

**0616AII Common Core State Standards**

1 When  $b > 0$  and  $d$  is a positive integer, the expression  $(3b)^{\frac{2}{d}}$  is equivalent to

1)  $\frac{1}{(\sqrt[d]{3b})^2}$

2)  $(\sqrt{3b})^d$

3)  $\frac{1}{\sqrt{3b^d}}$

4)  $(\sqrt[d]{3b})^2$

2 Julie averaged 85 on the first three tests of the semester in her mathematics class. If she scores 93 on each of the remaining tests, her average will be 90. Which equation could be used to determine how many tests,  $T$ , are left in the semester?

1)  $\frac{255 + 93T}{3T} = 90$

2)  $\frac{255 + 90T}{3T} = 93$

3)  $\frac{255 + 93T}{T + 3} = 90$

4)  $\frac{255 + 90T}{T + 3} = 93$

3 Given  $i$  is the imaginary unit,  $(2 - yi)^2$  in simplest form is

1)  $y^2 - 4yi + 4$

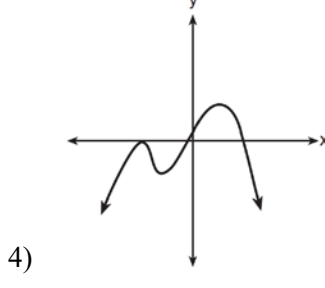
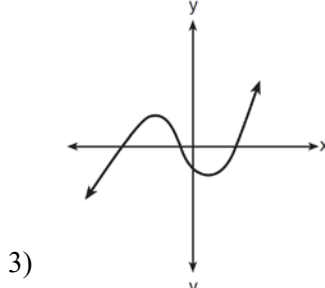
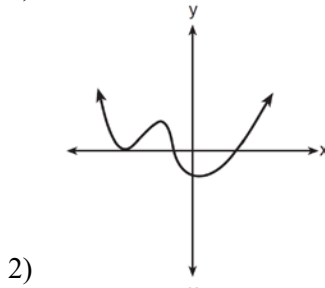
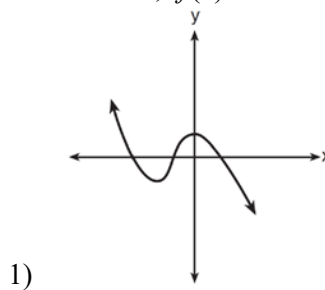
2)  $-y^2 - 4yi + 4$

3)  $-y^2 + 4$

4)  $y^2 + 4$

4 Which graph has the following characteristics?

- three real zeros
- as  $x \rightarrow -\infty, f(x) \rightarrow -\infty$
- as  $x \rightarrow \infty, f(x) \rightarrow \infty$



5 The solution set for the equation  $\sqrt{56 - x} = x$  is

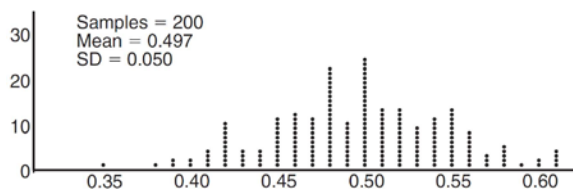
1)  $\{-8, 7\}$

2)  $\{-7, 8\}$

3)  $\{7\}$

4)  $\{\}$

- 6 The zeros for  $f(x) = x^4 - 4x^3 - 9x^2 + 36x$  are
- 1)  $\{0, \pm 3, 4\}$
  - 2)  $\{0, 3, 4\}$
  - 3)  $\{0, \pm 3, -4\}$
  - 4)  $\{0, 3, -4\}$
- 7 Anne has a coin. She does not know if it is a fair coin. She flipped the coin 100 times and obtained 73 heads and 27 tails. She ran a computer simulation of 200 samples of 100 fair coin flips. The output of the proportion of heads is shown below.



Given the results of her coin flips and of her computer simulation, which statement is most accurate?

