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The University of the State of New York

REGENTS HIGH SCHOOL EXAMINATION

ADVANCED ALGEBRA

Wednesday, January 27, 1960 - 9:15 a.m. to 12:15 p.m., only

Name of pupil		****
	Part I	
Answer all questions in allowed. Write your answe	this part. Each correct answer will receive 2 credits. r on the line at the right.	No partial credit will be
1 Express $\frac{5}{2-i}$ in the	form of $a + bi$.	1
2 Write an equation of the	the line that passes through the point $(3, -2)$ and the whose equation is $2x - 3y = 4$.	2
3 For what value of k w the x-axis?	ill the graph of $y = x^2 - 8x + k$ be tangent to	
4 Write in simplest for $(2)^6$	m the fourth term only in the expansion of	3
$\left(x^2+\frac{2}{x}\right)^6.$		4
	then $3x^9 + 2x^6 - 3$ is divided by $x + 1$.	5
6 Solve for $x: 4^x = \frac{1}{8}$		6
7 Find the real root of the		7
	the graph of $y = \log_{b} x$.	8
9 Find to the nearest hund	dredth the value of $\sqrt[3]{0.257}$.	9
10 Express in simplest form	$\frac{1+\frac{2}{a-2}}{1-\frac{a-5}{a-2}}.$	
	$1 - \frac{a-5}{a-2}$	10,

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ABVANCED ALDERRA — continued	
11 Two of the roots of the equation $2x^2 - 3x^2 + px + q = 0$ are 3 and -2 . Find the third root.	11
12 If $f(x) = x^a + 4x$, express $f(a - 2)$ as a product of two binomials.	12
13 Find the value of $3x^{\circ} + \left(\frac{4}{x}\right)^{-1} + \sqrt[6]{x^{\circ}}$ if $x = 8$.	13
14 If $f(x)$ is identically equal to $(x - 8) Q(x) + 7$, find the numerical value of $f(8)$.	l 14
15 Solve for x: $a^{x} = \frac{1-x}{1+x}$	15
16 An algebra examination contains 8 questions. Each student is to answer the first question and any 4 others. How many different selections of 5 questions may be made?	
17 How many <i>odd</i> numbers of 3 digits each can be written with the digits 1, 2, 3, 4, 5 if no digits are to be repeated?	17
18 A bag contains 3 black balls and 4 white balls. If 2 balls are drawn from the bag, what is the probability that both will be black?	18
19 Using k as a constant of variation, write an equation that represents the relationship: x varies directly as y and inversely as the square of z .	19
20 The slope of the line that passes through the points (-2, 3) and $(5, y)$ is $-\frac{4}{7}$. Find the value of y.	20
21 Express the repeating decimal 0.636363 as a common fraction.	21

Directions (22-25): Write on the line at the right of each of the following the number preceding the expression that best completes the statement.

22.....

23.....

24.....

25.....

22 If the graphs of 4x² + y² = 16 and y = 2x² - 2 are drawn on the same set of axes, the number of points they will have in common is (1) 1 (2) 2 (3) 3 (4) 4

- 23 The equation of the axis of symmetry of the parabola $y = ax^2 4x + 1$ is x = 1. The value of a is (1) -2 (2) +2 (3) -4 (4) +4
- 24 The equation $\sqrt{x+6} x = 0$ has (1) no root (2) -2 as its only root (3) 3 as its only root (4) the two roots 3 and -2
- 25 One machine can complete a job in p minutes and a second machine can do the job in q minutes. If both machines work together, the time in minutes required to complete the job is

