TWELFTH YEAR MATHEMATICS 12A (Advanced Algebra)

Monday, January 27, 1964-1:15 to 4:15 p.m., only

Part I

Answer all questions in this part. Each correct answer will receive 2½ credits. No partial credit will be allowed. Write your answers on the line to the right.

$2+i\sqrt{3}$	
1. Express the number — as an equivalent frac-	
$5-i\sqrt{3}$	
tion with a real denominator.	1
2. The graph defined by $y = 2x^2 + bx + c$ passes through the points (1,5) and (2,6). Find the value of b.	2
3. Express in the form $a + bi$ the product $2(\cos 119^{\circ} + i \sin 119^{\circ})$ (cos $121^{\circ} + i \sin 121^{\circ}$).	3
4. Solve for $x: 16^{3x} = 8^{x+4}$	4
5. Write the coordinates of the minimum point of the parabola $y = x^2 - 6x + 13$.	5
6. The sides of a triangle are segments of the lines whose	
equations are $x = 0$, $y = 0$ and $y = -x + 2$. Find the area of the triangle.	6
7. The line $y = 4x - 4$ is tangent to $y = x^2$. Find the	
coordinates of the point of tangency,	7
8. A and B can do a job in c days. If A does half as much work per day as B, express in terms of c the number of days it would take A alone to do the job.	8
9. Solve for $x: 7 - 2x < 5(x - 7)$	9
10. If the expression $x^5 + 2x^2 - k$, in which k is a constant, is divided by $x + 2$, the remainder is zero. Find the	10
value of k .	10
11. If 3 is one root of the equation $x^3 - 3x^2 + 9x - 27 = 0$, find the other two roots.	11
12. If $\log_a 2 = b$ and $\log_a 3 = c$, express $\log_a 24$ in	
terms of b and c .	12
13. Write an equation of the line perpendicular to $2x - 3y = 1$ and passing through $(2,7)$.	13
14. Find the value of x for which $\log (x - 2) + \log (x + 2) = \log (x^2 - 2x + 3)$.	14
15. Find to the nearest tenth the value of log ₂ 310.	15
16. Write the eighth term only in the expansion of $\left(1 - \frac{1}{r}\right)^{10}$.	
$\left(1-\frac{1}{x}\right)$	16

17. A quantity z varies directly with the product of x and y^2 . If z=3 when x=100 and y=3, find the positive value of y when z = 50 and x = 6. 17..... 18. How many odd numbers x such that 100 < x < 1,000can be formed from the digits 1, 2, 5, 8, 9, if repetition of digits is not permitted? 18..... 19. Find the minimum value of $x^3 - 12x + 3$ for x > 0. 19..... Directions (20-24): Indicate the correct completion for each of the following by writing the number 1, 2, 3 or 4 in the space provided at the right. 20. The sum of -3 - 2i and +5 - 3i is a complex number which, when represented graphically, lies in quadrant (1) I (2) II (3) III (4) IV 20..... 21. The 12th term of an arithmetic progression is 2x and the 17th term is 7x. The first term is (1) x (2) -9x (3) -13x(4) -14x21..... 22. The velocity v in feet per second of a moving body is given by the equation $v = 5t^3 - 9t$ where t is the time in seconds. The acceleration, measured in feet per second per second is a (1) constant (2) linear function of t (3) quadratic function 23. A root of $x^3 = 1$ is $(1) \frac{-1 + i\sqrt{3}}{2}$ (2) $\frac{1 - i\sqrt{3}}{2}$ (3) $\frac{1 + \sqrt{3}}{2}$ (4) $\frac{-1 - \sqrt{3}}{2}$ of t (4) cubic function of t22..... 23..... 24. Factors of the expression $a^2 + b^2$ are (1) (a + b) (a + b) (2) (a + bi) (a - bi) (3) (a + bi) (a + bi) (4) (a + b) (a - b)

Part II

Answer sixteen questions from this part, 25-48. Each correct answer will receive 21/2 credits. No partial credit will be allowed. Questions marked * are based upon optional topics in the syllabus. Write your answers on the line at the right.

25. If $f(x) = x^2 + 1$ and $g(x) = \sqrt{x}$, find the value of $f(\frac{1}{2}) - g(2.25)$.

26. A circle whose center is at (-2,2) passes through the point (-6,-1). Write an equation of this circle.

27. Mary is one of 10 students of whom two are to be chosen at random for a committee. What is the probability that Mary will be chosen for the committee?

28. The graphs of $y = \log_{10} x$ and x + y = 1 are drawn on the same set of axes. What are the coordinates of the point(s) of intersection?

26.....

25.....

27.....

28.....

41.....

real values of x. Answer (1), (2) or (3).

TWELFTH YEAR MATHEMATICS-12A-JANUARY 27, 1964-4

Directions (42-48): For each of those chosen, write in the space provided the number preceding the expression that best completes the statement.

