## 0619geo

1 On the set of axes below, triangle $A B C$ is graphed. Triangles $A^{\prime} B^{\prime} C^{\prime}$ and $A^{\prime \prime} B^{\prime \prime} C^{\prime \prime}$, the images of triangle $A B C$, are graphed after a sequence of rigid motions.


Identify which sequence of rigid motions maps $\triangle A B C$ onto $\triangle A^{\prime} B^{\prime} C$ and then maps $\triangle A^{\prime} B^{\prime} C^{\prime \prime}$ onto $\triangle A^{\prime \prime} B^{\prime \prime} C^{\prime \prime}$.

1) a rotation followed by another rotation
2) a reflection followed by a translation
3) a translation followed by a reflection
4) a reflection followed by a rotation

2 The table below shows the population and land area, in square miles, of four counties in New York State at the turn of the century.

| County | 2000 <br> Census Population | 2000 <br> Land Area <br> $\left(\mathrm{mi}^{2}\right)$ |
| :---: | :---: | :---: |
| Broome | 200,536 | 706.82 |
| Dutchess | 280,150 | 801.59 |
| Niagara | 219,846 | 522.95 |
| Saratoga | 200,635 | 811.84 |

Which county had the greatest population density?

1) Broome
2) Niagara
3) Dutchess
4) Saratoga

3 If a rectangle is continuously rotated around one of its sides, what is the three-dimensional figure formed?

1) rectangular prism
2) sphere
3) cylinder
4) cone

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4 Which transformation carries the parallelogram below onto itself?


1) a reflection over $y=x$
2) a rotation of $90^{\circ}$ counterclockwise about the origin
3) a reflection over $y=-x$
4) a rotation of $180^{\circ}$ counterclockwise about the origin

5 After a dilation centered at the origin, the image of $\overline{C D}$ is $\overline{C^{\prime} D^{\prime}}$. If the coordinates of the endpoints of these segments are $C(6,-4), D(2,-8), C^{\prime}(9,-6)$, and $D^{\prime}(3,-12)$, the scale factor of the dilation is

1) $\frac{3}{2}$
2) $\frac{2}{3}$
3) 3
4) $\frac{1}{3}$

6 A tent is in the shape of a right pyramid with a square floor. The square floor has side lengths of 8 feet. If the height of the tent at its center is 6 feet, what is the volume of the tent, in cubic feet?

1) 48
2) 128
3) 192
4) 384

7 The line $-3 x+4 y=8$ is transformed by a dilation centered at the origin. Which linear equation could represent its image?

1) $y=\frac{4}{3} x+8$
2) $y=\frac{3}{4} x+8$
3) $y=-\frac{3}{4} x-8$
4) $y=-\frac{4}{3} x-8$

8 In the diagram below, $\overline{A C}$ and $\overline{B D}$ intersect at $E$.


Which information is always sufficient to prove $\triangle A B E \cong \triangle C D E$ ?

1) $\overline{A B} \| \overline{C D}$
2) $\overline{A B} \cong \overline{C D}$ and $\overline{B E} \cong \overline{D E}$
3) $E$ is the midpoint of $\overline{A C}$.
4) $\overline{B D}$ and $\overline{A C}$ bisect each other.

9 The expression $\sin 57^{\circ}$ is equal to

1) $\tan 33^{\circ}$
2) $\cos 33^{\circ}$
3) $\tan 57^{\circ}$
4) $\cos 57^{\circ}$

10 What is the volume of a hemisphere that has a diameter of 12.6 cm , to the nearest tenth of a cubic centimeter?

1) 523.7
2) 1047.4
3) 4189.6
4) 8379.2

11 In the diagram below of $\triangle A B C, D$ is a point on $\overline{B A}, E$ is a point on $\overline{B C}$, and $\overline{D E}$ is drawn.


If $B D=5, D A=12$, and $B E=7$, what is the length of $\overline{B C}$ so that $\overline{A C} \| \overline{D E}$ ?