(1)
$$\frac{pq}{p+q}$$
 (2) $\frac{p+q}{2}$ (3) $\frac{p+q}{pq}$ (4) $p+q$

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ADVANCED ALGERRA - continued Part II Answer ten questions from this part. Each correct answer will receive 21/2 credits. No partial credit will be allowed. Questions marked * are based upon optional topics in the syllabus. Write your answer on the line at the right. 26 Write an equation whose roots are the roots of $x^3 - 2x^2 + x - 3 = 0$ each decreased by 2. 27 Write an equation whose roots are the roots of $x^3 + 2x - 2 = 0$ each multiplied by 3. 28 How many of the roots of the equation $2x^e - 3x^2 - 6 = 0$ are imaginary? 29..... 29 Find the rational root of $3x^3 + 7x^2 + 8x + 2 = 0$. 30 Between what two consecutive integers does the positive root of the 30..... equation $x^3 + 3x - 20 = 0$ lie? 31 A positive root of the equation $x^3 + 3x^2 + 8x - 4 = 0$ lies between 0.4 31..... and 0.5. Find this root to the nearest tenth. 32..... 32 Find all the roots of the equation $x^4 + 8x^2 - 9 = 0$. 33 If $y = x^2 - 3x$, express x in terms of y. 34 [Write the number preceding the correct answer in the space provided.] Which one of the following is a rational integral function in x? (1) $2x^2 - \sqrt{x} - 1$ (2) $\frac{2}{3}x^2 - x\sqrt{3} - 5$ (3) $x^2 - \frac{3}{r} - 5$ (4) $x^{\frac{3}{3}} - x - 5$ 34..... 35.... 35 If ${}_{n}C_{12} = {}_{n}C_{2}$ find *n*. 36 Write an equation with integral coefficients and of lowest possible 36.... degree, two of whose roots are 3 and i. 37 [Write the number preceding the correct answer in the space provided.] The graph of the equation $y = x^3 + 5x + 1$ (1) does not intersect the *x*-axis (2) intersects the x-axis in one and only one point (3) intersects the x-axis in exactly three points (4) intersects the *x*-axis in more than three points *38 An arrow is shot vertically upward. Its height h in feet after t seconds is given by the formula $h = 128t - 16t^2$. After how many seconds will it reach its maximum height? 38..... *39 Find the abscissa of the point of inflection of the graph of $y = x^3 - 3x^2 - 9x + 2$. 39....

*40 Find the slope of the line tangent to the graph of $y = x^2 - 3x - 1$ at the point (4, 3).

40....

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Part III

Answer ten questions from this part. Each correct answer will receive 2½ credits. No partial credit will be allowed. Questions marked * are based upon optional topics in the syllabus. Write your answer on the line at the right.

- 41 The first three terms of an arithmetic progression are x, (2x + 1) and (5x - 4). Find the value of x.
- 42 Find log, 15.4 to the nearest tenth.
- 43 Find to the nearest tenth the value of (26.3)1.4
- 44 If $y = 3^x$ and $x = \log_a y$, find the value of a.
- 45 If $a^r = b^{r+1}$, express x in terms of the logarithms of a and b.
- 46 The graphs of y = mx 1 and $(x 2)^2 + (y + 3)^2 = 25$ are drawn on the same set of axes. If the graph of the straight line passes through the center of the circle, find the value of m.
- 47 Write the number preceding the correct answer in the space provided. If P (x, y) is a point of the graph of $y = -x^2 + 4x + 1$, the maximum (1) 1 (2) 2 (3) 5 (4) 4value of y is

48 [Write the number preceding the correct answer in the space provided.] The probability that Tom will hit a target is $\frac{3}{5}$. The probability that

