D] 3%

442. If \( x \neq 0, \) then \( \frac{(x^2)^3}{x^5} \cdot 1000 \) is equivalent to
   [A] 1000  [B] 1000x  
   [C] 1000 + x  [D] 0

443. Which statement is logically equivalent to the statement "If Corey worked last summer, he buys a car"?
   [A] If Corey does not buy a car, he did not work last summer.
   [B] If Corey did not work last summer, he does not buy a car.
   [C] If you are an elephant, then you forget.
   [D] If Corey buys a car, he worked last summer.

444. Which statement is logically equivalent to the statement "If you are an elephant, then you do not forget"?
   [A] If you do not forget, then you are an elephant.
   [B] If you are an elephant, then you forget.
   [C] If you forget, then you are not an elephant.
   [D] If you do not forget, then you are not an elephant.

445. In the accompanying diagram, a ladder leaning against a building makes an angle of 58° with level ground. If the distance from the foot of the ladder to the building is 6 feet, find, to the nearest foot, how far up the building the ladder will reach.

446. The expression \( 90 \cdot 40 - 8 \cdot 18 \) simplifies to

447. The volume of a cube is 64 cubic inches. Its total surface area, in square inches, is

448. What is the contrapositive of the statement "If I study, then I pass the test"?
   [A] If I do not study, then I do not pass the test.
   [B] I pass the test if I study.
   [C] If I pass the test, then I study.
   [D] If I do not pass the test, then I do not study.
449. In the accompanying diagram, \( \triangle ABC \) is similar to but not congruent to \( \triangle A'B'C' \). Which transformation is represented by \( \triangle A'B'C' \)?

[C] rotation  [D] dilation

450. If the temperature in Buffalo is 23° Fahrenheit, what is the temperature in degrees Celsius? [Use the formula \( C = \frac{5}{9}(F - 32) \).]


451. The equation \( A = \frac{1}{2}(12)(3 + 7) \) is used to find the area of a trapezoid. Which calculation would not result in the correct area?

[A] 6(3+7)  [B] \( \frac{12}{2} \times \frac{10}{2} \)  
[C] 0.5(12)(10)  [D] \( \frac{12(3+7)}{2} \)

452. What is the sum of \( \frac{2}{x} \) and \( \frac{x}{2} \)?

[A] \( \frac{4+x^2}{2x} \)  [B] \( \frac{2+x}{2x} \)  
[C] 1  [D] \( \frac{4+x}{2x} \)

453. The accompanying diagram shows a section of the city of Tacoma. High Road, State Street, and Main Street are parallel and 5 miles apart. Ridge Road is perpendicular to the three parallel streets. The distance between the intersection of Ridge Road and State Street and where the railroad tracks cross State Street is 12 miles. What is the distance between the intersection of Ridge Road and Main Street and where the railroad tracks cross Main Street?

454. In the addition table for a subset of real numbers shown below, which number is the inverse of 3? Explain your answer.

\[
\begin{array}{c|cccc}
\oplus & 1 & 2 & 3 & 4 \\
1 & 2 & 3 & 4 & 1 \\
2 & 3 & 4 & 1 & 2 \\
3 & 4 & 1 & 2 & 3 \\
4 & 1 & 2 & 3 & 4 \\
\end{array}
\]
455. The formula for changing Celsius (C) temperature to Fahrenheit (F) temperature is 
\[ F = \frac{9}{5}C + 32 \]. Calculate, to the nearest degree, the Fahrenheit temperature when the Celsius temperature is -8.

456. Which phrase does not describe a triangle?

457. What is the value of \( x \) in the equation
\[ \frac{x}{2} + \frac{x}{6} = 2 \]?
[A] 12  [B] \( \frac{1}{4} \)  [C] 8  [D] 3

458. The ratio of two supplementary angles is 3:6. What is the measure of the smaller angle?

459. In a hockey league, 87 players play on seven different teams. Each team has at least 12 players. What is the largest possible number of players on any one team?

460. The image of point \( A \) after a dilation of 3 is (6,15). What was the original location of point \( A \)?
[A] (18,45)  [B] (3,12)  [C] (2,5)  [D] (9,18)

461. The expression \( 2\sqrt{50} - \sqrt{2} \) is equivalent to
[A] \( 2\sqrt{48} \)  [B] \( 9\sqrt{2} \)  [C] 10  [D] \( 49\sqrt{2} \)

462. Bob and Latoya both drove to a baseball game at a college stadium. Bob lives 70 miles from the stadium and Latoya lives 60 miles from it, as shown in the accompanying diagram. Bob drove at a rate of 50 miles per hour, and Latoya drove at a rate of 40 miles per hour. If they both left home at the same time, who got to the stadium first?

463. Line \( P \) and line \( C \) lie on a coordinate plane and have equal slopes. Neither line crosses the second or third quadrant. Lines \( P \) and \( C \) must
[A] form an angle of 45°  [B] be perpendicular  [C] be vertical  [D] be horizontal

464. The amount of time, \( t \), in seconds, it takes an object to fall a distance, \( d \), in meters, is expressed by the formula 
\[ t = \sqrt{\frac{d}{4.9}} \].

Approximately how long will it take an object to fall 75 meters?
[A] 0.26 sec  [B] 3.9 sec  [C] 7.7 sec  [D] 2.34 sec
465. Expressed in its simplest form, 
\((3x^3)(2y)^2(4x^4)\) is equivalent to

[A] \(24x^{12}y^2\)  
[B] \(24x^7y^2\)  
[C] \(48x^7y^2\)  
[D] \(48x^{12}y^2\)

466. On the accompanying set of axes, graph and label the following lines:

\(y = 5\)
\(x = -4\)
\(y = \frac{5}{4}x + 5\)

Calculate the area, in square units, of the triangle formed by the three points of intersection.

467. The formula for the volume of a right circular cylinder is \(V = \pi r^2h\). The value of \(h\) can be expressed as

[A] \(\frac{V}{\pi r^2}\)  
[B] \(V - \pi r^2\)  
[C] \(\frac{\pi r^2}{V}\)  
[D] \(\frac{V}{\pi r^2}\)

468. What is the additive inverse of \(\frac{2}{3}\)?

[A] \(-\frac{3}{2}\)  
[B] \(\frac{3}{2}\)  
[C] \(\frac{1}{3}\)  
[D] \(-\frac{2}{3}\)

469. At a concert, $720 was collected for hot dogs, hamburgers, and soft drinks. All three items sold for $1.00 each. Twice as many hot dogs were sold as hamburgers. Three times as many soft drinks were sold as hamburgers. The number of soft drinks sold was

[A] 480  
[B] 240  
[C] 120  
[D] 360

470. The weights of all the students in grade 9 are arranged from least to greatest. Which statistical measure separates the top half of this set of data from the bottom half?

[A] average  
[B] mean  
[C] mode  
[D] median

471. What is the total number of points equidistant from two intersecting straight roads and also 300 feet from the traffic light at the center of the intersection?

[A] 2  
[B] 0  
[C] 4  
[D] 1

472. The expression \(0.62 \times 10^3\) is equivalent to

[A] \(6.2 \times 10^4\)  
[B] \(6.2 \times 10^2\)  
[C] 62,000  
[D] 0.062

473. Solve for all values of \(x\) that satisfy the equation \(\frac{x}{x + 3} = \frac{5}{x + 7}\).
474. Which equation represents a line that is parallel to the line whose equation is \(2x + 3y = 12?\)

[A] \(4x - 6y = 2\)  
[B] \(6y - 4x = 2\)  
[C] \(6y + 4x = 2\)  
[D] \(6x + 4y = -2\)

475. A circular garden has a diameter of 12 feet. How many bags of topsoil must Linda buy to cover the garden if one bag covers an area of 3 square feet?

[A] 40  
[B] 13  
[C] 151  
[D] 38

476. The approximate number of seconds in a year is 32,000,000. When this number is written in scientific notation, the numerical value of the exponent is

[A] -7  
[B] 6  
[C] 7  
[D] 8

477. What is the value of \(x\) in the equation \(\frac{3}{4}x + 2 = \frac{5}{4}x - 6?\)

[A] -4  
[B] 16  
[C] -16  
[D] 4

478. A girl can ski down a hill five times as fast as she can climb up the same hill. If she can climb up the hill and ski down in a total of 9 minutes, how many minutes does it take her to climb up the hill?

[A] 7.5  
[B] 1.8  
[C] 7.2  
[D] 4.5

479. What is the value of \(w\) in the equation \(\frac{3}{4}w + 8 = \frac{1}{3}w - 7?\)

[A] -36  
[B] -0.2  
[C] -13.846  
[D] 2.4

480. Which ordered pair is not in the solution set of \(y > 2x + 1?\)

[A] (1,6)  
[B] (1,4)  
[C] (2,5)  
[D] (3,8)

481. Which number is rational?

[A] \(\sqrt{7}\)  
[B] \(\frac{5}{4}\)  
[C] \(\pi\)  
[D] \(\frac{3}{\sqrt{2}}\)

482. If \(3.85 \times 10^6\) is divided by \(385 \times 10^4\), the result is

[A] 0.01  
[B] 1  
[C] 3.85 \(\times 10^{10}\)  
[D] 3.85 \(\times 10^4\)

483. If \(7x + 2a = 3x + 5a\), then \(x\) is equivalent to

[A] \(\frac{3a}{4}\)  
[B] \(\frac{3a}{10}\)  
[C] \(\frac{7a}{4}\)  
[D] \(\frac{7a}{10}\)

484. In the accompanying diagram, \(\overline{CD} \parallel \overline{EF}\), \(\overline{AB}\) is a transversal, \(m\angle DGH = 2x\), and \(m\angle FHB = 5x - 51\). Find the measure, in degrees, of \(\angle BHE\).
485. Which expression is rational?

[A] \( \sqrt{3} \)  [B] \( \pi \)  [C] \( \frac{\sqrt{1}}{4} \)  [D] \( \frac{\sqrt{1}}{2} \)

486. If \( x > 0 \), the expression \((\sqrt{x})(\sqrt{2x})\) is equivalent to

[A] \( 2x \)  [B] \( x\sqrt{2} \)  [C] \( \sqrt{2x} \)  [D] \( x^2\sqrt{2} \)

487. Factored completely, the expression \( 2y^2 + 12y - 54 \) is equivalent to

[A] \( 2(y + 9)(y - 3) \)  [B] \( 2(y - 3)(y - 9) \)  [C] \( (y + 6)(2y - 9) \)  [D] \( (2y + 6)(y - 9) \)

488. If \( 9x + 2a = 3a - 4x \), then \( x \) equals

[A] \( \frac{a}{13} \)  [B] \( a \)  [C] \( \frac{5a}{12} \)  [D] \( -a \)

489. What is the converse of the statement "If it is Sunday, then I do not go to school"?

[A] If it is not Sunday, then I do not go to school.
[B] If it is not Sunday, then I go to school.
[C] If I go to school, then it is not Sunday.
[D] If I do not go to school, then it is Sunday.

