## The University of the State of New York

## 218th High School Examination

## ELEMENTARY ALGEBRA

Tuesday, January 22, 1918-1.15 to 4.15 p. m., only

Writest top of first page of answer paper (a) name of school where you have stadied, (b) number of weeks and recitations a week in elementary algebra. stadied, The minimum time requirement is flve recitations a week for a school year.

Answer the first six questions and four of the others. Credit will not be granted unless all operations (except mental ones) necessary to find results are given; simply indicating the operations is not sufficient. Each answer should be reduced to its simplest form.
1 Multiply $3 x^{2}+2 x y-8 y^{2}$ by $2 x^{2}-5 x y+4 y^{2}$
2 Perform the indicated operations [6] and check your work by substituting 3 for $x$ and 2 for $y$ [4]:

$$
\frac{x-y}{3 x+2 y}+\frac{12 x y}{9 x^{2}-4 y^{2}}-\frac{x+y}{3 x-2 y}
$$

3 Find the prime factors of each of the following: [10]

$$
\begin{align*}
& x^{3}-x-6 \\
& 2 a^{2}-a b-b^{2} \\
& a c+c b-a d-b d \\
& 2 a^{2}+5 a b-3 b^{2} \\
& x^{2}-25 y^{2} z^{2} \tag{4}
\end{align*}
$$

4a Simplify $\sqrt{18 a}-2 \sqrt{\frac{a}{2}}+3 \sqrt{50 a}$
$b$ Find the value of $\sqrt{b^{2}-4 a c}$ when

$$
\begin{array}{lll}
a=2 & b=3 & c=-5 \\
a=8 & b=-8 & c=2 \\
a=\frac{1}{b} & b=\frac{1}{2} & c=\frac{1}{4} \tag{6}
\end{array}
$$

5 Solve for $x\left[{ }^{[6]}\right.$ and check [4]: $\quad 2 x^{2}+x-21=0$
6 Solve for $x$ and $y[8]$ and check [2]:

$$
\begin{aligned}
x^{2}+y^{2} & =26 \\
x-y & =-4
\end{aligned}
$$

7 Solve for $y\left[{ }^{8}\right]$ and check [2]:

$$
\frac{3 y-2}{y+4}-\frac{y+5}{5-y}=\frac{4 y^{2}+3 y-3}{y^{2}-y-20}
$$

8 Extract the square root of

$$
10 x^{2}-4 x^{3}+x^{4}-12 x+9
$$

Check.
[3]

## Elementary Algebra - concluded

$9 a$ Solve for $v$ in terms of $h$ and $g$ :

$$
h=\frac{v^{2}}{2 g}
$$

What is the value of $v$ if $h=25$ and $g=32$ ?
$b$ How many pounds of sugar at $b$ cents a pound would cost as much as $e$ dozen of eggs at $c$ cents a dozen?
$10 A$ is 60 miles from $B$. An automobile at $A$ starts for $B$ at the rate of 20 miles an hour at the same time that an automobile at $B$ starts for $A$ at the rate of 25 miles an hour. How long will it be before the automobiles will pass each other? [ ${ }^{10}$ ]

11 a How many yards are there in $c$ inches?
$b$ A boy will be $y$ years old 2 years hence; how old was he 4 years ago?
c A book cost $d$ dollars; how many dollars will have to be paid for a second book if it costs $c$ cents more than the first?
$d$ A rectangle is $b$ inches long and $c$ inches wide; find its area and its perimeter.
12 Two farm cadets have set out 600 tomato plants; the number of plants in each row is 10 less than twice the number of rows. How many plants are there in each row?

13 A rectangular piece of paper is twice as long as a square piece and 3 inches wider; the area of the rectangular piece is 108 square inches. Find the dimensions of the square piece. [10]
14 Solve for $c$ correctly to two decimal places: [10]

$$
c^{2}+4 c-1=0
$$

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## DIRECTIONS FOR RATING

The Jirection, "Less than 605 of the credit shoold be granted when an error in enmprutation occurs," should be followed in rating all incorrect answers to goestions which fall under the topics mentioned in "Suggestions on the Rating of Regeats Eramination Papers in Mathematics" under "Elem. Alg. 12. " In all problems solved with two unknowns, no credit should be given for one equation correctly formed if the other is not given or is inaccurate.
No credir should be allowed for checks unless made in original statements. Ercept in schools where the "committee system" is used, teachers are arged $m$ mark pupers camalatively, that is, to add the credits earned by each answer to te total credits earned by preceding answers so that the mark given to the lust answer is the per cent to which the paper is entitled, e. g. consecutive ansers earning $5,7,4$ etc. respectively should be marked $5,12,16$ etc.
110 credits
Allow no partial credit.
210 credits
Allow 3 credits for reducing fractions to least common denominator.
Allow 3 credits for correct addition.
Allow 4 credits for correct check.
310 credits
Allow 2 credits each.
410 credits
a 4 credits.
Allow 3 credits for correct simplification (1 each).
Allow 1 credit for correct addition.
36 credits. Allow 2 credits each, 1 for correct substitution and addition, 1 for correct simplification.

## 510 credits

Allow 4 credits for first correct result.
Allow 2 credits for second correct result.
Allow 4 credits for correct checks ( 2 each).

## 610 credits

Allow 5 credits for first correct result.
Allow 3 eredits for other correct results ( 1 each).
Allow 2 eredits for correct checks ( 1 each).

## Directions for Rating-concluded

710 credits
Allow 5 credits for clearing fractions correctly.
Allow 3 credits for correct result.
Allow 2 credits for correct check.
810 credits
Allow 3 credits for first two correct terms of the root.
Allow 4 credits for third term of root if work is finished correctly.
Allow 3 credits for correct check.
910 credits
a 6 credits. Allow 3 credits for expressing $v$ in terms of $\hbar$ and $g$. Allow no partial credit. Allow 3 credits for correct value of $v$.
b 4 credits. Allow no partial credit.
$10 \quad 10$ credits
Allow 6 credits for correct equation.
Allow 4 credits for correct solution.
1110 credits
a Allow 2 credits.
$b$ Allow 2 credits.
c Allow 2 credits.
$d$ Allow 4 credits ( 2 each).
Allow no partial credit on $a, b, c$ or on either part of $d$.
1210 credits
Allow 6 eredits for correct equation.
Allow 4 credits for correct solution.
1310 credits
Allow 6 credits for correct equation.
Allow 4 credits for correct solution.
1410 credits
Allow 6 credits for finding $c=-2 \pm \sqrt{5}$
Allow 4 credits for finding correct decimal values (2 each).