42. When graphed on the same set of axes, the total number of points of intersection of the graphs of $y = \frac{12}{x}$ and $x^2 + y^2$

= 1 is (1) 0 (2) 2 (3) 3 (4) 4 *** 42.......

43. The points (1,1) and (-4,-14) determine a straight line. Point P whose abscissa is 3 lies on this line. The ordinate of 5

point P is (1) - (2) 7 (3) 3 (4) 11 43.......

44. If in the equation $y = 3^x$ the variable x is decreased by 3, then y is (1)decreased by 3 (2)divided by 3 (3)decreased by 27 (4)divided by 27 44......

45. Which of the following is a negative irrational number in the interval $-3 < x < \frac{-2?}{25}$ (1) $\sqrt{-2.5}$ (2) $-\sqrt{5}$ (3) $-\sqrt{2.5}$ (4) $-\sqrt{\frac{25}{4}}$

4

46. Given the equation $ax^2 + bx + c = 0$ in which a, b and c are positive integers and b is the mean proportional between a and c, then the roots of the equation are (1) real, rational, equal (2) real, rational, unequal (3) real, irrational, unequal (4) imaginary

46.......

47. If the roots of $x^2 - 3x + 1 = 0$ are m and n, then 3(m+n) + mn is (1) 8 (2) -8 (3) 10 (4) -10

48. The numbers p, q, r and k are real. One root of $x^4 + px^3 + qx^2 + rx + k = 0$ is 2 - i. Two of the roots are equal integers. The coefficient p (1) must be an even integer (2) must be an odd integer (3) may be either an even or an odd integer (4) need not be an integer

Percent	farming a
Rater's	Initials:

The University of the State of New York

REGENTS HIGH SCHOOL EXAMINATION

TWELFTH YEAR MATHEMATICS 12A (Advanced Algebra)

Monday, January 27, 1964 - 1:15 to 4:15 p.m., only

ANSWER SHEET

Pupil	Teacher	***************************************
School		
All of your	r answers should be recorded on this a	nswer sheet.
	Part I Answer all questions in this part.	
1	9	17
2	10	18
3	11	19
4	12	20
5	13	21
6	14	22
7	15	23
8	16	24

Your answers for part II should be placed in the proper spaces on the back of this sheet.



[OVER]

Manney Commencer of the Party o	William with the wind the prostreet to	41 maintanning
······	TARTH YEAR MATHEMATI	42
······	35 THE REAL PROPERTY AND AND ADDRESS OF THE PARTY OF THE	43
	36	44
	37	45
	38	46
250 le 1800	39	47
***************************************	40	48
	Accesser all questions in this part.	
	Transferring Commence &	
and the second second	manufacture and the second	
I have regularly studied twelfth ye tations per week.	ar mathematics 12A (advanced algebra) for	weeks and have had

FOR TEACHERS ONLY

SCORING KEY TWELFTH YEAR MATHEMATICS 12A (Advanced Algebra)

Monday, January 27, 1964 - 1:15 to 4:15 p.m., only

Use only red ink or pencil in rating Regents papers. Do not attempt to correct the pupil's work by making insertions or changes of any kind. Use checkmarks to indicate pupil errors.

Unless otherwise specified, mathematically correct variations in the answers will be allowed. In problems involving logarithms, answers should be left correct to four significant digits unless directions say otherwise. Units need not be given when the wording of the questions allows such omissions.

Part I

Allow 21 credits for each correct answer; allow no partial credit. For questions 20-24, allow credit if the pupil has written the correct answer instead of the number 1, 2, 3 or 4.

$$(1)\frac{1+i\sqrt{3}}{4}$$

$$(2) -5$$

$$(11) \pm 3i$$

$$(19) - 13$$

$$(3) - 1 - i\sqrt{3}$$

$$(12) 3b + c$$

$$(4)\frac{4}{3}$$

$$(13) \ 3x + 2y = 20$$

$$(14)\frac{7}{2}$$

8)
$$3c$$
 (16) $\frac{-120}{x^7}$ or $-120 x^{-7}$

Part II

Allow 2½ credits for each of not more than 16 correct answers; allow no partial credit. If more than sixteen questions have been answered, only the first sixteen of these should be considered. For questions 41–48, allow credit if the pupil has written the correct answer instead of the number 1, 2, 3 or 4.

$$(25) - \frac{1}{4}$$

$$(33)\frac{215}{99}$$

$$(26) (x+2)^2 + (y-2)^2 = 25$$

(34)
$$Fd^2 = km_1m_2$$

$$(27) \frac{1}{5}$$

(43) 2

$$(29) 9 + 9i$$

$$(38) -1.2$$

$$(31) n - 2$$

$$(39) \ 5x + 2y - 2 = 0$$

$$(32) \sqrt{2}$$

$$(40) \ x^2 - 4x + y^2 = 0$$