Dear Sir,

I have to acknowledge the receipt of your favor of May 14. in which you mention that you have finished the 6. first books of Euclid, plane trigonometry, surveying & algebra and ask whether I think a further pursuit of that branch of science would be useful to you. there are some propositions in the latter books of Euclid, & some of Archimedes, which are useful, & I have no doubt you have been made acquainted with them. trigonometry, so far as this, is most valuable to every man, there is scarcely a day in which he will not resort to it for some of the purposes of common life. the science of calculation also is indispensible as far as the extraction of the square & cuberoots; Algebra as far as the quadratic equation & the use of logarithms are often of value in ordinary cases: but all beyond these is but a luxury; a delicious luxury indeed; but not to be indulged in by one who is to have a profession to follow for his subsistence. in this light I view the conic sections, curves of the higher orders, perhaps even spherical trigonometry, Algebraical operations beyond the 2d dimension, and fluxions.

Letter from Thomas Jefferson to William G. Munford, Monticello, June 18, 1799.
# TABLE OF CONTENTS

## ALGEBRA

<table>
<thead>
<tr>
<th>PRENTICE HALL CHAPTER</th>
<th>QUESTION NUMBER</th>
</tr>
</thead>
<tbody>
<tr>
<td>CH1</td>
<td>1-110</td>
</tr>
<tr>
<td>Tools of Algebra</td>
<td></td>
</tr>
<tr>
<td>CH2</td>
<td>111-136</td>
</tr>
<tr>
<td>Functions and Their Graphs</td>
<td></td>
</tr>
<tr>
<td>CH3</td>
<td>137-184</td>
</tr>
<tr>
<td>Algebraic Concepts and Simple Equations</td>
<td></td>
</tr>
<tr>
<td>CH4</td>
<td>185-274</td>
</tr>
<tr>
<td>Equations and Inequalities</td>
<td></td>
</tr>
<tr>
<td>CH5</td>
<td>275-322</td>
</tr>
<tr>
<td>Graphing and Writing Linear Equations</td>
<td></td>
</tr>
<tr>
<td>CH6</td>
<td>323-395</td>
</tr>
<tr>
<td>Systems of Equations and Inequalities</td>
<td></td>
</tr>
<tr>
<td>CH7</td>
<td>396-406</td>
</tr>
<tr>
<td>Quadratic Equations and Functions</td>
<td></td>
</tr>
<tr>
<td>CH8</td>
<td>407-451</td>
</tr>
<tr>
<td>Exponents and Exponential Functions</td>
<td></td>
</tr>
<tr>
<td>CH9</td>
<td>452-533</td>
</tr>
<tr>
<td>Right Triangles and Radical Expressions</td>
<td></td>
</tr>
<tr>
<td>CH10</td>
<td>534-590</td>
</tr>
<tr>
<td>Polynomials</td>
<td></td>
</tr>
<tr>
<td>CH11</td>
<td>591-664</td>
</tr>
<tr>
<td>Rational Expressions and Functions</td>
<td></td>
</tr>
</tbody>
</table>
CHAPTER 1-1

CENTRAL TENDENCY

1. The weights of all the students in grade 9 are arranged from least to greatest. Which statistical measure separates the top half of this set of data from the bottom half?
   [A] median  [B] mean  
   [C] average  [D] mode

2. Rosario and Enrique are in the same mathematics class. On the first five tests, Rosario received scores of 78, 77, 64, 86, and 70. Enrique received scores of 90, 61, 79, 73, and 87. How much higher was Enrique's average than Rosario's average?
   [A] 15 points  [B] 3 points  
   [C] 2 points  [D] 4 points

3. On an English examination, two students received scores of 90, five students received 85, seven students received 75, and one student received 55. The average score on this examination was

4. Seth bought a used car that had been driven 20,000 miles. After he owned the car for 2 years, the total mileage of the car was 49,400. Find the average number of miles he drove each month during those 2 years.

5. The student scores on Mrs. Frederick’s mathematics test are shown on the stem-and-leaf plot below.

   Key: 4 | 3 = 43 points

   Find the median of these scores.

6. What was the median high temperature in Middletown during the 7-day period shown in the table below?

   | Daily High Temperature in Middletown |
   | Day       | Temperature (°F) |
   | Sunday    | 66               |
   | Monday    | 73               |
   | Tuesday   | 73               |
   | Wednesday | 75               |
   | Thursday  | 69               |
   | Friday    | 67               |
   | Saturday  | 63               |

7. Jorge made the accompanying stem-and-leaf plot of the weights, in pounds, of each member of the wrestling team he was coaching.

<table>
<thead>
<tr>
<th>Stem</th>
<th>Leaf</th>
</tr>
</thead>
<tbody>
<tr>
<td>10</td>
<td>9</td>
</tr>
<tr>
<td>11</td>
<td>2 8</td>
</tr>
<tr>
<td>12</td>
<td>3 4 4 6 8</td>
</tr>
<tr>
<td>13</td>
<td>1 3 5 5 9</td>
</tr>
<tr>
<td>14</td>
<td>2 3 7 7 9</td>
</tr>
<tr>
<td>15</td>
<td>1 3 7 8 8 8 9</td>
</tr>
<tr>
<td>16</td>
<td>3 8</td>
</tr>
</tbody>
</table>

Key: 16 I = 161

What is the mode of the weights?

8. Sara's test scores in mathematics were 64, 80, 88, 78, 60, 92, 84, 76, 86, 78, 72, and 90. Determine the mean, the median, and the mode of Sara's test scores.

9. The accompanying graph shows the high temperatures in Elmira, New York, for a 5-day period in January.

Which statement describes the data?
[A] median = mode  [B] mean = mode  
[C] median = mean  [D] mean < mode

10. From January 3 to January 7, Buffalo recorded the following daily high temperatures: 5°, 7°, 6°, 5°, and 7°. Which statement about the temperatures is true?
[A] mean < median  [B] mean = median  
[C] mean = mode  [D] median = mode

11. The ages of five children in a family are 3, 3, 5, 8, and 18. Which statement is true for this group of data?
[A] median > mean  [B] median = mode  
[C] mean > median  [D] mode > mean

12. Melissa's test scores are 75, 83, and 75. Which statement is true about this set of data?
[A] mean < mode  [B] mean = median  
[C] mode < median  [D] mode = median

13. What is the mean of the data in the accompanying table?

<table>
<thead>
<tr>
<th>Scores ($x_i$)</th>
<th>Frequency ($f_i$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>25</td>
<td>3</td>
</tr>
<tr>
<td>20</td>
<td>2</td>
</tr>
<tr>
<td>11</td>
<td>5</td>
</tr>
<tr>
<td>10</td>
<td>4</td>
</tr>
</tbody>
</table>


14. Two social studies classes took the same current events examination that was scored on the basis of 100 points. Mr. Wong's class had a median score of 78 and a range of 4 points, while Ms. Rizzo's class had a median score of 78 and a range of 22 points. Explain how these classes could have the same median score while having very different ranges.
AVERAGE KNOWN WITH MISSING DATA

15. The mean (average) weight of three dogs is 38 pounds. One of the dogs, Sparky, weighs 46 pounds. The other two dogs, Eddie and Sandy, have the same weight. Find Eddie's weight.

16. If 6 and \(x\) have the same mean (average) as 2, 4, and 24, what is the value of \(x\)?

17. TOP Electronics is a small business with five employees. The mean (average) weekly salary for the five employees is $360. If the weekly salaries of four of the employees are $340, $340, $345, and $425, what is the salary of the fifth employee?

18. During each marking period, there are five tests. If Vanita needs a 65 average to pass this marking period and her first four grades are 60, 72, 55, and 80, what is the lowest score she can earn on the last test to have a passing average?

19. The exact average of a set of six test scores is 92. Five of these scores are 90, 98, 96, 94, and 85. What is the other test score?

20. The students in Woodland High School's meteorology class measured the noon temperature every schoolday for a week. Their readings for the first 4 days were Monday, 56°F; Tuesday, 72°F; Wednesday, 67°F; and Thursday, 61°F. If the mean (average) temperature for the 5 days was exactly 63°F, what was the temperature on Friday?

21. For five algebra examinations, Maria has an average of 88. What must she score on the sixth test to bring her average up to exactly 90?

22. Judy needs a mean (average) score of 86 on four tests to earn a midterm grade of B. If the mean of her scores for the first three tests was 83, what is the lowest score on a 100-point scale that she can receive on the fourth test to have a midterm grade of B?

23. In his first three years coaching baseball at High Ridge High School, Coach Batty's team won 7 games the first year, 16 games the second year, and 4 games the third year. How many games does the team need to win in the fourth year so that the coach's average will be 10 wins per year?

24. On the first six tests in her social studies course, Jerelyn's scores were 92, 78, 86, 92, 95, and 91. Determine the median and the mode of her scores. If Jerelyn took a seventh test and raised the mean of her scores exactly 1 point, what was her score on the seventh test?

25. Tamika could not remember her scores from five mathematics tests. She did remember that the mean (average) was exactly 80, the median was 81, and the mode was 88. If all her scores were integers with 100 the highest score possible and 0 the lowest score possible, what was the lowest score she could have received on any one test?

26. Angelo, Brandon, and Carl work in the same office. Angelo's age is 4 years more than twice Carl's age. Brandon is 5 years younger than Carl. The average of the three ages is 41. Find the age of each of the men.
27. The test scores for 10 students in Ms. Sampson's homeroom were 61, 67, 81, 83, 87, 88, 89, 90, 98, and 100. Which frequency table is accurate for this set of data?

[A]  
<table>
<thead>
<tr>
<th>Interval</th>
<th>Frequency</th>
</tr>
</thead>
<tbody>
<tr>
<td>61–70</td>
<td>2</td>
</tr>
<tr>
<td>71–80</td>
<td>0</td>
</tr>
<tr>
<td>81–90</td>
<td>6</td>
</tr>
<tr>
<td>91–100</td>
<td>2</td>
</tr>
</tbody>
</table>

[B]  
<table>
<thead>
<tr>
<th>Interval</th>
<th>Frequency</th>
</tr>
</thead>
<tbody>
<tr>
<td>61–70</td>
<td>2</td>
</tr>
<tr>
<td>71–80</td>
<td>2</td>
</tr>
<tr>
<td>81–90</td>
<td>7</td>
</tr>
<tr>
<td>91–100</td>
<td>10</td>
</tr>
</tbody>
</table>

[C]  
<table>
<thead>
<tr>
<th>Interval</th>
<th>Frequency</th>
</tr>
</thead>
<tbody>
<tr>
<td>61–70</td>
<td>2</td>
</tr>
<tr>
<td>71–80</td>
<td>0</td>
</tr>
<tr>
<td>81–90</td>
<td>8</td>
</tr>
<tr>
<td>91–100</td>
<td>10</td>
</tr>
</tbody>
</table>

[D]  
<table>
<thead>
<tr>
<th>Interval</th>
<th>Frequency</th>
</tr>
</thead>
<tbody>
<tr>
<td>61–70</td>
<td>2</td>
</tr>
<tr>
<td>71–80</td>
<td>2</td>
</tr>
<tr>
<td>81–90</td>
<td>8</td>
</tr>
<tr>
<td>91–100</td>
<td>10</td>
</tr>
</tbody>
</table>

28. The following set of data represents the scores on a mathematics quiz: 58, 79, 81, 99, 68, 92, 76, 84, 53, 57, 81, 91, 77, 50, 65, 57, 51, 72, 84, 89. Complete the frequency table below and, on the accompanying grid, draw and label a frequency histogram of these scores.

<table>
<thead>
<tr>
<th>Mathematics Quiz Scores</th>
<th>Interval</th>
<th>Tally</th>
<th>Frequency</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>50–59</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>60–69</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>70–79</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>80–89</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>90–99</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

[Grid representation is not included in the text.]
29. The scores on a mathematics test were 70, 55, 61, 80, 85, 72, 65, 40, 74, 68, and 84. Complete the accompanying table, and use the table to construct a frequency histogram for these scores.

<table>
<thead>
<tr>
<th>Score</th>
<th>Tally</th>
<th>Frequency</th>
</tr>
</thead>
<tbody>
<tr>
<td>40–49</td>
<td></td>
<td></td>
</tr>
<tr>
<td>50–59</td>
<td></td>
<td></td>
</tr>
<tr>
<td>60–69</td>
<td></td>
<td></td>
</tr>
<tr>
<td>70–79</td>
<td></td>
<td></td>
</tr>
<tr>
<td>80–89</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

30. The accompanying histogram shows the heights of the students in Kyra's health class.

What is the total number of students in the class?


31. On a science quiz, 20 students received the following scores: 100, 95, 95, 90, 85, 85, 80, 80, 80, 80, 75, 75, 75, 70, 70, 65, 65, 60, 55. Construct a statistical graph, such as a histogram or a stem-and-leaf plot, to display this data. [Be sure to title the graph and label all axes or parts used.]

If your type of plot requires a grid, show your work here.

If no grid is necessary, show your work here.
32. Sarah's mathematics grades for one marking period were 85, 72, 97, 81, 77, 93, 100, 75, 86, 70, 96, and 80.
   a. Complete the tally sheet and frequency table below, and construct and label a frequency histogram for Sarah's grades using the accompanying grid.

<table>
<thead>
<tr>
<th>Interval (grades)</th>
<th>Tally</th>
<th>Frequency</th>
</tr>
</thead>
<tbody>
<tr>
<td>61–70</td>
<td></td>
<td></td>
</tr>
<tr>
<td>71–80</td>
<td></td>
<td></td>
</tr>
<tr>
<td>81–90</td>
<td></td>
<td></td>
</tr>
<tr>
<td>91–100</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

   b. Which interval contains the 75th percentile (upper quartile)?

33. In the time trials for the 400-meter run at the state sectionals, the 15 runners recorded the times shown in the table below.

<table>
<thead>
<tr>
<th>400-Meter Run</th>
</tr>
</thead>
<tbody>
<tr>
<td>Time (sec)</td>
</tr>
<tr>
<td>50.0–50.9</td>
</tr>
<tr>
<td>51.0–51.9</td>
</tr>
<tr>
<td>52.0–52.9</td>
</tr>
<tr>
<td>53.0–53.9</td>
</tr>
<tr>
<td>54.0–54.9</td>
</tr>
</tbody>
</table>

   a. Using the data from the frequency column, draw a frequency histogram on the grid provided below.

   b. What percent of the runners completed the time trial between 52.0 and 53.9 seconds?
34. Construct a stem-and-leaf plot listing the scores below in order from lowest to highest.
15, 25, 28, 32, 39, 40, 43, 26, 50, 75, 65, 19, 55, 72, 50

35. The following data consists of the weights, in pounds, of 30 adults:
Using the data, complete the accompanying cumulative frequency table and construct a cumulative frequency histogram on the grid below.

<table>
<thead>
<tr>
<th>Interval</th>
<th>Frequency</th>
<th>Cumulative Frequency</th>
</tr>
</thead>
<tbody>
<tr>
<td>51–100</td>
<td></td>
<td></td>
</tr>
<tr>
<td>101–150</td>
<td></td>
<td></td>
</tr>
<tr>
<td>151–200</td>
<td></td>
<td></td>
</tr>
<tr>
<td>201–250</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
36. The accompanying table shows the weights, in pounds, for the students in an algebra class. Using the data, complete the cumulative frequency table and construct a cumulative frequency histogram on the grid below.

<table>
<thead>
<tr>
<th>Interval</th>
<th>Frequency</th>
<th>Cumulative Frequency</th>
</tr>
</thead>
<tbody>
<tr>
<td>91–100</td>
<td>6</td>
<td></td>
</tr>
<tr>
<td>101–110</td>
<td>3</td>
<td></td>
</tr>
<tr>
<td>111–120</td>
<td>0</td>
<td></td>
</tr>
<tr>
<td>121–130</td>
<td>3</td>
<td></td>
</tr>
<tr>
<td>131–140</td>
<td>0</td>
<td></td>
</tr>
<tr>
<td>141–150</td>
<td>2</td>
<td></td>
</tr>
<tr>
<td>151–160</td>
<td>2</td>
<td></td>
</tr>
</tbody>
</table>

37. Tara buys two items that cost $d$ dollars each. She gives the cashier $20. Which expression represents the change she should receive?

[A] $20 - 2d$  
[B] $20 - d$  
[C] $2d - 20$  
[D] $20 + 2d$

38. The sum of Scott's age and Greg's age is 33 years. If Greg's age is represented by $g$, Scott's age is represented by

[A] $33g$  
[B] $33 - g$  
[C] $g + 33$  
[D] $g - 33$

39. Which expression represents "5 less than the product of 7 and $x"$?

[A] $5 - 7x$  
[B] $7(x - 5)$  
[C] $7x - 5$  
[D] $7 + x - 5$

40. A store advertises that during its Labor Day sale $15 will be deducted from every purchase over $100. In addition, after the deduction is taken, the store offers an early-bird discount of 20% to any person who makes a purchase before 10 a.m. If Hakeem makes a purchase of $x$ dollars, $x > 100$, at 8 a.m., what, in terms of $x$, is the cost of Hakeem's purchase?

[A] $0.80x - 12$  
[B] $0.20x - 15$  
[C] $0.85x - 20$  
[D] $0.20x - 3$

**CHAPTER 1-3**

**ORDER OF OPERATIONS**

41. On February 18, from 9 a.m. until 2 p.m., the temperature rose from $-14^\circ F$ to $36^\circ F$. What was the total increase in temperature during this time period?

[A] $50^\circ$  
[B] $36^\circ$  
[C] $32^\circ$  
[D] $22^\circ$

42. If the expression $3 - 4^2 + \frac{6}{2}$ is evaluated, what would be done last?

[A] adding  
[B] dividing  
[C] squaring  
[D] subtracting
43. What is the first step in simplifying the expression \((2 - 3 \times 4 + 5)^2\)?
   - [A] square 5
   - [B] multiply 3 by 4
   - [C] subtract 3 from 2
   - [D] add 4 and 5

44. The expression \(15 - 3[2 + 6(-3)]\) simplifies to
   - [A] 192
   - [B] 63
   - [C] -45
   - [D] -33

**EVALUATING VARIABLE EXPRESSIONS**

45. Brett was given the problem: "Evaluate \(2x^2 + 5\) when \(x = 3\)." Brett wrote that the answer was 41. Was Brett correct? Explain your answer.

46. If \(x = -4\) and \(y = 3\), what is the value of \(x - 3y^2\)?
   - [A] -85
   - [B] -13
   - [C] -23
   - [D] -31

47. If \(t = -3\), then \(3t^2 + 5t + 6\) equals
   - [A] -6
   - [B] -36
   - [C] 6
   - [D] 18

48. If \(a = 3\) and \(b = -1\), what is the value of \(ab - b^2\)?
   - [A] -4
   - [B] 4
   - [C] 2
   - [D] -2

49. What is the value of \(\frac{x^2 - 4y}{2}\), if \(x = 4\) and \(y = -3\)?
   - [A] 14
   - [B] -2
   - [C] 2
   - [D] 10

50. If \(x = 4\) and \(y = -2\), the value of \(\frac{1}{2}x y^2\) is
   - [A] -8
   - [B] -4
   - [C] 8
   - [D] 32

**CHAPTER 1-4**

**PROPERTIES OF INTEGERS**

51. If the number represented by \(n - 3\) is an odd integer, which expression represents the next greater odd integer?
   - [A] \(n - 1\)
   - [B] \(n + 1\)
   - [C] \(n - 5\)
   - [D] \(n - 2\)

52. If \(n + 4\) represents an odd integer, the next larger odd integer is represented by
   - [A] \(n + 2\)
   - [B] \(n + 3\)
   - [C] \(n + 5\)
   - [D] \(n + 6\)

53. Which expression represents the product of two consecutive odd integers, where \(n\) is an odd integer?
   - [A] \(n(n + 1)\)
   - [B] \(n(n + 3)\)
   - [C] \(n(n + 2)\)
   - [D] \(2n + 1\)

54. If \(n\) represents an odd number, which computation results in an answer that is an even number?
   - [A] \(3 \times n + 1\)
   - [B] \(3 \times n - 2\)
   - [C] \(2 \times n + 1\)
   - [D] \(2 \times n - 1\)

55. If \(a\) is an odd number, \(b\) an even number, and \(c\) an odd number, which expression will always be equivalent to an odd number?
   - [A] \(ac(b)^1\)
   - [B] \(ac(b)^2\)
   - [C] \(ac(b)^3\)
   - [D] \(a(bc)\)

56. If \(a\) and \(b\) are both odd integers, which expression must always equal an odd integer?
   - [A] \(a + b\)
   - [B] \(\frac{a}{b}\)
   - [C] \(a \cdot b\)
   - [D] \(a - b\)
57. Tom scored 23 points in a basketball game. He attempted 15 field goals and 6 free throws. If each successful field goal is 2 points and each successful free throw is 1 point, is it possible he successfully made all 6 of his free throws? Justify your answer.

**ABSOLUTE VALUE**

58. The expression \(-|-7|\) is equivalent to

[A] -7  [B] 0  [C] 1  [D] 7

59. If \(r = 2\) and \(s = -7\), what is the value of \(|r| - |s|\)?


**CHAPTER 1-6**

**RATIONAL NUMBERS**

60. The number 0.14114111411114 . . . is

[C] rational  [D] irrational

61. Write an irrational number and explain why it is irrational.

62. Which number below is irrational?

\(\sqrt{4}, \sqrt{20}, \sqrt{121}\)

Why is the number you chose an irrational number?