490. What is the value of \( x \) in the equation \( 13x - 2(x + 4) = 8x + 1 \)?


491. When \( \sqrt{72} \) is expressed in simplest \( a\sqrt{b} \) from, what is the value of \( a \)?

[A] 3  [B] 8  [C] 2  [D] 6

492. In which of the accompanying figures are segments \( XY \) and \( YZ \) perpendicular?

[A] neither figure 1 nor figure 2  [B] figure 2 only  [C] figure 1, only  [D] both figure 1 and figure 2

493. In the accompanying diagram of \( \triangle ABC \), \( AB \) is extended to \( D \), exterior angle \( CBD \) measures \( 145^\circ \), and \( m\angle C = 75^\circ \).

What is \( m\angle CAB \)?


494. Which ordered pair is the solution of the following system of equations?

\[
\begin{align*}
3x + 2y &= 4 \\
-2x + 2y &= 24
\end{align*}
\]

[A] (-4,-8)  [B] (2,-1)  [C] (-4,8)  [D] (2,-5)
495. Point $P$ is located on $AB$.
   a. Describe the locus of points that are
      (1) 3 units from $AB$
      (2) 5 units from point $P$
   b. How many points satisfy both conditions in part a?

496. In the accompanying diagram of parallelogram $ABCD$, diagonals $AC$ and $BD$ intersect at $E$, $BE = \frac{2}{3}x$, and $ED = x - 10$.

What is the value of $x$?

497. Tara buys two items that cost $d$ dollars each. She gives the cashier $20. Which expression represents the change she should receive?
[A] $20 + 2d$  [B] $20 - 2d$
[C] $2d - 20$  [D] $20 - d$

498. In the coordinate plane, the points (2,2) and (2,12) are the endpoints of a diameter of a circle. What is the length of the radius of the circle?

499. The expression $3^2 \cdot 3^3 \cdot 3^4$ is equivalent to
   [A] $27^{24}$  [B] $3^9$  [C] $3^{24}$  [D] $27^9$

500. If $x^3 < x < \frac{1}{x}$, then $x$ could be equal to
   [A] $\frac{1}{5}$  [B] $\frac{6}{5}$  [C] 1  [D] 5

501. Jeremy's bedroom has two doors leading into the hallway. His house has four doors leading to the outside. Using the doorways, in how many different ways can Jeremy leave his room and go outside?

502. Given the statement: "If two lines are cut by a transversal so that the corresponding angles are congruent, then the lines are parallel."
What is true about the statement and its converse?
[A] The statement and its converse are both true.
[B] The statement is false, but its converse is true.
[C] The statement is true, but its converse is false.
[D] The statement and its converse are both false.

503. The sum of $\sqrt{18}$ and $\sqrt{72}$ is
   [A] $\sqrt{90}$  [B] $3\sqrt{10}$
   [C] $9\sqrt{2}$  [D] $6\sqrt{3}$
504. In the accompanying diagram, right triangle $ABC$ is inscribed in circle $O$, diameter $AB = 26$, and $CB = 10$. Find, to the nearest square unit, the area of the shaded region.

505. Factor completely: $5n^2 - 80$

506. Seth has one less than twice the number of compact discs (CDs) that Jason has. Raoul has 53 more CDs than Jason has. If Seth gives Jason 25 CDs, Seth and Jason will have the same number of CDs. How many CDs did each of the three boys have to begin with?

507. What is the image of point (-3, 4) under the translation that shifts $(x,y)$ to $(x - 3, y + 2)$?

[A] (-6,6) [B] (0,6)
[C] (6,6) [D] (-6,8)

508. On a bookshelf, there are five different mystery books and six different biographies. How many different sets of four books can Emilio choose if two of the books must be mystery books and two of the books must be biographies?

509. The direct distance between city $A$ and city $B$ is 200 miles. The direct distance between city $B$ and city $C$ is 300 miles. Which could be the direct distance between city $C$ and city $A$?

[C] 50 miles [D] 650 miles

510. The expression $(2x^2 + 6x + 5) - (6x^2 + 3x + 5)$ is equivalent to

[A] $-4x^2 - 3x + 10$ [B] $-4x^2 + 3x$
[C] $4x^2 + 3x - 10$ [D] $4x^2 - 3x$

511. $M$ is the midpoint of $AB$. If the coordinates of $A$ are (-1,5) and the coordinates of $M$ are (3,3), what are the coordinates of $B$?

[A] (1,4) [B] (2,8)
[C] (-5,7) [D] (7,1)

512. Which point is on the circle whose equation is $x^2 + y^2 = 289$?

[A] (7,-10) [B] (-12,12)
[C] (8,-15) [D] (-1,-16)

513. If the area of a square garden is 48 square feet, what is the length, in feet, of one side of the garden?

[A] $16\sqrt{3}$ [B] $4\sqrt{3}$
[C] $4\sqrt{6}$ [D] $12\sqrt{2}$
514. Which expression represents the number of yards in $x$ feet?

- [A] $\frac{x}{3}$
- [B] $12x$
- [C] $3x$
- [D] $\frac{x}{12}$

515. Mr. Santana wants to carpet exactly half of his rectangular living room. He knows that the perimeter of the room is 96 feet and that the length of the room is 6 feet longer than the width. How many square feet of carpeting does Mr. Santana need?

516. The accompanying histogram shows the heights of the students in Kyra's health class.

What is the total number of students in the class?

- [A] 209
- [B] 16
- [C] 15
- [D] 5

517. A builder is building a rectangular deck with dimensions of 16 feet by 30 feet. To ensure that the sides form $90^\circ$ angles, what should each diagonal measure?

- [A] 34 ft
- [B] 46 ft
- [C] 16 ft
- [D] 30 ft

519. If the instructions for cooking a turkey state "Roast turkey at $325^\circ$ for 20 minutes per pound," how many hours will it take to roast a 20-pound turkey at $325^\circ$?

520. Given the true statement: "If a person is eligible to vote, then that person is a citizen." Which statement must also be true?

- [A] Marie is not eligible to vote; therefore, she is not a citizen.
- [B] Kayla is not a citizen; therefore, she is not eligible to vote.
- [C] Juan is a citizen; therefore, he is eligible to vote.
- [D] Morgan has never voted; therefore, he is not a citizen.

521. In the accompanying diagram, $\overline{AB} \parallel \overline{CD}$. From point $E$ on $\overline{AB}$, transversals $\overline{EF}$ and $\overline{EG}$ are drawn, intersecting $\overline{CD}$ at $H$ and $I$, respectively.

If $m\angle CHF = 20$ and $m\angle DIG = 60$, what is $m\angle HEI$?

- [A] 100
- [B] 60
- [C] 120
- [D] 80
522. Leo purchased five shirts, three pairs of pants, and four pairs of shoes. Which expression represents how many different outfits consisting of one shirt, one pair of pants, and one pair of shoes Leo can make?

[A] \( \binom{12}{3} \)  \[B\] \( 5 + 3 + 4 \)  
[C] \( \binom{12}{3} \)  \[D\] \( 5 \cdot 3 \cdot 4 \)

523. The Rivera family bought a new tent for camping. Their old tent had equal sides of 10 feet and a floor width of 15 feet, as shown in the accompanying diagram.

If the new tent is similar in shape to the old tent and has equal sides of 16 feet, how wide is the floor of the new tent?

524. A plot of land is in the shape of rhombus \( ABCD \) as shown below.

Which can not be the length of diagonal \( AC \)?

[A] 18 m  \[B\] 4 m  \[C\] 11 m  \[D\] 24 m

525. Which equation represents the locus of all points 5 units below the \( x \)-axis?

[A] \( y = 5 \)  \[B\] \( x = 5 \)  
[C] \( y = -5 \)  \[D\] \( x = -5 \)

526. Mr. James wanted to plant a garden that would be in the shape of a rectangle. He was given 80 feet of fencing to enclose his garden. He wants the length to be 10 feet more than twice the width. What are the dimensions, in feet, for a rectangular garden that will use exactly 80 feet of fencing?

527. The number 0.14114111411114 . . . is

[A] irrational  \[B\] integral  
[C] whole  \[D\] rational

528. A straight line with slope 5 contains the points (1,2) and (3, \( K \)). Find the value of \( K \). [The use of the accompanying grid is optional.]
529. The mean (average) weight of three dogs is 38 pounds. One of the dogs, Sparky, weighs 46 pounds. The other two dogs, Eddie and Sandy, have the same weight. Find Eddie's weight.

530. Find three consecutive odd integers such that the product of the first and the second exceeds the third by 8.

531. The cross section of an attic is in the shape of an isosceles trapezoid, as shown in the accompanying figure. If the height of the attic is 9 feet, $BC = 12$ feet, and $AD = 28$ feet, find the length of $AB$ to the nearest foot.

532. If $3(x - 2) = 2x + 6$, the value of $x$ is


533. Given the true statement "John is not handsome" and the false statement "John is handsome or smart." Determine the truth value for the statement "John is smart."

534. In the accompanying diagram of parallelogram $ABCD$, diagonals $\overline{AC}$ and $\overline{DB}$ intersect at $E$, $AE = 3x - 4$, and $EC = x + 12$.

What is the value of $x$?


535. In the accompanying diagram, point $P$ lies 3 centimeters from line $\ell$.

How many points are both 2 centimeters from line $\ell$ and 1 centimeter from point $P$?

[A] 2  [B] 1  [C] 0  [D] 4

536. Jordan and Missy are standing together in the schoolyard. Jordan, who is 6 feet tall, casts a shadow that is 54 inches long. At the same time, Missy casts a shadow that is 45 inches long. How tall is Missy?

[A] 38 in  [B] 5 ft  
[C] 86.4 in  [D] 5 ft 6 in
537. If the expression \(3 - 4^2 + \frac{6}{2}\) is evaluated, what would be done last?
   [A] subtracting  [B] adding  
   [C] squaring  [D] dividing

538. The distance between parallel lines \(\ell\) and \(m\) is 12 units. Point \(A\) is on line \(\ell\). How many points are equidistant from lines \(\ell\) and \(m\) and 8 units from point \(A\).

539. Which point is in the solution set of the system of inequalities shown in the accompanying graph?

   ![Graph](image)

   [A] (-4, 1)  [B] (2, 4)  
   [C] (4, -1)  [D] (0, 4)

540. Arielle has a collection of grasshoppers and crickets. She has 561 insects in all. The number of grasshoppers is twice the number of crickets. Find the number of each type of insect that she has.

   a Find the area of the shaded region.  
   b Write an expression for the area of the rectangle \(ABCD\) in terms of \(x\).
546. The expression $-\lvert -7 \rvert$ is equivalent to

[A] 7  [B] -7  [C] 0  [D] 1

547. Solve the following system of equations algebraically or graphically for $x$ and $y$:

\[ y = x^2 + 2x - 1 \]
\[ y = 3x + 5 \]

For an algebraic solution, show your work here.
For a graphic solution, show your work here.

548. Express both the perimeter and the area of the rectangle shown in the accompanying diagram as polynomials in simplest form.

549. A school district offers hockey and basketball. The result of a survey of 300 students showed:
120 students play hockey, only
90 students play basketball, only
30 students do not participate in either sport
Of those surveyed, how many students play both hockey and basketball?

