

The University of the State of New York REGENTS HIGH SCHOOL EXAMINATION



**Tuesday,** June 12, 2018 — 1:15 to 4:15 p.m., only

Steve Watson Student Name

School Name \_\_\_\_\_ www.jmap.org

The possession or use of any communications device is strictly prohibited when taking this examination. If you have or use any communications device, no matter how briefly, your examination will be invalidated and no score will be calculated for you.

Print your name and the name of your school on the lines above.

A separate answer sheet for **Part I** has been provided to you. Follow the instructions from the proctor for completing the student information on your answer sheet.

This examination has four parts, with a total of 37 questions. You must answer all questions in this examination. Record your answers to the Part I multiple-choice questions on the separate answer sheet. Write your answers to the questions in **Parts II**, **III**, and **IV** directly in this booklet. All work should be written in pen, except for graphs and drawings, which should be done in pencil. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. Utilize the information provided for each question to determine your answer. Note that diagrams are not necessarily drawn to scale.

The formulas that you may need to answer some questions in this examination are found at the end of the examination. This sheet is perforated so you may remove it from this booklet.

Scrap paper is not permitted for any part of this examination, but you may use the blank spaces in this booklet as scrap paper. A perforated sheet of scrap graph paper is provided at the end of this booklet for any question for which graphing may be helpful but is not required. You may remove this sheet from this booklet. Any work done on this sheet of scrap graph paper will *not* be scored.

When you have completed the examination, you must sign the statement printed at the end of the answer sheet, indicating that you had no unlawful knowledge of the questions or answers prior to the examination and that you have neither given nor received assistance in answering any of the questions during the examination. Your answer sheet cannot be accepted if you fail to sign this declaration.

## Notice ...

A graphing calculator and a straightedge (ruler) must be available for you to use while taking this examination.

DO NOT OPEN THIS EXAMINATION BOOKLET UNTIL THE SIGNAL IS GIVEN.

**ALGEBRA I** 

## Part I

Answer all 24 questions in this part. Each correct answer will receive 2 credits. No partial credit will be allowed. Utilize the information provided for each question to determine your answer. Note that diagrams are not necessarily drawn to scale. For each statement or question, choose the word or expression that, of those given, best completes the statement or answers the question. Record your answers on your separate answer sheet. [48]

1 The solution to 
$$4p + 2 < 2(p + 5)$$
 is  
(1)  $p > -6$  (3)  $p > 4$  So  
(2)  $p < -6$  (4)  $p < 4$  So  
(2)  $p < -6$  (4)  $p < 4$  So  
(3)  $p > 4$  So  
(4)  $p < 4$  So  
(5)  $p < 1 < 4$  (4)  $p < 4$  So  
(6)  $p + 1 < 2 < 2(p + 5)$  Use this space for  
(7)  $p + 1 < 4$  (2)  $p + 5$  computations.  
(7)  $p + 1 < 4$  (2)  $p + 5$  computations.  
(8)  $p + 1 < 4$  (9)  $p < 2(9^{2} - 3)$  (9)  $p = 2(9^{2} - 2)$  (9)  $p =$ 