- 1) 73 of the computer's next 100 coin flips will be heads.
  - 2) 50 of her next 100 coin flips will be heads.
  - 3) Her coin is not fair.
  - 4) Her coin is fair.
- 8 If  $g(c) = 1 - c^2$  and  $m(c) = c + 1$ , then which statement is *not* true?
- 1)  $g(c) \cdot m(c) = 1 + c - c^2 - c^3$
  - 2)  $g(c) + m(c) = 2 + c - c^2$
  - 3)  $m(c) - g(c) = c + c^2$
  - 4)  $\frac{m(c)}{g(c)} = \frac{-1}{1 - c}$

- 9 The heights of women in the United States are normally distributed with a mean of 64 inches and a standard deviation of 2.75 inches. The percent of women whose heights are between 64 and 69.5 inches, to the *nearest whole percent*, is
- 1) 6
  - 2) 48
  - 3) 68
  - 4) 95
- 10 The formula below can be used to model which scenario?

$$a_1 = 3000$$

$$a_n = 0.80a_{n-1}$$

- 1) The first row of a stadium has 3000 seats, and each row thereafter has 80 more seats than the row in front of it.
  - 2) The last row of a stadium has 3000 seats, and each row before it has 80 fewer seats than the row behind it.
  - 3) A bank account starts with a deposit of \$3000, and each year it grows by 80%.
  - 4) The initial value of a specialty toy is \$3000, and its value each of the following years is 20% less.
- 11 Sean's team has a baseball game tomorrow. He pitches 50% of the games. There is a 40% chance of rain during the game tomorrow. If the probability that it rains given that Sean pitches is 40%, it can be concluded that these two events are
- 1) independent
  - 2) dependent
  - 3) mutually exclusive
  - 4) complements
- 12 A solution of the equation  $2x^2 + 3x + 2 = 0$  is
- 1)  $-\frac{3}{4} + \frac{1}{4}i\sqrt{7}$
  - 2)  $-\frac{3}{4} + \frac{1}{4}i$
  - 3)  $-\frac{3}{4} + \frac{1}{4}\sqrt{7}$
  - 4)  $\frac{1}{2}$

- 13 The Ferris wheel at the landmark Navy Pier in Chicago takes 7 minutes to make one full rotation. The height,  $H$ , in feet, above the ground of one of the six-person cars can be modeled by

$$H(t) = 70 \sin\left(\frac{2\pi}{7}(t - 1.75)\right) + 80, \text{ where } t \text{ is time,}$$

in minutes. Using  $H(t)$  for one full rotation, this car's minimum height, in feet, is

- 1) 150
  - 2) 70
  - 3) 10
  - 4) 0
- 14 The expression  $\frac{4x^3 + 5x + 10}{2x + 3}$  is equivalent to

- 1)  $2x^2 + 3x - 7 + \frac{31}{2x + 3}$
- 2)  $2x^2 - 3x + 7 - \frac{11}{2x + 3}$
- 3)  $2x^2 + 2.5x + 5 + \frac{15}{2x + 3}$
- 4)  $2x^2 - 2.5x - 5 - \frac{20}{2x + 3}$

- 15 Which function represents exponential decay?

- 1)  $y = 2^{0.3t}$
- 2)  $y = 1.2^{3t}$
- 3)  $y = \left(\frac{1}{2}\right)^{-t}$
- 4)  $y = 5^{-t}$

- 16 Given  $f^{-1}(x) = -\frac{3}{4}x + 2$ , which equation represents  $f(x)$ ?

- 1)  $f(x) = \frac{4}{3}x - \frac{8}{3}$
- 2)  $f(x) = -\frac{4}{3}x + \frac{8}{3}$
- 3)  $f(x) = \frac{3}{4}x - 2$
- 4)  $f(x) = -\frac{3}{4}x + 2$

- 17 A circle centered at the origin has a radius of 10 units. The terminal side of an angle,  $\theta$ , intercepts the circle in Quadrant II at point  $C$ . The  $y$ -coordinate of point  $C$  is 8. What is the value of  $\cos \theta$ ?

- 1)  $-\frac{3}{5}$
- 2)  $-\frac{3}{4}$
- 3)  $\frac{3}{5}$
- 4)  $\frac{4}{5}$

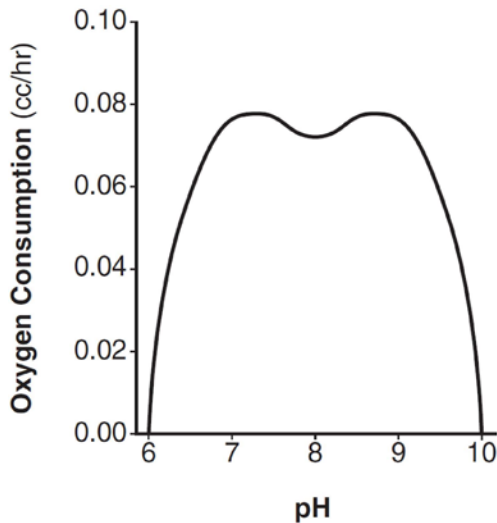
- 18 Which statement about the graph of  $c(x) = \log_6 x$  is *false*?