550. José wants to build a triangular pen for his pet rabbit. He has three lengths of boards already cut that measure 7 feet, 8 feet, and 16 feet. Explain why José cannot construct a pen in the shape of a triangle with sides of 7 feet, 8 feet, and 16 feet.

551. In the coordinate plane, what is the total number of points 5 units from the origin and equidistant from both the $x$- and $y$-axes?

[A] 1  [B] 0  [C] 2  [D] 4

552. A 10-foot ladder is to be placed against the side of a building. The base of the ladder must be placed at an angle of 72° with the level ground for a secure footing. Find, to the nearest inch, how far the base of the ladder should be from the side of the building and how far up the side of the building the ladder will reach.

553. Which letter has point symmetry?

554. In the accompanying diagram, a rectangular container with the dimensions 10 inches by 15 inches by 20 inches is to be filled with water, using a cylindrical cup whose radius is 2 inches and whose height is 5 inches. What is the maximum number of full cups of water that can be placed into the container without the water overflowing the container?

555. Tori computes the value of $8 \times 95$ in her head by thinking $8(100 - 5) = 8 \times 100 - 8 \times 5$. Which number property is she using?

[A] associative  [B] distributive  
[C] closure  [D] commutative

556. The midpoint $M$ of line segment $AB$ has coordinates (-3,4). If point $A$ is the origin, (0,0), what are the coordinates of point $B$? [The use of the accompanying grid is optional.]

557. Three times as many robins as cardinals visited a bird feeder. If a total of 20 robins and cardinals visited the feeder, how many robins?


558. A rectangular garden is going to be planted in a person's rectangular backyard, as shown in the accompanying diagram. Some dimensions of the backyard and the width of the garden are given. Find the area of the garden to the nearest square foot.

559. If the value of dependent variable $y$ increases as the value of independent variable $x$ increases, the graph of this relationship could be a

[A] horizontal line  [B] vertical line  
[C] line with a positive slope  [D] line with a negative slope

560. Using only 32-cent and 20-cent stamps, Charlie put $3.36 postage on a package he sent to his sister. He used twice as many 32-cent stamps as 20-cent stamps. Determine how many of each type of stamp he used.
561. As shown in the accompanying diagram, the length, width, and height of Richard's fish tank are 24 inches, 16 inches, and 18 inches, respectively. Richard is filling his fish tank with water from a hose at the rate of 500 cubic inches per minute. How long will it take, to the nearest minute, to fill the tank to a depth of 15 inches?

![Fish Tank Diagram](image)

562. John, Dan, Karen, and Beth went to a costume ball. They chose to go as Anthony and Cleopatra, and Romeo and Juliet. John got the costumes for Romeo and Cleopatra, but not his own costume. Dan saw the costumes for Juliet and himself. Karen went as Anthony. Beth drove two of her friends, who were dressed as Anthony and Cleopatra, to the ball. What costume did John wear?

563. What is the value of \( \frac{8!}{4!} \)?


564. Tom throws a ball into the air. The ball travels on a parabolic path represented by the equation \( h = -8t^2 + 40t \), where \( h \) is the height, in feet, and \( t \) is the time, in seconds.

\[ a \] On the accompanying set of axes, graph the equation from \( t = 0 \) to \( t = 5 \) seconds, including all integral values of \( t \) from 0 to 5.

\[ b \] What is the value of \( t \) at which \( h \) has its greatest value?

565. There were 100 more balcony tickets than main-floor tickets sold for a concert. The balcony tickets sold for $4 and the main-floor tickets sold for $12. The total amount of sales for both types of tickets was $3,056.

\[ a \] Write an equation or a system of equations that describes the given situation. Define the variables.

\[ b \] Find the number of balcony tickets that were sold.
566. What is the total number of points of intersection of the graphs of the equations \( x^2 + y^2 = 16 \) and \( y = x \)?


567. In the accompanying diagram of a construction, what does \( \overline{PC} \) represent?

[A] a median drawn to \( \overline{AB} \)
[B] the perpendicular bisector of \( \overline{AB} \)
[C] the bisector of \( \angle APB \)
[D] an altitude drawn to \( \overline{AB} \)

568. A woman has a ladder that is 13 feet long. If she sets the base of the ladder on level ground 5 feet from the side of a house, how many feet above the ground will the top of the ladder be when it rests against the house?


569. When \( 3x^2 - 2x + 1 \) is subtracted from \( 2x^2 + 7x + 5 \), the result will be

[A] \( x^2 - 9x - 4 \)  [B] \( -x^2 + 5x + 6 \)
[C] \( x^2 + 5x + 6 \)  [D] \( -x^2 + 9x + 4 \)

570. Which letter below has point symmetry, but does not have line symmetry?


571. The sum of \( 3x^2 + x + 8 \) and \( x^2 - 9 \) can be expressed as

[A] \( 3x^4 + x - 1 \)  [B] \( 4x^2 + x - 17 \)
[C] \( 4x^4 + x - 1 \)  [D] \( 4x^2 + x - 1 \)

572. In the accompanying diagram, a circle with radius 4 is inscribed in a square.

What is the area of the shaded region?

[A] \( 64\pi - 8\pi \)  [B] \( 16 - 8\pi \)
[C] \( 16 - 16\pi \)  [D] \( 64 - 16\pi \)

573. Which number is irrational?

[A] \( \frac{2}{3} \)  [B] \( \sqrt{9} \)  [C] 0.3333  [D] \( \sqrt{8} \)

574. The expression \( (50x^3 - 60x^2 + 10x) \div 10x \) is equivalent to

[A] \( 5x^2 - 60x^2 + 10x \)  [B] \( 5x^2 - 6x \)
[C] \( 5x^3 - 6x^2 + x \)  [D] \( 5x^2 - 6x + 1 \)
575. A treasure map shows a treasure hidden in a park near a tree and a statue. The map indicates that the tree and the statue are 10 feet apart. The treasure is buried 7 feet from the base of the tree and also 5 feet from the base of the statue. How many places are possible locations for the treasure to be buried? Draw a diagram of the treasure map, and indicate with an \( \times \) each possible location of the treasure.

576. The plot of land illustrated in the accompanying diagram has a perimeter of 34 yards. Find the length, in yards, of each side of the figure. Could these measures actually represent the measures of the sides of a triangle? Explain your answer.

577. The expression \( \frac{6\sqrt{20}}{3\sqrt{5}} \) is equivalent to

[A] \( 3\sqrt{15} \)  [B] 4  [C] 8  [D] \( 2\sqrt{15} \)

578. The owner of a movie theater was counting the money from 1 day's ticket sales. He knew that a total of 150 tickets were sold. Adult tickets cost $7.50 each and children's tickets cost $4.75 each. If the total receipts for the day were $891.25, how many of each kind of ticket were sold?

579. While solving the equation \( 4(x + 2) = 28 \), Becca wrote \( 4x + 8 = 28 \). Which property did she use?

[A] identity  [B] distributive  
[C] associative  [D] commutative

580. Three roses will be selected for a flower vase. The florist has 1 red rose, 1 white rose, 1 yellow rose, 1 orange rose and 1 pink rose from which to choose.

a How many different three rose selections can be formed from the 5 roses? 
b What is the probability that 3 roses selected at random will contain 1 red rose, 1 white rose, and 1 pink rose? 
c What is the probability that 3 roses selected at random will not contain an orange rose?

581. Which expression is an example of the associative property?

[A] \( (x + y) + z = x + (y + z) \)  
[B] \( x(y + z) = xy + xz \)  
[C] \( x \cdot 1 = x \)  
[D] \( x + y + z = z + y + x \)

582. In his will, a man leaves one-half of his money to his wife, one-half of what is then left to his older child, and one-half of what is then left to his younger child. His two cousins divide the remainder equally, each receiving $2,000. What was the total amount of money in the man's will?

[A] $24,000  
[B] $16,000  
[C] $32,000  
[D] $40,000
583. When Tony received his weekly allowance, he decided to purchase candy bars for all his friends. Tony bought three Milk Chocolate bars and four Creamy Nougat bars, which cost a total of $4.25 without tax. Then he realized this candy would not be enough for all his friends, so he returned to the store and bought an additional six Milk Chocolate bars and four Creamy Nougat bars, which cost a total of $6.50 without tax. How much did each type of candy bar cost?

584. Javon's homework is to determine the dimensions of his rectangular backyard. He knows that the length is 10 feet more than the width, and the total area is 144 square feet. Write an equation that Javon could use to solve this problem. Then find the dimensions, in feet, of his backyard.

585. During a 45-minute lunch period, Albert (A) went running and Bill (B) walked for exercise. Their times and distances are shown in the accompanying graph. How much faster was Albert running than Bill was walking, in miles per hour?

586. Which inequality is represented by the accompanying graph?

[A] $y \leq 3$  
[B] $y < 3$  
[C] $y > 3$  
[D] $y \geq 3$

587. Paul orders a pizza. Chef Carl randomly chooses two different toppings to put on the pizza from the following: pepperoni, onion, sausage, mushrooms, and anchovies. If Paul will not eat pizza with mushrooms, determine the probability that Paul will not eat the pizza Chef Carl has made.

588. What is the solution set of $m^2 - 3m - 10 = 0$?

[A] $\{5,-2\}$  
[B] $\{3,10\}$  
[C] $\{2,-5\}$  
[D] $\{3,-10\}$

589. Two angles are complementary. One angle has a measure that is five times the measure of the other angle. What is the measure, in degrees, of the larger angle?

590. In the set of positive integers, what is the solution set of the inequality $2x - 3 < 5$?

[A] $\{0, 1, 2, 3\}$  
[B] $\{1, 2, 3\}$  
[C] $\{1, 2, 3, 4\}$  
[D] $\{0, 1, 2, 3, 4\}$
591. The sum of the ages of the three Romano brothers is 63. If their ages can be represented as consecutive integers, what is the age of the middle brother?

592. A car travels 110 miles in 2 hours. At the same rate of speed, how far will the car travel in \( h \) hours?

\[
\text{[A]} \quad \frac{h}{220} \quad \text{[B]} \quad 220h \quad \text{[C]} \quad \frac{h}{55} \quad \text{[D]} \quad 55h
\]

593. Line \( \ell \) contains the points (0,4) and (2,0). Show that the point (-25,81) does or does not lie on line \( \ell \).

594. Draw and label a diagram of the path of an airplane climbing at an angle of 11° with the ground. Find, to the nearest foot, the ground distance the airplane has traveled when it has attained an altitude of 400 feet.

595. A tree casts a shadow that is 20 feet long. The angle of elevation from the end of the shadow to the top of the tree is 66°. Determine the height of the tree, to the nearest foot.

596. Which set can \textit{not} represent the lengths of the sides of a triangle?

\[
\text{[A]} \quad \{7,7,12\} \quad \text{[B]} \quad \{4,5,6\} \\
\text{[C]} \quad \{8,8,8\} \quad \text{[D]} \quad \{5,5,11\}
\]

597. During a recent winter, the ratio of deer to foxes was 7 to 3 in one county of New York State. If there were 210 foxes in the county, what was the number of deer in the county?

\[
\text{[A]} \quad 147 \quad \text{[B]} \quad 280 \quad \text{[C]} \quad 90 \quad \text{[D]} \quad 490
\]

598. In a circle whose center is (2,3), one endpoint of a diameter is (-1,5). Find the coordinates of the other endpoint of that diameter. [The use of the accompanying grid is optional.]