63. Which number is irrational?

[A] \(\sqrt{8}\)  [B] \(\sqrt{9}\)  [C] \(\frac{2}{3}\)  [D] 0.3333

64. Which expression represents an irrational number?

[A] 0  [B] \(\sqrt{2}\)  [C] 0.17  [D] \(\frac{1}{2}\)

65. Which is an irrational number?

[A] \(\frac{3}{4}\)  [B] \(\sqrt{3}\)  [C] 3.14  [D] \(\sqrt{9}\)

66. Which is an irrational number?

[A] \(\sqrt{9}\)  [B] 0  [C] \(\pi\)  [D] \(-\frac{1}{3}\)

67. Which is an irrational number?

[A] \(\pi\)  [B] \(0.\overline{3}\)  [C] \(\sqrt{49}\)  [D] \(\frac{3}{8}\)

68. Given: \(\sqrt{99}, \sqrt{164}, \sqrt{196}\)

Identify the expression that is a rational number and explain why it is rational.

69. Which number is rational?

[A] \(\sqrt{7}\)  [B] \(\pi\)  [C] \(\frac{\sqrt{3}}{2}\)  [D] \(\frac{5}{4}\)

70. Which is a rational number?

[A] \(5\sqrt{9}\)  [B] \(\sqrt{8}\)  [C] \(6\sqrt{2}\)  [D] \(\pi\)

71. Which expression is rational?

[A] \(\sqrt{\frac{1}{2}}\)  [B] \(\pi\)  [C] \(\sqrt{3}\)  [D] \(\sqrt{\frac{1}{4}}\)

**COMPARING REALS**

72. Kyoko's mathematics teacher gave her the accompanying cards and asked her to arrange the cards in order from least to greatest. In what order should Kyoko arrange the cards?

\[\pi, \sqrt{8}, 3.\overline{1}, 2\sqrt{3}, 2\frac{3}{8}\]
73. In which list are the numbers in order from least to greatest?

[A] \( \sqrt{3}, \pi, 3.2, 3 \frac{1}{3} \)  [B] \( 3.2, 3 \frac{1}{3}, \sqrt{3}, \pi \)

[C] \( 3.2, \pi, 3 \frac{1}{3}, \sqrt{3} \)  [D] \( \sqrt{3}, 3.2, \pi, 3 \frac{1}{3} \)

74. Which numbers are arranged from smallest to largest?

[A] \( \sqrt{9.1}, 3.14, \pi, \frac{22}{7} \)

[B] \( \sqrt{9.1}, 3.14, \frac{22}{7}, \pi \)

[C] \( \sqrt{9.1}, \pi, 3.14, \frac{22}{7} \)

[D] \( 3.14, \frac{22}{7}, \pi, \sqrt{9.1} \)

75. Which list is in order from smallest value to largest value?

[A] \( \sqrt{10}, \frac{22}{7}, \pi, 3.1 \)  [B] \( 3.1, \frac{22}{7}, \pi, \sqrt{10} \)

[C] \( 3.1, \pi, \frac{22}{7}, \sqrt{10} \)  [D] \( \pi, \frac{22}{7}, 3.1, \sqrt{10} \)

76. Which list shows the numbers \(-0.12, \frac{1}{8}, \frac{1}{9}, \frac{1}{82}\) in order from smallest to largest?

[A] \( \frac{1}{8}, \frac{1}{9}, -0.12, \frac{1}{82} \)

[B] \( \frac{1}{82}, -0.12, \frac{1}{9}, \frac{1}{8} \)

[C] \( \frac{1}{8}, \frac{1}{9}, \frac{1}{82}, -0.12 \)

[D] \( -0.12, \frac{1}{8}, \frac{1}{9}, \frac{1}{82} \)

77. Which expression has the smallest value?

[A] \(-\pi\)  [B] \(-\sqrt{10}\)

[C] \(-\frac{16}{5}\)  [D] \(-3.02\)

78. Which number has the greatest value?

[A] \( \frac{\pi}{2} \)  [B] \( 1\frac{2}{3} \)  [C] \( \sqrt{2} \)  [D] \( 1.5 \)

79. Which inequality is true if \( x = \frac{3.04}{1.48} \), \( y = 1.99 + 0.33 \), and \( z = (1.3)^3 \)?

[A] \( x < z < y \)  [B] \( x < y < z \)

[C] \( y < z < x \)  [D] \( y < x < z \)

80. If \( t^2 < t < \sqrt{t} \), then \( t \) could be

[A] \( 4 \)  [B] \( -\frac{1}{4} \)  [C] \( 0 \)  [D] \( \frac{1}{4} \)

81. If \( x^3 < x < \frac{1}{x} \), then \( x \) could be equal to

[A] \( 5 \)  [B] \( \frac{6}{5} \)  [C] \( 1 \)  [D] \( \frac{1}{5} \)

82. Let \( x \) and \( y \) be numbers such that \( 0 < x < y < 1 \), and let \( d = x - y \). Which graph could represent the location of \( d \) on the number line?

[A] 

[B] 

[C] 

[D]
83. If \( a < b \), \( c < d \), and \( a, b, c, \) and \( d \) are all greater than 0, which expression is always true?

[A] \( ac < bd \)  
[B] \( a - c + b - d = 0 \)  
[C] \( \frac{a}{d} > \frac{b}{c} \)  
[D] \( a + c > b + d \)

84. If \( a \) and \( b \) are integers, which equation is always true?

[A] \( a + b = b + a \)  
[B] \( \frac{a}{b} = \frac{b}{a} \)  
[C] \( a + 2b = b + 2a \)  
[D] \( a - b = b - a \)

85. If \( M \) and \( A \) represent integers, \( M + A = A + M \) is an example of which property?

[A] associative  
[B] distributive  
[C] commutative  
[D] closure

86. Which expression is an example of the associative property?

[A] \( (x + y) + z = x + (y + z) \)  
[B] \( x + y + z = z + y + x \)  
[C] \( x \cdot 1 = x \)  
[D] \( x(y + z) = xy + xz \)

87. Which equation illustrates the associative property of addition?

[A] \( 3(x + 2) = 3x + 6 \)  
[B] \( x + y = y + x \)  
[C] \( 3 + x + y = 3 + (x + y) \)  
[D] \( 3 + x = 0 \)

88. The equation \(*(\Delta + \Diamond) = *\Delta + *\Diamond\) is an example of the

[A] associative law  
[B] distributive law  
[C] commutative law  
[D] transitive law

89. Which equation illustrates the distributive property?

[A] \( 5(a + b) = 5a + 5b \)  
[B] \( a + 0 = a \)  
[C] \( a + (b + c) = (a + b) + c \)  
[D] \( a + b = b + a \)

90. Which equation illustrates the distributive property for real numbers?

[A] \( \sqrt{3} + 0 = \sqrt{3} \)  
[B] \(-3(5 + 7) = (-3)(5) + (-3)(7) \)  
[C] \((1.3 \times 0.07) \times 0.63 = 1.3 \times (0.07 \times 0.63) \)  
[D] \( \frac{1}{3} + \frac{1}{2} = \frac{1}{2} + \frac{1}{3} \)

91. Tori computes the value of \( 8 \times 95 \) in her head by thinking \( 8(100 - 5) = 8 \times 100 - 8 \times 5 \). Which number property is she using?

[A] closure  
[B] associative  
[C] distributive  
[D] commutative

92. What is the additive inverse of \( \frac{2}{3} \)?

[A] \( -\frac{2}{3} \)  
[B] \( \frac{3}{2} \)  
[C] \( -\frac{3}{2} \)  
[D] \( \frac{1}{3} \)

93. Which expression must be added to \( 3x - 7 \) to equal 0?

[A] \(-3x + 7\)  
[B] \(-3x - 7\)  
[C] 0  
[D] \(3x + 7\)
94. While solving the equation \(4(x + 2) = 28\), Becca wrote \(4x + 8 = 28\). Which property did she use?

- [A] distributive
- [B] identity
- [C] associative
- [D] commutative

95. Which property is illustrated by the equation \(\frac{3}{2}x + 0 = \frac{3}{2}x\)?

- [A] distributive property
- [B] additive inverse property
- [C] additive identity property
- [D] commutative property of addition

96. Which property of real numbers is illustrated by the equation \(-\sqrt{3} + \sqrt{3} = 0\)

- [A] additive identity
- [B] commutative property of addition
- [C] associative property of addition
- [D] additive inverse

97. If \(a \neq 0\) and the sum of \(x\) and \(\frac{1}{a}\) is 0, then

- [A] \(x = 1 - a\)
- [B] \(x = -\frac{1}{a}\)
- [C] \(x = -a\)
- [D] \(x = a\)

98. What is the multiplicative inverse of \(\frac{3}{4}\)?

- [A] \(-\frac{4}{3}\)
- [B] -1
- [C] \(\frac{4}{3}\)
- [D] \(-\frac{3}{4}\)

99. The multiplicative inverse of \(-\frac{1}{3}\) is

- [A] \(\frac{1}{3}\)
- [B] -3
- [C] 3
- [D] \(-\frac{1}{3}\)

100. Which equation illustrates the multiplicative inverse property?

- [A] \(-1 \cdot x = -x\)
- [B] \(1 \cdot 0 = 0\)
- [C] \(1 \cdot x = x\)
- [D] \(x \cdot \frac{1}{x} = 1\)

101. Which statement best illustrates the additive identity property?

- [A] \(6 + 2 = 2 + 6\)
- [B] \(6 + 0 = 6\)
- [C] \(6 + (-6) = 0\)
- [D] \(6(2) = 2(6)\)

102. Which equation is an illustration of the additive identity property?

- [A] \(x + 0 = x\)
- [B] \(x - x = 0\)
- [C] \(x \cdot \frac{1}{x} = 1\)
- [D] \(x \cdot 1 = x\)

103. Which equation illustrates the multiplicative identity element?

- [A] \(x \cdot \frac{1}{x} = 1\)
- [B] \(x \cdot 1 = x\)
- [C] \(x + 0 = x\)
- [D] \(x - x = 0\)

104. Which set is closed under division?

- [A] integers
- [B] \(\{1\}\)
- [C] whole numbers
- [D] counting numbers

105. Ramón said that the set of integers is not closed for one of the basic operations (addition, subtraction, multiplication, or division). You want to show Ramón that his statement is correct.

- For the operation for which the set of integers is not closed, write an example using:
  - a positive even integer and a zero
  - a positive and a negative even integer
  - two negative even integers

Be sure to explain why each of your examples illustrates that the set of integers is not closed for that operation.
106. The operation element @ is determined by the following table:

<table>
<thead>
<tr>
<th>@</th>
<th>a</th>
<th>b</th>
<th>c</th>
</tr>
</thead>
<tbody>
<tr>
<td>a</td>
<td>a</td>
<td>b</td>
<td>c</td>
</tr>
<tr>
<td>b</td>
<td>b</td>
<td>c</td>
<td>a</td>
</tr>
<tr>
<td>c</td>
<td>c</td>
<td>a</td>
<td>b</td>
</tr>
</tbody>
</table>

What is the identity element of this operation?

[A] b, only
[B] a, only
[C] a and b
[D] c

107. What is the identity element for ♦ in the accompanying table?

<table>
<thead>
<tr>
<th>♦</th>
<th>r</th>
<th>s</th>
<th>t</th>
<th>u</th>
</tr>
</thead>
<tbody>
<tr>
<td>r</td>
<td>t</td>
<td>r</td>
<td>u</td>
<td>s</td>
</tr>
<tr>
<td>s</td>
<td>r</td>
<td>s</td>
<td>t</td>
<td>u</td>
</tr>
<tr>
<td>t</td>
<td>u</td>
<td>t</td>
<td>s</td>
<td>r</td>
</tr>
<tr>
<td>u</td>
<td>s</td>
<td>u</td>
<td>r</td>
<td>t</td>
</tr>
</tbody>
</table>

[A] u
[B] s
[C] t
[D] r

108. An addition table for a subset of real numbers is shown below. Which number is the identity element? Explain your answer.

<table>
<thead>
<tr>
<th>+</th>
<th>0</th>
<th>1</th>
<th>2</th>
<th>3</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0</td>
<td>1</td>
<td>2</td>
<td>3</td>
</tr>
<tr>
<td>1</td>
<td>1</td>
<td>2</td>
<td>3</td>
<td>4</td>
</tr>
<tr>
<td>2</td>
<td>2</td>
<td>3</td>
<td>4</td>
<td>0</td>
</tr>
<tr>
<td>3</td>
<td>3</td>
<td>4</td>
<td>0</td>
<td>1</td>
</tr>
</tbody>
</table>

109. The operation * for the set \{p,r,s,v\} is defined in the accompanying table. What is the inverse element of r under the operation *?

<table>
<thead>
<tr>
<th>*</th>
<th>p</th>
<th>r</th>
<th>s</th>
<th>v</th>
</tr>
</thead>
<tbody>
<tr>
<td>p</td>
<td>s</td>
<td>v</td>
<td>p</td>
<td>r</td>
</tr>
<tr>
<td>r</td>
<td>v</td>
<td>p</td>
<td>s</td>
<td>r</td>
</tr>
<tr>
<td>s</td>
<td>p</td>
<td>r</td>
<td>s</td>
<td>v</td>
</tr>
<tr>
<td>v</td>
<td>r</td>
<td>s</td>
<td>v</td>
<td>p</td>
</tr>
</tbody>
</table>

[A] r
[B] p
[C] s
[D] v

110. In the addition table for a subset of real numbers shown below, which number is the inverse of 3? Explain your answer.

<table>
<thead>
<tr>
<th>⊕</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>2</td>
<td>3</td>
<td>4</td>
<td>1</td>
</tr>
<tr>
<td>2</td>
<td>3</td>
<td>4</td>
<td>1</td>
<td>2</td>
</tr>
<tr>
<td>3</td>
<td>4</td>
<td>1</td>
<td>2</td>
<td>3</td>
</tr>
<tr>
<td>4</td>
<td>1</td>
<td>2</td>
<td>3</td>
<td>4</td>
</tr>
</tbody>
</table>
CHAPTER 2-2

RELATING GRAPHS TO EVENTS

111. John left his home and walked 3 blocks to his school, as shown in the accompanying graph.

What is one possible interpretation of the section of the graph from point B to point C?

[A] John arrived at school and stayed throughout the day.
[B] John reached the top of a hill and began walking on level ground.
[C] John waited before crossing a busy street.
[D] John returned home to get his mathematics homework.

112. The accompanying graph shows the amount of water left in Rover's water dish over a period of time.

How long did Rover wait from the end of his first drink to the start of his second drink of water?


113. The accompanying graph shows Marie's distance from home (A) to work (F) at various times during her drive.

a Marie left her briefcase at home and had to return to get it. State which point represents when she turned back around to go home and explain how you arrived at that conclusion.
b Marie also had to wait at the railroad tracks for a train to pass. How long did she wait?

114. A bug travels up a tree, from the ground, over a 30-second interval. It travels fast at first and then slows down. It stops for 10 seconds, then proceeds slowly, speeding up as it goes. Which sketch best illustrates the bug's distance (d) from the ground over the 30-second interval (t)?
CHAPTER 2-6

THREE VIEWS OF A FUNCTION

115. Which linear equation represents the data in the accompanying table?

<table>
<thead>
<tr>
<th>c</th>
<th>d</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>20.00</td>
</tr>
<tr>
<td>1</td>
<td>21.50</td>
</tr>
<tr>
<td>2</td>
<td>23.00</td>
</tr>
<tr>
<td>3</td>
<td>24.50</td>
</tr>
</tbody>
</table>

[A] \( d = 20.00c + 1.50 \)  [B] \( d = 1.50c \)  
[C] \( d = 1.50c + 20.00 \)  [D] \( d = 21.50c \)

116. If \( x \) and \( y \) are defined as indicated by the accompanying table, which equation correctly represents the relationship between \( x \) and \( y \)?

<table>
<thead>
<tr>
<th>( x )</th>
<th>( y )</th>
</tr>
</thead>
<tbody>
<tr>
<td>2</td>
<td>1</td>
</tr>
<tr>
<td>3</td>
<td>3</td>
</tr>
<tr>
<td>5</td>
<td>7</td>
</tr>
<tr>
<td>7</td>
<td>11</td>
</tr>
</tbody>
</table>

[A] \( y = 2x + 2 \)  [B] \( y = 2x + 3 \)  
[C] \( y = 2x - 3 \)  [D] \( y = x + 2 \)

117. Which equation could represent the relationship between the \( x \) and \( y \) values shown in the accompanying table?

<table>
<thead>
<tr>
<th>( x )</th>
<th>( y )</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>2</td>
</tr>
<tr>
<td>1</td>
<td>3</td>
</tr>
<tr>
<td>2</td>
<td>6</td>
</tr>
<tr>
<td>3</td>
<td>11</td>
</tr>
<tr>
<td>4</td>
<td>18</td>
</tr>
</tbody>
</table>

[A] \( y = x + 2 \)  [B] \( y = x^2 + 2 \)  
[C] \( y = x^2 \)  [D] \( y = 2^x \)

CONVERSIONS

118. The formula for changing Celsius (C) temperature to Fahrenheit (F) temperature is 

\[
F = \frac{9}{5} C + 32
\]

Calculate, to the nearest degree, the Fahrenheit temperature when the Celsius temperature is -8.

119. If the temperature in Buffalo is 23°C Fahrenheit, what is the temperature in degrees Celsius? [Use the formula \( C = \frac{5}{9}(F - 32) \).]


120. The formula \( C = \frac{5}{9}(F - 32) \) can be used to find the Celsius temperature (C) for a given Fahrenheit temperature (F). What Celsius temperature is equal to a Fahrenheit temperature of 77°F?


121. The formula \( C = \frac{5}{9}(F - 32) \) is used to convert Fahrenheit temperature, \( F \), to Celsius temperature, \( C \). What temperature, in degrees Fahrenheit, is equivalent to a temperature of 10°C Celsius?
122. Connor wants to compare Celsius and Fahrenheit temperatures by drawing a conversion graph. He knows that $-40^\circ C = -40^\circ F$ and that $20^\circ C = 68^\circ F$. On the accompanying grid, construct the conversion graph and, using the graph, determine the Celsius equivalent of $25^\circ F$.

![Conversion Graph for Celsius and Fahrenheit Temperatures](image)

123. Which inequality represents the probability, $x$, of any event happening?

[A] $x \geq 0$  
[B] $0 \leq x \leq 1$  
[C] $x < 1$  
[D] $0 < x < 1$

124. Mary chooses an integer at random from 1 to 6. What is the probability that the integer she chooses is a prime number?

[A] $\frac{4}{6}$  
[B] $\frac{5}{6}$  
[C] $\frac{3}{6}$  
[D] $\frac{2}{6}$

125. A box contains six black balls and four white balls. What is the probability of selecting a black ball at random from the box?

[A] $\frac{6}{10}$  
[B] $\frac{1}{10}$  
[C] $\frac{4}{6}$  
[D] $\frac{6}{4}$

126. A six-sided number cube has faces with the numbers 1 through 6 marked on it. What is the probability that a number less than 3 will occur on one toss of the number cube?

[A] $\frac{3}{6}$  
[B] $\frac{4}{6}$  
[C] $\frac{1}{6}$  
[D] $\frac{2}{6}$

127. The faces of a cube are numbered from 1 to 6. What is the probability of not rolling a 5 on a single toss of this cube?

[A] $\frac{4}{5}$  
[B] $\frac{1}{5}$  
[C] $\frac{5}{6}$  
[D] $\frac{1}{6}$

128. A fair coin is thrown in the air four times. If the coin lands with the head up on the first three tosses, what is the probability that the coin will land with the head up on the fourth toss?

[A] 0  
[B] $\frac{1}{2}$  
[C] $\frac{1}{16}$  
[D] $\frac{1}{8}$

129. A fair coin is tossed three times. What is the probability that the coin will land tails up on the second toss?

[A] $\frac{2}{3}$  
[B] $\frac{1}{2}$  
[C] $\frac{1}{3}$  
[D] $\frac{3}{4}$

130. When a fair coin was tossed ten times, it landed heads up the first seven times. What is the probability that on the eighth toss the coin will land with tails up?

[A] $\frac{3}{7}$  
[B] $\frac{7}{10}$  
[C] $\frac{3}{10}$  
[D] $\frac{1}{2}$

131. Seth tossed a fair coin five times and got five heads. The probability that the next toss will be a tail is

[A] $\frac{5}{6}$  
[B] $\frac{1}{6}$  
[C] $\frac{1}{2}$  
[D] 0
132. If the probability that it will rain on Thursday is \( \frac{5}{6} \), what is the probability that it will not rain on Thursday?

[A] 0  [B] \( \frac{1}{6} \)  [C] 1  [D] \( \frac{5}{6} \)

133. The party registration of the voters in Jonesville is shown in the table below.

<table>
<thead>
<tr>
<th>Party Registration</th>
<th>Number of Voters Registered</th>
</tr>
</thead>
<tbody>
<tr>
<td>Democrat</td>
<td>6,000</td>
</tr>
<tr>
<td>Republican</td>
<td>5,300</td>
</tr>
<tr>
<td>Independent</td>
<td>3,700</td>
</tr>
</tbody>
</table>

If one of the registered Jonesville voters is selected at random, what is the probability that the person selected is not a Democrat?