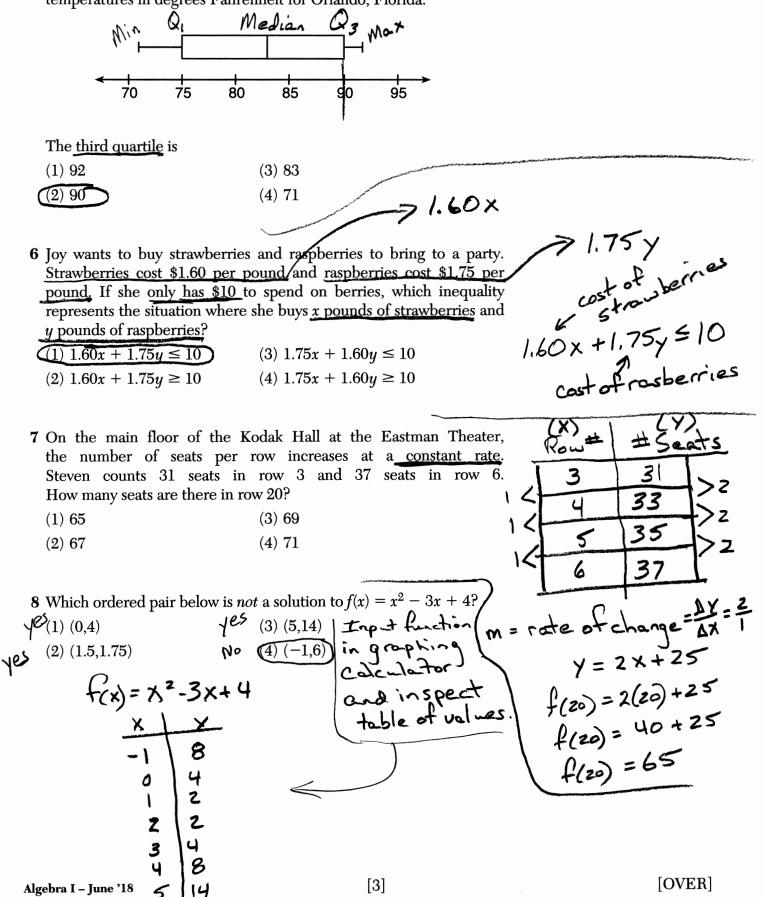
$$p(x) = x^{2} - 2x - 24$$
  

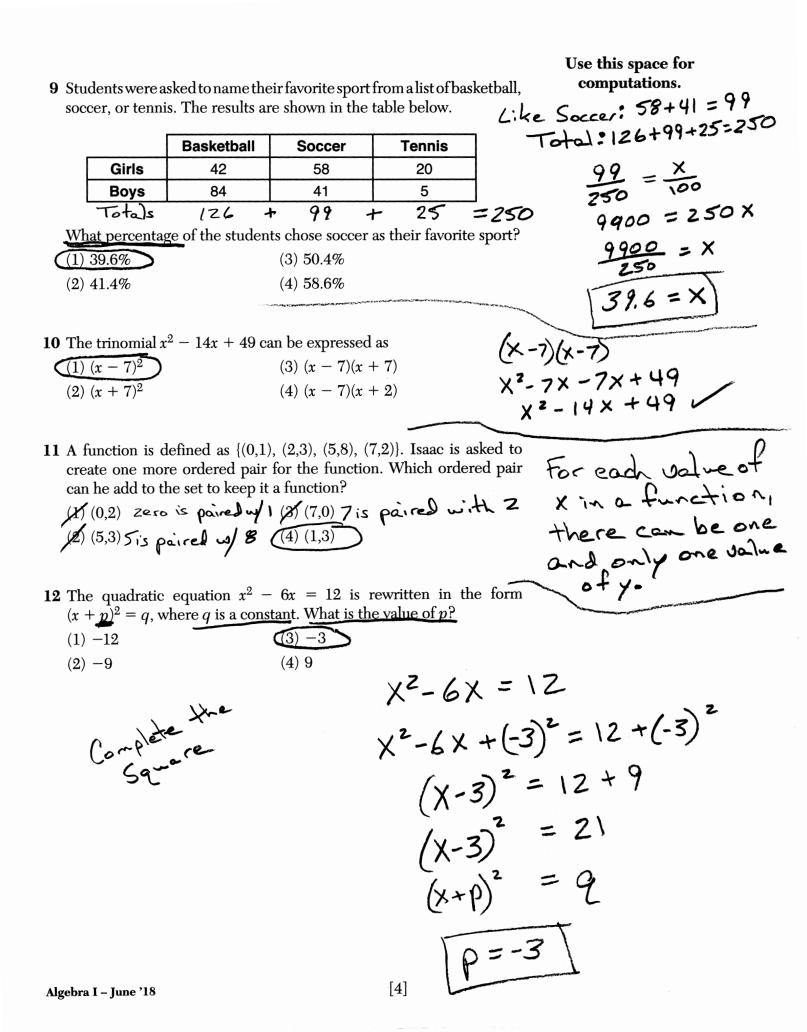
$$0 = x^{2} - 2x - 24$$
  

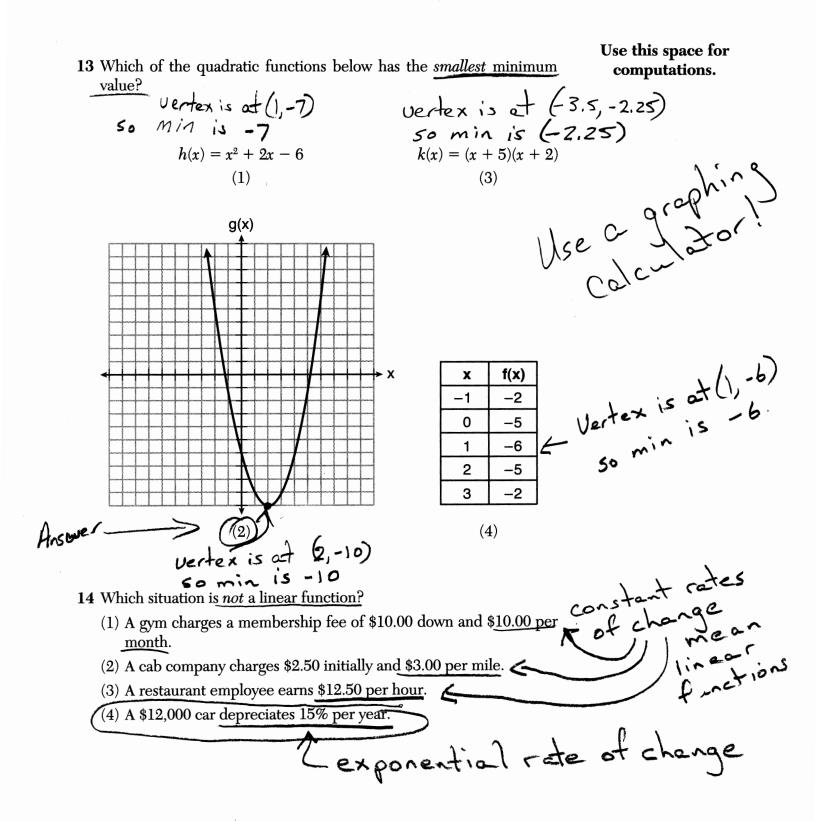
$$0 = (x - 6)(x + 4)$$
  
if  $x - 6 = 0$   
then  $x = 6$   
if  $x + 4 = 0$   
then  $x = -4$ 

[2]

- Use this space for computations.
- **5** The box plot below summarizes the data for the average monthly high temperatures in degrees Fahrenheit for Orlando, Florida.







[OVER]

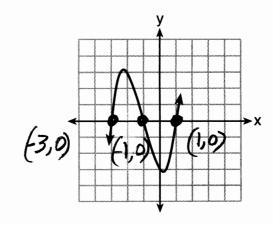
Use this space for 15 The Utica Boilermaker is a 15-kilometer road race. Sara is signed up computations. to run this race and has done the following training runs: Use the formula page! ΛL. 10 miles 1 km = 0.62 miles 🖌 II. 44,880 feet 15 km = 15(0.62) miles X III. 15,560 yards 15 km = 9.3 miles Which run(s) are at least 15 kilometers? 15km < 10 miles (1) I, only (3) I and III mile = 5280 ft 9.3 miles = 9.3 (5280ft) (2) II, only (4) II and III 9.3 miles = 49,104 ft. 16 If  $f(x) = x^2 + 2$ , which interval describes the range of this function? 