- 1) The asymptote has equation  $y = 0$ .
- 2) The graph has no  $y$ -intercept.
- 3) The domain is the set of positive reals.
- 4) The range is the set of all real numbers.

- 19 The equation  $4x^2 - 24x + 4y^2 + 72y = 76$  is equivalent to

- 1)  $4(x - 3)^2 + 4(y + 9)^2 = 76$
- 2)  $4(x - 3)^2 + 4(y + 9)^2 = 121$
- 3)  $4(x - 3)^2 + 4(y + 9)^2 = 166$
- 4)  $4(x - 3)^2 + 4(y + 9)^2 = 436$

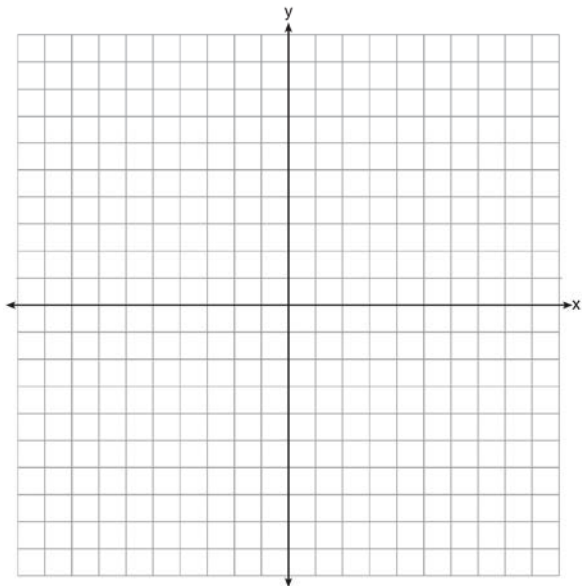
- 20 There was a study done on oxygen consumption of snails as a function of pH, and the result was a degree 4 polynomial function whose graph is shown below.



Which statement about this function is *incorrect*?

- 1) The degree of the polynomial is even.
  - 2) There is a positive leading coefficient.
  - 3) At two pH values, there is a relative maximum value.
  - 4) There are two intervals where the function is decreasing.
- 21 Last year, the total revenue for Home Style, a national restaurant chain, increased 5.25% over the previous year. If this trend were to continue, which expression could the company's chief financial officer use to approximate their monthly percent increase in revenue? [Let  $m$  represent months.]
- 1)  $(1.0525)^m$
  - 2)  $(1.0525)^{\frac{12}{m}}$
  - 3)  $(1.00427)^m$
  - 4)  $(1.00427)^{\frac{m}{12}}$
- 22 Which value, to the *nearest tenth*, is *not* a solution of  $p(x) = q(x)$  if  $p(x) = x^3 + 3x^2 - 3x - 1$  and  $q(x) = 3x + 8$ ?
- 1)  $-3.9$
  - 2)  $-1.1$
  - 3)  $2.1$
  - 4)  $4.7$
- 23 The population of Jamesburg for the years 2010-2013, respectively, was reported as follows: 250,000 250,937 251,878 252,822  
How can this sequence be recursively modeled?
- 1)  $j_n = 250,000(1.00375)^{n-1}$
  - 2)  $j_n = 250,000 + 937^{(n-1)}$
  - 3)  $j_1 = 250,000$   
 $j_n = 1.00375j_{n-1}$
  - 4)  $j_1 = 250,000$   
 $j_n = j_{n-1} + 937$
- 24 The voltage used by most households can be modeled by a sine function. The maximum voltage is 120 volts, and there are 60 cycles *every second*. Which equation best represents the value of the voltage as it flows through the electric wires, where  $t$  is time in seconds?
- 1)  $V = 120 \sin(t)$
  - 2)  $V = 120 \sin(60t)$
  - 3)  $V = 120 \sin(60\pi t)$
  - 4)  $V = 120 \sin(120\pi t)$
- 25 Solve for  $x$ :  $\frac{1}{x} - \frac{1}{3} = -\frac{1}{3x}$
- 26 Describe how a controlled experiment can be created to examine the effect of ingredient  $X$  in a toothpaste.
- 27 Determine if  $x - 5$  is a factor of  $2x^3 - 4x^2 - 7x - 10$ . Explain your answer.

- 28 On the axes below, graph *one* cycle of a cosine function with amplitude 3, period  $\frac{\pi}{2}$ , midline  $y = -1$ , and passing through the point  $(0, 2)$ .