[A] 0.400  [B] 0.667  [C] 0.600  [D] 0.333

134. If Laquisha can enter school by any one of three doors and the school has two staircases to the second floor, in how many different ways can Laquisha reach a room on the second floor? Justify your answer by drawing a tree diagram or listing a sample space.

135. The Grimaldis have three children born in different years.
   a. Draw a tree diagram or list a sample space to show all the possible arrangements of boy and girl children in the Grimaldi family.
   b. Using your information from part a, what is the probability that the Grimaldis have three boys?

136. Kimberly has three pair of pants: one black, one red, and one tan. She also has four shirts: one pink, one white, one yellow, and one green. Draw a tree diagram or list the sample space showing all possible outfits that she could wear, if an outfit consists of one pair of pants and one shirt. How many different outfits can Kimberly wear?

CHAPTER 3-2

SOLVING TWO STEP EQUATIONS

137. Solve for \( x \):

\[
\frac{1}{16}x + \frac{1}{4} = \frac{1}{2}
\]

138. If \( 2x + 5 = -25 \) and \( -3m - 6 = 48 \), what is the product of \( x \) and \( m \)?


139. If \( -2x + 3 = 7 \) and \( 3x + 1 = 5 + y \), the value of \( y \) is

[A] 0  [B] 10  [C] 1  [D] -10

140. How many times larger than \( \frac{1}{4}x \) is \( 5x \)?

[A] \( \frac{5}{4} \)  [B] 20  [C] \( \frac{4}{5} \)  [D] 9

141. At the beginning of her mathematics class, Mrs. Reno gives a warm-up problem. She says, "I am thinking of a number such that 6 less than the product of 7 and this number is 85." Which number is she thinking of?

[A] 637  [B] 13  [C] 84  [D] \( \frac{2}{7} \)
142. Mr. Perez owns a sneaker store. He bought 350 pairs of basketball sneakers and 150 pairs of soccer sneakers from the manufacturers for $62,500. He sold all the sneakers and made a 25% profit. If he sold the soccer sneakers for $130 per pair, how much did he charge for one pair of basketball sneakers?

143. Every month, Omar buys pizzas to serve at a party for his friends. In May, he bought three more than twice the number of pizzas he bought in April. If Omar bought 15 pizzas in May, how many pizzas did he buy in April?

CHAPTER 3-3

COMBINING LIKE TERMS

144. The expression $\frac{5x}{6} + \frac{x}{4}$ is equivalent to

[A] $\frac{5x}{24}$  [B] $\frac{3x}{5}$  [C] $\frac{13x}{12}$  [D] $\frac{5x^2}{10}$

145. Ashanti and Maria went to the store to buy snacks for their back-to-school party. They bought bags of chips, pretzels, and nachos. They bought three times as many bags of pretzels as bags of chips, and two fewer bags of nachos than bags of pretzels. If $x$ represents the number of bags of chips they bought, express, in terms of $x$, how many bags of snacks they bought in all.

146. What is the solution of the equation $3y - 5y + 10 = 36$?


147. What is the value of $x$ in the equation $\frac{x}{2} + \frac{x}{6} = 2$?

[A] 3  [B] 12  [C] 8  [D] $\frac{1}{4}$

148. What is the solution set of the equation $\frac{x}{5} + \frac{x}{2} = 14$?

[A] $\{49\}$  [B] $\{10\}$  [C] $\{4\}$  [D] $\{20\}$

149. Sara's telephone service costs $21 per month plus $0.25 for each local call, and long-distance calls are extra. Last month, Sara's bill was $36.64, and it included $6.14 in long-distance charges. How many local calls did she make?

150. The sum of the ages of the three Romano brothers is 63. If their ages can be represented as consecutive integers, what is the age of the middle brother?

CHAPTER 3-4

USING THE DISTRIBUTIVE PROPERTY

151. Which equation illustrates the distributive property of multiplication over addition?

[A] $6(3a + 4b) = 6(4b + 3a)$  
[B] $6(3a + 4b) = 18a + 24b$  
[C] $6(3a + 4b) = 18a + 4b$  
[D] $6(3a + 4b) = (3a + 4b)6$

152. Solve for $x$: $15x - 3(3x + 4) = 6$

[A] $\frac{1}{3}$  [B] $-\frac{1}{2}$  [C] 1  [D] 3

153. What is the value of $n$ in the equation $0.6(n + 10) = 36$?

[A] 5  [B] -4  [C] -0.4  [D] 4

154. What is the value of $p$ in the equation $2(3p - 4) = 10$?

[A] $\frac{1}{3}$  [B] $2\frac{1}{3}$  [C] 3  [D] 1
155. Parking charges at Superior Parking Garage are $5.00 for the first hour and $1.50 for each additional 30 minutes. If Margo has $12.50, what is the maximum amount of time she will be able to park her car at the garage?

[A] 2 $\frac{1}{2}$ hours  [B] 6 $\frac{1}{2}$ hours  
[C] 3 $\frac{1}{2}$ hours  [D] 6 hours

156. Mario paid $44.25 in taxi fare from the hotel to the airport. The cab charged $2.25 for the first mile plus $3.50 for each additional mile. How many miles was it from the hotel to the airport?


157. A candy store sells 8-pound bags of mixed hazelnuts and cashews. If $c$ pounds of cashews are in a bag, the price $p$ of the bag can be found using the formula $p = 2.59c + 1.72(8 - c)$. If one bag is priced at $18.11, how many pounds of cashews does it contain?

158. In his will, a man leaves one-half of his money to his wife, one-half of what is then left to his older child, and one-half of what is then left to his younger child. His two cousins divide the remainder equally, each receiving $2,000. What was the total amount of money in the man's will?

[A] $16,000  [B] $40,000  
[C] $32,000  [D] $24,000

159. A boy got 50% of the questions on a test correct. If he had 10 questions correct out of the first 12, and $\frac{1}{4}$ of the remaining questions correct, how many questions were on the test?


160. There are 28 students in a mathematics class. If $\frac{1}{4}$ of the students are called to the guidance office, $\frac{1}{3}$ of the remaining students are called to the nurse, and, finally, $\frac{1}{2}$ of those left go to the library, how many students remain in the classroom?

161. In a town election, candidates $A$ and $B$ were running for mayor. There were 30,500 people eligible to vote, and $\frac{3}{4}$ of them actually voted. Candidate $B$ received $\frac{1}{3}$ of the votes cast. How many people voted for candidate $B$? What percent of the votes cast, to the nearest tenth of a percent, did candidate $A$ receive?

162. After an ice storm, the following headlines were reported in the Glacier County Times: Monday: Ice Storm Devastates County - 8 out of every 10 homes lose electrical power Tuesday: Restoration Begins - Power restored to $\frac{1}{2}$ of affected homes Wednesday: More Freezing Rain - Power lost by 20% of homes that had power on Tuesday Based on these headlines, what fractional portion of homes in Glacier County had electrical power on Wednesday?
MATH TOOLBOX P. 133

LOGICAL REASONING

163. At a school costume party, seven girls wore masks and nine boys did not. If there were 15 boys at the party and 20 students did not wear masks, what was the total number of students at the party?


164. Frank, George, and Hernando are a plumber, a cabinet maker, and an electrician, though not necessarily in that order. Each can do all work appropriate to his own field, but no work in other fields. Frank was not able to install a new electric line in his home. Hernando was not able to make cabinets. George is also a building contractor who hired one of the other people to do his electrical work. Which statement must be true?

[A] Frank is a plumber.
[B] Frank is an electrician.
[C] Hernando is an electrician.
[D] George is a cabinet maker.

165. John, Dan, Karen, and Beth went to a costume ball. They chose to go as Anthony and Cleopatra, and Romeo and Juliet. John got the costumes for Romeo and Cleopatra, but not his own costume. Dan saw the costumes for Juliet and himself. Karen went as Anthony. Beth drove two of her friends, who were dressed as Anthony and Cleopatra, to the ball. What costume did John wear?

CHAPTER 3-6

PROBABILITY OF MULTIPLE EVENTS

166. Selena and Tracey play on a softball team. Selena has 8 hits out of 20 times at bat, and Tracey has 6 hits out of 16 times at bat. Based on their past performance, what is the probability that both girls will get a hit next time at bat?

[A] \( \frac{31}{40} \)  [B] \( \frac{48}{320} \)  [C] 1  [D] \( \frac{14}{36} \)

167. Bob and Laquisha have volunteered to serve on the Junior Prom Committee. The names of twenty volunteers, including Bob and Laquisha, are put into a bowl. If two names are randomly drawn from the bowl without replacement, what is the probability that Bob's name will be drawn first and Laquisha's name will be drawn second?

[A] \( \frac{1}{20} \cdot \frac{1}{19} \)  [B] \( \frac{1}{20} \cdot \frac{1}{20} \)  
[C] \( \frac{2}{20!} \)  [D] \( \frac{2}{20} \)

168. A student council has seven officers, of which five are girls and two are boys. If two officers are chosen at random to attend a meeting with the principal, what is the probability that the first officer chosen is a girl and the second is a boy?

[A] \( \frac{10}{42} \)  [B] \( \frac{7}{13} \)  [C] \( \frac{2}{7} \)  [D] \( \frac{7}{14} \)

169. The probability that the Cubs win their first game is \( \frac{1}{3} \). The probability that the Cubs win their second game is \( \frac{3}{7} \). What is the probability that the Cubs win both games?

[A] \( \frac{2}{5} \)  [B] \( \frac{1}{7} \)  [C] \( \frac{6}{7} \)  [D] \( \frac{16}{21} \)
170. There are four students, all of different heights, who are to be randomly arranged in a line. What is the probability that the tallest student will be first in line and the shortest student will be last in line?

171. Mr. Yee has 10 boys and 15 girls in his mathematics class. If he chooses two students at random to work on the blackboard, what is the probability that both students chosen are girls?

CHAPTER 3-7

PERCENTS

172. A 14-gram serving of mayonnaise contains 11 grams of fat. What percent of the mayonnaise, to the nearest tenth of a percent, is fat?

173. A recent survey shows that the average man will spend 141,288 hours sleeping, 85,725 hours working, 81,681 hours watching television, 9,945 hours commuting, 1,662 hours kissing, and 363,447 hours on other tasks during his lifetime. What percent of his life, to the nearest tenth of a percent, does he spend sleeping?

174. Twenty-five percent of 88 is the same as what percent of 22?

[A] 100%  [B] \(12 \frac{1}{2}\)%  
[C] 40%  [D] 50%

175. Ninety percent of the ninth grade students at Richbartville High School take algebra. If 180 ninth grade students take algebra, how many ninth grade students do not take algebra?

176. Linda paid $48 for a jacket that was on sale for 25% of the original price. What was the original price of the jacket?


177. Sue bought a picnic table on sale for 50% off the original price. The store charged her 10% tax and her final cost was $22.00. What was the original price of the picnic table?

178. A painting that regularly sells for a price of $55 is on sale for 20% off. The sales tax on the painting is 7%. Will the final total cost of the painting differ depending on whether the salesperson deducts the discount before adding the sales tax or takes the discount after computing the sum of the original price and the sales tax on $55?

179. Walter is a waiter at the Towne Diner. He earns a daily wage of $50, plus tips that are equal to 15% of the total cost of the dinners he serves. What was the total cost of the dinners he served if he earned $170 on Tuesday?

180. In bowling leagues, some players are awarded extra points called their "handicap." The "handicap" in Anthony's league is 80% of the difference between 200 and the bowler's average. Anthony's average is 145. What is Anthony's "handicap"?

181. The Edison Lightbulb Company tests 5% of their daily production of lightbulbs. If 500 bulbs were tested on Tuesday, what was the total number of bulbs produced that day?

[A] 10,000  [B] 100,000  
[C] 25  [D] 1,000
182. Rashawn bought a CD that cost $18.99 and paid $20.51, including sales tax. What was the rate of the sales tax?

[A] 8%  [B] 2%  [C] 3%  [D] 5%

183. The world population was 4.2 billion people in 1982. The population in 1999 reached 6 billion. Find the percent of change from 1982 to 1999.

184. A factory packs CD cases into cartons for a music company. Each carton is designed to hold 1,152 CD cases. The Quality Control Unit in the factory expects an error of less than 5% over or under the desired packing number. What is the least number and the most number of CD cases that could be packed in a carton and still be acceptable to the Quality Control Unit?

185. A hockey team played \( n \) games, losing four of them and winning the rest. The ratio of games won to games lost is

[A] \( \frac{n-4}{4} \)  [B] \( \frac{4}{n} \)  [C] \( \frac{4}{n-4} \)  [D] \( \frac{n}{4} \)

186. If the instructions for cooking a turkey state "Roast turkey at 325° for 20 minutes per pound," how many hours will it take to roast a 20-pound turkey at 325°?

187. In a molecule of water, there are two atoms of hydrogen and one atom of oxygen. How many atoms of hydrogen are in 28 molecules of water?


188. A cake recipe calls for 1.5 cups of milk and 3 cups of flour. Seth made a mistake and used 5 cups of flour. How many cups of milk should he use to keep the proportions correct?

[A] 2.25  [B] 2.5  [C] 1.75  [D] 2

189. A total of $450 is divided into equal shares. If Kate receives four shares, Kevin receives three shares, and Anna receives the remaining two shares, how much money did Kevin receive?


190. During a recent winter, the ratio of deer to foxes was 7 to 3 in one county of New York State. If there were 210 foxes in the county, what was the number of deer in the county?


191. Sterling silver is made of an alloy of silver and copper in the ratio of 37:3. If the mass of a sterling silver ingot is 600 grams, how much silver does it contain?

[A] 48.65 g  [B] 450 g  [C] 555 g  [D] 200 g

192. There are 357 seniors in Harris High School. The ratio of boys to girls is 7:10. How many boys are in the senior class?


193. The profits in a business are to be shared by the three partners in the ratio of 3 to 2 to 5. The profit for the year was $176,500. Determine the number of dollars each partner is to receive.

194. At the Phoenix Surfboard Company, $306,000 in profits was made last year. This profit was shared by the four partners in the ratio 3:3:5:7. How much more money did the partner with the largest share make than one of the partners with the smallest share?
SPEED

195. A car travels 110 miles in 2 hours. At the same rate of speed, how far will the car travel in \( h \) hours?

\[
\text{[A]} \quad \frac{h}{220} \quad \text{[B]} \quad \frac{h}{55} \quad \text{[C]} \quad 220h \quad \text{[D]} \quad 55h
\]

196. A rocket car on the Bonneville Salt Flats is traveling at a rate of 640 miles per hour. How much time would it take for the car to travel 384 miles at this rate?

\[
\text{[A]} \quad 245 \text{ minutes} \quad \text{[B]} \quad 1.7 \text{ hours} \quad \text{[C]} \quad 256 \text{ minutes} \quad \text{[D]} \quad 36 \text{ minutes}
\]

197. Running at a constant speed, Andrea covers 15 miles in \( 2 \frac{1}{2} \) hours. At this speed, how many minutes will it take her to run 2 miles?

198. A truck traveling at a constant rate of 45 miles per hour leaves Albany. One hour later a car traveling at a constant rate of 60 miles per hour also leaves Albany traveling in the same direction on the same highway. How long will it take for the car to catch up to the truck, if both vehicles continue in the same direction on the highway?

199. A bicyclist leaves Bay Shore traveling at an average speed of 12 miles per hour. Three hours later, a car leaves Bay Shore, on the same route, traveling at an average speed of 30 miles per hour. How many hours after the car leaves Bay Shore will the car catch up to the cyclist?

\[
\text{[A]} \quad 8 \quad \text{[B]} \quad 2 \quad \text{[C]} \quad 5 \quad \text{[D]} \quad 4
\]

200. A truck travels 40 miles from point \( A \) to point \( B \) in exactly 1 hour. When the truck is halfway between point \( A \) and point \( B \), a car starts from point \( A \) and travels at 50 miles per hour. How many miles has the car traveled when the truck reaches point \( B \)?

\[
\text{[A]} \quad 25 \quad \text{[B]} \quad 60 \quad \text{[C]} \quad 40 \quad \text{[D]} \quad 50
\]

201. Two trains leave the same station at the same time and travel in opposite directions. One train travels at 80 kilometers per hour and the other at 100 kilometers per hour. In how many hours will they be 900 kilometers apart?

202. Bob and Latoya both drove to a baseball game at a college stadium. Bob lives 70 miles from the stadium and Latoya lives 60 miles from it, as shown in the accompanying diagram. Bob drove at a rate of 50 miles per hour, and Latoya drove at a rate of 40 miles per hour. If they both left home at the same time, who got to the stadium first?

203. A girl can ski down a hill five times as fast as she can climb up the same hill. If she can climb up the hill and ski down in a total of 9 minutes, how many minutes does it take her to climb up the hill?

\[
\text{[A]} \quad 7.2 \quad \text{[B]} \quad 7.5 \quad \text{[C]} \quad 4.5 \quad \text{[D]} \quad 1.8
\]
204. During a 45-minute lunch period, Albert (A) went running and Bill (B) walked for exercise. Their times and distances are shown in the accompanying graph. How much faster was Albert running than Bill was walking, in miles per hour?

![Graph showing exercise times for Albert (A) and Bill (B).]

205. On her first trip, Sari biked 24 miles in \( T \) hours. The following week Sari biked 32 miles in \( T \) hours. Determine the ratio of her average speed on her second trip to her average speed on her first trip.

\[
\frac{32}{24} = \frac{4}{3}
\]

[A] \( \frac{3}{4} \)  [B] \( \frac{3}{2} \)  [C] \( \frac{2}{3} \)  [D] \( \frac{4}{3} \)

206. On a trip, a student drove 40 miles per hour for 2 hours and then drove 30 miles per hour for 3 hours. What is the student's average rate of speed, in miles per hour, for the whole trip?

\[
\frac{40 \times 2 + 30 \times 3}{2 + 3} = \frac{100}{5} = 20 \text{ miles per hour}
\]


207. If Jamar can run \( \frac{3}{5} \) of a mile in 2 minutes 30 seconds, what is his rate in miles per minute?

\[
\frac{\frac{3}{5}}{150} = \frac{1}{50} \text{ miles per minute}
\]

[A] \( 4 \frac{1}{6} \)  [B] \( 4 \frac{1}{5} \)  [C] \( \frac{6}{25} \)  [D] \( 3 \frac{1}{10} \)

208. On a map, 1 centimeter represents 40 kilometers. How many kilometers are represented by 8 centimeters?

\[
8 \times 40 = 320 \text{ kilometers}
\]


209. An image of a building in a photograph is 6 centimeters wide and 11 centimeters tall. If the image is similar to the actual building and the actual building is 174 meters wide, how tall is the actual building, in meters?

\[
\frac{6}{11} = \frac{174}{x} \\
x = \frac{174 \times 11}{6} = 308 \text{ meters}
\]

210. Jordan and Missy are standing together in the schoolyard. Jordan, who is 6 feet tall, casts a shadow that is 54 inches long. At the same time, Missy casts a shadow that is 45 inches long. How tall is Missy?

\[
\frac{6 \times 12}{54} = \frac{72}{54} = \frac{4}{3} \text{ feet}
\]

[A] 5 ft 6 in  [B] 38 in  [C] 86.4 in  [D] 5 ft

211. If a girl 1.2 meters tall casts a shadow 2 meters long, how many meters tall is a tree that casts a shadow 75 meters long at the same time?

\[
\frac{1.2}{2} = \frac{x}{75} \\
x = \frac{1.2 \times 75}{2} = 45 \text{ meters}
\]

212. A 12-foot tree casts a 16-foot shadow. How many feet tall is a nearby tree that casts a 20-foot shadow at the same time?

\[
\frac{12}{16} = \frac{x}{20} \\
x = \frac{12 \times 20}{16} = 15 \text{ feet}
\]

213. What is the value of \( n \) in the equation \( 3n - 8 = 32 - n \)?

\[
4n = 40 \Rightarrow n = 10
\]


214. Solve for \( m \): \( 0.6m + 3 = 2m + 0.2 \)

\[
0.4m = -2.8 \\
m = -7
\]

215. Solve for \( x \): \( 2(x - 3) = 1.2 - x \)

\[
3x = 1.2 + 6 \\
x = 2.4
\]

216. If \( 3(x - 2) = 2x + 6 \), the value of \( x \) is

\[
x = 6
\]

217. If \(2(x + 3) = x + 10\), then \(x\) equals


218. What is the value of \(x\) in the equation \(13x - 2(x + 4) = 8x + 1\)?


219. Solve for \(x\): \(3.3 - x = 3(x - 1.7)\)

220. What is the value of \(x\) in the equation \(5(2x - 7) = 15x - 10\)?

[A] -5    [B] 0.6    [C] 1    [D] -9

221. What is the value of \(x\) in the equation \(6(x - 2) = 36 - 10x\)?

[A] 6    [B] 1.5    [C] 3    [D] -6

222. What is the value of \(x\) in the equation \(\frac{3}{4}x + 2 = \frac{5}{4}x - 6\)?


223. What is the value of \(w\) in the equation \(\frac{1}{2}w + 7 = 2w - 2\)?

[A] \(3 \frac{1}{3}\)    [B] 6    [C] 3.6    [D] 2

224. What is the value of \(w\) in the equation \(\frac{3}{4}w + 8 = \frac{1}{3}w - 7\)?


225. If \(x + y = 9x + y\), then \(x\) is equal to

[A] \(\frac{1}{5}y\)    [B] 8    [C] 0    [D] \(y\)

226. If \(9x + 2a = 3a - 4x\), then \(x\) equals

[A] \(a\)    [B] \(\frac{5a}{12}\)    [C] \(-a\)    [D] \(\frac{a}{13}\)

227. If \(7x + 2a = 3x + 5a\), then \(x\) is equivalent to

[A] \(\frac{7a}{10}\)    [B] \(\frac{7a}{4}\)    [C] \(\frac{3a}{4}\)    [D] \(\frac{3a}{10}\)

228. If one-half of a number is 8 less than two-thirds of the number, what is the number?


229. The number of people on the school board is represented by \(x\). Two subcommittees with an equal number of members are formed, one with \(\frac{2}{3}x - 5\) members and the other with \(\frac{x}{4}\) members. How many people are on the school board?