1) 23.8
2) 16.8
3) 15.6
4) 8.6

12 A quadrilateral must be a parallelogram if

1) one pair of sides is parallel and one pair of angles is congruent
2) one pair of sides is both parallel and congruent
3) one pair of sides is congruent and one pair of angles is congruent
4) the diagonals are congruent

13 In the diagram below of circle $O$, chords $\overline{J T}$ and $\overline{E R}$ intersect at $M$.


If $E M=8$ and $R M=15$, the lengths of $\overline{J M}$ and $\overline{T M}$ could be

1) 12 and 9.5
2) 14 and 8.5
3) 16 and 7.5
4) 18 and 6.5

14 Triangles $J O E$ and $S A M$ are drawn such that $\angle E \cong \angle M$ and $\overline{E J} \cong \overline{M S}$. Which mapping would not always lead to $\triangle J O E \cong \triangle S A M$ ?

1) $\angle J$ maps onto $\angle S$
2) $\angle O$ maps onto $\angle A$
3) $\overline{E O}$ maps onto $\overline{M A}$
4) $\overline{J O}$ maps onto $\overline{S A}$
$15 \frac{\text { In } \triangle A B C \text { shown below, } \angle A C B \text { is a right angle, } E \text { is a point on } \overline{A C} \text {, and } \overline{E D} \text { is drawn perpendicular to hypotenuse }}{}$


If $A B=9, B C=6$, and $D E=4$, what is the length of $\overline{A E}$ ?

1) 5
2) 6
3) 7
4) 8

16 Which equation represents a line parallel to the line whose equation is $-2 x+3 y=-4$ and passes through the point $(1,3)$ ?

1) $y-3=-\frac{3}{2}(x-1)$
2) $y-3=\frac{2}{3}(x-1)$
3) $y+3=-\frac{3}{2}(x+1)$
4) $y+3=\frac{2}{3}(x+1)$

17 In rhombus $T I G E$, diagonals $\overline{T G}$ and $\overline{I E}$ intersect at $R$. The perimeter of $T I G E$ is 68 , and $T G=16$.


What is the length of diagonal $\overline{I E}$ ?

1) 15
2) 30
3) 34
4) 52

18 In circle $O$ two secants, $\overline{A B P}$ and $\overline{C D P}$, are drawn to external point $P$. If $\widetilde{\mathrm{m} A C}=72^{\circ}$, and $\mathrm{m} \overparen{B D}=34^{\circ}$, what is the measure of $\angle P$ ?

1) $19^{\circ}$
2) $38^{\circ}$
3) $53^{\circ}$
4) $106^{\circ}$

19 What are the coordinates of point $C$ on the directed segment from $A(-8,4)$ to $B(10,-2)$ that partitions the segment such that $A C: C B$ is $2: 1$ ?

1) $(1,1)$
2) $(-2,2)$
3) $(2,-2)$
4) $(4,0)$

20 The equation of a circle is $x^{2}+8 x+y^{2}-12 y=144$. What are the coordinates of the center and the length of the radius of the circle?

1) center $(4,-6)$ and radius 12
2) center (4,-6) and radius 14
3) center ( $-4,6$ ) and radius 12
4) center ( $-4,6$ ) and radius 14

21 In parallelogram $P Q R S, \overline{Q P}$ is extended to point $T$ and $\overline{S T}$ is drawn.


If $\overline{S T} \cong \overline{S P}$ and $\mathrm{m} \angle R=130^{\circ}$, what is $\mathrm{m} \angle P S T$ ?

1) $130^{\circ}$
2) $80^{\circ}$
3) $65^{\circ}$
4) $50^{\circ}$

22 A 12 -foot ladder leans against a building and reaches a window 10 feet above ground. What is the measure of the angle, to the nearest degree, that the ladder forms with the ground?

1) 34
2) 40
3) 50
4) 56

23 In the diagram of equilateral triangle $A B C$ shown below, $E$ and $F$ are the midpoints of $\overline{A C}$ and $\overline{B C}$, respectively.


If $E F=2 x+8$ and $A B=7 x-2$, what is the perimeter of trapezoid $A B F E$ ?

1) 36
2) 60
3) 100
4) 120

24 Which information is not sufficient to prove that a parallelogram is a square?

1) The diagonals are both congruent and 3) The diagonals are perpendicular and one perpendicular. pair of adjacent sides are congruent.
2) The diagonals are congruent and one pair 4) The diagonals are perpendicular and one of adjacent sides are congruent. pair of adjacent sides are perpendicular.