44,800ft 2 49, 104 ft.  $\underbrace{(3) [2,\infty)}_{(4) (-\infty,2]} \operatorname{range}$  $X_{(1)}(-\infty,\infty)$  domain Imile = 1760 yards (2) [0,∞) 9. 3 miles = 9.3 (1760 yards) Put in graphing calculator and inspect the graphi 9.3 miles = 16,368 yards 17 The amount Mike gets paid weekly can be represented by the 15,560 yds ~ 16,368 yds expression 2.50a + 290, where a is the <u>number of cell phone</u> accessories he sells that week. What is the constant term in this expression and what does it represent? (1) 2.50a, the amount he is guaranteed to be paid each week (2) 2.50a, the amount he earns when he sells a accessories (3) 290, the amount he is guaranteed to be paid each week (4) 290, the amount he earns when he sells a accessories

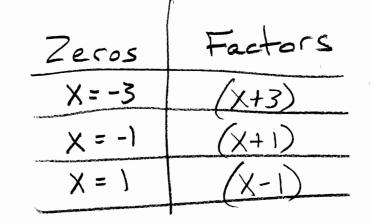
Mike gets \$2.50 for every cell phone accessory plus a constant amount of \$29000 each week.

[6]

# 18 A cubic function is graphed on the set of axes below.

Use this space for computations.