CHAPTER 4-3

ABSOLUTE VALUE EQUATIONS

230. What is the solution set of the equation \(|x^2 - 2x| = 3x - 6|\)?

[A] \(\{2,\pm3\}\)    [B] \(\{\pm3\}\)

[C] \(\{2,3\}\)    [D] \(\{2\}\)

CHAPTER 4-4

TRANSFORMING FORMULAS

231. The equation \(P = 2L + 2W\) is equivalent to

[A] \(L = \frac{P + 2W}{2}\)    [B] \(L = P - W\)

[C] \(L = \frac{P - 2W}{2}\)    [D] \(2L = \frac{P}{2W}\)
232. In the equation $A = p + prt$, $t$ is equivalent to

[A] $\frac{A - pr}{p}$  [B] $\frac{A - p}{pr}$  
[C] $\frac{A}{pr} - p$  [D] $\frac{A}{p} - pr$

233. The formula for the volume of a right circular cylinder is $V = \pi r^2 h$. The value of $h$ can be expressed as

[A] $\frac{\pi r^2}{V}$  [B] $V - \pi r^2$  
[C] $\frac{V}{\pi r^2}$  [D] $\frac{V}{\pi r^2}$

234. The formula for potential energy is $P = mgh$, where $P$ is potential energy, $m$ is mass, $g$ is gravity, and $h$ is height. Which expression can be used to represent $g$?

[A] $P - mh$  [B] $P - m - h$  
[C] $\frac{P}{mh}$  [D] $\frac{P}{m} - h$

235. Shoe sizes and foot length are related by the formula $S = 3F - 24$, where $S$ represents the shoe size and $F$ represents the length of the foot, in inches.

a. Solve the formula for $F$.

b. To the nearest tenth of an inch, how long is the foot of a person who wears a size $10\frac{1}{2}$ shoe?

236. The volume of any spherical balloon can be found by using the formula $V = \frac{4}{3}\pi r^3$. Write an equation for $r$ in terms of $V$ and $\pi$.

237. If $2m + 2p = 16$, $p$ equals

[A] $8 - m$  [B] $16 - m$  
[C] $16 + 2m$  [D] $9m$

238. If $bx - 2 = K$, then $x$ equals

[A] $\frac{2 - K}{b}$  [B] $\frac{K - 2}{b}$  
[C] $\frac{K}{b} + 2$  [D] $\frac{K + 2}{b}$

239. If $c = 2m + d$, then $m$ is equal to

[A] $\frac{c - d}{2}$  [B] $d - 2c$  
[C] $c - \frac{d}{2}$  [D] $\frac{c - d}{2}$

240. If $x = 2a - b^2$, then $a$ equals

[A] $\frac{b^2 - x}{2}$  [B] $\frac{x - b^2}{2}$  
[C] $\frac{x + b^2}{2}$  [D] $x + b^2$

241. If $2ax - 5x = 2$, then $x$ is equivalent to

[A] $\frac{2 + 5a}{2a}$  [B] $7 - 2a$  
[C] $\frac{1}{a - 5}$  [D] $\frac{2}{2a - 5}$

242. If $\frac{x}{4} - \frac{a}{b} = 0$, $b \neq 0$, then $x$ is equal to

[A] $\frac{-a}{4b}$  [B] $\frac{4a}{b}$  [C] $\frac{a}{4b}$  [D] $\frac{-4a}{b}$

243. If $\sqrt{x - a} = b, x > a$, which expression is equivalent to $x$?

[A] $b^2 - a$  [B] $b - a$  
[C] $b + a$  [D] $b^2 + a$
CHAPTER 4-7

SOLVING INEQUALITIES

244. The inequality \( \frac{1}{2}x + 3 < 2x - 6 \) is equivalent to

[A] \( x > -\frac{5}{6} \)  \quad  [B] \( x > 6 \)
[C] \( x < -\frac{5}{6} \)  \quad  [D] \( x < 6 \)

245. Which graph best represents the solution set for the inequality \( x > \sqrt{2} \)?

[A]  
[B]  
[C]  
[D]  

248. In order to be admitted for a certain ride at an amusement park, a child must be greater than or equal to 36 inches tall and less than 48 inches tall. Which graph represents these conditions?

[A]  
[B]  
[C]  
[D]  

249. Which graph represents the solution set for \( 2x - 4 \leq 8 \) and \( x + 5 \geq 7 \)?

[A]  
[B]  
[C]  
[D]  

250. The manufacturer of Ron\'s car recommends that the tire pressure be at least 26 pounds per square inch and less than 35 pounds per square inch. On the accompanying number line, graph the inequality that represents the recommended tire pressure.

251. If \( a + b \) is less than \( c + d \), and \( d + e \) is less than \( a + b \), then \( e \) is

[A] less than \( c \)  \quad  [B] less than \( d \)
[C] greater than \( d \)  \quad  [D] equal to \( c \)
252. On June 17, the temperature in New York City ranged from 90° to 99°, while the temperature in Niagara Falls ranged from 60° to 69°. The difference in the temperatures in these two cities must be between

[C] 20° and 30°    [D] 20° and 40°

MATH TOOLBOX P. 201

VENN DIAGRAMS

253. The accompanying diagram shows the results of a survey asking which sports the members of the Key Club watch on television.

Which statement or statements are true?
I   The most watched sport is tennis.
II   The least watched sport is baseball.
III  More Key Club members watch tennis than football.

[A] II and III, only    [B] I and II, only
[C] I, only             [D] II, only

254. The accompanying Venn diagram shows the number of students who take various courses. All students in circle A take mathematics. All in circle B take science. All in circle C take technology. What percentage of the students take mathematics or technology?

255. The accompanying Venn diagram shows the results of a survey asking 100 people if they get news by reading newspapers or by watching television.

What is the probability that a person selected at random from this survey does not claim television as a source of getting the news?

[A] $\frac{75}{100}$    [B] $\frac{35}{100}$    [C] $\frac{15}{100}$    [D] $\frac{55}{100}$

256. In a class of 450 students, 300 are taking a mathematics course and 260 are taking a science course. If 140 of these students are taking both courses, how many students are not taking either of these courses?

257. In a class of 50 students, 18 take music, 26
take art, and 2 take both art and music. How
many students in the class are not enrolled in
either music or art?

258. The senior class at South High School
consists of 250 students. Of these students,
130 have brown hair, 160 have brown eyes,
and 90 have both brown hair and brown eyes.
How many members of the senior class have
neither brown hair nor brown eyes?

259. In a telephone survey of 100 households, 32
households purchased Brand A cereal and 45
purchased Brand B cereal. If 10 households
purchased both items, how many of the
households surveyed did not purchase either
Brand A or Brand B cereal?

260. In a survey of 400 teenage shoppers at a large
mall, 240 said they shopped at Abernathy's,
210 said they shopped at Bongo Republic,
and 90 said they shopped at both stores. How
many of the teenage shoppers surveyed did
not shop at either store?

261. In Clark Middle School, there are 60 students
in seventh grade. If 25 of these students take
art only, 18 take music only, and 9 do not take
either art or music, how many take both art
and music?

262. A car dealer has 22 vehicles on his lot. If 8 of
the vehicles are vans and 6 of the vehicles are
red, and 10 vehicles are neither vans nor red,
how many red vans does he have on his lot?

263. A school district offers hockey and
basketball. The result of a survey of 300
students showed:
120 students play hockey, only
90 students play basketball, only
30 students do not participate in either sport
Of those surveyed, how many students play
both hockey and basketball?

264. Seventy-eight students participate in one or
more of three sports: baseball, tennis, and
golf. Four students participate in all three
sports: five play both baseball and golf, only;
two play both tennis and golf, only; and three
play both baseball and tennis, only. If seven
students play only tennis and one plays only
golf, what is the total number of students who
play only baseball?

265. There are 30 students on a school bus. Of
these students, 24 either play in the school
band or sing in the chorus. Six of the students
play in the school band but do not sing in the
chorus. Fourteen of the students sing in the
chorus and also play in the school band. How
many students on the school bus sing in the
chorus but do not play in the band?

266. Jose surveyed 20 of his friends to find out
what equipment they use to play recorded
movies. He found that 12 of his friends have
only DVD players, 5 have both DVD players
and VCRs, and 2 have neither type of player.
The rest of his friends have only VCRs. What
is the total number of his friends that have
VCRs?

267. In Ms. Wright's English class, 16 students are
in band, 7 students play sports, 3 students
participate in both activities, and 9 students
are not in band and do not play sports. How
many students are in Ms. Wright's English
class?

CHAPTER 4-9
INTERPRETING SOLUTIONS

268. In the set of positive integers, what is the
solution set of the inequality 2x - 3 < 5?
[A] {0, 1, 2, 3} [B] {1, 2, 3}
[C] {1, 2, 3, 4} [D] {0, 1, 2, 3, 4}
269. Which number is in the solution set of the inequality $5x + 3 > 38$?

270. Find all negative odd integers that satisfy the following inequality:
   $-3x + 1 \leq 17$

271. There are 461 students and 20 teachers taking buses on a trip to a museum. Each bus can
    seat a maximum of 52. What is the least number of buses needed for the trip?

272. In a hockey league, 87 players play on seven different teams. Each team has at least 12
    players. What is the largest possible number of players on any one team?

273. A doughnut shop charges $0.70 for each doughnut and $0.30 for a carryout box.
    Shirley has $5.00 to spend. At most, how many doughnuts can she buy if she also wants
    them in one carryout box?

274. A swimmer plans to swim at least 100 laps during a 6-day period. During this period, the
    swimmer will increase the number of laps completed each day by one lap. What is the least
    number of laps the swimmer must complete on the first day?

   [A] $\frac{3}{4}$  [B] $-\frac{4}{3}$  [C] $\frac{4}{3}$  [D] $-\frac{3}{4}$

275. If the value of dependent variable $y$ increases as the value of independent variable $x$
    increases, the graph of this relationship could be a
   [A] vertical line  [B] horizontal line
   [C] line with a positive slope  [D] line with a negative slope

CHAPTER 5-1

SLOPE AND DIRECT VARIATION

276. What is the slope of line $\ell$ in the accompanying diagram?

   ![Diagram of line $\ell$]

   [A] $\frac{2}{3}$  [B] $-\frac{2}{3}$  [C] $\frac{3}{2}$  [D] $-\frac{3}{2}$

277. What is the slope of line $\ell$ shown in the accompanying diagram?

   ![Diagram of line $\ell$]

   [A] $\frac{3}{4}$  [B] $-\frac{4}{3}$  [C] $\frac{4}{3}$  [D] $-\frac{3}{4}$
278. The accompanying figure shows the graph of the equation \( x = 5 \).

What is the slope of the line \( x = 5 \)?

279. If a line is horizontal, its slope is
[A] 1  [B] negative  [C] 0  [D] undefined

280. A straight line with slope 5 contains the points (1,2) and (3,\( K \)). Find the value of \( K \).
[The use of the accompanying grid is optional.]

MATH TOOLBOX P. 221

CONVERSIONS

281. Which expression represents the number of yards in \( x \) feet?
[A] \( \frac{x}{3} \)  [B] \( \frac{x}{12} \)  [C] 12\( x \)  [D] 3\( x \)

282. If rain is falling at the rate of 2 inches per hour, how many inches of rain will fall in \( x \) minutes?
[A] \( \frac{x}{30} \)  [B] \( \frac{60}{x} \)  [C] \( \frac{30}{x} \)  [D] 2\( x \)

283. Andy is 6 feet tall. If 1 inch equals 2.54 centimeters, how tall is Andy, to the nearest centimeter?

284. If a United States dollar is worth $1.41 in Canadian money, how much is $100 in Canadian money worth in United States money, to the nearest cent?

CHAPTER 5-3

285. Which table does not show an example of direct variation?

[A] \[
\begin{array}{cc}
2 & 24 \\
4 & 12 \\
6 & 8 \\
8 & 6 \\
\end{array}
\]  
[B] \[
\begin{array}{cc}
1 & 4 \\
2 & 8 \\
3 & 12 \\
4 & 16 \\
\end{array}
\]  
[C] \[
\begin{array}{cc}
1 & \frac{1}{2} \\
2 & 1 \\
3 & \frac{3}{2} \\
4 & 2 \\
\end{array}
\]  
[D] \[
\begin{array}{cc}
-4 & -20 \\
-3 & -15 \\
-2 & -10 \\
-1 & -5 \\
\end{array}
\]
286. Which equation represents the direct variation relationship of the equation \( \frac{x}{y} = \frac{1}{2} \)?

[A] \( y = 3x \)  \quad [B] \( y = x + \frac{1}{2} \)

[C] \( x = 2y \)  \quad [D] \( y = 2x \)

287. Julio's wages vary directly as the number of hours that he works. If his wages for 5 hours are $29.75, how much will he earn for 30 hours?

CHAPTER 5-4

SLOPE INTERCEPT FORM OF A LINE

288. An equation of the line that has a slope of 3 and a \( y \)-intercept of -2 is

[A] \( y = 3x - 2 \)  \quad [B] \( x = 3y - 2 \)

[C] \( y = -2x + 3 \)  \quad [D] \( y = -x \)

289. What is the slope of the line whose equation is \( 2y = 5x + 4 \)?

[A] \( \frac{5}{2} \)  \quad [B] 5  \quad [C] 2  \quad [D] \( \frac{2}{5} \)

290. What is the \( y \)-intercept of the graph of the line whose equation is \( y = -\frac{2}{5}x + 4 \)?

[A] \( -\frac{5}{2} \)  \quad [B] 0  \quad [C] 4  \quad [D] \( -\frac{2}{5} \)

291. If point (-1,0) is on the line whose equation is \( y = 2x + b \), what is the value of \( b \)?

[A] 0  \quad [B] 2  \quad [C] 1  \quad [D] 3

CHAPTER 5-5

GRAPHING AND WRITING LINEAR EQUATIONS

292. Which graph represents the equation \( x = 2 \)?

[A] \[\text{Graph A}\]  \quad [B] \[\text{Graph B}\]

[C] \[\text{Graph C}\]  \quad [D] \[\text{Graph D}\]

293. Which statement describes the graph of \( x = 4 \)?

[A] It has a slope of 4.

[B] It is parallel to the \( y \)-axis.

[C] It passes through the point (0, 4).

[D] It is parallel to the \( x \)-axis.

294. Line \( \ell \) contains the points (0,4) and (2,0). Show that the point (-25,81) does or does not lie on line \( \ell \).

295. Write the equation for the line shown in the accompanying graph. Explain your answer.
296. The accompanying graph represents the yearly cost of playing 0 to 5 games of golf at the Shadybrook Golf Course. What is the total cost of joining the club and playing 10 games during the year?

![Yearly Cost Graph](image)

297. The accompanying table shows the enrollment of a preschool from 1980 through 2000. Write a linear regression equation to model the data in the table.

<table>
<thead>
<tr>
<th>Year (x)</th>
<th>Enrollment (y)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1980</td>
<td>14</td>
</tr>
<tr>
<td>1985</td>
<td>20</td>
</tr>
<tr>
<td>1990</td>
<td>22</td>
</tr>
<tr>
<td>1995</td>
<td>28</td>
</tr>
<tr>
<td>2000</td>
<td>37</td>
</tr>
</tbody>
</table>

298. The 1999 win-loss statistics for the American League East baseball teams on a particular date is shown in the accompanying chart.

<table>
<thead>
<tr>
<th></th>
<th>W</th>
<th>L</th>
</tr>
</thead>
<tbody>
<tr>
<td>New York</td>
<td>52</td>
<td>34</td>
</tr>
<tr>
<td>Boston</td>
<td>49</td>
<td>39</td>
</tr>
<tr>
<td>Toronto</td>
<td>47</td>
<td>43</td>
</tr>
<tr>
<td>Tampa Bay</td>
<td>39</td>
<td>49</td>
</tr>
<tr>
<td>Baltimore</td>
<td>36</td>
<td>51</td>
</tr>
</tbody>
</table>

Find the mean for the number of wins, \( \bar{W} \), and the mean for the number of losses, \( \bar{L} \), and determine if the point \((\bar{W}, \bar{L})\) is a point on the line of best fit. Justify your answer.

299. A real estate agent plans to compare the price of a cottage, \( y \), in a town on the seashore to the number of blocks, \( x \), the cottage is from the beach. The accompanying table shows a random sample of sales and location data. Write a linear regression equation that relates the price of a cottage to its distance from the beach.

Use the equation to predict the price of a cottage, to the nearest dollar, located three blocks from the beach.

<table>
<thead>
<tr>
<th>Number of Blocks from the Beach (x)</th>
<th>Price of a Cottage (y)</th>
</tr>
</thead>
<tbody>
<tr>
<td>5</td>
<td>$132,000</td>
</tr>
<tr>
<td>0</td>
<td>$310,000</td>
</tr>
<tr>
<td>4</td>
<td>$204,000</td>
</tr>
<tr>
<td>2</td>
<td>$238,000</td>
</tr>
<tr>
<td>1</td>
<td>$275,000</td>
</tr>
<tr>
<td>7</td>
<td>$60,800</td>
</tr>
</tbody>
</table>
300. The availability of leaded gasoline in New York State is decreasing, as shown in the accompanying table.

<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Gallons Available (in thousands)</td>
<td>150</td>
<td>124</td>
<td>104</td>
<td>76</td>
<td>50</td>
</tr>
</tbody>
</table>

Determine a linear relationship for $x$ (years) versus $y$ (gallons available), based on the data given. The data should be entered using the year and gallons available (in thousands), such as (1984,150).

If this relationship continues, determine the number of gallons of leaded gasoline available in New York State in the year 2005.

If this relationship continues, during what year will leaded gasoline first become unavailable in New York State?

301. The accompanying table illustrates the number of movie theaters showing a popular film and the film's weekly gross earnings, in millions of dollars.

<table>
<thead>
<tr>
<th>Number of Theaters ($x$)</th>
<th>Gross Earnings ($y$, millions of dollars)</th>
</tr>
</thead>
<tbody>
<tr>
<td>443</td>
<td>2.57</td>
</tr>
<tr>
<td>455</td>
<td>2.65</td>
</tr>
<tr>
<td>493</td>
<td>3.73</td>
</tr>
<tr>
<td>530</td>
<td>4.05</td>
</tr>
<tr>
<td>560</td>
<td>4.76</td>
</tr>
<tr>
<td>657</td>
<td>4.76</td>
</tr>
<tr>
<td>723</td>
<td>3.15</td>
</tr>
<tr>
<td>1,064</td>
<td>9.35</td>
</tr>
</tbody>
</table>

Write the linear regression equation for this set of data, rounding values to five decimal places.

Using this linear regression equation, find the approximate gross earnings, in millions of dollars, generated by 610 theaters. Round your answer to two decimal places.

Find the minimum number of theaters that would generate at least 7.65 million dollars in gross earnings in one week.

302. In a mathematics class of ten students, the teacher wanted to determine how a homework grade influenced a student's performance on the subsequent test. The homework grade and subsequent test grade for each student are given in the accompanying table.

<table>
<thead>
<tr>
<th>Homework Grade ($x$)</th>
<th>Test Grade ($y$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>94</td>
<td>98</td>
</tr>
<tr>
<td>95</td>
<td>94</td>
</tr>
<tr>
<td>92</td>
<td>95</td>
</tr>
<tr>
<td>87</td>
<td>89</td>
</tr>
<tr>
<td>82</td>
<td>85</td>
</tr>
<tr>
<td>80</td>
<td>78</td>
</tr>
<tr>
<td>75</td>
<td>73</td>
</tr>
<tr>
<td>65</td>
<td>67</td>
</tr>
<tr>
<td>50</td>
<td>45</td>
</tr>
<tr>
<td>20</td>
<td>40</td>
</tr>
</tbody>
</table>

a Give the equation of the linear regression line for this set of data.

b A new student comes to the class and earns a homework grade of 78. Based on the equation in part $a$, what grade would the teacher predict the student would receive on the subsequent test, to the nearest integer?
303. The table below shows the results of an experiment that relates the height at which a ball is dropped, \( x \), to the height of its first bounce, \( y \).