599. Megan decides to go out to eat. The menu at the restaurant has four appetizers, three soups, seven entrees, and five desserts. If Megan decides to order an appetizer or a soup, and one entree, and two different desserts, how many different choices can she make?

600. Which expression represents an irrational number?

\[
\text{[A]} \quad 0 \quad \text{[B]} \quad 0.17 \quad \text{[C]} \quad \frac{1}{2} \quad \text{[D]} \quad \sqrt{2}
\]
601. Two triangles are similar. The lengths of the sides of the smaller triangle are 3, 5, and 6, and the length of the longest side of the larger triangle is 18. What is the perimeter of the larger triangle?


602. In right triangle \( ABC \), \( m \angle C = 3y - 10 \), \( m \angle B = y + 40 \), and \( m \angle A = 90 \). What type of right triangle is triangle \( ABC \)?


603. Greg is in a car at the top of a roller-coaster ride. The distance, \( d \), of the car from the ground as the car descends is determined by the equation \( d = 144 - 16t^2 \), where \( t \) is the number of seconds it takes the car to travel down to each point on the ride. How many seconds will it take Greg to reach the ground? For an algebraic solution show your work here. For a graphic solution show your work here.

604. Mr. Perez owns a sneaker store. He bought 350 pairs of basketball sneakers and 150 pairs of soccer sneakers from the manufacturers for $62,500. He sold all the sneakers and made a 25% profit. If he sold the soccer sneakers for $130 per pair, how much did he charge for one pair of basketball sneakers?

605. On the first six tests in her social studies course, Jerelyn's scores were 92, 78, 86, 92, 95, and 91. Determine the median and the mode of her scores. If Jerelyn took a seventh test and raised the mean of her scores exactly 1 point, what was her score on the seventh test?

606. Which equation illustrates the multiplicative identity element?

[A] \( x - x = 0 \)    [B] \( x \cdot 1 = x \)

[C] \( x + 0 = x \)    [D] \( \frac{1}{x} = 1 \)

607. The larger root of the equation \( (x + 4)(x - 3) = 0 \) is


608. A dog is tied with a rope to a stake in the ground. The length of the rope is 5 yards. What is the area, in square yards, in which the dog can roam?

[A] \( 25\pi \)    [B] \( 10\pi \)    [C] 25    [D] 20
609. Which diagram represents the figure with the greatest volume?

[A]  

[B]  

[C]  

[D]  

610. Which polynomial is the quotient of \( \frac{6x^3 + 9x^2 + 3x}{3x} \)?

[A] \( 2x^2 + 3x \)  
[B] \( 6x^2 + 9x \)  
[C] \( 2x + 3 \)  
[D] \( 2x^2 + 3x + 1 \)  

611. If the length of the legs of a right triangle are 5 and 7, what is the length of the hypotenuse?

[A] \( 2\sqrt{3} \)  
[B] \( \sqrt{2} \)  
[C] \( 2\sqrt{6} \)  
[D] \( \sqrt{74} \)  

612. Find all negative odd integers that satisfy the following inequality:  
\(-3x + 1 \leq 17\)  

613. Which equation illustrates the distributive property?

[A] \( 5(a + b) = 5a + 5b \)  
[B] \( a + (b + c) = (a + b) + c \)  
[C] \( a + 0 = a \)  
[D] \( a + b = b + a \)  

614. A recent survey shows that the average man will spend 141,288 hours sleeping, 85,725 hours working, 81,681 hours watching television, 9,945 hours commuting, 1,662 hours kissing, and 363,447 hours on other tasks during his lifetime. What percent of his life, to the nearest tenth of a percent, does he spend sleeping? 

615. Which letter demonstrates line symmetry but not point symmetry?

[A] S  
[B] T  
[C] H  
[D] N  

616. Ms. Brewer's art class is drawing reflected images. She wants her students to draw images reflected in a line. Which diagram represents a correctly drawn image?
617. Virginia has a circular rug on her square living room floor, as represented in the accompanying diagram. If her entire living room floor measures 100 square feet, what is the area of the part of the floor covered by the rug?

![Diagram of a circular rug on a square living room floor]

618. What is the converse of the statement "If it is sunny, I will go swimming"?

[A] If I do not go swimming, then it is not sunny.

[B] If it is not sunny, I will not go swimming.

[C] I will go swimming if and only if it is sunny.

[D] If I go swimming, it is sunny.

619. What is the solution set of the equation 

\[ 3x^2 - 34x - 24 = 0 \] ?

[A] \(-2, 6\)  

[B] \(-6, 2\)  

[C] \(-\frac{2}{3}, 12\)  

[D] \(-12, \frac{2}{3}\)

620. Currently, Tyrone has $60 and his sister has $135. Both get an allowance of $5 each week. Tyrone decides to save his entire allowance, but his sister spends all of hers each week plus an additional $10 each week. After how many weeks will they each have the same amount of money?

[The use of the grid is optional.]

621. Keesha wants to tile the floor shown in the accompanying diagram. If each tile measures 1 foot by 1 foot and costs $2.99, what will be the total cost, including an 8% sales tax, for tiling the floor?
622. A ship on the ocean surface detects a sunken ship on the ocean floor at an angle of depression of 50°. The distance between the ship on the surface and the sunken ship on the ocean floor is 200 meters. If the ocean floor is level in this area, how far above the ocean floor, to the nearest meter, is the ship on the surface?

625. A painting that regularly sells for a price of $55 is on sale for 20% off. The sales tax on the painting is 7%. Will the final total cost of the painting differ depending on whether the salesperson deducts the discount before adding the sales tax or takes the discount after computing the sum of the original price and the sales tax on $55?

623. If $x = -2$ and $y = -1$, which point on the accompanying set of axes represents the translation $(x, y) \rightarrow (x + 2, y - 3)$?

626. Ben had twice as many nickels as dimes. Altogether, Ben had $4.20. How many nickels and how many dimes did Ben have?

624. If $x = 3$, which statement is false?

627. The sum of $3x^2 + 4x - 2$ and $x^2 - 5x + 3$ is

[A] $4x^2 - x - 1$  
[B] $4x^2 + x - 1$

[C] $4x^2 - x + 1$  
[D] $4x^2 + x + 1$

628. When $3x^2 - 8x$ is subtracted from $2x^2 + 3x$, the difference is

[A] $-x^2 - 11x$  
[B] $-x^2 + 11x$

[C] $x^2 - 5x$  
[D] $-x^2 - 5x$

629. Solve for $x$: $3.3 - x = 3(x - 1.7)$

630. A factory packs CD cases into cartons for a music company. Each carton is designed to hold 1,152 CD cases. The Quality Control Unit in the factory expects an error of less than 5% over or under the desired packing number. What is the least number and the most number of CD cases that could be packed in a carton and still be acceptable to the Quality Control Unit?
631. How many different five-digit numbers can be formed from the digits 1, 2, 3, 4, and 5 if each digit is used only once?


632. A set of five quadrilaterals consists of a square, a rhombus, a rectangle, an isosceles trapezoid, and a parallelogram. Lu selects one of these figures at random. What is the probability that both pairs of the figure's opposite sides are parallel?

[A] $\frac{2}{5}$  [B] 1  [C] $\frac{3}{4}$  [D] $\frac{4}{5}$

633. The statement "$x$ is not the square of an integer and $x$ is a multiple of 3" is true when $x$ is equal to


634. How many feet from the base of a house must a 39-foot ladder be placed so that the top of the ladder will reach a point on the house 36 feet from the ground?

635. A person standing on level ground is 2,000 feet away from the foot of a 420-foot-tall building, as shown in the accompanying diagram. To the nearest degree, what is the value of $x$?

636. Tamara has two sisters. One of the sisters is 7 years older than Tamara. The other sister is 3 years younger than Tamara. The product of Tamara's sisters' ages is 24. How old is Tamara?

637. The accompanying graph shows Marie's distance from home ($A$) to work ($F$) at various times during her drive.

a Marie left her briefcase at home and had to return to get it. State which point represents when she turned back around to go home and explain how you arrived at that conclusion.

b Marie also had to wait at the railroad tracks for a train to pass. How long did she wait?

638. Fran's favorite photograph has a length of 6 inches and a width of 4 inches. She wants to have it made into a poster with dimensions that are similar to those of the photograph. She determined that the poster should have a length of 24 inches. How many inches wide will the poster be?
639. In the accompanying diagram, line $\ell$ is parallel to line $m$, and line $t$ is a transversal.

Which must be a true statement?

[A] $m\angle 1 + m\angle 8 = 180$
[B] $m\angle 2 + m\angle 5 = 180$
[C] $m\angle 1 + m\angle 4 = 180$
[D] $m\angle 3 + m\angle 6 = 180$

640. Which transformation does not always result in an image that is congruent to the original figure?

[A] dilation  [B] reflection
[C] rotation  [D] translation

641. The manufacturer of Ron's car recommends that the tire pressure be at least 26 pounds per square inch and less than 35 pounds per square inch. On the accompanying number line, graph the inequality that represents the recommended tire pressure.

642. Sal keeps quarters, nickels, and dimes in his change jar. He has a total of 52 coins. He has three more quarters than dimes and five fewer nickels than dimes. How many dimes does Sal have?


643. Solve for $x$: $x^2 + 3x - 40 = 0$

644. Twenty-five percent of 88 is the same as what percent of 22?

[A] $12\frac{1}{2}$%  [B] 100%
[C] 50%  [D] 40%

645. As shown in the accompanying diagram, radio station KMA is increasing its radio listening radius from 40 miles to 50 miles. How many additional square miles of listening area, to the nearest tenth, will the radio station gain?

646. What is the value of $n$ in the equation $3n - 8 = 32 - n$?

647. The statement "If \( x \) is prime, then it is odd" is false when \( x \) equals


648. What is the sum of \( 6 \times 10^3 \) and \( 3 \times 10^2 \)?

[A] \( 9 \times 10^5 \)  [B] \( 9 \times 10^6 \)  [C] \( 6.3 \times 10^5 \)  [D] \( 18 \times 10^2 \)

649. What is the value of \( n \) in the equation \( 0.6(n+10) = 3.6 \)?

[A] 5  [B] -4  [C] 4  [D] -0.4

650. When \( 3a^2 - 7a + 6 \) is subtracted from \( 4a^2 - 3a + 4 \), the result is

[A] \( a^2 + 4a - 2 \)  [B] \( 7a^2 - 10a + 10 \)  [C] \( a^2 - 10a - 2 \)  [D] \( -a^2 - 4a + 2 \)

651. Dylan says that all isosceles triangles are acute triangles. Mary Lou wants to prove that Dylan is not correct. Sketch an isosceles triangle that Mary Lou could use to show that Dylan's statement is not true. In your sketch, state the measure of each angle of the isosceles triangle.

652. In bowling leagues, some players are awarded extra points called their "handicap." The "handicap" in Anthony's league is 80% of the difference between 200 and the bowler's average. Anthony's average is 145. What is Anthony's "handicap"?