25 Triangle $A^{\prime} B^{\prime} C^{\prime}$ is the image of triangle $A B C$ after a dilation with a scale factor of $\frac{1}{2}$ and centered at point $A$. Is triangle $A B C$ congruent to triangle $A^{\prime} B^{\prime} C^{\prime}$ ? Explain your answer.

26 Determine and state the area of triangle $P Q R$, whose vertices have coordinates $P(-2,-5), Q(3,5)$, and $R(6,1)$. [The use of the set of axes below is optional.]


27 A support wire reaches from the top of a pole to a clamp on the ground. The pole is perpendicular to the level ground and the clamp is 10 feet from the base of the pole. The support wire makes a $68^{\circ}$ angle with the ground. Find the length of the support wire to the nearest foot.

28 In the diagram below, circle $O$ has a radius of 10 .


If $\mathrm{m} \overparen{A B}=72^{\circ}$, find the area of shaded sector $A O B$, in terms of $\pi$.

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29 On the set of axes below, $\triangle A B C \cong \triangle S T U$.


Describe a sequence of rigid motions that maps $\triangle A B C$ onto $\triangle S T U$.

30 In right triangle $P R T, \mathrm{~m} \angle P=90^{\circ}$, altitude $\overline{P Q}$ is drawn to hypotenuse $\overline{R T}, R T=17$, and $P R=15$.


Determine and state, to the nearest tenth, the length of $\overline{R Q}$.

31 Given circle $O$ with radius $\overline{O A}$, use a compass and straightedge to construct an equilateral triangle inscribed in circle $O$. [Leave all construction marks.]


32 Riley plotted $A(-1,6), B(3,8), C(6,-1)$, and $D(1,0)$ to form a quadrilateral. Prove that Riley's quadrilateral $A B C D$ is a trapezoid. [The use of the set of axes on the next page is optional.] Riley defines an isosceles trapezoid as a trapezoid with congruent diagonals. Use Riley's definition to prove that $A B C D$ is not an isosceles trapezoid.


33 A child-sized swimming pool can be modeled by a cylinder. The pool has a diameter of $6 \frac{1}{2}$ feet and a height of 12 inches. The pool is filled with water to $\frac{2}{3}$ of its height. Determine and state the volume of the water in the pool, to the nearest cubic foot. One cubic foot equals 7.48 gallons of water. Determine and state, to the nearest gallon, the number of gallons of water in the pool.

34 Nick wanted to determine the length of one blade of the windmill pictured below. He stood at a point on the ground 440 feet from the windmill's base. Using surveyor's tools, Nick measured the angle between the ground and the highest point reached by the top blade and found it was $38.8^{\circ}$. He also measured the angle between the ground and the lowest point of the top blade, and found it was $30^{\circ}$.


Determine and state a blade's length, $x$, to the nearest foot.

35 Given: Quadrilateral MATH, $\overline{H M} \cong \overline{A T}, \overline{H T} \cong \overline{A M}, \overline{H E} \perp \overline{M E A}$, and $\overline{H A} \perp \overline{A T}$


Prove: $T A \bullet H A=H E \bullet T H$

## 0619geo

Answer Section
1 ANS: 4
PTS: 2
REF: 061901geo NAT: G.CO.A. 5
TOP: Compositions of Transformations KEY: identify
2 ANS: 3
Broome: $\frac{200536}{706.82} \approx 284$ Duchess: $\frac{280150}{801.59} \approx 349$ Niagara: $\frac{219846}{522.95} \approx 420$ Saratoga: $\frac{200635}{811.84} \approx 247$
PTS: 2 REF: 061902geo NAT: G.MG.A. 2 TOP: Density
3 ANS: 2 PTS: 2 REF: 061903geo NAT: G.GMD.B. 4
TOP: Rotations of Two-Dimensional Objects
4 ANS: 4 PTS: 2 REF: 061904geo NAT: G.CO.A. 3
TOP: Mapping a Polygon onto Itself
5 ANS: 1
$\frac{9}{6}=\frac{3}{2}$
PTS: 2 REF: 061905geo NAT: G.SRT.A. 1 TOP: Line Dilations
6 ANS: 2
$V=\frac{1}{3}(8)^{2} \cdot 6=128$