Tom will not hit the target is

- (1) $\frac{5}{8}$ (2) $\frac{5}{3}$ (3) $\frac{2}{5}$ (4) $\frac{3}{8}$
- 49 A man went on a trip of m miles traveling by a train whose average speed was r miles per hour. He returned by a plane whose average speed was three times that of the train. If the return trip was also a distance of m miles and the total traveling time for the round trip was 8 hours, express m in terms of r.
- 50 A man engages in a shooting contest. Each time he hits the target, he receives 10 cents and each time he misses, he pays 5 cents. If after 20 shots the man has lost 10 cents, how many times did he hit the target?
- 51 An open box is to be made from a sheet of tin 12 inches square by cutting equal squares from the four corners and bending up the sides. If x represents the side of the square to be cut out, express the volume of the box in terms of x.
- 52 Given the formulas $S = \frac{1}{2}gt^2$ and V = gt where g is a constant. Express S as a function of V.
- •53 Find to the nearest degree the amplitude of 2 + 5i.
- *54 Express 4 (cos $150^{\circ} + i \sin 150^{\circ}$) in a + bi form.
- *55 Express one of the roots of $x^3 + 8 = 0$ in polar form.

I have studied advanced algebra for weeks and have had recitations per week

I do so declare

(Signature)

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Name of teacher

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FOR TEACHERS ONLYInstructions for rating
ADVANCED ALGEBRAWednesday, January 27, 1960 — 9:15 a.m. to 12:15 p.m., only

Use only red ink or pencil in rating Regents papers. Do not attempt to correct the pupil's work by making insertions or changes of any kind. Use check marks to indicate pupil errors.

Unless otherwise specified, mathematically correct variations in the answers will be allowed. In problems involving logarithms, answers should be left correct to four significant digits unless directions say otherwise. Units need not be given when the wording of the questions allows such omissions.

Part I

Allow 2 credits for each correct answer; allow no partial credit. For questions 22-25, allow credit if the pupil has written the correct answer instead of the number 1, 2, 3 or 4.

(1) $2+i$	$(11) \frac{1}{2}$
(2) $2x - 3y = 12$	(12) $(a-2)(a+2)$
(3) 16	(13) 11
(4) 160 <i>x</i> ⁸	(14) 7
(5) -4	(15) $\frac{1-a^2}{1+a^2}$
(6) $-\frac{3}{2}$	(16) 35
$(7) \frac{4}{9}$	(17) 36
(8) 1	$(18) \frac{1}{7}$
(9) .64	(19) $xz^2 = ky$
(10) $\frac{a}{3}$	(20) —1
	$(21) \frac{7}{11}$
	(22) 2
	(23) 2
	(24) 3
	(25) 1

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After 28 seconds for each of not more than ten correct anymers; after no partial credit. If more than ton questions have been anonward, only the first ten of these should be completent. If not after credit if anywers to questions 26, 27 and 36 are not expressed as equations. For questions 38 and 37, allow tredit if the papel has written the correct answer instead of the sumdar 3, 2, 3 or 4.

$(26) \ y^{2} + 4y^{2} + 3y - 1 = 0$	(34) 2
(27) y ¹ + 3Ry - 34 = 0	(35) 15
(28) four	$(M) \ x^* - 3x^* + x - 3 = 0$
(2) - j - a shift printer of a	(37) 2
(30) 2 and 3	(38) 4
(31) 0.4	(.39) 1
(32) +1,-1,+3,-3	(40) 5
$(33) \frac{3 \pm \sqrt{9 + 4y}}{3 \pm \sqrt{9 + 4y}}$	

Part III

Allow 2½ credits for each of not more than ten correct answers; allow no partial credit. If more than ten questions have been answered, only the first ten of these should be considered. For questions 47 and 48, allow credit if the pupil has written the correct answer instead of the number 1, 2, 3 or 4.

(41) 3	(49) 6r
(42) 1.7	(50) 6
(43) 97.3	(51) $(12-2x)(12-2x)x$
(44) 3	$(52) \frac{V^2}{2g}$
$(45) \ \frac{\log b}{\log a - \log b}$	2g (53) 68°
(46) -1	$(54) - 2\sqrt{3} + 2i$
(47) 3	(55) 2 ($\cos 60^\circ + i \sin 60^\circ$)
(48) 3	or 2 (cos $180^{\circ} + i \sin 180^{\circ}$) or 2 (cos $300^{\circ} + i \sin 300^{\circ}$)