653. The statement "\( x \geq 4 \) and \( 2x - 4 < 6 \)" is true when \( x \) is equal to


654. Seth is thinking of a number between 20 and 30. The number is prime and not more than 2 away from a perfect square. What is the number?

655. Which geometric figure has one and only one line of symmetry?


656. In isosceles triangle \( \triangle DOG \), the measure of the vertex angle is three times the measure of one of the base angles. Which statement about \( \triangle DOG \) is true?

[A] \( \triangle DOG \) is an acute triangle.  
[B] \( \triangle DOG \) is a right triangle.  
[C] \( \triangle DOG \) is a scalene triangle.  
[D] \( \triangle DOG \) is an obtuse triangle.
657. If \( n + 4 \) represents an odd integer, the next larger odd integer is represented by

[A] \( n + 3 \)  \quad [B] \( n + 5 \)  \quad [C] \( n + 2 \)  \quad [D] \( n + 6 \)

658. The world population was 4.2 billion people in 1982. The population in 1999 reached 6 billion. Find the percent of change from 1982 to 1999.

659. Which image represents a line reflection?

[A] \( \begin{array}{l} p \hfill \end{array} \quad \begin{array}{l} p \hfill \end{array} \)  \quad [B] \( \begin{array}{l} p \hfill \end{array} \quad \begin{array}{l} q \hfill \end{array} \)  \quad [C] \( \begin{array}{l} p \hfill \end{array} \quad \begin{array}{l} p \hfill \end{array} \)  \quad [D] \( \begin{array}{l} p \hfill \end{array} \quad \begin{array}{l} q \hfill \end{array} \)

660. The probability that the Cubs win their first game is \( \frac{1}{3} \). The probability that the Cubs win their second game is \( \frac{3}{7} \). What is the probability that the Cubs win both games?

[A] \( \frac{16}{21} \)  \quad [B] \( \frac{2}{5} \)  \quad [C] \( \frac{6}{7} \)  \quad [D] \( \frac{1}{7} \)

661. Stan was trying to guess Melanie's age. She told him her age was an even number and a multiple of three. What could be Melanie's age?

[A] 16  \quad [B] 15  \quad [C] 12  \quad [D] 10

662. The ninth graders at a high school are raising money by selling T-shirts and baseball caps. The number of T-shirts sold was three times the number of caps. The profit they received for each T-shirt sold was $5.00, and the profit on each cap was $2.50. If the students made a total profit of $210, how many T-shirts and how many caps were sold?

663. The school cafeteria offers five sandwich choices, four desserts, and three beverages. How many different meals consisting of one sandwich, one dessert, and one beverage can be ordered?

[A] 60  \quad [B] 12  \quad [C] 3  \quad [D] 1

664. Which expression is equivalent to \( x^{-4} \)?

[A] \( x^4 \)  \quad [B] \(-4x \)  \quad [C] \( \frac{1}{x^4} \)  \quad [D] 0

665. In Jackson County, Wyoming, license plates are made with two letters (\( A \) through \( Z \)) followed by three digits (0 through 9). The plates are made according to the following restrictions:

- the first letter must be \( J \) or \( W \), and the second letter can be any of the 26 letters in the alphabet
- no digit can be repeated

How many different license plates can be made with these restrictions?
666. As seen in the accompanying diagram, a person can travel from New York City to Buffalo by going north 170 miles to Albany and then west 280 miles to Buffalo.

![Diagram](image)

a) If an engineer wants to design a highway to connect New York City directly to Buffalo, at what angle, \( x \), would she need to build the highway? Find the angle to the nearest degree.

b) To the nearest mile, how many miles would be saved by traveling directly from New York City to Buffalo rather than by traveling first to Albany and then to Buffalo?

667. After an ice storm, the following headlines were reported in the *Glacier County Times*:

Monday: Ice Storm Devastates County - 8 out of every 10 homes lose electrical power
Tuesday: Restoration Begins - Power restored to \( \frac{1}{2} \) of affected homes
Wednesday: More Freezing Rain - Power lost by 20% of homes that had power on Tuesday

Based on these headlines, what fractional portion of homes in Glacier County had electrical power on Wednesday?

668. The statement "If \( x \) is divisible by 8, then it is divisible by 6" is false if \( x \) equals


669. From January 3 to January 7, Buffalo recorded the following daily high temperatures: 5°, 7°, 6°, 5°, and 7°. Which statement about the temperatures is true?

[A] mean = mode  [B] mean = median  
[C] mean < median  [D] median = mode

670. In a town election, candidates \( A \) and \( B \) were running for mayor. There were 30,500 people eligible to vote, and \( \frac{3}{4} \) of them actually voted. Candidate \( B \) received \( \frac{1}{3} \) of the votes cast. How many people voted for candidate \( B \)? What percent of the votes cast, to the nearest tenth of a percent, did candidate \( A \) receive?

671. Which coordinate point is in the solution set for the system of inequalities shown in the accompanying graph?

![Graph](image)

[A] (0,1)  [B] (2,2)  
[C] (1,-1)  [D] (3,1)
672. In a recent poll, 600 people were asked whether they liked Chinese food. A circle graph was constructed to show the results. The central angles for two of the three sectors are shown in the accompanying diagram. How many people had no opinion?

673. The formula \( C = \frac{5}{9}(F - 32) \) can be used to find the Celsius temperature \( C \) for a given Fahrenheit temperature \( F \). What Celsius temperature is equal to a Fahrenheit temperature of 77°?

\[ \text{[A]} \ 45° \quad \text{[B]} \ 25° \quad \text{[C]} \ 8° \quad \text{[D]} \ 171° \]

674. Using only a ruler and compass, construct the bisector of angle \( BAC \) in the accompanying diagram.

675. Seventy-eight students participate in one or more of three sports: baseball, tennis, and golf. Four students participate in all three sports; five play both baseball and golf, only; two play both tennis and golf, only; and three play both baseball and tennis, only. If seven students play only tennis and one plays only golf, what is the total number of students who play only baseball?

\[ \text{[A]} \ 12 \quad \text{[B]} \ 60 \quad \text{[C]} \ 44 \quad \text{[D]} \ 56 \]

676. What is the slope of line \( \ell \) in the accompanying diagram?

\[ \text{[A]} \ \frac{3}{2} \quad \text{[B]} \ -\frac{3}{2} \quad \text{[C]} \ -\frac{2}{3} \quad \text{[D]} \ \frac{2}{3} \]

677. When the point \((2, -5)\) is reflected in the \(x\)-axis, what are the coordinates of its image?

\[ \text{[A]} \ (-2, 5) \quad \text{[B]} \ (2, 5) \quad \text{[C]} \ (5, 2) \quad \text{[D]} \ (-5, 2) \]

678. If \( a \neq 0 \) and the sum of \( x \) and \( \frac{1}{a} \) is 0, then

\[ \text{[A]} \ x = a \quad \text{[B]} \ x = -a \quad \text{[C]} \ x = 1 - a \quad \text{[D]} \ x = -\frac{1}{a} \]
679. The accompanying figure shows the graph of the equation \( x = 5 \).

![Graph of \( x = 5 \)]

What is the slope of the line \( x = 5 \)?


680. When \( 3x^2 - 6x \) is divided by \( 3x \), the result is

[A] \( x + 2 \)  [B] \( 2x \)  [C] \( -2x \)  [D] \( x - 2 \)

681. The line \( 3x - 2y = 12 \) has

[A] a slope of 3 and a \( y \)-intercept of -2  
[B] a slope of -3 and a \( y \)-intercept of -6  
[C] a slope of \( -\frac{3}{2} \) and a \( y \)-intercept of 6  
[D] a slope of \( \frac{3}{2} \) and a \( y \)-intercept of -6

682. Which is an equation of the line of symmetry for the parabola in the accompanying diagram?

![Diagram of parabola]

[A] \( y = 3 \)  [B] \( x = 2 \)  [C] \( x = 4 \)  [D] \( x = 3 \)

683. In the accompanying graph, if point \( P \) has coordinates \((a,b)\), which point has coordinates \((-b,a)\)?

![Graph with points A, B, C, D, and P]

684. A rectangular park is three blocks longer than it is wide. The area of the park is 40 square blocks. If \( w \) represents the width, write an equation in terms of \( w \) for the area of the park. Find the length and the width of the park.

685. If the Math Olympiad Club consists of eighteen students, how many different teams of four students can be formed for competitions?


686. Mr. Gonzalez owns a triangular plot of land \( BCD \) with \( DB = 25 \) yards and \( BC = 16 \) yards. He wishes to purchase the adjacent plot of land in the shape of right triangle \( ABD \), as shown in the accompanying diagram, with \( AD = 15 \) yards. If the purchase is made, what will be the total number of square yards in the area of his plot of land, \( \Delta ACD \)?

687. Solve for \( x \):
\[
2(x - 3) = 1.2 - x
\]

688. What is the value of \( 3^{-2} \)?

[A] \( \frac{1}{9} \)  [B] \( -\frac{1}{9} \)  [C] -9  [D] 9

689. The expression \( \sqrt{50} \) can be simplified to

[A] \( 5\sqrt{2} \)  [B] \( 25\sqrt{2} \)  [C] \( 2\sqrt{25} \)  [D] \( 5\sqrt{10} \)

690. In rectangle \( ABCD \), \( AC = 3x + 15 \) and \( BD = 4x - 5 \). Find the length of \( AC \).

691. If the circumference of a circle is \( 10\pi \) inches, what is the area, in square inches, of the circle?

[A] \( 100\pi \)  [B] \( 50\pi \)  [C] \( 25\pi \)  [D] \( 10\pi \)

692. The length of a side of a square window in Jessica's bedroom is represented by \( 2x - 1 \). Which expression represents the area of the window?

[A] \( 4x^2 + 4x - 1 \)  [B] \( 4x^2 - 4x + 1 \)  [C] \( 4x^2 + 1 \)  [D] \( 2x^2 + 1 \)

693. The product of \( 4x^2y \) and \( 2xy^3 \) is

[A] \( 8x^3y^3 \)  [B] \( 8x^3y^4 \)  [C] \( 8x^2y^3 \)  [D] \( 8x^2y^4 \)

694. For which value of \( x \) is the expression \( \frac{x - 7}{x + 2} \) undefined?

[A] -2  [B] 2  [C] 7  [D] 0
695. Two numbers are in the ratio 2:5. If 6 is subtracted from their sum, the result is 50. What is the larger number?  

696. Mr. Smith's class voted on their favorite ice cream flavors, and the results are shown in the accompanying diagram. If there are 20 students in Mr. Smith's class, how many students chose coffee ice cream as their favorite flavor?

---

697. The ratio of the corresponding sides of two similar squares is 1 to 3. What is the ratio of the area of the smaller square to the area of the larger square?  

698. A planned building was going to be 100 feet long, 75 feet deep, and 30 feet high. The owner decides to increase the volume of the building by 10% without changing the dimensions of the depth and the height. What will be the new length of this building?  
[C] 112 ft  [D] 110 ft

699. Ashanti is surveying for a new parking lot shaped like a parallelogram. She knows that three of the vertices of parallelogram $ABCD$ are $A(0,0)$, $B(5,2)$, and $C(6,5)$. Find the coordinates of point $D$ and sketch parallelogram $ABCD$ on the accompanying set of axes. Justify mathematically that the figure you have drawn is a parallelogram.