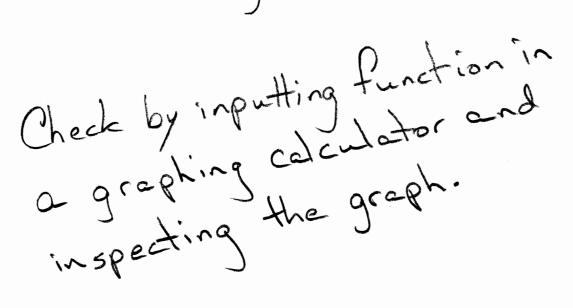




Which function could represent this graph?

(1) $f(x) = (x - 3)(x - 1)(x + 1)$
(2) $g(x) = (x + 3)(x + 1)(x - 1)$
(3) $h(x) = (x - 3)(x - 1)(x + 3)$
(4) $k(x) = (x + 3)(x + 1)(x - 3)$

O = (X+3)(X+1)(X-1) g(X) = (X+3)(X+1)(X-1)

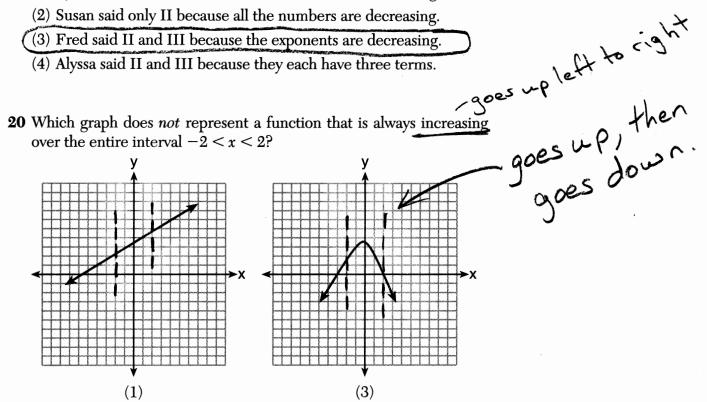


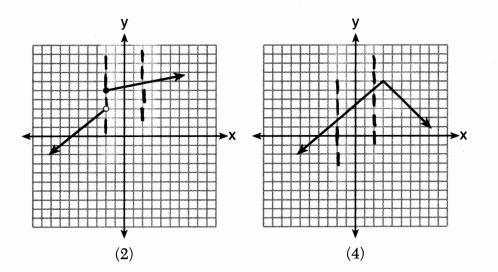
19 Mrs. Allard asked her students to identify which of the polynomials below are in standard form and explain why.

I. 
$$15x^4 - 6x + 3x^2 - 1$$
 No  
II.  $12x^3 + 8x + 4$  Yes  
III.  $2x^5 + 8x^2 + 10x$  Yes

Which student's response is correct?

- (1) Tyler said I and II because the coefficients are decreasing.
- (2) Susan said only II because all the numbers are decreasing.





Use this space for 21 At an ice cream shop, the profit, P(c), is modeled by the function computations. You can't sell a negative # of cones or pa-P(c) = 0.87c, where <u>c</u> represents the number of ice cream cones sold. An appropriate domain for this function is (1) an integer  $\leq 0$ X(3) a rational number  $\leq 0$  $\mathbf{X}(4)$  a rational number  $\geq 0$ (2) an integer  $\geq 0$ fraction of a cone. **22** How many real-number solutions does  $4x^2 + 2x + 5 = 0$  have? (3) zero (1) one b<sup>2</sup>-4ac (2) two (4) infinitely many a=4, b=2,c=5  $(-2)^{2} - 4(4)(5)$ **23** Students were asked to write a formula for the length of a rectangle by using the formula for its perimeter,  $p = 2\ell + 2w$ . Three of their 4 - 80  $\ell = \frac{1}{2}p - w$   $\rho = 2\ell + 2w$   $\rho - 2w = 2\ell$   $\rho - 2w = 2\ell$ responses are shown below. -76 solutions Check in graphing celerlator: The  $\checkmark III. \quad \ell = \frac{p-2w}{2}$ parabola does not cross the -w =D Which responses are correct? Ξp X-axis, 50 there are no zeros (3) I and III, only (1) I and II, only (4) I, II, and III (2) II and III, only (solutions) **24** If  $a_n = n(a_{n-1})$  and  $a_1 = 1$ , what is the value of  $a_5$ ? (3) 120 (1) 5(4) 720(2) 201 24