<table>
<thead>
<tr>
<th>Drop Height (( x )) (cm)</th>
<th>Bounce Height (( y )) (cm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>100</td>
<td>26</td>
</tr>
<tr>
<td>90</td>
<td>23</td>
</tr>
<tr>
<td>80</td>
<td>21</td>
</tr>
<tr>
<td>70</td>
<td>18</td>
</tr>
<tr>
<td>60</td>
<td>16</td>
</tr>
</tbody>
</table>

Find \( \bar{x} \), the mean of the drop heights.
Find \( \bar{y} \), the mean of the bounce heights.
Find the linear regression equation that best fits the data.
Show that \((\bar{x}, \bar{y})\) is a point on the line of regression. [The use of the grid is optional.]

304. Two different tests were designed to measure understanding of a topic. The two tests were given to ten students with the following results:

<table>
<thead>
<tr>
<th>Test x</th>
<th>75</th>
<th>78</th>
<th>75</th>
<th>95</th>
<th>90</th>
<th>67</th>
<th>96</th>
<th>88</th>
<th>70</th>
<th>78</th>
</tr>
</thead>
<tbody>
<tr>
<td>Test y</td>
<td>81</td>
<td>73</td>
<td>85</td>
<td>85</td>
<td>80</td>
<td>73</td>
<td>66</td>
<td>75</td>
<td>70</td>
<td>78</td>
</tr>
</tbody>
</table>

Construct a scatter plot for these scores, and then write an equation for the line of best fit (round slope and intercept to the nearest hundredth).

Find the correlation coefficient.
Predict the score, to the nearest integer, on test \( y \) for a student who scored 87 on test \( x \).
305. Since 1990, fireworks usage nationwide has grown, as shown in the accompanying table, where \( t \) represents the number of years since 1990, and \( p \) represents the fireworks usage per year, in millions of pounds.

<table>
<thead>
<tr>
<th>Number of Years Since 1990 (( t ))</th>
<th>Fireworks Usage per Year, In Millions of Pounds (( p ))</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>67.6</td>
</tr>
<tr>
<td>2</td>
<td>88.8</td>
</tr>
<tr>
<td>4</td>
<td>119.0</td>
</tr>
<tr>
<td>6</td>
<td>120.1</td>
</tr>
<tr>
<td>7</td>
<td>132.5</td>
</tr>
<tr>
<td>8</td>
<td>118.3</td>
</tr>
<tr>
<td>9</td>
<td>159.2</td>
</tr>
<tr>
<td>11</td>
<td>161.6</td>
</tr>
</tbody>
</table>

Find the equation of the linear regression model for this set of data, where \( t \) is the independent variable. Round values to four decimal places.

Using this equation, determine in what year fireworks usage would have reached 99 million pounds.

Based on this linear model, how many millions of pounds of fireworks would be used in the year 2008? Round your answer to the nearest tenth.

306. A factory is producing and stockpiling metal sheets to be shipped to an automobile manufacturing plant. The factory ships only when there is a minimum of 2,050 sheets in stock. The accompanying table shows the day, \( x \), and the number of sheets in stock, \( f(x) \).

<table>
<thead>
<tr>
<th>Day (( x ))</th>
<th>Sheets in Stock (( f(x) ))</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>860</td>
</tr>
<tr>
<td>2</td>
<td>930</td>
</tr>
<tr>
<td>3</td>
<td>1000</td>
</tr>
<tr>
<td>4</td>
<td>1150</td>
</tr>
<tr>
<td>5</td>
<td>1200</td>
</tr>
<tr>
<td>6</td>
<td>1360</td>
</tr>
</tbody>
</table>

Write the linear regression equation for this set of data, rounding the coefficients to four decimal places.

Use this equation to determine the day the sheets will be shipped.

### CHAPTER 5-7

**STANDARD FORM OF A LINE**

307. The line \( 3x - 2y = 12 \) has

[A] a slope of \( \frac{3}{2} \) and a \( y \)-intercept of -6

[B] a slope of -3 and a \( y \)-intercept of -6

[C] a slope of \( -\frac{3}{2} \) and a \( y \)-intercept of 6

[D] a slope of 3 and a \( y \)-intercept of -2

308. What is the slope of the line whose equation is \( 3x - 4y - 16 = 0 \) ?

[A] \( \frac{3}{4} \)  
[B] 3  
[C] -4  
[D] \( \frac{4}{3} \)
309. What is the slope of the linear equation $5y - 10x = -15$?

310. The graph of the equation $x + 3y = 6$ intersects the y-axis at the point whose coordinates are
   [A] (0,18)  [B] (6,0)  [C] (0,2)  [D] (0,6)

311. Point $(k, -3)$ lies on the line whose equation is $x - 2y = -2$. What is the value of $k$?

312. The graph of the equation $2x + 6y = 4$ passes through point $(x, -2)$. What is the value of $x$?

### CHAPTER 5-8

**PARALLEL AND PERPENDICULAR LINES**

313. Which equation represents a line parallel to the line $y = 2x - 5$?
   [A] $y = -\frac{1}{2}x - 5$  [B] $y = 2x + 5$
   [C] $y = 5x - 2$  [D] $y = -2x - 5$

314. Which equation represents a line that is parallel to the line whose equation is $2x + 3y = 12$?
   [A] $6x + 4y = -2$  [B] $6y + 4x = 2$
   [C] $4x - 6y = 2$  [D] $6y - 4x = 2$

315. Which equation represents a line that is perpendicular to the line whose equation is $-2y = 3x + 7$?
   [A] $y = \frac{3}{2}x - 3$  [B] $y = x + 7$
   [C] $2y = 3x - 3$  [D] $y = \frac{2}{3}x - 3$

316. Which line is perpendicular to the line whose equation is $5y + 6 = -3x$?
   [A] $y = \frac{5}{3}x + 7$  [B] $y = -\frac{3}{5}x + 7$
   [C] $y = -\frac{5}{3}x + 7$  [D] $y = \frac{3}{5}x + 7$

317. Which statement describes the lines whose equations are $y = \frac{1}{3}x + 12$ and $6y = 2x + 6$?
   [A] They intersect each other.
   [B] They are perpendicular to each other.
   [C] They are segments.
   [D] They are parallel to each other.

318. Shanaya graphed the line represented by the equation $y = x - 6$.
   Write an equation for a line that is parallel to the given line.
   Write an equation for a line that is perpendicular to the given line.
   Write an equation for a line that is identical to the given line but has different coefficients.

319. Line $P$ and line $C$ lie on a coordinate plane and have equal slopes. Neither line crosses the second or third quadrant. Lines $P$ and $C$ must
   [A] be perpendicular
   [B] be vertical
   [C] be horizontal
   [D] form an angle of $45^\circ$
320. Which properties best describe the coordinate graph of two distinct parallel lines?

[A] different slopes and different intercepts
[B] same slopes and same intercepts
[C] same slopes and different intercepts
[D] different slopes and same intercepts

321. If two lines are parallel and the slope of one of the lines is \(m\), what is the product of their slopes?

[A] \(m^2\)  [B] 0  [C] 1  [D] 2m

322. If the product of \(x\) and \(\frac{1}{m}\) is \(-1\), \(m \neq 0\), then \(x\) is equivalent to

[A] \(-\frac{1}{m}\)  [B] \(m\)  [C] \(1 - m\)  [D] \(-m\)

CHAPTER 6-3

SOLVING LINEAR SYSTEMS

323. Which ordered pair is the solution of the following system of equations?

\[3x + 2y = 4\]
\[-2x + 2y = 24\]

[A] (2, -5)  [B] (-4, -8)
[C] (2, -1)  [D] (-4, 8)

324. What point is the intersection of the graphs of the lines \(2x - y = 3\) and \(x + y = 3\)?

[A] (3, 0)  [B] (3, 3)
[C] (2, 1)  [D] (1, 2)

325. Which ordered pair satisfies the system of equations below?

\[3x - y = 8\]
\[x + y = 2\]

[A] (2.5, 0.5)  [B] (3, -1)
[C] (2.5, -0.5)  [D] (5, -3)

326. What is the value of \(y\) in the following system of equations?

\[2x + 3y = 6\]
\[2x + y = -2\]


327. When solved graphically, which system of equations will have exactly one point of intersection?

[A] \(y = 0.5x + 30\)  [B] \(y = -x - 20\)
\(y = 0.5x - 30\)
\(y = x + 17\)

[C] \(y = \frac{3}{5}x + 12\)  [D] \(y = -x + 15\)
\(y = -x + 25\)
\(y = 0.6x - 19\)

CHAPTER 6-4

WRITING LINEAR SYSTEMS

328. Tanisha and Rachel had lunch at the mall. Tanisha ordered three slices of pizza and two colas. Rachel ordered two slices of pizza and three colas. Tanisha's bill was $6.00, and Rachel's bill was $5.25. What was the price of one slice of pizza? What was the price of one cola?

329. When Tony received his weekly allowance, he decided to purchase candy bars for all his friends. Tony bought three Milk Chocolate bars and four Creamy Nougat bars, which cost a total of $4.25 without tax. Then he realized this candy would not be enough for all his friends, so he returned to the store and bought an additional six Milk Chocolate bars and four Creamy Nougat bars, which cost a total of $6.50 without tax. How much did each type of candy bar cost?
330. Alexandra purchases two doughnuts and three cookies at a doughnut shop and is charged $3.30. Briana purchases five doughnuts and two cookies at the same shop for $4.95. All the doughnuts have the same price and all the cookies have the same price. Find the cost of one doughnut and find the cost of one cookie.

331. Ramón rented a sprayer and a generator. On his first job, he used each piece of equipment for 6 hours at a total cost of $90. On his second job, he used the sprayer for 4 hours and the generator for 8 hours at a total cost of $100. What was the hourly cost of each piece of equipment?

332. At the local video rental store, José rents two movies and three games for a total of $15.50. At the same time, Meg rents three movies and one game for a total of $12.05. How much money is needed to rent a combination of one game and one movie?

333. The cost of a long-distance telephone call is determined by a flat fee for the first 5 minutes and a fixed amount for each additional minute. If a 15-minute telephone call costs $3.25 and a 23-minute call costs $5.17, find the cost of a 30-minute call.

334. Three times as many robins as cardinals visited a bird feeder. If a total of 20 robins and cardinals visited the feeder, how many were robins?

335. Sal keeps quarters, nickels, and dimes in his change jar. He has a total of 52 coins. He has three more quarters than dimes and five fewer nickels than dimes. How many dimes does Sal have?

336. At a concert, $720 was collected for hot dogs, hamburgers, and soft drinks. All three items sold for $1.00 each. Twice as many hot dogs were sold as hamburgers. Three times as many soft drinks were sold as hamburgers. The number of soft drinks sold was


337. Seth has one less than twice the number of compact discs (CDs) that Jason has. Raoul has 53 more CDs than Jason has. If Seth gives Jason 25 CDs, Seth and Jason will have the same number of CDs. How many CDs did each of the three boys have to begin with?

338. A group of 148 people is spending five days at a summer camp. The cook ordered 12 pounds of food for each adult and 9 pounds of food for each child. A total of 1,410 pounds of food was ordered.

a Write an equation or a system of equations that describes the above situation and define your variables.

b Using your work from part a, find:
   (1) the total number of adults in the group
   (2) the total number of children in the group

339. Arielle has a collection of grasshoppers and crickets. She has 561 insects in all. The number of grasshoppers is twice the number of crickets. Find the number of each type of insect that she has.

340. Mary and Amy had a total of 20 yards of material from which to make costumes. Mary used three times more material to make her costume than Amy used, and 2 yards of material was not used. How many yards of materials did Amy use for her costume?

341. Ben had twice as many nickels as dimes. Altogether, Ben had $4.20. How many nickels and how many dimes did Ben have?
342. Using only 32-cent and 20-cent stamps, Charlie put $3.36 postage on a package he sent to his sister. He used twice as many 32-cent stamps as 20-cent stamps. Determine how many of each type of stamp he used.

343. The owner of a movie theater was counting the money from 1 day's ticket sales. He knew that a total of 150 tickets were sold. Adult tickets cost $7.50 each and children's tickets cost $4.75 each. If the total receipts for the day were $891.25, how many of each kind of ticket were sold?

344. There were 100 more balcony tickets than main-floor tickets sold for a concert. The balcony tickets sold for $4 and the main-floor tickets sold for $12. The total amount of sales for both types of tickets was $3,056.
   a. Write an equation or a system of equations that describes the given situation. Define the variables.
   b. Find the number of balcony tickets that were sold.

345. The ninth graders at a high school are raising money by selling T-shirts and baseball caps. The number of T-shirts sold was three times the number of caps. The profit they received for each T-shirt sold was $5.00, and the profit on each cap was $2.50. If the students made a total profit of $210, how many T-shirts and how many caps were sold?

346. The tickets for a dance recital cost $5.00 for adults and $2.00 for children. If the total number of tickets sold was 295 and the total amount collected was $1,220, how many adult tickets were sold? [Only an algebraic solution can receive full credit.]

347. A ribbon 56 centimeters long is cut into two pieces. One of the pieces is three times longer than the other. Find the lengths, in centimeters, of both pieces of ribbon.

348. Sharu has $2.35 in nickels and dimes. If he has a total of thirty-two coins, how many of each coin does he have?

349. The ratio of Tariq's telephone bill to Pria's telephone bill was 7:5. Tariq's bill was $14 more than Pria's bill. What was Tariq's bill?

350. Two numbers are in the ratio 2:5. If 6 is subtracted from their sum, the result is 50. What is the larger number?

351. Jamie is 5 years older than her sister Amy. If the sum of their ages is 19, how old is Jamie?

352. A total of 600 tickets were sold for a concert. Twice as many tickets were sold in advance than were sold at the door. If the tickets sold in advance cost $25 each and the tickets sold at the door cost $32 each, how much money was collected for the concert?
**BREAK EVEN**

353. Two health clubs offer different membership plans. The graph below represents the total cost of belonging to Club $A$ and Club $B$ for one year.

![Health Club Fees Graph]

$a$ If the yearly cost includes a membership fee plus a monthly charge, what is the membership fee for Club $A$?

$b$ (1) What is the number of the month when the total cost is the same for both clubs?

(2) What is the total cost for Club $A$ when both plans are the same?

$c$ What is the monthly charge for Club $B$?

354. The Eye Surgery Institute just purchased a new laser machine for $500,000 to use during eye surgery. The Institute must pay the inventor $550 each time the machine is used. If the Institute charges $2,000 for each laser surgery, what is the minimum number of surgeries that must be performed in order for the Institute to make a profit?

355. At Ron's Rental, a person can rent a big-screen television for $10 a month plus a one-time "wear-and-tear" fee of $100. At Josie's Rental, the charge is $20 a month and an additional charge of $20 for delivery with no "wear-and-tear" fee.

$a$ If $c$ equals the cost, write one equation representing the cost of the rental for $m$ months at Ron's Rental and one equation representing the cost of the rental for $m$ months at Josie's Rental.

$b$ On the accompanying grid, graph and label each equation.

$c$ From your graph, determine in which month Josie's cost will equal Ron's cost.
356. The senior class is sponsoring a dance. The cost of a student disk jockey is $40, and tickets sell for $2 each. Write a linear equation and, on the accompanying grid, graph the equation to represent the relationship between the number of tickets sold and the profit from the dance. Then find how many tickets must be sold to break even.

357. Currently, Tyrone has $60 and his sister has $135. Both get an allowance of $5 each week. Tyrone decides to save his entire allowance, but his sister spends all of hers each week plus an additional $10 each week. After how many weeks will they each have the same amount of money? [The use of the grid is optional.]

358. Juan has a cellular phone that costs $12.95 per month plus 25¢ per minute for each call. Tiffany has a cellular phone that costs $14.95 per month plus 15¢ per minute for each call. For what number of minutes do the two plans cost the same?

359. A hotel charges $20 for the use of its dining room and $2.50 a plate for each dinner. An association gives a dinner and charges $3 a plate but invites four nonpaying guests. If each person has one plate, how many paying persons must attend for the association to collect the exact amount needed to pay the hotel?


360. The Excel Cable Company has a monthly fee of $32.00 and an additional charge of $8.00 for each premium channel. The Best Cable Company has a monthly fee of $26.00 and additional charge of $10.00 for each premium channel. The Horton family is deciding which of these two cable companies to subscribe to.

   a  For what number of premium channels will the total monthly subscription fee for the Excel and Best Cable companies be the same?
   b  The Horton family decides to subscribe to 2 premium channels for a period of one year.
      (1) Which cable company should they subscribe to in order to spend less money?
      (2) How much money will the Hortons save in one year by using the less expensive company?

361. A cellular telephone company has two plans. Plan A charges $11 a month and $0.21 per minute. Plan B charges $20 a month and $0.10 per minute. After how much time, to the nearest minute, will the cost of plan A be equal to the cost of plan B?

   [A] 81 hr 48 min  [B] 1 hr 36 min
   [C] 81 hr 8 min    [D] 1 hr 22 m
362. Island Rent-a-Car charges a car rental fee of $40 plus $5 per hour or fraction of an hour. Wayne's Wheels charges a car rental fee of $25 plus $7.50 per hour or fraction of an hour. Under what conditions does it cost less to rent from Island Rent-a-Car? [The use of the accompanying grid is optional.]

CHARTER 6-5

LINEAR INEQUALITIES AND SYSTEMS

363. In the graph of , which quadrant is completely shaded?


364. Which ordered pair is not in the solution set of ?

[A] (1,4) [B] (3,8) [C] (1,6) [D] (2,5)

365. Which inequality is represented by the accompanying graph?

[A] \( y > 3 \) [B] \( y < 3 \) 
[C] \( y \leq 3 \) [D] \( y \geq 3 \)

366. Which ordered pair is in the solution set of the system of inequalities shown in the accompanying graph?

[A] (1,5) [B] (3,2) [C] (0,0) [D] (0,1)
CHAPTER 6-6

367. Which point is in the solution set of the system of inequalities shown in the accompanying graph?

[A] (4, -1)  [B] (-4, 1)
[C] (0, 4)  [D] (2, 4)

368. Which coordinate point is in the solution set for the system of inequalities shown in the accompanying graph?

[A] (1,-1)  [B] (0,1)
[C] (3,1)  [D] (2,2)

369. Graph the following systems of inequalities on the accompanying set of axes and label the solution set S:

\[ y > x - 4 \]
\[ y + x \geq 2 \]

[Only a graphic solution can receive full credit.]
CHAPTER 6-7

LINEAR PROGRAMMING

370. A company manufactures bicycles and skateboards. The company's daily production of bicycles cannot exceed 10, and its daily production of skateboards must be less than or equal to 12. The combined number of bicycles and skateboards cannot be more than 16. If \( x \) is the number of bicycles and \( y \) is the number of skateboards, graph on the accompanying set of axes the region that contains the number of bicycles and skateboards the company can manufacture daily.

CHAPTER 6-8

SOLVING NONLINEAR SYSTEMS

371. The accompanying diagram shows the graphs of a linear equation and a quadratic equation.

How many solutions are there to this system of equations?

[A] 3  [B] 1  [C] 2  [D] 0

372. The graphs of the equations \( y = x^2 + 4x - 1 \) and \( y + 3 = x \) are drawn on the same set of axes. At which point do the graphs intersect?

[A] (-2, 1)  [B] (1, -2)  
[C] (-2, -5)  [D] (1, 4)

373. Solve the following system of equations algebraically.

\[
\begin{align*}
  y &= x^2 + 4x - 2 \\
  y &= 2x + 1 
\end{align*}
\]
374. Solve the following system of equations:
\[ y = x^2 + 4x + 1 \]
\[ y = 5x + 3 \]
[The use of the grid is optional.]

375. Solve the following system of equations algebraically or graphically for \( x \) and \( y \):
\[ y = x^2 + 2x - 1 \]
\[ y = 3x + 5 \]
For an algebraic solution, show your work here.
For a graphic solution, show your work here.

376. A rocket is launched from the ground and follows a parabolic path represented by the equation \( y = -x^2 + 10x \). At the same time, a flare is launched from a height of 10 feet and follows a straight path represented by the equation \( y = -x + 10 \). Using the accompanying set of axes, graph the equations that represent the paths of the rocket and the flare, and find the coordinates of the point or points where the paths intersect.

377. What is the total number of points of intersection in the graphs of the equations \( x^2 + y^2 = 16 \) and \( y = 4 \)?
[A] 3  [B] 1  [C] 2  [D] 0

378. What is the total number of points of intersection of the graphs of the equations \( x^2 + y^2 = 16 \) and \( y = x \)?
379. On the set of axes provided below, sketch a circle with a radius of 3 and center at (2,1) and also sketch the graph of the line $2x + y = 8$.

b What is the total number of points of intersection of the two graphs?

380. Solve the following system of equations algebraically or graphically:

$$x^2 + y^2 = 25$$
$$3y - 4x = 0$$

[The use of the accompanying grid is optional.]

381. What is the total number of points of intersection for the graphs of the equations $y = x^2$ and $y = -x^2$?

[A] 1 [B] 2 [C] 0 [D] 3

382. What is one solution of the accompanying system of equations?

$$y = -x^2 + 5$$
$$y = -0.5x^2 + 3$$

[A] (3,5) [B] (-2,1) [C] (0,5) [D] (0,3)

383. A pelican flying in the air over water drops a crab from a height of 30 feet. The distance the crab is from the water as it falls can be represented by the function $h(t) = -16t^2 + 30$, where $t$ is time, in seconds. To catch the crab as it falls, a gull flies along a path represented by the function $g(t) = -8t + 15$. Can the gull catch the crab before the crab hits the water? Justify your answer. [The use of the accompanying grid is optional.]
384. The price of a stock, \(A(x)\), over a 12-month period decreased and then increased according to the equation \(A(x) = 0.75x^2 - 6x + 20\), where \(x\) equals the number of months. The price of another stock, \(B(x)\), increased according to the equation \(B(x) = 2.75x + 1.50\) over the same 12-month period. Graph and label both equations on the accompanying grid. State all prices, to the nearest dollar, when both stock values were the same.