---

700. Subtract $5x^2 - 7x - 6$ from $9x^2 + 3x - 4$.

701. Which numbers are arranged from smallest to largest?  
[A] $\sqrt{9.1}$, $3.14$, $\pi$, $\frac{22}{7}$  
[B] $\sqrt{9.1}$, $\pi$, $3.14$, $\frac{22}{7}$  
[C] $\sqrt{9.1}$, $3.14$, $\frac{22}{7}$, $\pi$  
[D] $3.14$, $\frac{22}{7}$, $\pi$, $\sqrt{9.1}$
702. If the length of a rectangular prism is doubled, its width is tripled, and its height remains the same, what is the volume of the new rectangular prism?

[A] double the original volume
[B] triple the original volume
[C] nine times the original volume
[D] six times the original volume

703. Which statement about quadrilaterals is true?

[A] All quadrilaterals have equal sides.
[B] All quadrilaterals are parallelograms.
[C] All quadrilaterals have four right angles.
[D] All quadrilaterals have four sides.

704. A fair coin is tossed three times. What is the probability that the coin will land tails up on the second toss?

[A] \( \frac{2}{3} \)  [B] \( \frac{1}{3} \)  [C] \( \frac{3}{4} \)  [D] \( \frac{1}{2} \)

705. A cardboard box has length \( x - 2 \), width \( x + 1 \), and height \( 2x \).

a Write an expression, in terms of \( x \), to represent the volume of the box.

b If \( x = 8 \) centimeters, what is the number of cubic centimeters in the volume of the box?

706. What is the value of \( \frac{x^2 - 4y}{2} \), if \( x = 4 \) and \( y = -3 \)?


707. Expressed as a single fraction, what is \( \frac{1}{x+1} + \frac{1}{x} \), \( x \neq 0, -1 \)?

[A] \( \frac{3}{x^2} \)  [B] \( \frac{2}{2x+1} \)

[C] \( \frac{2x+1}{x^2+x} \)  [D] \( \frac{2x+3}{x^2+x} \)

708. What is the solution set of the equation \( x^2 + 11x + 28 = 0 \)?

[A] \{ -3, -4 \}  [B] \{ -7, -4 \}

[C] \{ -7, 4 \}  [D] \{ 3, 4 \}

709. As shown in the accompanying diagram, the star in position 1 on a computer screen transforms to the star in position 2.

This transformation is best described as a

[A] line reflection  [B] translation
[C] dilation  [D] rotation

710. Which equation is an illustration of the additive identity property?

[A] \( x \cdot 1 = x \)  [B] \( x + 0 = x \)

[C] \( x - x = 0 \)  [D] \( \frac{1}{x} \)
711. The Grimaldis have three children born in different years.
   a. Draw a tree diagram or list a sample space to show all the possible arrangements of boy and girl children in the Grimaldi family.
   b. Using your information from part a, what is the probability that the Grimaldis have three boys?

712. The accompanying diagram shows a flagpole that stands on level ground. Two cables, \( r \) and \( s \), are attached to the pole at a point 16 feet above the ground. The combined length of the two cables is 50 feet. If cable \( r \) is attached to the ground 12 feet from the base of the pole, what is the measure of the angle, \( x \), to the nearest degree, that cable \( s \) makes with the ground?

713. Which point on the accompanying number line best represents the position of \( \sqrt{5} \)?

714. Two hikers started at the same location. One traveled 2 miles east and then 1 mile north. The other traveled 1 mile west and then 3 miles south. At the end of their hikes, how many miles apart are the two hikers? [The use of the accompanying grid is optional.]

715. What is the measure, in degrees, of each exterior angle of a regular hexagon?

716. If the number of molecules in 1 mole of a substance is \( 6.02 \times 10^{23} \), then the number of molecules in 100 moles is
   [A] \( 6.02 \times 10^{24} \)  [B] \( 6.02 \times 10^{25} \)
   [C] \( 6.02 \times 10^{21} \)  [D] \( 6.02 \times 10^{22} \)

717. The value of 5! is
   [A] 20  [B] 120  [C] 5  [D] \( \frac{1}{5} \)
718. Parking charges at Superior Parking Garage are $5.00 for the first hour and $1.50 for each additional 30 minutes. If Margo has $12.50, what is the maximum amount of time she will be able to park her car at the garage?

[A] $3\frac{1}{2}$ hours  [B] 6 hours  
[C] $6\frac{1}{2}$ hours  [D] $2\frac{1}{2}$ hours

719. Bob and Laquisha have volunteered to serve on the Junior Prom Committee. The names of twenty volunteers, including Bob and Laquisha, are put into a bowl. If two names are randomly drawn from the bowl without replacement, what is the probability that Bob's name will be drawn first and Laquisha's name will be drawn second?

[A] $\frac{1}{20} \cdot \frac{1}{20}$  [B] $\frac{2}{20!}$  
[C] $\frac{2}{20}$  [D] $\frac{1}{20} \cdot \frac{1}{19}$

720. The senior class at South High School consists of 250 students. Of these students, 130 have brown hair, 160 have brown eyes, and 90 have both brown hair and brown eyes. How many members of the senior class have neither brown hair nor brown eyes?

721. The height of a golf ball hit into the air is modeled by the equation $h = -16t^2 + 48t$, where $h$ represents the height, in feet, and $t$ represents the number of seconds that have passed since the ball was hit. What is the height of the ball after 2 seconds?


722. At the beginning of her mathematics class, Mrs. Reno gives a warm-up problem. She says, "I am thinking of a number such that 6 less than the product of 7 and this number is 85." Which number is she thinking of?

[A] 67  [B] 84  [C] $\frac{112}{7}$  [D] 13

723. Solve the following system of equations algebraically or graphically:

$x^2 + y^2 = 25$
$3y - 4x = 0$

[The use of the accompanying grid is optional.]

724. What is the length of one side of the square whose perimeter has the same numerical value as its area?

725. What is the value of \( x \) in the equation \( \frac{x}{2x+1} = \frac{4}{3} \)?

\[ [A] -5 \quad [B] -\frac{5}{4} \quad [C] -\frac{1}{5} \quad [D] -\frac{4}{5} \]

726. What is the inverse of the statement “If I do not buy a ticket, then I do not go to the concert”?

[A] If I do not go to the concert, then I do not buy a ticket.
[B] If I go to the concert, then I buy a ticket.
[C] If I buy a ticket, then I do not go to the concert.
[D] If I buy a ticket, then I go to the concert.

727. A picture held by a magnet to a refrigerator slides to the bottom of the refrigerator, as shown in the accompanying diagram.

This change of position is an example of a

[A] reflection  
[B] rotation  
[C] dilation  
[D] translation

728. What is the slope of the linear equation \( 5y - 10x = -15 \)?

[A] -10  
[B] -15  
[C] 10  
[D] 2

729. The Pentagon building in Washington, D.C., is shaped like a regular pentagon. If the length of one side of the Pentagon is represented by \( n + 2 \), its perimeter would be represented by

[A] \( n + 10 \)  
[B] \( 10n \)  
[C] \( 5n + 10 \)  
[D] \( 5n + 2 \)

730. The accompanying Venn diagram shows the results of a survey asking 100 people if they get news by reading newspapers or by watching television.

What is the probability that a person selected at random from this survey does not claim television as a source of getting the news?

\[
\begin{array}{c|c|c|c|c}
\text{Newspapers} & \text{Television} & \text{Total} \\
15 & 40 & 25 & 70 \\
20 & 15 & 35 & 100 \\
\hline
100 & 100 & 55 & 100 \\
75 & 35 & 15 & 100 \\
\end{array}
\]

[A] 75  
[B] 35  
[C] 55  
[D] 15
731. The distance from Earth to the Sun is approximately 93 million miles. A scientist would write that number as

[A] $9.3 \times 10^7$
[B] $93 \times 10^7$
[C] $93 \times 10^{10}$
[D] $9.3 \times 10^6$

732. A storage container in the shape of a right circular cylinder is shown in the accompanying diagram.

![Diagram of a right circular cylinder]

What is the volume of this container, to the nearest hundredth?

[A] 125.66 in$^3$
[B] 251.33 in$^3$
[C] 56.55 in$^3$
[D] 502.65 in$^3$

733. The distance from Earth to the imaginary planet Med is $1.7 \times 10^7$ miles. If a spaceship is capable of traveling 1,420 miles per hour, how many days will it take the spaceship to reach the planet Med? Round your answer to the nearest day.

734. Using only a compass and a straightedge, construct the perpendicular bisector of $\overline{AB}$ and label it $c$. [Leave all construction marks.]

735. Judy needs a mean (average) score of 86 on four tests to earn a midterm grade of B. If the mean of her scores for the first three tests was 83, what is the lowest score on a 100-point scale that she can receive on the fourth test to have a midterm grade of B?

736. The perimeter of $\triangle A'B'C'$, the image of $\triangle ABC$, is twice as large as the perimeter of $\triangle ABC$. What type of transformation has taken place?

[C] dilation  [D] rotation
737. The product of $3x^5$ and $2x^4$ is

[A] $6x^{20}$  [B] $6x^9$  [C] $5x^{20}$  [D] $5x^9$

738. Every month, Omar buys pizzas to serve at a party for his friends. In May, he bought three more than twice the number of pizzas he bought in April. If Omar bought 15 pizzas in May, how many pizzas did he buy in April?

739. If the mass of a proton is $1.67 \times 10^{-24}$ gram, what is the mass of 1,000 protons?

[A] $1.67 \times 10^{-22}$  [B] $1.67 \times 10^{-27}$
[C] $1.67 \times 10^{-23}$  [D] $1.67 \times 10^{-21}$

740. Which inequality is represented in the accompanying graph?

[A] $-3 \leq x < 4$  [B] $-3 < x < 4$
[C] $-3 \leq x \leq 4$  [D] $-3 < x \leq 4$

741. Jamie is 5 years older than her sister Amy. If the sum of their ages is 19, how old is Jamie?


742. Mark says, "The number I see is odd." Jan says, "That same number is prime." The teacher says, "Mark is correct or Jan is correct." Some integers would make the teacher's statement true while other integers would make it false. Give and explain one example of when the teacher's statement is true. Give and explain one example of when the teacher's statement is false.

743. Which statement describes the graph of $x = 4$?

[A] It passes through the point (0, 4).
[B] It is parallel to the $y$-axis.
[C] It has a slope of 4.
[D] It is parallel to the $x$-axis.

744. Nine hundred students were asked whether they thought their school should have a dress code. A circle graph was constructed to show the results. The central angles for two of the three sectors are shown in the accompanying diagram. What is the number of students who felt that the school should have no dress code?

745. What point is the intersection of the graphs of the lines $2x - y = 3$ and $x + y = 3$?

[A] (1, 2)  [B] (2, 1)  [C] (3, 3)  [D] (3, 0)

746. Three brothers have ages that are consecutive even integers. The product of the first and third boys' ages is 20 more than twice the second boy's age. Find the age of each of the three boys.
747. In the accompanying diagram, which transformation changes the solid-line parabola to the dotted-line parabola?