426

5x24

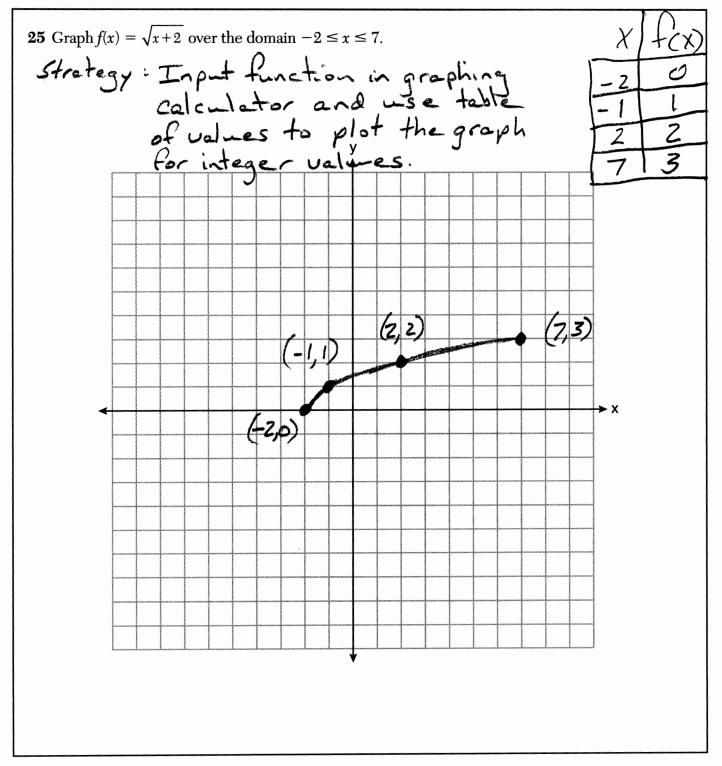
[OVER]

3×2

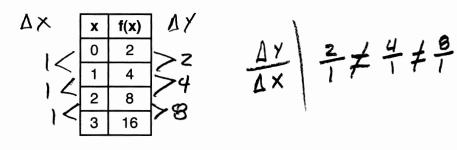
2×1

#### Part II

Answer all 8 questions in this part. Each correct answer will receive 2 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. Utilize the information provided for each question to determine your answer. Note that diagrams are not necessarily drawn to scale. For all questions in this part, a correct numerical answer with no work shown will receive only 1 credit. All answers should be written in pen, except for graphs and drawings, which should be done in pencil. [16]



26 Caleb claims that the ordered pairs shown in the table below are from a nonlinear function.



State if Caleb is correct. Explain your reasoning.

Celeb is correct. The function does not have a constant rate of change, so it is not a linear function.