385. What is the total number of points of intersection of the graphs of the equations \(xy = 12\) and \(y = -x^2 + 3\)?


386. The height of a golf ball hit into the air is modeled by the equation \(h = -16t^2 + 48t\), where \(h\) represents the height, in feet, and \(t\) represents the number of seconds that have passed since the ball was hit. What is the height of the ball after 2 seconds?


387. Which is an equation of the line of symmetry for the parabola in the accompanying diagram?

[A] \(x = 2\)  [B] \(y = 3\)  [C] \(x = 4\)  [D] \(x = 3\)

388. Which is an equation of the parabola shown in the accompanying diagram?

[A] \(y = x^2 + 2x + 3\)  [B] \(y = -x^2 + 2x + 3\)  [C] \(y = -x^2 - 2x + 3\)  [D] \(y = x^2 - 2x + 3\)
389. Which quadratic function is shown in the accompanying graph?

[A] \( y = -\frac{1}{2}x^2 \)  
[B] \( y = -2x^2 \)  
[C] \( y = 2x^2 \)  
[D] \( y = \frac{1}{2}x^2 \)  

390. Which equation represents the parabola shown in the accompanying graph?

[A] \( y = 6x^2 \)  
[B] \( y = 6x + 1 \)  
[C] \( y = 6 \)  
[D] \( y = -x^2 + 1 \)  

391. Which equation is best represented by the accompanying graph?

[A] \( y = 6x^2 \)  
[B] \( y = 6x + 1 \)  
[C] \( y = 6 \)  
[D] \( y = -x^2 + 1 \)  

392. What is the equation of a parabola that goes through points (0,1), (-1,6), and (2,3)?

[A] \( y = 2x^2 - 3x + 1 \)  
[B] \( y = 2x^2 + 1 \)  
[C] \( y = x^2 - 3x + 1 \)  
[D] \( y = x^2 + 1 \)  

393. For which quadratic equation is the axis of symmetry \( x = 3 \)?

[A] \( y = x^2 + x + 3 \)  
[B] \( y = -x^2 + 3x + 5 \)  
[C] \( y = -x^2 + 6x + 2 \)  
[D] \( y = x^2 + 6x + 3 \)  

394. The graph of \( y = (x - 3)^2 \) is shifted left 4 units and down 2 units. What is the axis of symmetry of the transformed graph?

[A] \( x = -2 \)  
[B] \( x = 1 \)  
[C] \( x = -1 \)  
[D] \( x = 7 \)  

\[ f(x) = -(x - 3)^2 + 1 \]  
\[ f(x) = (x + 1)^2 - 3 \]  
\[ f(x) = -(x + 3)^2 + 1 \]  
\[ f(x) = -(x - 3)^2 - 3 \]
395. A small rocket is launched from a height of 72 feet. The height of the rocket in feet, \( h \), is represented by the equation 
\[ h(t) = -16t^2 + 64t + 72, \]
where \( t \) = time, in seconds. Graph this equation on the accompanying grid. Use your graph to determine the number of seconds that the rocket will remain at or above 100 feet from the ground. [Only a graphic solution can receive full credit.]

396. An acorn falls from the branch of a tree to the ground 25 feet below. The distance, \( S \), the acorn is from the ground as it falls is represented by the equation 
\[ S(t) = -16t^2 + 25, \]
where \( t \) represents time, in seconds. Sketch a graph of this situation on the accompanying grid. Calculate, to the nearest hundredth of a second, the time the acorn will take to reach the ground.
MINIMUM AND MAXIMUM OF QUADRATICS

397. Amy tossed a ball in the air in such a way that the path of the ball was modeled by the equation \( y = -x^2 + 6x \). In the equation, \( y \) represents the height of the ball in feet and \( x \) is the time in seconds.
   a. Graph \( y = -x^2 + 6x \) for \( 0 \leq x \leq 6 \) on the grid provided below.
   
   ![Graph of y = -x^2 + 6x with grid]

   b. At what time, \( x \), is the ball at its highest point?

398. An architect is designing a museum entranceway in the shape of a parabolic arch represented by the equation \( y = -x^2 + 20x \), where \( 0 \leq x \leq 20 \) and all dimensions are expressed in feet. On the accompanying set of axes, sketch a graph of the arch and determine its maximum height, in feet.
399. Tom throws a ball into the air. The ball travels on a parabolic path represented by the equation \( h = -8t^2 + 40t \), where \( h \) is the height, in feet, and \( t \) is the time, in seconds.

\( a \) On the accompanying set of axes, graph the equation from \( t = 0 \) to \( t = 5 \) seconds, including all integral values of \( t \) from 0 to 5.

\( b \) What is the value of \( t \) at which \( h \) has its greatest value?

400. An arch is built so that it is 6 feet wide at the base. Its shape can be represented by a parabola with the equation \( y = -2x^2 + 12x \), where \( y \) is the height of the arch.

\( a \) Graph the parabola from \( x = 0 \) to \( x = 6 \) on the grid below.

\( b \) Determine the maximum height, \( y \), of the arch.

CHAPTER 7-4

SQUARE ROOTS

401. The expression \( \sqrt{93} \) is a number between

[A] 8 and 9 \hspace{1cm} [B] 3 and 9
[C] 9 and 10 \hspace{1cm} [D] 46 and 47

402. Which point on the accompanying number line best represents the position of \( \sqrt{5} \)?

[A] B \hspace{1cm} [B] C \hspace{1cm} [C] D \hspace{1cm} [D] A
403. The expression $\sqrt{54} - b$ is equivalent to a positive integer when $b$ is equal to


404. The amount of time, $t$, in seconds, it takes an object to fall a distance, $d$, in meters, is expressed by the formula $t = \sqrt{\frac{d}{4.9}}$.

Approximately how long will it take an object to fall 75 meters?

[A] 0.26 sec       [B] 7.7 sec       [C] 2.34 sec       [D] 3.9 sec

CHAPTER 7-5

SOLVING QUADRATICS BY FACTORING

405. What is the solution set of the equation $3x^2 = 48$?

[A] {4,4}       [B] {4,-4}       [C] {-2,-8}       [D] {2,8}

406. Greg is in a car at the top of a roller-coaster ride. The distance, $d$, of the car from the ground as the car descends is determined by the equation $d = 144 - 16t^2$, where $t$ is the number of seconds it takes the car to travel down to each point on the ride. How many seconds will it take Greg to reach the ground? For an algebraic solution show your work here.

For a graphic solution show your work here.

CHAPTER 8-4

ZERO AND NEGATIVE POWERS

407. What is the value of $3^{-2}$?

[A] $\frac{1}{9}$       [B] -9       [C] 9       [D] $-\frac{1}{9}$

408. What is the value of $2^{-3}$?

[A] $\frac{1}{6}$       [B] -6       [C] -8       [D] $\frac{1}{8}$

409. What is the value of $3^0 + 3^{-2}$?

[A] 0       [B] $\frac{1}{9}$       [C] 6       [D] $\frac{1}{9}$

410. Which expression is equivalent to $x^{-1} \cdot y^2$?

[A] $xy^{-2}$       [B] $\frac{x}{y^2}$       [C] $\frac{y^2}{x}$       [D] $xy^2$
411. Which expression is equivalent to $x^{-4}$?

[A] $-4x$  [B] $\frac{1}{x^4}$  [C] $x^4$  [D] 0

412. If $f(x) = 4x^0 + (4x)^{-1}$, what is the value of $f(4)$?

[A] $-12$  [B] 0  [C] $4\frac{1}{16}$  [D] $1\frac{1}{16}$

413. Solve for $x$: $x^3 = \frac{27}{64}$

CHAPTER 8-5

SCIENTIFIC NOTATION

414. Expressed in decimal notation, $4.726 \times 10^{-3}$ is

[A] 4.726  [B] 0.004726  [C] 472.6  [D] 0.04726

415. The number $8.375 \times 10^{-3}$ is equivalent to

[A] 8.375  [B] 0.008375  [C] 0.0008375  [D] 0.08375

416. The number $1.56 \times 10^{-2}$ is equivalent to

[A] 0.00156  [B] 0.156  [C] 0.0156  [D] 156

417. The expression $0.62 \times 10^3$ is equivalent to

[A] $6.2 \times 10^2$  [B] 62,000  [C] 0.62  [D] $6.2 \times 10^4$

418. Which expression is equivalent to $6.02 \times 10^{21}$?

[A] $60.2 \times 10^{21}$  [B] $6020 \times 10^{21}$  [C] $602 \times 10^{21}$  [D] $0.602 \times 10^{21}$

419. If 0.0347 is written by a scientist in the form $3.47 \times 10^n$, the value of $n$ is


420. According to the 2000 census, the population of New York State was approximately 18,900,000. How is this number expressed in scientific notation?

[A] $1.89 \times 10^7$  [B] $1890 \times 10^4$  [C] $189 \times 10^6$  [D] $18.9 \times 10^6$

421. The distance from Earth to the Sun is approximately 93 million miles. A scientist would write that number as

[A] $93 \times 10^7$  [B] $93 \times 10^{10}$  [C] $9.3 \times 10^6$  [D] $9.3 \times 10^7$

422. A micron is a unit used to measure specimens viewed with a microscope. One micron is equivalent to 0.00003937 inch. How is this number expressed in scientific notation?

[A] $3.937 \times 10^{-8}$  [B] $3.937 \times 10^5$  [C] $39.37 \times 10^8$  [D] $3.937 \times 10^{-5}$

423. The approximate number of seconds in a year is 32,000,000. When this number is written in scientific notation, the numerical value of the exponent is


424. The mass of an orchid seed is approximately 0.0000035 gram. Written in scientific notation, that mass is equivalent to $3.5 \times 10^n$. What is the value of $n$?


425. The size of a certain type of molecule is 0.00009078 inch. If this number is expressed as $9.078 \times 10^n$, what is the value of $n$?

426. What is the sum of \(6 \times 10^3\) and \(3 \times 10^2\)?

[A] \(6.3 \times 10^3\)  
[B] \(9 \times 10^6\)  
[C] \(9 \times 10^5\)  
[D] \(18 \times 10^4\)

427. If \(3.85 \times 10^6\) is divided by \(385 \times 10^4\), the result is

[A] 0.01  
[B] 1  
[C] \(3.85 \times 10^4\)  
[D] \(3.85 \times 10^6\)

428. What is the value of \(\frac{6.3 \times 10^8}{3 \times 10^6}\) in scientific notation?

[A] \(2.1 \times 10^5\)  
[B] \(2.1 \times 10^{-4}\)  
[C] \(2.1 \times 10^4\)  
[D] \(2.1 \times 10^{-2}\)

429. If the number of molecules in 1 mole of a substance is \(6.02 \times 10^{23}\), then the number of molecules in 100 moles is

[A] \(6.02 \times 10^{22}\)  
[B] \(6.02 \times 10^{24}\)  
[C] \(6.02 \times 10^{21}\)  
[D] \(6.02 \times 10^{25}\)

430. If the mass of a proton is \(1.67 \times 10^{-24}\) gram, what is the mass of 1,000 protons?

[A] \(1.67 \times 10^{-27}\)  
[B] \(1.67 \times 10^{-21}\)  
[C] \(1.67 \times 10^{-23}\)  
[D] \(1.67 \times 10^{-22}\)

431. The distance from Earth to the imaginary planet Med is \(1.7 \times 10^7\) miles. If a spaceship is capable of traveling 1,420 miles per hour, how many days will it take the spaceship to reach the planet Med? Round your answer to the nearest day.

432. Two objects are \(2.4 \times 10^{20}\) centimeters apart. A message from one object travels to the other at a rate of \(1.2 \times 10^5\) centimeters per second. How many seconds does it take the message to travel from one object to the other?

[A] \(2.0 \times 10^4\)  
[B] \(2.0 \times 10^{15}\)  
[C] \(2.88 \times 10^{25}\)  
[D] \(1.2 \times 10^{15}\)

**CHAPTER 8-6**

**OPERATIONS WITH POWERS**

433. The expression \(8^{-4} \cdot 8^6\) is equivalent to

[A] \(8^{-2}\)  
[B] \(8^{-24}\)  
[C] \(8^{10}\)  
[D] \(8^2\)

434. The expression \(3^2 \cdot 3^3 \cdot 3^4\) is equivalent to

[A] \(3^9\)  
[B] \(27^{24}\)  
[C] \(3^{24}\)  
[D] \(27^9\)

435. The expression \(2^3 \cdot 4^2\) is equivalent to

[A] \(2^7\)  
[B] \(8^5\)  
[C] \(2^{12}\)  
[D] \(8^6\)

436. The expression \((x^2z^3)(xy^2z)\) is equivalent to

[A] \(x^3y^2z^4\)  
[B] \(x^2y^2z^3\)  
[C] \(x^4y^2z^5\)  
[D] \(x^3y^3z^4\)

437. The product of \(2x^3\) and \(6x^5\) is

[A] \(10x^{15}\)  
[B] \(12x^8\)  
[C] \(12x^{15}\)  
[D] \(10x^8\)

438. The product of \(3x^2y\) and \(-4xy^3\) is

[A] \(12x^3y^3\)  
[B] \(-12x^3y^4\)  
[C] \(12x^3y^4\)  
[D] \(-12x^2y^3\)

439. The product of \(3x^5\) and \(2x^4\) is

[A] \(6x^{20}\)  
[B] \(5x^{20}\)  
[C] \(6x^9\)  
[D] \(5x^9\)
440. The product of $4x^2y$ and $2xy^3$ is

[A] $8x^3y^3$  
[B] $8x^3y^4$  
[C] $8x^2y^4$  
[D] $8x^3y^3$

441. What is the product of $10x^4y^2$ and $3xy^3$?

[A] $30x^5y^6$  
[B] $30x^4y^6$  
[C] $30x^4y^5$  
[D] $30x^5y^5$

442. What is the product of $\frac{1}{3}x^2y$ and $\frac{1}{6}xy^3$?

[A] $\frac{1}{9}x^3y^4$  
[B] $\frac{1}{18}x^3y^4$  
[C] $\frac{1}{2}x^2y^3$  
[D] $\frac{1}{18}x^2y^3$

### CHAPTER 8-7

443. The expression $(6x^3y^6)^2$ is equivalent to

[A] $36x^5y^8$  
[B] $12x^6y^{12}$  
[C] $36x^6y^{12}$  
[D] $6x^6y^{12}$

444. Expressed in its simplest form, $(3x^3)(2y)^2(4x^4)$ is equivalent to

[A] $24x^{12}y^2$  
[B] $48x^7y^2$  
[C] $48x^{12}y^2$  
[D] $24x^7y^2$

445. The product of $(5ab)$ and $(-2a^2b)^3$ is

[A] $-40a^6b^4$  
[B] $-30a^7b^4$  
[C] $-30a^6b^4$  
[D] $-40a^7b^4$

### CHAPTER 8-8

446. When $-9x^5$ is divided by $-3x^3$, $x \neq 0$, the quotient is

[A] $27x^8$  
[B] $-3x^2$  
[C] $-27x^{15}$  
[D] $3x^2$

447. The quotient of $-\frac{15x^8}{5x^3}$, $x \neq 0$, is

[A] $-3x^4$  
[B] $-10x^4$  
[C] $-10x^6$  
[D] $-3x^6$

448. The expression $-\frac{32x^8}{4x^2}$, $x \neq 0$, is equivalent to

[A] $-8x^6$  
[B] $-8x^4$  
[C] $8x^4$  
[D] $8x^6$

449. If $x \neq 0$, then $\frac{(x^2)^3}{x^5} \cdot 1000$ is equivalent to

[A] $1000x$  
[B] $1000$  
[C] $0$  
[D] $1000 + x$

450. The expression $\frac{5x^6y^2}{x^8y}$ is equivalent to

[A] $\frac{5y}{x^2}$  
[B] $5x^2y$  
[C] $5x^{14}y^3$  
[D] $\frac{5y^3}{x^{14}}$

451. The expression $\frac{(b^{2n+1})^3}{b^n \cdot b^{4n+3}}$ is equivalent to

[A] $b^{-3n}$  
[B] $\frac{b^n}{2}$  
[C] $b^{-3n+1}$  
[D] $b^n$
CHAPTER 9-1

PYTHAGORAS

452. The set of integers {3,4,5} is a Pythagorean triple. Another such set is
   [A] {8,15,17}  [B] {6,7,8}  
   [C] {6,12,13}  [D] {6,8,12}  

453. If the length of the legs of a right triangle are 5 and 7, what is the length of the hypotenuse?
   [A] $\sqrt{74}$  [B] $2\sqrt{6}$  
   [C] $2\sqrt{3}$  [D] $\sqrt{2}$  

454. If the length of a rectangular television screen is 20 inches and its height is 15 inches, what is the length of its diagonal, in inches?

455. The NuFone Communications Company must run a telephone line between two poles at opposite ends of a lake, as shown in the accompanying diagram. The length and width of the lake are 75 feet and 30 feet, respectively. 

  What is the distance between the two poles, to the nearest foot?

456. A wall is supported by a brace 10 feet long, as shown in the diagram below. If one end of the brace is placed 6 feet from the base of the wall, how many feet up the wall does the brace reach?

457. The accompanying diagram shows a kite that has been secured to a stake in the ground with a 20-foot string. The kite is located 12 feet from the ground, directly over point $X$. What is the distance, in feet, between the stake and point $X$?

458. How many feet from the base of a house must a 39-foot ladder be placed so that the top of the ladder will reach a point on the house 36 feet from the ground?

459. A woman has a ladder that is 13 feet long. If she sets the base of the ladder on level ground 5 feet from the side of a house, how many feet above the ground will the top of the ladder be when it rests against the house?
460. In the accompanying diagram of right triangles $ABD$ and $DBC$, $AB = 5$, $AD = 4$, and $CD = 1$. Find the length of $BC$, to the nearest tenth.

461. In the accompanying diagram, triangle $A$ is similar to triangle $B$. Find the value of $n$.

462. A straw is placed into a rectangular box that is 3 inches by 4 inches by 8 inches, as shown in the accompanying diagram. If the straw fits exactly into the box diagonally from the bottom left front corner to the top right back corner, how long is the straw, to the nearest tenth of an inch?

463. The accompanying diagram shows a semicircular arch over a street that has a radius of 14 feet. A banner is attached to the arch at points $A$ and $B$, such that $AE = EB = 5$ feet. How many feet above the ground are these points of attachment for the banner?

464. A builder is building a rectangular deck with dimensions of 16 feet by 30 feet. To ensure that the sides form $90^\circ$ angles, what should each diagonal measure?


CHAPTER 9-2

DISTANCE

465. The coordinates of point $R$ are (-3,2) and the coordinates of point $T$ are (4,1). What is the length of $RT$?

[A] $5\sqrt{2}$ [B] $2\sqrt{2}$
[C] $4\sqrt{3}$ [D] $\sqrt{10}$

466. Katrina hikes 5 miles north, 7 miles east, and then 3 miles north again. To the nearest tenth of a mile, how far, in a straight line, is Katrina from her starting point?
467. To get from his high school to his home, Jamal travels 5.0 miles east and then 4.0 miles north. When Sheila goes to her home from the same high school, she travels 8.0 miles east and 2.0 miles south. What is the measure of the shortest distance, to the nearest tenth of a mile, between Jamal's home and Sheila's home? [The use of the accompanying grid is optional.]

468. Two hikers started at the same location. One traveled 2 miles east and then 1 mile north. The other traveled 1 mile west and then 3 miles south. At the end of their hikes, how many miles apart are the two hikers? [The use of the accompanying grid is optional.]

469. Jerry and Jean Jogger start at the same time from point A shown on the accompanying set of axes. Jerry jogs at a rate of 5 miles per hour traveling from point A to point R to point S and then to point C. Jean jogs directly from point A to point C on \( \overline{AC} \) at the rate of 3 miles per hour. Which jogger reaches point C first? Explain or show your reasoning.

470. Determine the distance between point \( A(-1,-3) \) and point \( B(5,5) \). Write an equation of the perpendicular bisector of \( \overline{AB} \). [The use of the accompanying grid is optional.]
471. The coordinates of $A$ are (-9, 2) and the coordinates of $G$ are (3, 14). What are the coordinates of the midpoint of $AG$?

[A] (-6,6)  [B] (-6,16)  
[C] (-3,8)  [D] (-21,-10)

472. $M$ is the midpoint of $AB$. If the coordinates of $A$ are (-1,5) and the coordinates of $M$ are (3,3), what are the coordinates of $B$?

[A] (1,4)  [B] (7,1)  
[C] (2,8)  [D] (-5,7)

473. The midpoint of $AB$ is (-1,5) and the coordinates of point $A$ are (-3,2). What are the coordinates of point $B$?

[A] (1,10)  [B] (0,7)  
[C] (1,8)  [D] (-5,8)

474. A line segment on the coordinate plane has endpoints (2,4) and (4,$y$). The midpoint of the segment is point (3,7). What is the value of $y$?