- 29 A suburban high school has a population of 1376 students. The number of students who participate in sports is 649. The number of students who participate in music is 433. If the probability that a student participates in either sports or music is  $\frac{974}{1376}$ , what is the probability that a student participates in both sports and music?
- 30 The directrix of the parabola  $12(y + 3) = (x - 4)^2$  has the equation  $y = -6$ . Find the coordinates of the focus of the parabola.

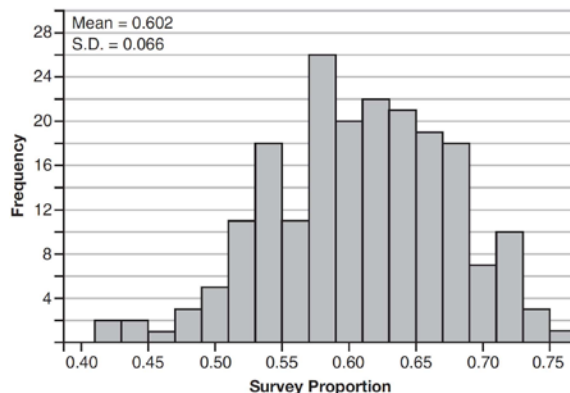
- 31 Algebraically prove that  $\frac{x^3 + 9}{x^3 + 8} = 1 + \frac{1}{x^3 + 8}$ , where  $x \neq -2$ .
- 32 A house purchased 5 years ago for \$100,000 was just sold for \$135,000. Assuming exponential growth, approximate the annual growth rate, to the *nearest percent*.

- 33 Solve the system of equations shown below algebraically.

$$(x - 3)^2 + (y + 2)^2 = 16$$

$$2x + 2y = 10$$

- 34 Alexa earns \$33,000 in her first year of teaching and earns a 4% increase in each successive year. Write a geometric series formula,  $S_n$ , for Alexa's total earnings over  $n$  years. Use this formula to find Alexa's total earnings for her first 15 years of teaching, to the *nearest cent*.
- 35 Fifty-five students attending the prom were randomly selected to participate in a survey about the music choice at the prom. Sixty percent responded that a DJ would be preferred over a band. Members of the prom committee thought that the vote would have 50% for the DJ and 50% for the band. A simulation was run 200 times, each of sample size 55, based on the premise that 60% of the students would prefer a DJ. The approximate normal simulation results are shown below.



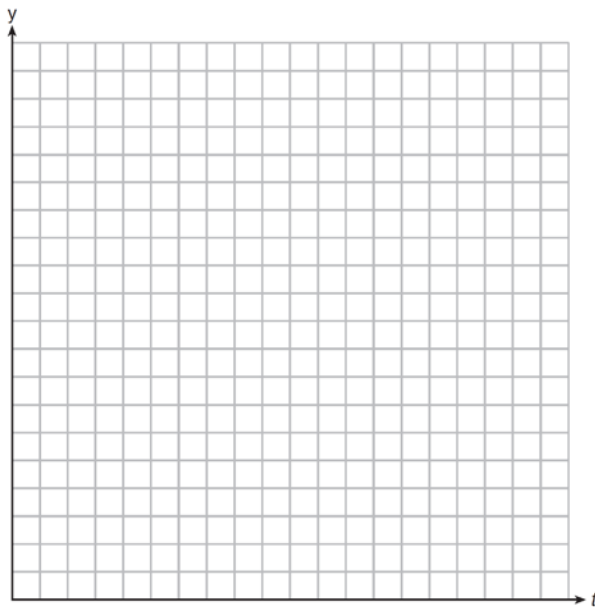
Using the results of the simulation, determine a plausible interval containing the middle 95% of the data. Round all values to the *nearest hundredth*. Members of the prom committee are concerned that a vote of all students attending the prom may produce a 50% – 50% split. Explain what statistical evidence supports this concern.

- 36 Which function shown below has a greater average rate of change on the interval  $[-2,4]$ ? Justify your answer.

$x$	$f(x)$
-4	0.3125
-3	0.625
-2	1.25
-1	2.5
0	5
1	10
2	20
3	40
4	80
5	160
6	320

$$g(x) = 4x^3 - 5x^2 + 3$$

- 37 Drugs break down in the human body at different rates and therefore must be prescribed by doctors carefully to prevent complications, such as overdosing. The breakdown of a drug is represented by the function  $N(t) = N_0(e)^{-rt}$ , where  $N(t)$  is the amount left in the body,  $N_0$  is the initial dosage,  $r$  is the decay rate, and  $t$  is time in hours. Patient  $A$ ,  $A(t)$ , is given 800 milligrams of a drug with a decay rate of 0.347. Patient  $B$ ,  $B(t)$ , is given 400 milligrams of another drug with a decay rate of 0.231. Write two functions,  $A(t)$  and  $B(t)$ , to represent the breakdown of the respective drug given to each patient. Graph each function on the set of axes below.