27 Solve for x to the nearest tenth: 
$$x^{2} + x - 5 = 0$$
.  

$$A = 1 \quad b = 1 \quad C = -5^{-1}$$

$$X = \frac{-b \pm \sqrt{b^{2} - 4ac}}{2a}$$

$$X = \frac{-(1) \pm \sqrt{(1)^{2} - 4(1)(-5)}}{2(1)}$$

$$X = \frac{-1 \pm \sqrt{1 + 20}}{2}$$

$$X = \frac{-1 \pm \sqrt{1 + 20}}{2}$$

$$X = \frac{-1 \pm \sqrt{21}}{2}$$

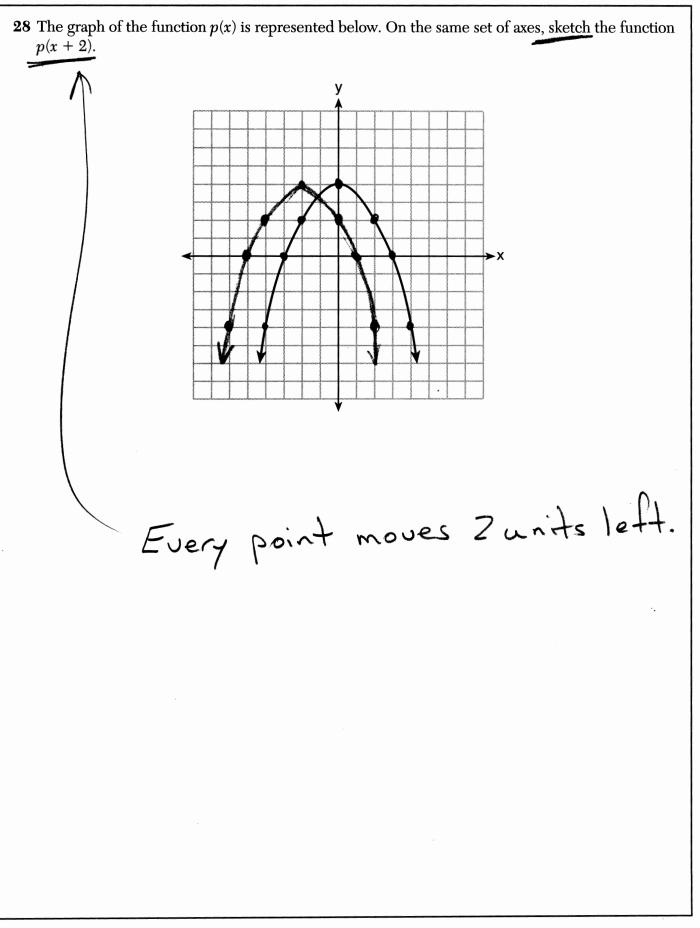
$$X = \frac{-1 \pm \sqrt{21}}{2}$$

$$X = \frac{-1 \pm \sqrt{258}}{2} = \frac{3.58}{2} = 1.79 = \overline{1.8}$$

$$X = \frac{-1 - 4.58}{2} = -\frac{5.58}{2} = -2.79 = \overline{-2.8}$$
Check using graphing calculator.  

$$X = 1.7912878 \quad Y = 0$$

$$X = -2.791288 \quad Y = 0$$



**29** When an apple is dropped from a tower <u>256 feet</u> high, the function  $h(t) = -16t^2 + 256$  models the height of the apple, in feet, after t seconds. Determine, algebraically, the number of seconds it takes the apple to hit the ground.  $h(t) = -16t^2 + 256$  $\dot{O} = -16t^2 + 256$ h(t) = 0 $16t^2 = 256$  $t^2 = 16$ t = 4 seconds ] answer Check  $h(4) = -16(4)^{2} + 256$  h(4) = -16(16) + 256 h(4) = -256 + 256h(4) = 0 V

**30** Solve the equation below algebraically for the exact value of x.

$$6 = \frac{2}{3}(x+5) = 4x + \frac{2}{3}(x+5)$$

$$6 = 4x + \frac{2}{3}x + \frac{19}{3}$$

$$M(5) \qquad 18 = 12x + 2x + 10$$

$$B = 14x$$

$$D(14) \qquad \frac{14}{14} = X$$

$$answer \qquad \boxed{\frac{14}{12}} = X$$

$$Check \qquad 6 - \frac{2}{3}(\frac{4}{7}+5) = 4(\frac{4}{7})$$

$$6 - \frac{2}{3}(5\frac{4}{7}) = \frac{16}{7}$$

$$6 - \frac{2}{3}(\frac{39}{7}) = \frac{16}{7}$$

$$6 - \frac{2}{3}(\frac{39}{7}) = \frac{16}{7}$$

$$6 - \frac{2}{3}(\frac{39}{7}) = \frac{16}{7}$$

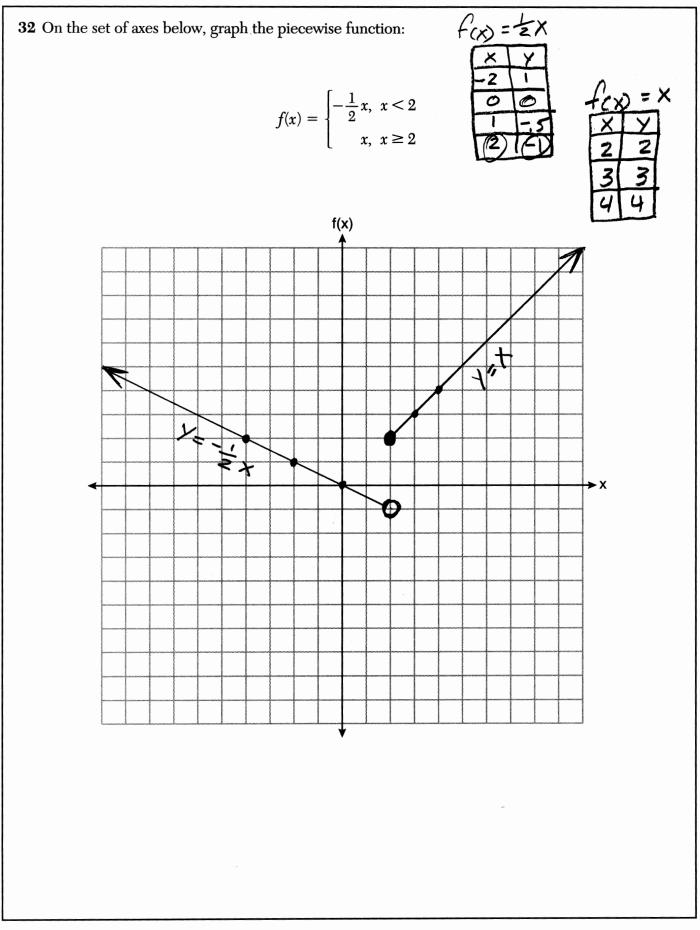
$$\frac{126}{21} - \frac{78}{21} = \frac{48}{21}$$