475. The coordinates of the midpoint of $AB$ are (2,4), and the coordinates of point $B$ are (3,7). What are the coordinates of point $A$? [The use of the accompanying grid is optional.]

476. The midpoint $M$ of line segment $AB$ has coordinates (-3,4). If point $A$ is the origin, (0,0), what are the coordinates of point $B$? [The use of the accompanying grid is optional.]
CHAPTER 9-3

BASIC TRIGONOMETRIC RATIOS

477. Which ratio represents \( \cos A \) in the accompanying diagram of \( \triangle ABC \)?

\[ \frac{12}{13}, \frac{5}{13}, \frac{13}{5}, \frac{12}{5} \]

478. In the accompanying diagram of right triangle \( ABC \), \( AB = 8 \), \( BC = 15 \), \( AC = 17 \), and \( m\angle ABC = 90 \).

What is \( \tan \angle C \)?

\[ \frac{8}{15}, \frac{8}{17}, \frac{17}{15}, \frac{15}{17} \]

479. The angle of elevation from a point 25 feet from the base of a tree on level ground to the top of the tree is 30°. Which equation can be used to find the height of the tree?

\[ 30^2 + 25^2 = x^2 \quad \text{[B]} \quad \tan 30^\circ = \frac{x}{25} \]

\[ \cos 30^\circ = \frac{x}{25} \quad \text{[D]} \quad \sin 30^\circ = \frac{x}{25} \]

480. A surveyor needs to determine the distance across the pond shown in the accompanying diagram. She determines that the distance from her position to point \( P \) on the south shore of the pond is 175 meters and the angle from her position to point \( X \) on the north shore is 32°. Determine the distance, \( PX \), across the pond, rounded to the nearest meter.

481. Joe is holding his kite string 3 feet above the ground, as shown in the accompanying diagram. The distance between his hand and a point directly under the kite is 95 feet. If the angle of elevation to the kite is 50°, find the height, \( h \), of his kite, to the nearest foot.

(Not drawn to scale)
482. Find, to the nearest tenth of a foot, the height of the tree represented in the accompanying diagram.

483. From a point on level ground 25 feet from the base of a tower, the angle of elevation to the top of the tower is 78°, as shown in the accompanying diagram. Find the height of the tower, to the nearest tenth of a foot.

484. In the accompanying diagram, a ladder leaning against a building makes an angle of 58° with level ground. If the distance from the foot of the ladder to the building is 6 feet, find, to the nearest foot, how far up the building the ladder will reach.

485. A tree casts a shadow that is 20 feet long. The angle of elevation from the end of the shadow to the top of the tree is 66°. Determine the height of the tree, to the nearest foot.

486. Draw and label a diagram of the path of an airplane climbing at an angle of 11° with the ground. Find, to the nearest foot, the ground distance the airplane has traveled when it has attained an altitude of 400 feet.
487. As seen in the accompanying diagram, a person can travel from New York City to Buffalo by going north 170 miles to Albany and then west 280 miles to Buffalo.

![Diagram](image)

a If an engineer wants to design a highway to connect New York City directly to Buffalo, at what angle, \( x \), would she need to build the highway? Find the angle to the nearest degree.

b To the nearest mile, how many miles would be saved by traveling directly from New York City to Buffalo rather than by traveling first to Albany and then to Buffalo?

488. A 10-foot ladder is to be placed against the side of a building. The base of the ladder must be placed at an angle of 72° with the level ground for a secure footing. Find, to the nearest inch, how far the base of the ladder should be from the side of the building and how far up the side of the building the ladder will reach.

![Diagram](image)

489. In the accompanying diagram, \( x \) represents the length of a ladder that is leaning against a wall of a building, and \( y \) represents the distance from the foot of the ladder to the base of the wall. The ladder makes a 60° angle with the ground and reaches a point on the wall 17 feet above the ground. Find the number of feet in \( x \) and \( y \).

![Diagram](image)

490. As shown in the accompanying diagram, a ladder is leaning against a vertical wall, making an angle of 70° with the ground and reaching a height of 10.39 feet on the wall. Find, to the nearest foot, the length of the ladder. Find, to the nearest foot, the distance from the base of the ladder to the wall.

![Diagram](image)
491. A person standing on level ground is 2,000 feet away from the foot of a 420-foot-tall building, as shown in the accompanying diagram. To the nearest degree, what is the value of $x$?

![Diagram of a person standing near a building]

492. Ron and Francine are building a ramp for performing skateboard stunts, as shown in the accompanying diagram. The ramp is 7 feet long and 3 feet high. What is the measure of the angle, $x$, that the ramp makes with the ground, to the nearest tenth of a degree?

![Diagram of a ramp with dimensions]

493. In the accompanying diagram, the base of a 15-foot ladder rests on the ground 4 feet from a 6-foot fence.

![Diagram of a ladder against a building]

(a) If the ladder touches the top of the fence and the side of a building, what angle, to the nearest degree, does the ladder make with the ground?

(b) Using the angle found in part (a), determine how far the top of the ladder reaches up the side of the building, to the nearest foot.

494. The accompanying diagram shows a flagpole that stands on level ground. Two cables, $r$ and $s$, are attached to the pole at a point 16 feet above the ground. The combined length of the two cables is 50 feet. If cable $r$ is attached to the ground 12 feet from the base of the pole, what is the measure of the angle, $x$, to the nearest degree, that cable $s$ makes with the ground?

![Diagram of a flagpole with cables]

495. A ship on the ocean surface detects a sunken ship on the ocean floor at an angle of depression of 50°. The distance between the ship on the surface and the sunken ship on the ocean floor is 200 meters. If the ocean floor is level in this area, how far above the ocean floor, to the nearest meter, is the ship on the surface?

496. A person measures the angle of depression from the top of a wall to a point on the ground. The point is located on level ground 62 feet from the base of the wall and the angle of depression is 52°. How high is the wall, to the nearest tenth of a foot?

497. At Mogul's Ski Resort, the beginner's slope is inclined at an angle of 12.3°, while the advanced slope is inclined at an angle of 26.4°. If Rudy skis 1,000 meters down the advanced slope while Valerie skis the same distance on the beginner's slope, how much longer was the horizontal distance that Valerie covered?

[A] 81.3 m  
[B] 977.0 m  
[C] 895.7 m  
[D] 231.6 m
CHAPTER 9-4

SIMPLIFYING RADICALS

498. The expression $\sqrt{50}$ can be simplified to
   [A] $25\sqrt{2}$          [B] $5\sqrt{10}$
   [C] $5\sqrt{2}$          [D] $2\sqrt{25}$

499. When $\sqrt{72}$ is expressed in simplest $a\sqrt{b}$ form, what is the value of $a$?
   [A] 6          [B] 3          [C] 8          [D] 2

500. Simplify: $\sqrt{50r^2s^4}$

501. If $a > 0$, then $\sqrt{9a^2+16a^2}$ equals
   [A] $\sqrt{7a}$          [B] $5\sqrt{a}$          [C] $5a$          [D] $7a$

CHAPTER 9-5

OPERATIONS WITH RADICALS

502. The sum of $\sqrt{18}$ and $\sqrt{72}$ is
   [A] $3\sqrt{10}$          [B] $6\sqrt{3}$
   [C] $\sqrt{90}$          [D] $9\sqrt{2}$

503. The sum of $\sqrt{75}$ and $\sqrt{3}$ is
   [A] 18          [B] 15          [C] $6\sqrt{3}$          [D] $\sqrt{78}$

504. The expression $\sqrt{27} + \sqrt{12}$ is equivalent to
   [A] $\sqrt{39}$          [B] $5\sqrt{6}$
   [C] $5\sqrt{3}$          [D] $6\sqrt{3}$

505. The expression $\sqrt{50} + \sqrt{32}$ is equivalent to
   [A] 6          [B] $9\sqrt{2}$          [C] $\sqrt{82}$          [D] 18

506. The expression $\sqrt{28} + \sqrt{63}$ is equivalent to
   [A] $5\sqrt{7}$          [B] $13\sqrt{7}$
   [C] $6\sqrt{7}$          [D] $\sqrt{91}$

507. What is the sum of $\sqrt{50}$ and $\sqrt{32}$?
   [A] $20\sqrt{20}$          [B] $\sqrt{2}$
   [C] $9\sqrt{2}$          [D] $\sqrt{82}$

508. What is the sum of $5\sqrt{7}$ and $3\sqrt{28}$?
   [A] $8\sqrt{35}$          [B] $60\sqrt{7}$
   [C] $11\sqrt{7}$          [D] $9\sqrt{7}$

509. The expression $2\sqrt{50} - \sqrt{2}$ is equivalent to
   [A] 10          [B] $49\sqrt{2}$
   [C] $9\sqrt{2}$          [D] $2\sqrt{48}$

510. Expressed in simplest radical form, the product of $\sqrt{6} \cdot \sqrt{15}$ is
   [A] $3\sqrt{10}$          [B] $3\sqrt{15}$
   [C] $9\sqrt{10}$          [D] $\sqrt{90}$

511. If $x > 0$, the expression $(\sqrt{x})(\sqrt{2x})$ is equivalent to
   [A] $\sqrt{2x}$          [B] $2x$
   [C] $x\sqrt{2}$          [D] $x^2\sqrt{2}$

512. The expression $\frac{6\sqrt{20}}{3\sqrt{5}}$ is equivalent to
   [A] 4          [B] 8          [C] $3\sqrt{15}$          [D] $2\sqrt{15}$

513. The expression $\sqrt{90} \cdot \sqrt{40} - \sqrt{8} \cdot \sqrt{18}$ simplifies to
CHAPTER 9-6

SOLVING RADICALS

514. If \( \sqrt{2x - 1} + 2 = 5 \), then \( x \) is equal to

[A] 4      [B] 2      [C] 5      [D] 1

515. What is the solution of the equation \( \sqrt{2x - 3} - 3 = 6 \)?


516. The solution set of the equation \( \sqrt{x + 6} = x \) is

[A] {-2, 3}   [B] {3}   [C] {}   [D] {-2}

517. What is the solution set of the equation \( \sqrt{9x + 10} = x \)

[A] {9}      [B] {-1}   [C] {10}   [D] {10, -1}

518. What is the solution set of the equation \( x = 2\sqrt{2x - 3} \)?

[A] {2}      [B] {}      [C] {2, 6}   [D] {6}

519. Solve for all values of \( q \) that satisfy the equation \( \sqrt{3q} + 7 = q + 3 \).

520. Solve algebraically: \( \sqrt{x + 5} + 1 = x \)

521. Solve algebraically for \( x \): \( \sqrt{3x + 1} + 1 = x \)

522. A wrecking ball suspended from a chain is a type of pendulum. The relationship between the rate of speed of the ball, \( R \), the mass of the ball, \( m \), the length of the chain, \( L \), and the force, \( F \), is \( R = 2\pi \sqrt{\frac{mL}{F}} \). Determine the force, \( F \), to the nearest hundredth, when \( L = 12 \), \( m = 50 \), and \( R = 0.6 \).

523. The lateral surface area of a right circular cone, \( s \), is represented by the equation \( s = \pi r \sqrt{r^2 + h^2} \), where \( r \) is the radius of the circular base and \( h \) is the height of the cone. If the lateral surface area of a large funnel is 236.64 square centimeters and its radius is 4.75 centimeters, find its height, to the nearest hundredth of a centimeter.

524. The equation \( V = 20\sqrt{C + 273} \) relates speed of sound, \( V \), in meters per second, to air temperature, \( C \), in degrees Celsius. What is the temperature, in degrees Celsius, when the speed of sound is 320 meters per second? [The use of the accompanying grid is optional.]
525. The number of people, $y$, involved in recycling in a community is modeled by the function $y = 90\sqrt{3x} + 400$, where $x$ is the number of months the recycling plant has been open. Construct a table of values, sketch the function on the grid, and find the number of people involved in recycling exactly 3 months after the plant opened. After how many months will 940 people be involved in recycling?

526. The path of a rocket is represented by the equation $y = \sqrt{25 - x^2}$. The path of a missile designed to intersect the path of the rocket is represented by the equation $x = \frac{3}{2} \sqrt{y}$. The value of $x$ at the point of intersection is 3. What is the corresponding value of $y$?


CHAPTER 9-7

PROPERTIES OF RADICALS

527. What is the domain of $h(x) = \sqrt{x^2 - 4x - 5}$?

[A] $\{x|-1 \leq x \leq 5\}$  [B] $\{x|-5 \leq x \leq 1\}$  
[C] $\{x|x \geq 1 or x \leq -5\}$  [D] $\{x|x \geq 5 or x \leq -1\}$

528. Which statement is true for all real number values of $x$?

[A] $\sqrt{x^2} = x$  [B] $|x - 1| > (x - 1)$
[C] $\sqrt{x^2} = |x|$  [D] $|x - 1| > 0$

529. The formula $S = 20\sqrt{t + 273}$ is used to determine the speed of sound, $S$, in meters per second, near Earth's surface, where $t$ is the surface temperature, in degrees Celsius. Which graph best represents this function?

[A]  
[B]  
[C]  
[D]  

530. What is the axis of symmetry of the graph of the equation $x = y^2$?

[A] line $y = -x$  [B] $y$-axis
[C] line $y = x$  [D] $x$-axis
MATH TOOLBOX P. 450

CHAPTER 10-1

OPERATIONS WITH POLYNOMIALS

534. The sum of $3x^2 + x + 8$ and $x^2 - 9$ can be expressed as
[A] $4x^2 + x - 17$    [B] $3x^4 + x - 1$
[C] $4x^4 + x - 1$    [D] $4x^2 + x - 1$

535. The sum of $3x^2 + 4x - 2$ and $x^2 - 5x + 3$ is
[A] $4x^2 + x - 1$    [B] $4x^2 + x + 1$
[C] $4x^2 - x + 1$    [D] $4x^2 - x - 1$

536. The expression $2x^2 - x^2$ is equivalent to
[A] $x^2$    [B] $-2x^4$    [C] 2    [D] $x^0$

537. The expression $(3x^2 + 2xy + 7) - (6x^2 - 4xy + 3)$ is equivalent to
[A] $3x^2 - 6xy - 4$    [B] $-3x^2 - 2xy + 4$
[C] $3x^2 - 2xy + 4$    [D] $-3x^2 + 6xy + 4$

538. The expression $(2x^2 + 6x + 5) - (6x^2 + 3x + 5)$ is equivalent to
[A] $-4x^2 + 3x$    [B] $-4x^2 - 3x + 10$
[C] $4x^2 - 3x$    [D] $4x^2 + 3x - 10$

539. The expression $(x^2 - 5x - 2) - (-6x^2 - 7x - 3)$ is equivalent to
[A] $7x^2 - 12x - 5$    [B] $7x^2 + 2x + 1$
[C] $7x^2 - 2x + 1$    [D] $7x^2 + 2x - 5$

540. When $3a^2 - 2a + 5$ is subtracted from $a^2 + a - 1$, the result is
[A] $-2a^2 + 3a - 6$    [B] $-2a^2 + 3a + 6$
[C] $2a^2 - 3a - 6$    [D] $2a^2 - 3a + 6$
541. If $2x^2 - 4x + 6$ is subtracted from $5x^2 + 8x - 2$, the difference is

[A] $3x^2 + 4x + 4$  [B] $3x^2 + 12x - 8$
[C] $-3x^2 + 4x + 4$  [D] $-3x^2 - 12x + 8$

542. When $3x^2 - 2x + 1$ is subtracted from $2x^2 + 7x + 5$, the result will be

[A] $-x^2 + 5x + 6$  [B] $-x^2 + 9x + 4$
[C] $x^2 - 9x - 4$  [D] $x^2 + 5x + 6$

543. When $-2x^2 + 4x + 2$ is subtracted from $x^2 + 6x - 4$, the result is

[A] $2x^2 - 2x - 6$  [B] $-x^2 + 10x - 2$
[C] $-3x^2 - 2x + 6$  [D] $3x^2 + 2x - 6$

544. If $2x^2 - x + 6$ is subtracted from $x^2 + 3x - 2$, the result is

[A] $-x^2 + 2x - 8$  [B] $-x^2 + 4x - 8$
[C] $x^2 - 4x + 8$  [D] $x^2 + 2x - 8$

545. When $3x^2 - 8x$ is subtracted from $2x^2 + 3x$, the difference is

[A] $x^2 - 5x$  [B] $-x^2 - 11x$
[C] $-x^2 + 11x$  [D] $-x^2 - 5x$

546. When $3a^2 - 7a + 6$ is subtracted from $4a^2 - 3a + 4$, the result is

[A] $7a^2 - 10a + 10$  [B] $a^2 + 4a - 2$
[C] $-a^2 - 4a + 2$  [D] $a^2 - 10a - 2$

547. Subtract $5x^2 - 7x - 6$ from $9x^2 + 3x - 4$.

CHAPTER 10-2

FACTORING POLYNOMIALS

548. If $3x$ is one factor of $3x^2 - 9x$, what is the other factor?

[A] $x - 3$  [B] $x^2 - 6x$
[C] $3x$  [D] $x + 3$

549. If one factor of $56x^4y^3 - 42x^2y^6$ is $14x^2y^3$, what is the other factor?

[A] $4x^2y - 3xy^3$  [B] $4x^2 - 3y^2$
[C] $4x^2 - 3y^3$  [D] $4x^2y - 3xy^2$

OPERATIONS WITH POLYNOMIALS

550. When $3x^2 - 6x$ is divided by $3x$, the result is

[A] $2x$  [B] $-2x$
[C] $x - 2$  [D] $x + 2$

551. The expression $(50x^3 - 60x^2 + 10x) ÷ 10x$ is equivalent to

[A] $5x^2 - 6x + 1$  [B] $5x^2 - 6x$
[C] $5x^3 - 6x^2 + x$  [D] $5x^2 - 60x^2 + 10x$

CHAPTER 10-3

552. What is the product of $(c + 8)$ and $(c - 5)$?

[C] $c^2 - 40$  [D] $c^2 + 3c - 40$

553. The expression $(x - 6)^2$ is equivalent to

[A] $x^2 - 36$  [B] $x^2 + 36$
[C] $x^2 - 12x + 36$  [D] $x^2 + 12x + 36$
554. The expression \((a^2 + b^2)^2\) is equivalent to

[A] \(a^4 + 4a^2b^2 + b^4\)  
[B] \(a^4 + b^4\)  
[C] \(a^4 + a^2b^2 + b^4\)  
[D] \(a^4 + 2a^2b^2 + b^4\)

**CHAPTER 10-4**

**FACTORING POLYNOMIALS**

555. Which expression is a factor of \(x^2 + 2x - 15\)

[A] \((x + 3)\)  
[B] \((x - 3)\)  
[C] \((x - 5)\)  
[D] \((x + 15)\)

556. Which expression is a factor of \(n^2 + 3n - 54\)?

[A] \(n + 9\)  
[B] \(n^2 + 9\)  
[C] \(n - 9\)  
[D] \(n + 6\)

557. What are the factors of \(x^2 - 10x - 24\)?

[A] \((x - 4)(x - 6)\)  
[B] \((x + 12)(x - 2)\)  
[C] \((x - 12)(x + 2)\)  
[D] \((x - 4)(x + 6)\)

558. Factored completely, the expression \(2y^2 + 12y - 54\) is equivalent to

[A] \((2y + 6)(y - 9)\)  
[B] \(2(y - 3)(y - 9)\)  
[C] \((y + 6)(2y - 9)\)  
[D] \(2(y + 9)(y - 3)\)

559. Factor completely: \(3x^2 + 15x - 42\)

**CHAPTER 10-5**

560. What is a common factor of \(x^2 - 9\) and \(x^2 - 5x + 6\)?

[A] \(x^2\)  
[B] \(x - 2\)  
[C] \(x - 3\)  
[D] \(x + 3\)

561. Expressed in factored form, the binomial \(4a^2 - 9b^2\) is equivalent to

[A] \((2a - 9b)(2a + b)\)  
[B] \((2a + 3b)(2a - 3b)\)  
[C] \((2a - 3b)(2a - 3b)\)  
[D] \((4a - 3b)(a + 3b)\)

562. One of the factors of \(4x^2 - 9\) is

[A] \((2x + 3)\)  
[B] \((4x - 3)\)  
[C] \((x - 3)\)  
[D] \((x + 3)\)

563. Factor completely: \(3x^2 - 27\)

[A] \(3(x - 3)^2\)  
[B] \((3x + 3)(x - 9)\)  
[C] \(3(x^2 - 27)\)  
[D] \(3(x + 3)(x - 3)\)

564. Written in simplest factored form, the binomial \(2x^2 - 50\) can be expressed as

[A] \((x - 5)(x + 5)\)  
[B] \(2(x - 5)(x - 5)\)  
[C] \(2(x - 5)(x + 5)\)  
[D] \(2(x - 50)\)

565. Factor completely: \(3ax^2 - 27a\)

566. Factor completely: \(5n^2 - 80\)

**CHAPTER 10-6**

**SOLVING QUADRATICS BY FACTORING**

567. The larger root of the equation \((x + 4)(x - 3) = 0\) is

[A] \(-3\)  
[B] \(4\)  
[C] \(3\)  
[D] \(-4\)

568. One of the roots of the equation \(x^2 + 3x - 18 = 0\) is 3. What is the other root?

[A] \(6\)  
[B] \(15\)  
[C] \(-21\)  
[D] \(-6\)

569. What is the solution set of the equation \(x^2 - 5x = 0\)?

[A] \(\{0\}\)  
[B] \(\{0, 5\}\)  
[C] \(\{0, -5\}\)  
[D] \(\{5\}\)
570. The solution set for the equation \(x^2 - 2x - 15 = 0\) is

- [A] \(\{5, -3\}\)
- [B] \(\{5, 3\}\)
- [C] \(\{-5, 3\}\)
- [D] \(\{-5, -3\}\)

571. The solution set of the equation \(x^2 - 4x - 12 = 0\) is

- [A] \(\{-4, 3\}\)
- [B] \(\{-6, 2\}\)
- [C] \(\{-3, 4\}\)
- [D] \(\{-2, 6\}\)

572. What is the solution set of \(m^2 - 3m - 10 = 0\)?

- [A] \(\{3, -10\}\)
- [B] \(\{5, -2\}\)
- [C] \(\{2, -5\}\)
- [D] \(\{3, 10\}\)

573. What is the solution set of the equation \(x^2 - 5x - 24 = 0\)?

- [A] \(\{3, -8\}\)
- [B] \(\{3, 8\}\)
- [C] \(\{-3, 8\}\)
- [D] \(\{-3, 8\}\)

574. What is the solution set for the equation \(x^2 - 5x + 6 = 0\)?

- [A] \(\{-6, 1\}\)
- [B] \(\{6, -1\}\)
- [C] \(\{2, 3\}\)
- [D] \(\{-2, -3\}\)

575. What is the solution set of the equation \(x^2 + 11x + 28 = 0\)?

- [A] \(\{-7, -4\}\)
- [B] \(\{-3, -4\}\)
- [C] \(\{-7, 4\}\)
- [D] \(\{3, 4\}\)

576. Solve for \(x\): \(x^2 + 3x - 40 = 0\)

577. Solve for \(x\): \(x^2 + 3x - 28 = 0\)

578. Solve for \(x\): \(x^2 + 2x - 24 = 0\)

579. The solution set for the equation \(x^2 - 5x = 6\) is

- [A] \(\{2, -3\}\)
- [B] \(\{-2, 3\}\)
- [C] \(\{1, -6\}\)
- [D] \(\{-1, 6\}\)

580. If \((x - 4)\) is a factor of \(x^2 - x - w = 0\), then the value of \(w\) is

- [A] \(-3\)
- [B] \(3\)
- [C] \(12\)
- [D] \(-12\)

581. One root of the equation \(2x^2 - x - 15 = 0\) is

- [A] \(\frac{5}{2}\)
- [B] \(-3\)
- [C] \(3\)
- [D] \(\frac{3}{2}\)

582. What is the solution set of the equation \(3x^2 - 34x - 24 = 0\)?

- [A] \(\{-12, \frac{2}{3}\}\)
- [B] \(\{-6, 2\}\)
- [C] \(\{-\frac{2}{3}, 12\}\)
- [D] \(\{-2, 6\}\)

583. When Albert flips open his mathematics textbook, he notices that the product of the page numbers of the two facing pages that he sees is 156. Which equation could be used to find the page numbers that Albert is looking at?