To the *nearest hour*,  $t$ , when does the amount of the given drug remaining in patient  $B$  begin to exceed the amount of the given drug remaining in patient  $A$ ? The doctor will allow patient  $A$  to take another 800 milligram dose of the drug once only 15% of the original dose is left in the body. Determine, to the *nearest tenth of an hour*, how long patient  $A$  will have to wait to take another 800 milligram dose of the drug.

## 0616AII Common Core State Standards

## Answer Section

- 1 ANS: 4                    PTS: 2                    REF: 061601aai           NAT: N.RN.A.2  
 TOP: Radicals and Rational Exponents           KEY: variables
- 2 ANS: 3                    PTS: 2                    REF: 061602aai           NAT: A.CED.A.1  
 TOP: Modeling Rationals

3 ANS: 2

$$(2 - yi)(2 - yi) = 4 - 4yi + y^2 i^2 = -y^2 - 4yi + 4$$

PTS: 2                    REF: 061603aai           NAT: N.CN.A.2           TOP: Operations with Complex Numbers

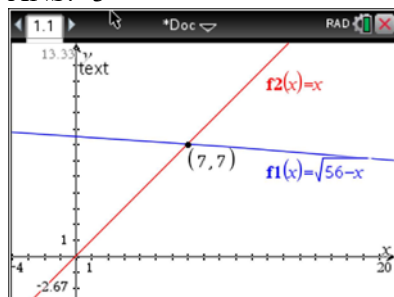
4 ANS: 3

The graph shows three real zeros, and has end behavior matching the given end behavior.

PTS: 2                    REF: 061604aai           NAT: A.APR.B.3           TOP: Zeros of Polynomials

KEY: AII

5 ANS: 3



$$\sqrt{56-x} = x \quad -8 \text{ is extraneous.}$$

$$56-x = x^2$$

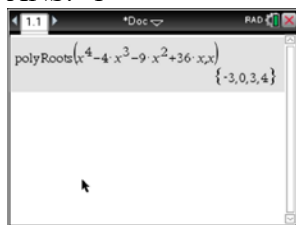
$$0 = x^2 + x - 56$$

$$0 = (x+8)(x-7)$$

$$x = 7$$

PTS: 2                    REF: 061605aai           NAT: A.REI.A.2           TOP: Solving Radicals  
 KEY: extraneous solutions

6 ANS: 1



$$x^4 - 4x^3 - 9x^2 + 36x = 0$$

$$x^3(x - 4) - 9x(x - 4) = 0$$

$$(x^3 - 9x)(x - 4) = 0$$

$$x(x^2 - 9)(x - 4) = 0$$

$$x(x + 3)(x - 3)(x - 4) = 0$$

$$x = 0, \pm 3, 4$$

PTS: 2 REF: 061606aia NAT: A.APR.B.3 TOP: Zeros of Polynomials  
KEY: All

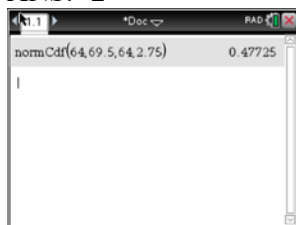
7 ANS: 3 PTS: 2 REF: 061607aia NAT: S.IC.A.2  
TOP: Analysis of Data

8 ANS: 4

$$\frac{m(c)}{g(c)} = \frac{c+1}{1-c^2} = \frac{c+1}{(1+c)(1-c)} = \frac{1}{1-c}$$

PTS: 2 REF: 061608aia NAT: F.BF.A.1 TOP: Operations with Functions

9 ANS: 2



$\bar{x} + 2\sigma$  represents approximately 48% of the data.