[A] line reflection, only  
[B] rotation, only  
[C] translation  
[D] line reflection or rotation

748. Al says, "If \(ABCD\) is a parallelogram, then \(ABCD\) is a rectangle." Sketch a quadrilateral \(ABCD\) that shows that Al's statement is not always true. Your sketch must show the length of each side and the measure of each angle for the quadrilateral you draw.

749. The accompanying circle graph shows how the Marino family spends its income each month.

What is the measure, in degrees, of the central angle that represents the percentage of income spent on food?

[A] 360  
[B] 90  
[C] 25  
[D] 50

750. Six members of a school's varsity tennis team will march in a parade. How many different ways can the players be lined up if Angela, the team captain, is always at the front of the line?

751. The solution set for the equation \(x^2 - 5x = 6\) is

[A] \(\{1, -6\}\)  
[B] \(\{-2, 3\}\)  
[C] \(\{2, -3\}\)  
[D] \(\{-1, 6\}\)

752. In a game, each player receives 5 cards from a deck of 52 different cards. How many different groupings of cards are possible in this game?

[A] \(5\)  
[B] \(\binom{52}{5}\)  
[C] \(\frac{52!}{5!}\)  
[D] \(\binom{52}{5}\)
753. In a certain quadrilateral, two opposite sides are parallel, and the other two opposite sides are not congruent. This quadrilateral could be a
[A] parallelogram  [B] square
[C] trapezoid  [D] rhombus

754. Which number is in the solution set of the inequality $5x + 3 > 38$?

755. If there are four teams in a league, how many games will have to be played so that each team plays every other team once?

756. The number $1.56 \times 10^{-2}$ is equivalent to
[A] 0.00156  [B] 0.156
[C] 0.0156  [D] 156

757. One function of a movie projector is to enlarge the image on the film. This procedure is an example of a
[A] translation  [B] dilation
[C] line of symmetry  [D] line reflection

758. Factor completely: $3ax^2 - 27a$

759. There are 357 seniors in Harris High School. The ratio of boys to girls is 7:10. How many boys are in the senior class?

760. What are the factors of $x^2 - 10x - 24$?
[A] $(x - 12)(x + 2)$  [B] $(x - 4)(x - 6)$
[C] $(x - 4)(x + 6)$  [D] $(x + 12)(x - 2)$

761. The equation $\Delta + \hat{\varphi} = \Delta + \hat{\varphi}$ is an example of the
[A] commutative law  [B] distributive law
[C] transitive law  [D] associative law

762. The operation element @ is determined by the following table:

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<tr>
<th></th>
<th>a</th>
<th>b</th>
<th>c</th>
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<tbody>
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<tr>
<td>b</td>
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</tr>
<tr>
<td>c</td>
<td>c</td>
<td>a</td>
<td>b</td>
</tr>
</tbody>
</table>

What is the identity element of this operation?
[A] $a$, only  [B] $a$ and $b$
[C] $b$, only  [D] $c$

763. A micron is a unit used to measure specimens viewed with a microscope. One micron is equivalent to 0.00003937 inch. How is this number expressed in scientific notation?
[A] $3937 \times 10^{-8}$  [B] $3.937 \times 10^{-5}$
[C] $3937 \times 10^8$  [D] $3.937 \times 10^5$
764. Draw all the symmetry lines on the accompanying figure.

765. The product of $2x^3$ and $6x^5$ is
   \[ \text{[A]} \ 10x^{15} \quad \text{[B]} \ 12x^{15} \quad \text{[C]} \ 10x^8 \quad \text{[D]} \ 12x^8 \]

766. If $t^2 < t < \sqrt{t}$, then $t$ could be
   \[ \text{[A]} \ 4 \quad \text{[B]} \ -\frac{1}{4} \quad \text{[C]} \ 0 \quad \text{[D]} \ \frac{1}{4} \]

767. The accompanying circle graph shows how Shannon earned $600 during her summer vacation.

What is the measure of the central angle of the section labeled "Chores"?
   \[ \text{[A]} \ 90^\circ \quad \text{[B]} \ 30^\circ \quad \text{[C]} \ 120^\circ \quad \text{[D]} \ 60^\circ \]

768. If $3x$ is one factor of $3x^2 - 9x$, what is the other factor?
   \[ \text{[A]} \ x^2 - 6x \quad \text{[B]} \ x + 3 \quad \text{[C]} \ x - 3 \quad \text{[D]} \ 3x \]

769. Triangle $SUN$ has coordinates $S(0,6)$, $U(3,5)$, and $N(3,0)$. On the accompanying grid, draw and label $\triangle SUN$. Then, graph and state the coordinates of $\triangle S'U'N'$, the image of $\triangle SUN$ after a reflection in the $y$-axis.

770. The students in Woodland High School's meteorology class measured the noon temperature every schoolday for a week. Their readings for the first 4 days were Monday, $56^\circ$; Tuesday, $72^\circ$; Wednesday, $67^\circ$; and Thursday, $61^\circ$. If the mean (average) temperature for the 5 days was exactly $63^\circ$, what was the temperature on Friday?

771. In Clark Middle School, there are 60 students in seventh grade. If 25 of these students take art only, 18 take music only, and 9 do not take either art or music, how many take both art and music?
772. At Ron’s Rental, a person can rent a big-screen television for $10 a month plus a one-time "wear-and-tear" fee of $100. At Josie's Rental, the charge is $20 a month and an additional charge of $20 for delivery with no "wear-and-tear" fee.

a If \( c \) equals the cost, write one equation representing the cost of the rental for \( m \) months at Ron's Rental and one equation representing the cost of the rental for \( m \) months at Josie's Rental.

b On the accompanying grid, graph and label each equation.

c From your graph, determine in which month Josie's cost will equal Ron's cost.

773. A locker combination system uses three digits from 0 to 9. How many different three-digit combinations with no digit repeated are possible?

[A] 720   [B] 504   [C] 30   [D] 1,000

774. A straw is placed into a rectangular box that is 3 inches by 4 inches by 8 inches, as shown in the accompanying diagram. If the straw fits exactly into the box diagonally from the bottom left front corner to the top right back corner, how long is the straw, to the nearest tenth of an inch?

775. An addition table for a subset of real numbers is shown below. Which number is the identity element? Explain your answer.

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<th>+</th>
<th>0</th>
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<td>4</td>
<td>0</td>
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</tbody>
</table>

776. Which expression is equivalent to \( \frac{a}{x} + \frac{b}{2x} \)?

[A] \( \frac{2a + b}{x} \)  
[B] \( \frac{a + b}{2x} \)  
[C] \( \frac{2a + b}{2x} \)  
[D] \( \frac{a + b}{3x} \)
777. If two sides of a triangle are 1 and 3, the third side may be

778. A total of $450 is divided into equal shares. If Kate receives four shares, Kevin receives three shares, and Anna receives the remaining two shares, how much money did Kevin receive?

779. On a scale drawing of a new school playground, a triangular area has sides with lengths of 8 centimeters, 15 centimeters, and 17 centimeters. If the triangular area located on the playground has a perimeter of 120 meters, what is the length of its longest side?
[A] 24 m   [B] 40 m   [C] 51 m   [D] 45 m

780. A truck traveling at a constant rate of 45 miles per hour leaves Albany. One hour later a car traveling at a constant rate of 60 miles per hour also leaves Albany traveling in the same direction on the same highway. How long will it take for the car to catch up to the truck, if both vehicles continue in the same direction on the highway?

781. Let $x$ and $y$ be numbers such that $0 < x < y < 1$, and let $d = x - y$. Which graph could represent the location of $d$ on the number line?

782. A ribbon 56 centimeters long is cut into two pieces. One of the pieces is three times longer than the other. Find the lengths, in centimeters, of both pieces of ribbon.

783. Solve algebraically for $x$: \[rac{1}{x} = \frac{x + 1}{6}\]

784. Mary and Amy had a total of 20 yards of material from which to make costumes. Mary used three times more material to make her costume than Amy used, and 2 yards of material was not used. How many yards of materials did Amy use for her costume?

785. Which expression is equivalent to $6.02 \times 10^{23}$?
[A] $60.2 \times 10^{21}$   [B] $6020 \times 10^{21}$   [C] $0.602 \times 10^{21}$   [D] $602 \times 10^{21}$
786. Triangle $A'B'C'$ is the image of $\triangle ABC$ under a dilation such that $A'B' = 3AB$. Triangles $ABC$ and $A'B'C'$ are

[A] neither congruent nor similar
[B] both congruent and similar
[C] congruent but not similar
[D] similar but not congruent

787. Seth tossed a fair coin five times and got five heads. The probability that the next toss will be a tail is

[A] $\frac{5}{6}$  [B] $\frac{1}{6}$  [C] 0  [D] $\frac{1}{2}$

788. The accompanying graph shows the amount of water left in Rover's water dish over a period of time.

How long did Rover wait from the end of his first drink to the start of his second drink of water?

[A] 60 sec  [B] 75 sec
[C] 30 sec  [D] 10 sec

789. What is the value of $2^{-3}$?

[A] -8  [B] $\frac{1}{8}$  [C] $\frac{1}{6}$  [D] -6

790. What is the area of a square whose perimeter is represented by $12x$?

[A] $9x^2$  [B] $6x\sqrt{2}$
[C] $144x^2$  [D] $12x^2$

791. If $x = -3$ and $y = 2$, which point on the accompanying graph represents $(-x, -y)$?


792. The perimeter of a square is 56. Express the length of a diagonal of the square in simplest radical form.

793. The dimensions of a brick, in inches, are 2 by 4 by 8. How many such bricks are needed to have a total volume of exactly 1 cubic foot?

794. Five friends met for lunch, and they all shook hands. Each person shook the other person's right hand only once. What was the total number of handshakes?
795. How many times larger than \( \frac{1}{4}x \) is 5x?

[A] \( \frac{4}{5} \)  [B] \( \frac{5}{4} \)  [C] 20  [D] 9

796. If \( M \) and \( A \) represent integers, \( M + A = A + M \) is an example of which property?


797. In a molecule of water, there are two atoms of hydrogen and one atom of oxygen. How many atoms of hydrogen are in 28 molecules of water?


798. Which table does not show an example of direct variation?

[A] \[
\begin{array}{c|c}
 x & y \\
 \hline
 2 & 24 \\
 4 & 12 \\
 6 & 8 \\
 8 & 6 \\
\end{array}
\]

[B] \[
\begin{array}{c|c}
 x & y \\
 \hline
 1 & 4 \\
 2 & 8 \\
 3 & 12 \\
 4 & 16 \\
\end{array}
\]

[C] \[
\begin{array}{c|c}
 x & y \\
 \hline
 1 & \frac{1}{3} \\
 2 & 1 \\
 3 & \frac{3}{2} \\
 4 & 2 \\
\end{array}
\]

[D] \[
\begin{array}{c|c}
 x & y \\
 \hline
 -4 & -20 \\
 -3 & -15 \\
 -2 & -10 \\
 -1 & -5 \\
\end{array}
\]

799. What is the inverse of the statement "If Julie works hard, then she succeeds"?

[A] If Julie succeeds, then she works hard.
[B] If Julie does not succeed, then she does not work hard.
[C] If Julie does not work hard, then she does not succeed.
[D] If Julie works hard, then she does not succeed.