$$\frac{48}{21} = \frac{48}{21}$$

**31** Is the product of  $\sqrt{16}$  and  $\frac{4}{7}$  rational or irrational? Explain your reasoning.

A rational number is a number that  
can be expressed as the ratio of  
two integers, as in 
$$\frac{1}{6}$$
, where both  
a and b are integers.  
NI6 is rational because  $JI6 = 4 = \frac{4}{7}$ .  
 $\frac{4}{7}$  is rational because it is a ratio  
of two integers,  
 $(J16)(\frac{4}{7}) = (\frac{4}{7})(\frac{4}{7}) = \frac{16}{7} e^{integer}$   
Answer  
Explanation  
The product of two  
rational numbers is  
always rational.

[16]



## Part III

Answer all 4 questions in this part. Each correct answer will receive 4 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. Utilize the information provided for each question to determine your answer. Note that diagrams are not necessarily drawn to scale. For all questions in this part, a correct numerical answer with no work shown will receive only 1 credit. All answers should be written in pen, except for graphs and drawings, which should be done in pencil. [16]

**33** A population of rabbits in a lab, p(x), can be modeled by the function  $p(x) = 20(1.014)^x$ , where x represents the number of days since the population was first counted. Explain what 20 and 1.014 represent in the context of the problem. 20 represents the initial # of rabbits 1,014 represents the rate of growth Determine, to the nearest tenth, the average rate of change from day 50 to day 100. Step<sup>2</sup> Input p(x) = 20(1.014)\* in graphing calculator Step<sup>2</sup> Use table to find # of rabbits on day 50 and day 100 Day Hex) # Rabbits 50 40.08 100 80.32 Step<sup>3</sup> Calculate average rate of change.  $M = \frac{Y_2 - Y_1}{X_2 - X_1} = \frac{80.32 - 40.08}{100 - 50} = \frac{40.24}{50} \approx \boxed{-8}$ per do

Algebra I - June '18

**34** There are two parking garages in Beacon Falls. Garage A charges \$7.00 to park for the first 2 hours, and each additional hour costs \$3.00. Garage *B* charges \$3.25 per hour to park.

When a person parks for at least 2 hours, write equations to model the cost of parking for a total of x hours in Garage A and Garage B.

For 
$$X \ge 2$$
,  $A_{(X)} = 7 + 3(X-2)$   
For  $X \ge 2$ ,  $B_{(X)} = 6.50 + 3.25(X-2)$ 

Determine algebraically the number of hours when the cost of parking at both garages will be the same.