PTS: 2 REF: 061609aia NAT: S.ID.A.4 TOP: Normal Distributions  
KEY: percent

10 ANS: 4  
The scenario represents a decreasing geometric sequence with a common ratio of 0.80.

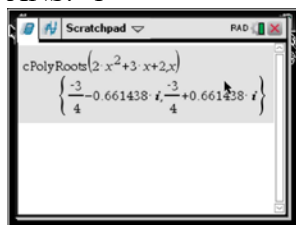
PTS: 2 REF: 061610aia NAT: F.BF.A.2 TOP: Sequences

11 ANS: 1  
The probability of rain equals the probability of rain, given that Sean pitches.

PTS: 2 REF: 061611aia NAT: S.CP.A.3 TOP: Conditional Probability



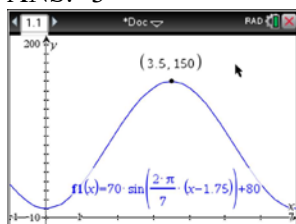
12 ANS: 1



$$x = \frac{-3 \pm \sqrt{3^2 - 4(2)(2)}}{2(2)} = \frac{-3 \pm \sqrt{-7}}{4} = -\frac{3}{4} \pm \frac{i\sqrt{7}}{4}$$

PTS: 2 REF: 061612aai NAT: A.REI.B.4 TOP: Solving Quadratics  
KEY: complex solutions | quadratic formula

13 ANS: 3



$H(t)$  is at a minimum at  $70(-1) + 80 = 10$

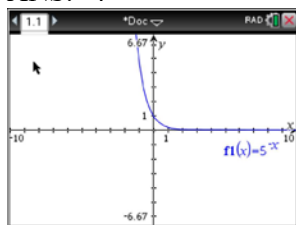
PTS: 2 REF: 061613aai NAT: F.IF.B.4 TOP: Graphing Trigonometric Functions  
KEY: maximum/minimum

14 ANS: 2

$$\begin{array}{r} 2x^2 - 3x + 7 \\ 2x + 3 \overline{) 4x^3 + 0x^2 + 5x + 10} \\ \underline{4x^3 + 6x^2} \phantom{+ 10} \\ -6x^2 + 5x \phantom{+ 10} \\ \underline{-6x^2 - 9x} \phantom{+ 10} \\ 14x + 10 \\ \underline{14x + 21} \\ -11 \end{array}$$