800. If \( 2x + 5 = -25 \) and \( -3m - 6 = 48 \), what is the product of \( x \) and \( m \)?


801. To measure the length of a hiking trail, a worker uses a device with a 2-foot-diameter wheel that counts the number of revolutions the wheel makes. If the device reads 1,100.5 revolutions at the end of the trail, how many miles long is the trail, to the nearest tenth of a mile?

802. What is the sum of \( \sqrt{50} \) and \( \sqrt{32} \)?

[A] \( 9\sqrt{2} \)  [B] \( 20\sqrt{20} \)  [C] \( \sqrt{82} \)  [D] \( \sqrt{2} \)

803. Mary says, "The number I am thinking of is divisible by 2 or it is divisible by 3." Mary's statement is false if the number she is thinking of is

804. In \( \triangle ABC \), the measure of \( \angle B \) is 21 less than four times the measure of \( \angle A \), and the measure of \( \angle C \) is 1 more than five times the measure of \( \angle A \). Find the measure, in degrees, of each angle of \( \triangle ABC \).

805. A 12-foot tree casts a 16-foot shadow. How many feet tall is a nearby tree that casts a 20-foot shadow at the same time?

806. What is the solution set for the equation \( x^2 - 5x + 6 = 0 \)?

- [A] \{2,3\}
- [B] \{-6,1\}
- [C] \{-2,-3\}
- [D] \{6,-1\}

807. In which list are the numbers in order from least to greatest?

- [A] \(3.2, \pi, 3\frac{1}{3}, \sqrt{3}\)
- [B] \(\sqrt{3}, 3.2, \pi, 3\frac{1}{3}\)
- [C] \(\sqrt{3}, \pi, 3.2, 3\frac{1}{3}\)
- [D] \(3.2, 3\frac{1}{3}, \sqrt{3}, \pi\)

808. Cole's Ice Cream Stand serves sixteen different flavors of ice cream, three types of syrup, and seven types of sprinkles. If an ice cream sundae consists of one flavor of ice cream, one type of syrup, and one type of sprinkles, how many different ice cream sundaes can Cole serve?

- [A] 26
- [B] 336
- [C] 3
- [D] 10,836

809. There are 12 people on a basketball team, and the coach needs to choose 5 to put into a game. How many different possible ways can the coach choose a team of 5 if each person has an equal chance of being selected?

- [A] \(\binom{12}{5}\)
- [B] \(\binom{5}{12}\)
- [C] \(\binom{12}{5}\)
- [D] \(\binom{5}{12}\)

810. In the accompanying diagram, \( \triangle ABC \) and \( \triangle ABD \) are isosceles triangles with \( m\angle CAB = 50 \) and \( m\angle BDA = 55 \). If \( AB = AC \) and \( AB = BD \), what is \( m\angle CBD \)?

811. Which equation represents the direct variation relationship of the equation \( \frac{x}{y} = \frac{1}{2} \)?

- [A] \(y = 2x\)
- [B] \(y = x + \frac{1}{2}\)
- [C] \(x = 2y\)
- [D] \(y = 3x\)

812. If \( \frac{x}{a} - \frac{a}{4b} = 0, b \neq 0 \), then \( x \) is equal to

- [A] \(-\frac{a}{4b}\)
- [B] \(\frac{a}{4b}\)
- [C] \(-\frac{4a}{b}\)
- [D] \(\frac{4a}{b}\)
813. Which shape does not have rotational symmetry?
[A] circle  [B] regular pentagon  
[C] trapezoid  [D] square

814. In the accompanying diagram of right triangles $ABD$ and $DBC$, $AB = 5$, $AD = 4$, and $CD = 1$. Find the length of $BC$, to the nearest tenth.

815. A roll of candy is shown in the accompanying diagram.

The shape of the candy is best described as a
[A] cylinder  [B] pyramid  
[C] cone  [D] rectangular solid

816. Which equation illustrates the distributive property for real numbers?
[A] $\frac{1}{3} + \frac{1}{2} = \frac{1}{2} + \frac{1}{3}$
[B] $(1.3 \times 0.07) \times 0.63 = 1.3 \times (0.07 \times 0.63)$
[C] $\sqrt{3} + 0 = \sqrt{3}$
[D] $-3(5 + 7) = (-3)(5) + (-3)(7)$

817. Which diagram shows a dotted line that is not a line of symmetry?

818. What is the diameter of a circle whose circumference is 5?
[A] $\frac{2.5}{\pi}$  [B] $\frac{5}{\pi}$  [C] $\frac{2.5}{\pi^2}$  [D] $\frac{5}{\pi^2}$

819. Which expression is undefined when $w = 3$?
[A] $\frac{w + 1}{w^2 - 3w}$  [B] $\frac{w - 3}{w + 1}$
[C] $\frac{w^2 + 2w}{5w}$  [D] $\frac{3w}{3w^2}$

820. Sara is building a triangular pen for her pet rabbit. If two of the sides measure 8 feet and 15 feet, the length of the third side could be
821. The coordinates of the endpoints of $\overline{AB}$ are $A(2,6)$ and $B(4,2)$. Is the image $\overline{A''B''}$ the same if it is reflected in the $x$-axis, then dilated by $\frac{1}{2}$ as the image is if it is dilated by $\frac{1}{2}$, then reflected in the $x$-axis? Justify your answer.

822. Debbie goes to a diner famous for its express lunch menu. The menu has five appetizers, three soups, seven entrees, six vegetables, and four desserts. How many different meals consisting of either an appetizer or a soup, one entree, one vegetable, and one dessert can Debbie order?

823. The plan of a parcel of land is represented by trapezoid $ABCD$ in the accompanying diagram. If the area of $\triangle ABE$ is 600 square feet, find the minimum number of feet of fence needed to completely enclose the entire parcel of land, $ABCD$.

824. Chantrice is pulling a wagon along a smooth, horizontal street. The path of the center of one of the wagon wheels is best described as

[A] two parallel lines
[B] a line parallel to the road
[C] a line perpendicular to the road
[D] a circle

825. Which transformation does not always produce an image that is congruent to the original figure?

[A] dilation  
[B] rotation  
[C] translation  
[D] reflection

826. What is the value of $\frac{6.3 \times 10^8}{3 \times 10^4}$ in scientific notation?

[A] $2.1 \times 10^5$  
[B] $2.1 \times 10^{-2}$  
[C] $2.1 \times 10^{-4}$  
[D] $2.1 \times 10^4$
827. The formula for potential energy is \( P = mgh \), where \( P \) is potential energy, \( m \) is mass, \( g \) is gravity, and \( h \) is height. Which expression can be used to represent \( g \)?

[A] \( P - m - h \)  
[B] \( P - mh \)  
[C] \( \frac{P}{mh} \)  
[D] \( \frac{P}{m} - h \)

828. If \( a \) and \( b \) are integers, which equation is always true?

[A] \( a + 2b = b + 2a \)  
[B] \( \frac{a}{b} = \frac{b}{a} \)  
[C] \( a + b = b + a \)  
[D] \( a - b = b - a \)

829. A hotel charges $20 for the use of its dining room and $2.50 a plate for each dinner. An association gives a dinner and charges $3 a plate but invites four nonpaying guests. If each person has one plate, how many paying persons must attend for the association to collect the exact amount needed to pay the hotel?

[A] 44  
[B] 60  
[C] 40  
[D] 20

830. There are 30 students on a school bus. Of these students, 24 either play in the school band or sing in the chorus. Six of the students play in the school band but do not sing in the chorus. Fourteen of the students sing in the chorus and also play in the school band. How many students on the school bus sing in the chorus but do not play in the band?

831. Which list shows the numbers \( -0.12, \frac{1}{82}, \frac{1}{9}, \frac{1}{8} \) in order from smallest to largest?

[A] \( \frac{1}{82}, -0.12, \frac{1}{9}, \frac{1}{8} \)  
[B] \( -0.12, \frac{1}{8}, \frac{1}{9}, \sqrt{\frac{1}{82}} \)  
[C] \( -0.12, \frac{1}{8}, \frac{1}{9}, \sqrt{\frac{1}{82}} \)  
[D] \( \frac{1}{8}, \frac{1}{9}, \sqrt{\frac{1}{82}}, -0.12 \)

832. In the accompanying diagram, \( ABCD \) is a straight line, and angle \( E \) in triangle \( BEC \) is a right angle.

\[ \text{What does } a^\circ + d^\circ \text{ equal?} \]

[A] 180°  
[B] 270°  
[C] 135°  
[D] 160°

833. If \( x = -4 \) and \( y = 3 \), what is the value of \( x - 3y^2 \)?

[A] -13  
[B] -31  
[C] -85  
[D] -23
834. A wheel has a radius of 5 feet. What is the minimum number of complete revolutions that the wheel must make to roll at least 1,000 feet?

835. If asphalt pavement costs $0.78 per square foot, determine, to the nearest cent, the cost of paving the shaded circular road with center O, an outside radius of 50 feet, and an inner radius of 36 feet, as shown in the accompanying diagram.

836. Walter is a waiter at the Towne Diner. He earns a daily wage of $50, plus tips that are equal to 15% of the total cost of the dinners he serves. What was the total cost of the dinners he served if he earned $170 on Tuesday?

837. In the accompanying diagram of \( \triangle BCD \), \( m \angle C = 70 \), \( m \angle CDE = 130 \), and side \( \overline{BD} \) is extended to \( A \) and to \( E \). Find \( m \angle CBA \).

838. What is the image of point \((2, 5)\) under the translation that shifts \((x, y)\) to \((x + 3, y - 2)\)?

[A] \((0,3)\)  
[B] \((0,8)\)  
[C] \((5,8)\)  
[D] \((5,3)\)

839. Which inequality is represented in the graph below?

[A] \(-4 < x \leq 2\)  
[B] \(-4 \leq x \leq 2\)  
[C] \(-4 < x < 2\)  
[D] \(-4 \leq x < 2\)

840. The accompanying diagram shows the graphs of a linear equation and a quadratic equation.

How many solutions are there to this system of equations?

[A] 0  
[B] 1  
[C] 3  
[D] 2

841. One of the factors of \(4x^2 - 9\) is

[A] \((x - 3)\)  
[B] \((x + 3)\)  
[C] \((4x - 3)\)  
[D] \((2x + 3)\)

842. Sara’s test scores in mathematics were 64, 80, 88, 78, 60, 92, 84, 76, 86, 78, 72, and 90. Determine the mean, the median, and the mode of Sara’s test scores.
843. If \( r = 2 \) and \( s = -7 \), what is the value of \( |r| - |s| \)?


844. What is the identity element for \( \bullet \) in the accompanying table?

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<thead>
<tr>
<th>( \bullet )</th>
<th>( r )</th>
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</table>

[A] \( t \)  [B] \( u \)  [C] \( s \)  [D] \( r \)

845. From a point on level ground 25 feet from the base of a tower, the angle of elevation to the top of the tower is 78°, as shown in the accompanying diagram. Find the height of the tower, to the nearest tenth of a foot.