PTS: 2 REF: 061906geo NAT: G.GMD.A. 3 TOP: Volume
KEY: pyramids
7 ANS: 2
The slope of $-3 x+4 y=8$ is $\frac{3}{4}$.
PTS: 2 REF: 061907geo NAT: G.SRT.A. 1 TOP: Line Dilations
8 ANS: 4


PTS: 2
KEY: statements
9 ANS: 2
$90-57=33$
PTS: 2 REF: 061909geo NAT: G.SRT.C. 7 TOP: Cofunctions

10 ANS: 1
$V=\frac{1}{2} \times \frac{4}{3} \pi r^{3}=\frac{1}{2} \times \frac{4}{3} \pi \cdot\left(\frac{12.6}{2}\right)^{3} \approx 523.7$
PTS: 2 REF: 061910geo NAT: G.GMD.A. 3 TOP: Volume
KEY: spheres
11 ANS: 1
$5 x=12 \cdot 7 \quad 16.8+7=23.8$
$5 x=84$
$x=16.8$

PTS: 2 REF: 061911geo NAT: G.SRT.B. 5 TOP: Side Splitter Theorem
12 ANS: 3 PTS: 2 REF: 061912geo NAT: G.CO.C. 11
TOP: Parallelograms
13 ANS: 3
$8 \cdot 15=16 \cdot 7.5$
PTS: 2 REF: 061913geo NAT: G.C.A. 2 TOP: Chords, Secants and Tangents
KEY: intersecting chords, length
14 ANS: 4
d) is SSA

PTS: 2 REF: 061914geo NAT: G.CO.B. 7 TOP: Triangle Congruency
15 ANS: 2
$\frac{4}{x}=\frac{6}{9}$
$x=6$

PTS: 2
REF: 061915geo NAT: G.SRT.B. 5 TOP: Similarity
KEY: basic
16 ANS: 2
$m=\frac{-(-2)}{3}=\frac{2}{3}$

PTS: 2 REF: 061916geo NAT: G.GPE.B. 5 TOP: Parallel and Perpendicular Lines
KEY: write equation of parallel line
17 ANS: 2
$E R=\sqrt{17^{2}-8^{2}}=15$
PTS: 2 REF: 061917geo NAT: G.CO.C.11 TOP: Special Quadrilaterals

18 ANS: 1


PTS: 2 REF: 061918geo NAT: G.C.A. 2 TOP: Chords, Secants and Tangents KEY: secants drawn from common point, angle
19 ANS: 4
$-8+\frac{2}{3}(10--8)=-8+\frac{2}{3}(18)=-8+12=44+\frac{2}{3}(-2-4)=4+\frac{2}{3}(-6)=4-4=0$
PTS: 2 REF: 061919geo NAT: G.GPE.B. 6 TOP: Directed Line Segments
20 ANS: 4
$x^{2}+8 x+16+y^{2}-12 y+36=144+16+36$

$$
(x+4)^{2}+(y-6)^{2}=196
$$

PTS: 2
REF: 061920geo NAT: G.GPE.A. 1 TOP: Equations of Circles
KEY: completing the square
21 ANS: 2


PTS: 2 REF: 061921geo NAT: G.CO.C. 11 TOP: Interior and Exterior Angles of Polygons
22 ANS: 4
$\sin x=\frac{10}{12}$

$$
x \approx 56
$$

PTS: 2 REF: 061922geo NAT: G.SRT.C. 8 TOP: Using Trigonometry to Find an Angle

23 ANS: 3
$2(2 x+8)=7 x-2 \quad A B=7(6)-2=40$. Since $\overline{E F}$ is a midsegment, $E F=\frac{40}{2}=20$. Since $\triangle A B C$ is equilateral, $4 x+16=7 x-2$
$18=3 x$
$6=x$
$A E=B F=\frac{40}{2}=20.40+20+20+20=100$
PTS: 2 REF: 061923geo NAT: G.CO.C. 10 TOP: Midsegments
24 ANS: 3 PTS: 2 REF: 061924geo NAT: G.CO.C. 11
TOP: Special Quadrilaterals
25 ANS:
No, because dilations do not preserve distance.
PTS: 2 REF: 061925geo NAT: G.SRT.A. 2 TOP: Dilations
26 ANS:


PTS: 2 REF: 061926geo NAT: G.GPE.B. 7 TOP: Polygons in the Coordinate Plane
27 ANS:
$\cos 68=\frac{10}{x}$
$x \approx 27$
PTS: 2 REF: 061927geo NAT: G.SRT.C. 8 TOP: Using Trigonometry to Find a Side
28 ANS:
$\frac{72}{360}(\pi)\left(10^{2}\right)=20 \pi$
PTS: 2 REF: 061928geo NAT: G.C.B. 5 TOP: Sectors
29 ANS:
$R_{90^{\circ}}$ or $T_{2,-6} \circ R_{(-4,2), 90^{\circ}}$ or $R_{270^{\circ}}{ }^{\circ} r_{\text {x-xxis }}{ }^{\circ} r_{y \text {-axis }}$
PTS: 2 REF: 061929geo NAT: G.CO.A. 5 TOP: Compositions of Transformations KEY: identify

30 ANS:
$17 x=15^{2}$
$17 x=225$

$$
x \approx 13.2
$$

PTS: 2 REF: 061930geo NAT: G.SRT.B. 5 TOP: Similarity
KEY: leg
31 ANS:


PTS: 2 REF: 061931geo NAT: G.CO.D. 13 TOP: Constructions
32 ANS:
 $m_{\overline{A D}}=\frac{0-6}{1--1}=-3 \overline{A D} \| \overline{B C}$ because their slopes are equal. $A B C D$ is a trapezoid $m_{B C}=\frac{-1-8}{6-3}=-3$
because it has a pair of parallel sides. $A C=\sqrt{(-1-6)^{2}+(6--1)^{2}}=\sqrt{98} A B C D$ is not an isosceles trapezoid

$$
B D=\sqrt{(8-0)^{2}+(3-1)^{2}}=\sqrt{68}
$$

because its diagonals are not congruent.
PTS: 4
REF: 061932geo
NAT: G.GPE.B. 4 TOP: Quadrilaterals in the Coordinate Plane KEY: grids

33 ANS:
$V=\frac{2}{3} \pi\left(\frac{6.5}{2}\right)^{2}(1) \approx 2222 \cdot 7.48 \approx 165$
PTS: 4 REF: 061933geo NAT: G.GMD.A. 3 TOP: Volume
KEY: cylinders
34
ANS:
$\begin{aligned} & \tan 30=\frac{y}{440} \quad \tan 38.8 \\ &=\frac{h}{440} \quad 353.8-254 \approx 100 \\ & y \approx 254 \quad h\end{aligned}$
PTS: 4 REF: 061934geo NAT: G.SRT.C. 8 TOP: Using Trigonometry to Find a Side
KEY: advanced
35 ANS:
Quadrilateral $M A T H, \overline{H M} \cong \overline{A T}, \overline{H T} \cong \overline{A M}, \overline{H E} \perp \overline{M E A}$, and $\overline{H A} \perp \overline{A T}$ (given); $\angle H E A$ and $\angle T A H$ are right angles (perpendicular lines form right angles); $\angle H E A \cong \angle T A H$ (all right angles are congruent); MATH is a parallelogram (a quadrilateral with two pairs of congruent opposite sides is a parallelogram); $\overline{M A} \| \overline{T H}$ (opposite sides of a parallelogram are parallel); $\angle T H A \cong \angle E A H$ (alternate interior angles of parallel lines and a transversal are congruent); $\triangle H E A \sim \triangle T A H$ (AA); $\frac{H A}{T H}=\frac{H E}{T A}$ (corresponding sides of similar triangles are in proportion); $T A \bullet H A=H E \bullet T H$ (product of means equals product of extremes).

PTS: 6 REF: 061935geo NAT: G.SRT.B. 5 TOP: Quadrilateral Proofs