PTS: 2 REF: 061614aai NAT: A.APR.D.6 TOP: Rational Expressions

15 ANS: 4



$$y = 5^{-t} = \left(\frac{1}{5}\right)^t$$

PTS: 2 REF: 061615aai NAT: F.IF.C.8 TOP: Modeling Exponential Functions

16 ANS: 2

$$x = -\frac{3}{4}y + 2$$

$$-4x = 3y - 8$$

$$-4x + 8 = 3y$$

$$-\frac{4}{3}x + \frac{8}{3} = y$$

PTS: 2

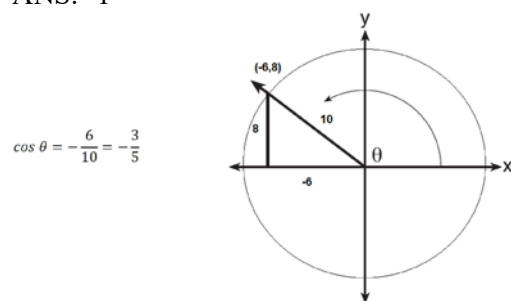
REF: 061616aai

NAT: F.BF.B.4

TOP: Inverse of Functions

KEY: equations

17 ANS: 1



PTS: 2

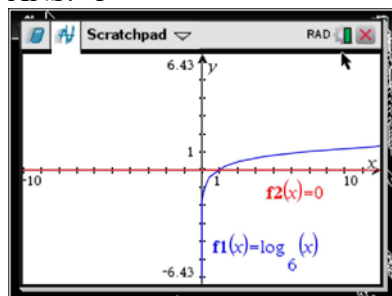
REF: 061617aai

NAT: F.TF.A.2

TOP: Determining Trigonometric Functions

KEY: extension to reals

18 ANS: 1



PTS: 2

REF: 061618aai

NAT: F.IF.C.7

TOP: Graphing Logarithmic Functions

19 ANS: 4

$$4(x^2 - 6x + 9) + 4(y^2 + 18y + 81) = 76 + 36 + 324$$

$$4(x - 3)^2 + 4(y + 9)^2 = 436$$

PTS: 2

REF: 061619aai

NAT: G.GPE.A.1

TOP: Equations of Circles

KEY: completing the square

20 ANS: 2

PTS: 2

REF: 061620aai

NAT: F.IF.B.4

TOP: Graphing Polynomial Functions

21 ANS: 3

$$1.0525^{\frac{1}{12}} \approx 1.00427$$

PTS: 2

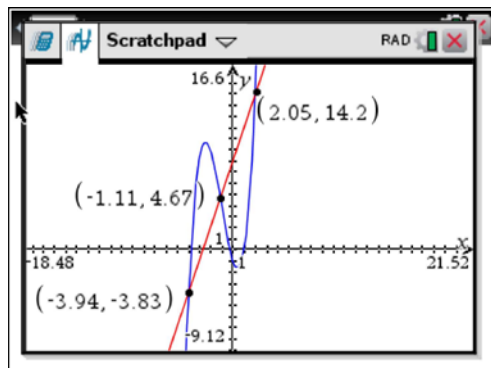
REF: 061621aai

NAT: F.BF.A.1

TOP: Modeling Exponential Functions

KEY: AII

22 ANS: 4



PTS: 2

REF: 061622aai

NAT: A.REI.D.11

TOP: Other Systems

KEY: AII

23 ANS: 3

PTS: 2

REF: 061623aai

NAT: F.BF.A.2

TOP: Sequences

24 ANS: 4

$$\text{period} = \frac{2\pi}{B}$$

$$\frac{1}{60} = \frac{2\pi}{B}$$

$$B = 120\pi$$

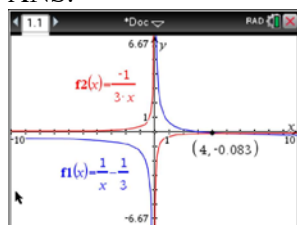
PTS: 2

REF: 061624aai

NAT: F.TF.B.5

TOP: Modeling Trigonometric Functions

25 ANS:



$$\frac{1}{x} - \frac{1}{3} = -\frac{1}{3-x}$$

$$\frac{3-x}{3x} = -\frac{1}{3-x}$$

$$3-x = -1$$

$$x = 4$$

PTS: 2

REF: 061625aai

NAT: A.REI.A.2

TOP: Solving Rationals

KEY: rational solutions

26 ANS:

Randomly assign participants to two groups. One group uses the toothpaste with ingredient  $X$  and the other group uses the toothpaste without ingredient  $X$ .

PTS: 2

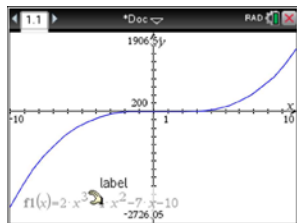
REF: 061626aai

NAT: S.IC.B.3

TOP: Analysis of Data

KEY: type

27 ANS:



$$x - 5 \overline{) 2x^3 - 4x^2 - 7x - 10} \quad \begin{array}{l} 2x^2 + 6x + 23 \\ \hline \end{array} \quad \text{Since there is a remainder, } x - 5 \text{ is not a factor.}$$

$$\underline{2x^3 - 10x^2}$$

$$6x^2 - 7x$$

$$\underline{6x^2 - 30x}$$

$$23x - 10$$

$$\underline{23x - 115}$$

$$105$$

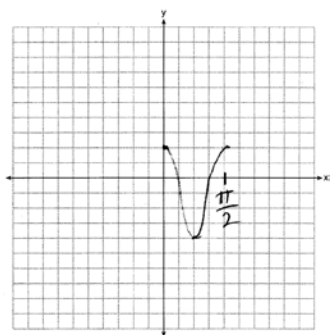
PTS: 2

REF: 061627aai

NAT: A.APR.B.2

TOP: Remainder Theorem

28 ANS:



PTS: 2

REF: 061628aai

NAT: F.IF.C.7

TOP: Graphing Trigonometric Functions

KEY: graph

29 ANS:

$$P(S \cap M) = P(S) + P(M) - P(S \cup M) = \frac{649}{1376} + \frac{433}{1376} - \frac{974}{1376} = \frac{108}{1376}$$

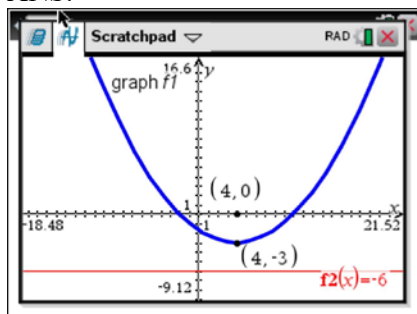
PTS: 2

REF: 061629aai

NAT: S.CP.B.7

TOP: Theoretical Probability

30 ANS:



The vertex of the parabola is  $(4, -3)$ . The  $x$ -coordinate of the focus and the vertex is the same. Since the distance from the vertex to the directrix is 3, the distance from the vertex to the focus is 3, so the  $y$ -coordinate of the focus is 0. The coordinates of the focus are  $(4, 0)$ .