- [A] \(x(x + 1) = 156\)
- [B] \((x + 1) + (x + 2) = 156\)
- [C] \((x + 1)(x + 3) = 156\)
- [D] \(x + (x + 1) = 156\)

584. Three brothers have ages that are consecutive even integers. The product of the first and third boys' ages is 20 more than twice the second boy's age. Find the age of each of the three boys.

585. Tamara has two sisters. One of the sisters is 7 years older than Tamara. The other sister is 3 years younger than Tamara. The product of Tamara's sisters' ages is 24. How old is Tamara?

586. Find three consecutive odd integers such that the product of the first and the second exceeds the third by 8.
587. The graph of a quadratic equation is shown in the accompanying diagram. The scale on the axes is a unit scale. Write an equation of this graph in standard form.

![Graph of a quadratic equation]

588. A ball is thrown straight up at an initial velocity of 54 feet per second. The height of the ball \( t \) seconds after it is thrown is given by the formula \( h(t) = 54t - 12t^2 \). How many seconds after the ball is thrown will it return to the ground?


589. If the equation \( x^2 - kx - 36 = 0 \) has \( x = 12 \) as one root, what is the value of \( k? \)


590. For which equation is the sum of the roots equal to the product of the roots?

[A] \( x^2 - 4x + 4 = 0 \)  [B] \( x^2 + 3x - 6 = 0 \)
[C] \( x^2 + x + 1 = 0 \)  [D] \( x^2 - 8x - 4 = 0 \)

---

**CHAPTER 11-2**

**RATIONAL FUNCTIONS**

591. What is the domain of the function \( f(x) = \frac{2x^2}{x^2 - 9} \)?

[A] all real numbers except 0  [B] all real numbers  
[C] all real numbers except 3 and -3  [D] all real numbers except 3

592. What is the domain of the function \( f(x) = \frac{3x^2}{x^2 - 49} \)?

[A] \( \{x \mid x \in \text{real numbers, } x \neq 7\} \)  [B] \( \{x \mid x \in \text{real numbers, } x \neq 0\} \)  
[C] \( \{x \mid x \in \text{real numbers, } x \neq \pm 7\} \)  [D] \( \{x \mid x \in \text{real numbers}\} \)

593. If \( f(x) = \frac{1}{\sqrt{2x - 4}} \), the domain of \( f(x) \) is

[A] \( x < 2 \)  [B] \( x \geq 2 \)  
[C] \( x = 2 \)  [D] \( x > 2 \)

---

**CHAPTER 11-3**

**RATIONAL EXPRESSIONS**

594. For which value of \( x \) is the expression \( \frac{x - 7}{x + 2} \) undefined?


595. For which value of \( x \) is the expression \( \frac{3x - 6}{x - 4} \) undefined?

[A] -4  [B] 2  [C] 4  [D] 0
596. For which value of \( x \) is the expression \( \frac{3}{x-2} \) undefined?
\[ \text{[A]} -2 \quad \text{[B]} 3 \quad \text{[C]} 0 \quad \text{[D]} 2 \]

597. For which value of \( x \) will the fraction \( \frac{3}{2x+4} \) be undefined?
\[ \text{[A]} 2 \quad \text{[B]} -4 \quad \text{[C]} 0 \quad \text{[D]} -2 \]

598. Which expression is undefined when \( w = 3 \)?
\[ \text{[A]} \frac{w-3}{w+1} \quad \text{[B]} \frac{w^2+2w}{5w} \]
\[ \text{[C]} \frac{3w}{3w^2} \quad \text{[D]} \frac{w+1}{w^2-3w} \]

599. If \( x \neq 0 \), the expression \( \frac{x^2+2x}{x} \) is equivalent to
\[ \text{[A]} 2 \quad \text{[B]} 3x \quad \text{[C]} x + 2 \quad \text{[D]} 4 \]

600. Which polynomial is the quotient of \( \frac{6x^3 + 9x^2 + 3x}{3x} \)?
\[ \text{[A]} 2x^2 + 3x + 1 \quad \text{[B]} 6x^2 + 9x \]
\[ \text{[C]} 2x + 3 \quad \text{[D]} 2x^2 + 3x \]

601. Simplify: \( \frac{x^2 + 6x + 5}{x^2 - 25} \)

602. Simplify: \( \frac{9x^2 - 15xy}{9x^2 - 25y^2} \)

**MULTIPLICATION AND DIVISION OF RATIONALS**

603. Perform the indicated operation and express the result in simplest terms:
\( \frac{x}{x + 3} \div \frac{3x}{x^2 - 9} \)

**CHAPTER 11-4**

**ADDITION AND SUBTRACTION OF RATIONALS**

604. What is the least common denominator of \( \frac{1}{2}, \frac{2}{7x}, \text{and} \frac{5}{x} \)?
\[ \text{[A]} 2x \quad \text{[B]} 14x^2 \quad \text{[C]} 14x \quad \text{[D]} 9x \]

605. Which expression is equivalent to \( \frac{a}{x} + \frac{b}{2x} \)?
\[ \text{[A]} \frac{2a+b}{x} \quad \text{[B]} \frac{2a+b}{2x} \]
\[ \text{[C]} \frac{a+b}{2x} \quad \text{[D]} \frac{a+b}{3x} \]

606. The sum of \( \frac{3}{x} + \frac{2}{5}, x \neq 0 \), is
\[ \text{[A]} \frac{1}{x} \quad \text{[B]} \frac{5}{x+5} \]
\[ \text{[C]} \frac{2x+15}{5x} \quad \text{[D]} \frac{2x+15}{x+5} \]

607. What is the sum of \( \frac{2}{x} \) and \( \frac{x}{2} \)?
\[ \text{[A]} \frac{4+x^2}{2x} \quad \text{[B]} 1 \]
\[ \text{[C]} \frac{2+x}{2x} \quad \text{[D]} \frac{4+x}{2x} \]

608. What is the sum of \( \frac{3}{7n} \) and \( \frac{7}{3n} \)?
\[ \text{[A]} \frac{10}{21n} \quad \text{[B]} \frac{1}{n} \quad \text{[C]} \frac{58}{21n} \quad \text{[D]} \frac{42}{21n} \]
609. The expression \( \frac{y - \frac{1}{2}}{x} \) is equivalent to

[A] \( \frac{1 - y}{2x} \)  \hspace{1cm}  [B] \( \frac{y - 1}{x - 2} \)

[C] \( \frac{2y - x}{2x} \)  \hspace{1cm}  [D] \( \frac{x - 2y}{2x} \)

610. Expressed as a single fraction, what is \( \frac{1}{x + 1} + \frac{1}{x}, x \neq 0, -1 \)?

[A] \( \frac{3}{x^2} \)  \hspace{1cm}  [B] \( \frac{2x + 3}{x^2 + x} \)

[C] \( \frac{2}{2x + 1} \)  \hspace{1cm}  [D] \( \frac{2x + 1}{x^2 + x} \)

CHAPTER 11-5

SOLVING RATIONALS

611. What is the value of \( x \) in the equation \( \frac{x}{2x + 1} = \frac{4}{3} \)?

[A] \(-5\)  \hspace{1cm}  [B] \(\frac{-4}{5}\)  \hspace{1cm}  [C] \(\frac{-5}{4}\)  \hspace{1cm}  [D] \(\frac{-1}{5}\)

612. Solve algebraically for \( x \): \( \frac{1}{x} = \frac{x + 1}{6} \)

613. Solve for all values of \( x \) that satisfy the equation \( \frac{x}{x + 3} = \frac{5}{x + 7} \).

CHAPTER 11-6

MULTIPLICATION COUNTING PRINCIPLE

614. Max goes through the cafeteria line and counts seven different meals and three different desserts that he can choose. Which expression can be used to determine how many different ways Max can choose a meal and a dessert?

[A] \( ^7P_3 \)  \hspace{1cm}  [B] \( ^7C_3 \)

[C] \( 7! \cdot 3! \)  \hspace{1cm}  [D] \( 7 \cdot 3 \)

615. How many different outfits consisting of a hat, a pair of slacks, and a sweater can be made from two hats, three pairs of slacks, and four sweaters?

[A] 9  \hspace{1cm}  [B] 24  \hspace{1cm}  [C] 29  \hspace{1cm}  [D] 12

616. Juan has three blue shirts, two green shirts, seven red shirts, five pairs of denim pants, and two pairs of khaki pants. How many different outfits consisting of one shirt and one pair of pants are possible?

[A] 420  \hspace{1cm}  [B] 84  \hspace{1cm}  [C] 130  \hspace{1cm}  [D] 19

617. Paloma has 3 jackets, 6 scarves, and 4 hats. Determine the number of different outfits consisting of a jacket, a scarf, and a hat that Paloma can wear.

618. Robin has 8 blouses, 6 skirts, and 5 scarves. Which expression can be used to calculate the number of different outfits she can choose, if an outfit consists of a blouse, a skirt, and a scarf?

[A] \( 8! \cdot 6! \cdot 5! \)  \hspace{1cm}  [B] \( ^8C_3 \)

[C] \( 8 + 6 + 5 \)  \hspace{1cm}  [D] \( 8 \cdot 6 \cdot 5 \)
619. Leo purchased five shirts, three pairs of pants, and four pairs of shoes. Which expression represents how many different outfits consisting of one shirt, one pair of pants, and one pair of shoes Leo can make?

[A] \(5 + 3 + 4\)  
[B] \(\binom{12}{3}\)  
[C] \(12 \cdot P_3\)  
[D] \(5 \cdot 3 \cdot 4\)

620. The school cafeteria offers five sandwich choices, four desserts, and three beverages. How many different meals consisting of one sandwich, one dessert, and one beverage can be ordered?

[A] 3  
[B] 1  
[C] 12  
[D] 60

621. A deli has five types of meat, two types of cheese, and three types of bread. How many different sandwiches, consisting of one type of meat, one type of cheese, and one type of bread, does the deli serve?

[A] 10  
[B] 25  
[C] 30  
[D] 75

622. Cole’s Ice Cream Stand serves sixteen different flavors of ice cream, three types of syrup, and seven types of sprinkles. If an ice cream sundae consists of one flavor of ice cream, one type of syrup, and one type of sprinkles, how many different ice cream sundaes can Cole serve?

[A] 26  
[B] 3  
[C] 336  
[D] 10,836

623. Debbie goes to a diner famous for its express lunch menu. The menu has five appetizers, three soups, seven entrees, six vegetables, and four desserts. How many different meals consisting of either an appetizer or a soup, one entree, one vegetable, and one dessert can Debbie order?

624. In a school building, there are 10 doors that can be used to enter the building and 8 stairways to the second floor. How many different routes are there from outside the building to a class on the second floor?

[A] 18  
[B] 80  
[C] 10  
[D] 1

625. Jeremy’s bedroom has two doors leading into the hallway. His house has four doors leading to the outside. Using the doorways, in how many different ways can Jeremy leave his room and go outside?

[A] 4  
[B] 8  
[C] 6  
[D] 5

626. A certain car comes in three body styles with a choice of two engines, a choice of two transmissions, and a choice of six colors. What is the minimum number of cars a dealer must stock to have one car of every possible combination?

[A] 36  
[B] 42  
[C] 72  
[D] 13

627. When Kimberly bought her new car, she found that there were 72 different ways her car could be equipped. Her choices included four choices of engine and three choices of transmission. If her only other choice was color, how many choices of color did she have?

[A] 12  
[B] 65  
[C] 60  
[D] 6

PERMUTATIONS

628. The value of \(5!\) is

[A] \(\frac{1}{5}\)  
[B] 20  
[C] 120  
[D] 5

629. The value of \(\frac{7!}{3!}\) is

[A] 24  
[B] 4  
[C] 7  
[D] 840

630. What is the value of \(\frac{8!}{4!}\)?

[A] 2  
[B] 2!  
[C] 1,680  
[D] 4!
631. Which value is equivalent to \( _3P_3 \)?  

632. How many different 6-letter arrangements can be formed using the letters in the word “ABSENT,” if each letter is used only once?  

633. How many different 4-letter arrangements can be formed using the letters of the word "JUMP," if each letter is used only once?  

634. What is the total number of different four-letter arrangements that can be formed from the letters in the word "VERTICAL," if each letter is used only once in an arrangement?  

635. A locker combination system uses three digits from 0 to 9. How many different three-digit combinations with no digit repeated are possible?  
   [A] 30  [B] 720  [C] 504  [D] 1,000

636. How many different five-digit numbers can be formed from the digits 1, 2, 3, 4, and 5 if each digit is used only once?  

637. All seven-digit telephone numbers in a town begin with 245. How many telephone numbers may be assigned in the town if the last four digits do not begin or end in a zero?

638. Julia has four different flags that she wants to hang on the wall of her room. How many different ways can the flags be arranged in a row?  

639. Six members of a school's varsity tennis team will march in a parade. How many different ways can the players be lined up if Angela, the team captain, is always at the front of the line?

640. There were seven students running in a race. How many different arrangements of first, second, and third place are possible?

641. The telephone company has run out of seven-digit telephone numbers for an area code. To fix this problem, the telephone company will introduce a new area code. Find the number of new seven-digit telephone numbers that will be generated for the new area code if both of the following conditions must be met:  
   o The first digit cannot be a zero or a one.  
   o The first three digits cannot be the emergency number (911) or the number used for information (411).

642. In Jackson County, Wyoming, license plates are made with two letters (A through Z) followed by three digits (0 through 9). The plates are made according to the following restrictions:  
   o the first letter must be J or W, and the second letter can be any of the 26 letters in the alphabet  
   o no digit can be repeated  
   How many different license plates can be made with these restrictions?
643. A certain state is considering changing the arrangement of letters and numbers on its license plates. The two options the state is considering are:
Option 1: three letters followed by a four-digit number with repetition of both letters and digits allowed
Option 2: four letters followed by a three-digit number without repetition of either letters or digits
[Zero may be chosen as the first digit of the number in either option.]
Which option will enable the state to issue more license plates? How many more different license plates will that option yield?

CHAPTER 11-7

COMBINATIONS

644. The expression \( _9C_2 \) is equivalent to
[A] \( _9P_2 \)  
[B] \( _9P_7 \)  
[C] \( \frac{9!}{2!} \)  
[D] \( _9C_7 \)

645. How many different three-member teams can be selected from a group of seven students?
[A] 1  
[B] 210  
[C] 35  
[D] 5,040

646. If the Math Olympiad Club consists of eighteen students, how many different teams of four students can be formed for competitions?
[A] 66  
[B] 73,440  
[C] 72  
[D] 3,060

647. How many different three-member teams can be formed from six students?
[A] 20  
[B] 120  
[C] 720  
[D] 216

648. There are 12 people on a basketball team, and the coach needs to choose 5 to put into a game. How many different possible ways can the coach choose a team of 5 if each person has an equal chance of being selected?
[A] \( _{12}C_{12} \)  
[B] \( _{12}P_5 \)  
[C] \( _{12}C_5 \)  
[D] \( _{12}P_5 \)

649. How many different five-member teams can be made from a group of eight students, if each student has an equal chance of being chosen?
[A] 40  
[B] 56  
[C] 336  
[D] 6,720

650. In the next Olympics, the United States can enter four athletes in the diving competition. How many different teams of four divers can be selected from a group of nine divers?
[A] 6,561  
[B] 126  
[C] 3,024  
[D] 36

651. Alan, Becky, Jesus, and Mariah are four students in the chess club. If two of these students will be selected to represent the school at a national convention, how many combinations of two students are possible?

652. Five people have volunteered to work on an awards dinner at Madison High School. How many different committees of four can be formed from the five people?
[A] 20  
[B] 10  
[C] 1  
[D] 5

653. A committee of five members is to be randomly selected from a group of nine freshmen and seven sophomores. Which expression represents the number of different committees of three freshmen and two sophomores that can be chosen?
[A] \( _{9}C_3 \cdot _7C_2 \)  
[B] \( _{9}C_3 + _7C_2 \)  
[C] \( _{9}P_3 \cdot _7P_2 \)  
[D] \( _{16}C_3 \cdot _{16}C_2 \)

654. An algebra class of 21 students must send 5 students to meet with the principal. How many different groups of 5 students could be formed from this class?

655. In a game, each player receives 5 cards from a deck of 52 different cards. How many different groupings of cards are possible in this game?
[A] \( \frac{52!}{5!} \)  
[B] \( _{52}P_5 \)  
[C] 5!  
[D] \( _{52}C_5 \)
656. Megan decides to go out to eat. The menu at the restaurant has four appetizers, three soups, seven entrees, and five desserts. If Megan decides to order an appetizer or a soup, and one entree, and two different desserts, how many different choices can she make?

657. On a bookshelf, there are five different mystery books and six different biographies. How many different sets of four books can Emilio choose if two of the books must be mystery books and two of the books must be biographies?

658. If there are four teams in a league, how many games will have to be played so that each team plays every other team once?


659. Five friends met for lunch, and they all shook hands. Each person shook the other person's right hand only once. What was the total number of handshakes?

660. Three roses will be selected for a flower vase. The florist has 1 red rose, 1 white rose, 1 yellow rose, 1 orange rose and 1 pink rose from which to choose.

a) How many different three rose selections can be formed from the 5 roses?

b) What is the probability that 3 roses selected at random will contain 1 red rose, 1 white rose, and 1 pink rose?

c) What is the probability that 3 roses selected at random will not contain an orange rose?

661. Paul orders a pizza. Chef Carl randomly chooses two different toppings to put on the pizza from the following: pepperoni, onion, sausage, mushrooms, and anchovies. If Paul will not eat pizza with mushrooms, determine the probability that Paul will not eat the pizza Chef Carl has made.

662. Sal has a small bag of candy containing three green candies and two red candies. While waiting for the bus, he ate two candies out of the bag, one after another, without looking. What is the probability that both candies were the same color?

663. Alexi's wallet contains four $1 bills, three $5 bills, and one $10 bill. If Alexi randomly removes two bills without replacement, determine whether the probability that the bills will total $15 is greater than the probability that the bills will total $2.

664. A bookshelf contains six mysteries and three biographies. Two books are selected at random without replacement.

a) What is the probability that both books are mysteries?

b) What is the probability that one book is a mystery and the other is a biography?