$$A_{(x)} = B_{(x)}$$

$$7 + 3(x-2) = 6.50 + 3.25(x-2)$$

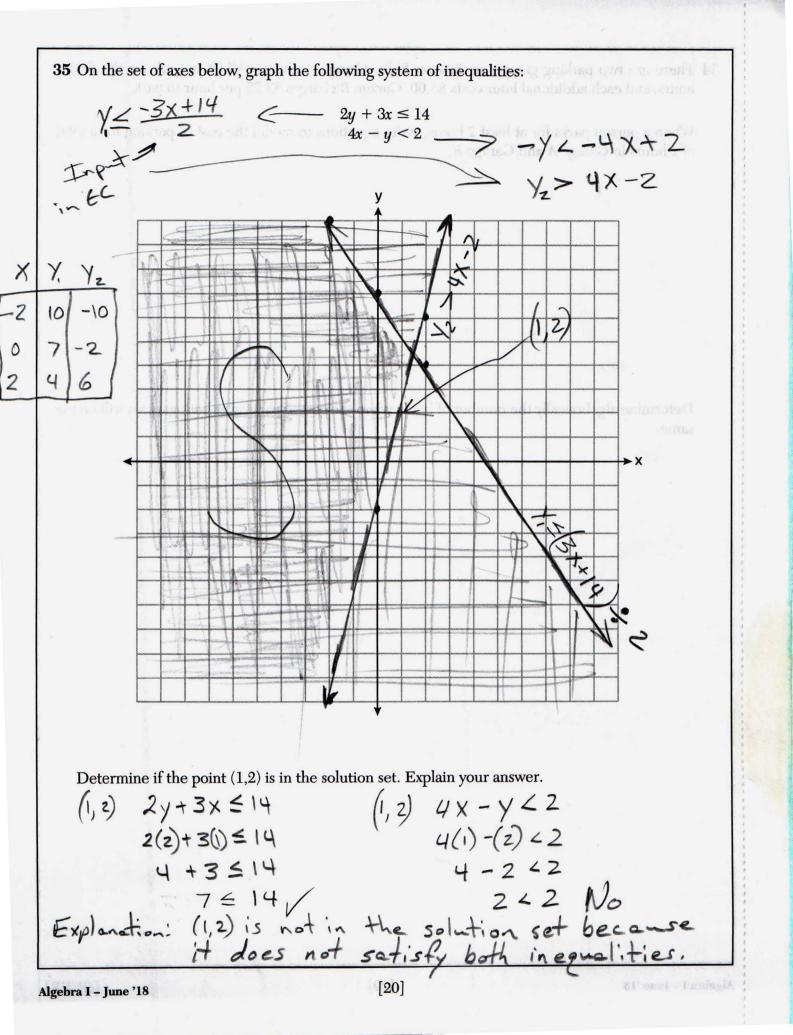
$$7 + 3x - 6 = 6.50 + 3.25x - 6.50$$

$$3x + 1 = 3.25x$$

$$1 = .25x$$

$$\frac{1}{.25} = x$$

$$\frac{1}{.4} = \frac{1}{.4} = \frac$$



**36** The percentage of students scoring 85 or better on a mathematics final exam and an English final exam during a recent school year for seven schools is shown in the table below.

a consister so amongalis) and the conservation of a state of the construction	Scoring 85 or Better		ili e lle information provide raver to scale. A correct mu
wings, which should be inju-	Mathematics, x	English, y	S ans ers should be weater- a peak.
	27	46	
and the state of the state of the state	12	28	W. Delerches a load that sorts
	Carros (13d) le sala	alator 45 aulia	ar an an an an an ar an
( hing	10	34	where of \$17.75 paids of the
Input in graphing calculator.	30	56	
Trent 1 tor.	45	67	<sup>10</sup> Dytes only collect dime equilation on an enrichle the
- alcula	20	42	and Decombine of the LG LA. (19) 13

Write the linear regression equation for these data, rounding all values to the nearest hundredth.

 $y = a \times + b$  a = .9577 b = 23.9486 y = .9205y = .9205

 $Y = .96 \times + 23.95$ 

State the correlation coefficient of the linear regression equation, to the *nearest hundredth*. Explain the meaning of this value in the context of these data.

#### Part IV

Answer the question in this part. A correct answer will receive 6 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. Utilize the information provided to determine your answer. Note that diagrams are not necessarily drawn to scale. A correct numerical answer with no work shown will receive only 1 credit. All answers should be written in pen, except for graphs and drawings, which should be done in pencil. [6]

37 Dylan has a bank that sorts coins as they are dropped into it. A panel on the front displays the total number of coins inside as well as the total value of these coins. The panel shows 90 coins with a d= # dimes value of \$17.55 inside of the bank. Convert to 1755 cents  $2 = \pm q$  marters If Dylan only collects dimes and quarters, write a system of equations in two variables or an equation in one variable that could be used to model this situation.  $E_{2.1} \quad 10d + 25q = 1755$   $E_{2.2} \quad d + q = 90$   $E_{2.2 + imes 10} \quad 10d + 10q = 900$ Using your equation or system of equations, algebraically determine the number of quarters Dylan has in his bank. 10d + 25q = 175510d + 10q = 900Subtract 159 = 8559 = 855 9 = 57

**Question 37 is continued on the next page.** 

## **Question 37 continued**

Dylan's mom told him that she would replace each one of his dimes with a quarter. If he uses all of his coins, determine if Dylan would then have enough money to buy a game priced at \$20.98 if he must also pay an 8% sales tax. Justify your answer.

If Dylan's mom replaces each dime with a guarter, then Dylen will have 90 quarters. 90 × 25 = 2250 cents or \$ 22,50 The game costs \$ 20.98 plus 8% sales tax. # 20,98 × 1.08 # 22,65 Dylan will not have enough.

He needs \$ 22.65, but only has \$ 22.50.