PTS: 2 REF: 061630aai NAT: G.GPE.A.2 TOP: Graphing Quadratic Functions

31 ANS:

$$\frac{x^3 + 9}{x^3 + 8} = \frac{x^3 + 8}{x^3 + 8} + \frac{1}{x^3 + 8}$$

$$\frac{x^3 + 9}{x^3 + 8} = \frac{x^3 + 9}{x^3 + 8}$$

PTS: 2 REF: 061631aai NAT: A.APR.C.4 TOP: Polynomial Identities

32 ANS:

$$A = Pe^{rt}$$

$$135000 = 100000e^{5r}$$

$$1.35 = e^{5r}$$

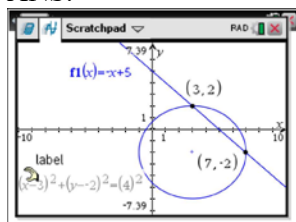
$$\ln 1.35 = \ln e^{5r}$$

$$\ln 1.35 = 5r$$

$$.06 \approx r \text{ or } 6\%$$

PTS: 2 REF: 061632aai NAT: F.LE.A.4 TOP: Exponential Growth

33 ANS:



$$y = -x + 5 \quad y = -7 + 5 = -2$$

$$(x-3)^2 + (-x+5+2)^2 = 16 \quad y = -3 + 5 = 2$$

$$x^2 - 6x + 9 + x^2 - 14x + 49 = 16$$

$$2x^2 - 20x + 42 = 0$$

$$x^2 - 10x + 21 = 0$$

$$(x-7)(x-3) = 0$$

$$x = 7, 3$$

PTS: 4 REF: 061633aai NAT: A.REI.C.7 TOP: Quadratic-Linear Systems

KEY: All

34 ANS:

$$S_n = \frac{33000 - 33000(1.04)^n}{1 - 1.04} \quad S_{15} = \frac{33000 - 33000(1.04)^{15}}{1 - 1.04} \approx 660778.39$$

PTS: 4 REF: 061634aai NAT: A.SSE.B.4 TOP: Series

35 ANS:

$0.602 \pm 2 \cdot 0.066 = 0.47 - 0.73$ . Since 0.50 falls within the 95% interval, this supports the concern there may be an even split.

PTS: 4 REF: 061635aai NAT: S.IC.B.5 TOP: Analysis of Data

36 ANS:

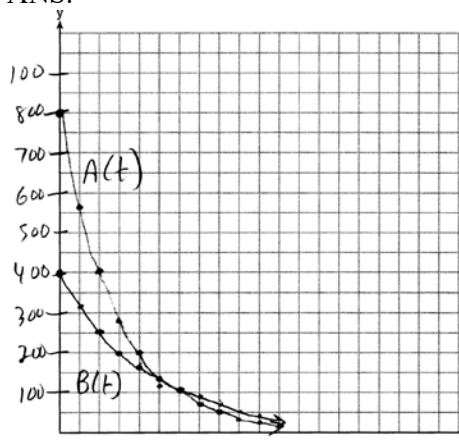
$$\frac{f(4) - f(-2)}{4 - (-2)} = \frac{80 - 1.25}{6} = 13.125 \quad g(x) \text{ has a greater rate of change}$$

$$\frac{g(4) - g(-2)}{4 - (-2)} = \frac{179 - -49}{6} = 38$$

PTS: 4 REF: 061636aai NAT: F.IF.B.6 TOP: Rate of Change

KEY: All

37 ANS:



$$A(t) = 800e^{-0.347t}$$

$$800e^{-0.347t} = 400e^{-0.231t} \quad 0.15 = e^{-0.347t}$$

$$B(t) = 400e^{-0.231t}$$

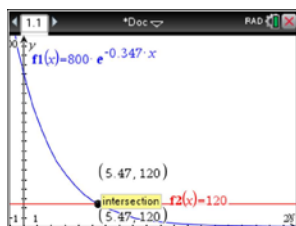
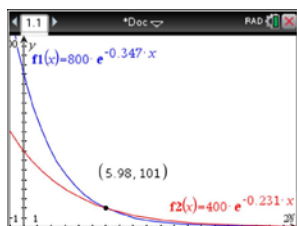
$$\ln 2e^{-0.347t} = \ln e^{-0.231t} \quad \ln 0.15 = \ln e^{-0.347t}$$

$$\ln 2 + \ln e^{-0.347t} = \ln e^{-0.231t} \quad \ln 0.15 = -0.347t \cdot \ln e$$

$$\ln 2 - 0.347t = -0.231t \quad 5.5 \approx t$$

$$\ln 2 = 0.116t$$

$$6 \approx t$$



PTS: 6

REF: 061637a11

NAT: A.REI.D.11

TOP: Other Systems

KEY: All