The University of the State of New York REGENTS HIGH SCHOOL EXAMINATION

GEOMETRY

Thursday, August 17, 2023 — 12:30 to 3:30 p.m., only

Student Name: My, Sibol
School Name: MAP

The possession or use of any communications device is strictly prohibited when taking this examination. If you have or use any communications device, no matter how briefly, your examination will be invalidated and no score will be calculated for you.

Print your name and the name of your school on the lines above.

A separate answer sheet for **Part I** has been provided to you. Follow the instructions from the proctor for completing the student information on your answer sheet.

This examination has four parts, with a total of 35 questions. You must answer all questions in this examination. Record your answers to the Part I multiple-choice questions on the separate answer sheet. Write your answers to the questions in **Parts II**, **III**, and **IV** directly in this booklet. All work should be written in pen, except graphs and drawings, which should be done in pencil. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. Utilize the information provided for each question to determine your answer. Note that diagrams are not necessarily drawn to scale.

The formulas that you may need to answer some questions in this examination are found at the end of the examination. This sheet is perforated so you may remove it from this booklet.

Scrap paper is not permitted for any part of this examination, but you may use the blank spaces in this booklet as scrap paper. A perforated sheet of scrap graph paper is provided at the end of this booklet for any question for which graphing may be helpful but is not required. You may remove this sheet from this booklet. Any work done on this sheet of scrap graph paper will *not* be scored.

When you have completed the examination, you must sign the statement printed at the end of the answer sheet, indicating that you had no unlawful knowledge of the questions or answers prior to the examination and that you have neither given nor received assistance in answering any of the questions during the examination. Your answer sheet cannot be accepted if you fail to sign this declaration.

Notice ...

A graphing calculator, a straightedge (ruler), and a compass must be available for you to use while taking this examination.

DO NOT OPEN THIS EXAMINATION BOOKLET UNTIL THE SIGNAL IS GIVEN.

Part I

Answer all 24 questions in this part. Each correct answer will receive 2 credits. No partial credit will be allowed. Utilize the information provided for each question to determine your answer. Note that diagrams are not necessarily drawn to scale. For each statement or question, choose the word or expression that, of those given, best completes the statement or answers the question. Record your answers on your separate answer sheet. [48]

1 A plane intersects a sphere. Which two-dimensional shape is formed by this cross section?

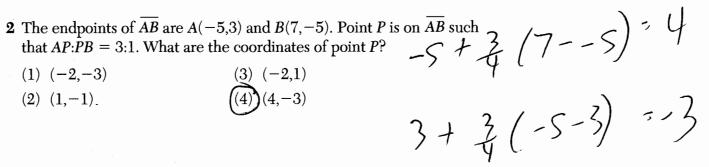
Use this space for computations.

- (1) rectangle
- (2) triangle

- square

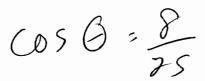


$$(3)$$
 $(-2,1)$



- 3 Zach placed the foot of an extension ladder 8 feet from the base of the house and extended the ladder 25 feet to reach the house. To the nearest degree, what is the measure of the angle the ladder makes with the ground?
 - (1) 18

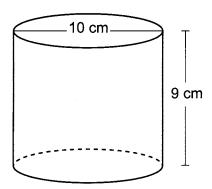
(2) 19



$$\theta \approx 70$$

Use this space for computations.

4 Darnell models a cup with the cylinder below. He measured the diameter of the cup to be 10 cm and the height to be 9 cm.



If Darnell fills the cup with water to a height of 8 cm, what is the volume of the water in the cup, to the *nearest cubic centimeter*?

 \bigcirc 628

(2) 707

- (3) 2513
- (4) 2827

	7	π	15	2	8	S	20	011
V	•	ι '	/	1	0		•	

5 Which quadrilateral has diagonals that are always perpendicular?

(1) rectangle

(3) trapezoid

(2) rhombus

(4) parallelogram

6 Which regular polygon would carry onto itself after a rotation of 300° about its center?

(1) decagon

(3) octagon

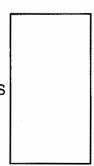
(2) nonagon

(4) hexagon

[3]

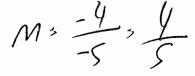
300 is a multiple of 60

Use this space for 7 The rectangle drawn below is continuously rotated about side *S*. computations.



Which three-dimensional figure is formed by this rotation?

- (1) rectangular prism
- (3) cylinder
- (2) square pyramid
- (4) cone
- 8 An equation of the line perpendicular to the line whose equation is 4x - 5y = 6 and passes through the point (-2,3) is



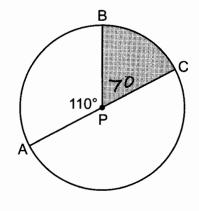
(1)
$$y + 3 = -\frac{5}{4}(x - 2)$$
 (3) $y + 3 = \frac{4}{5}(x - 2)$

(3)
$$y + 3 = \frac{4}{5}(x - 2)$$

(2)
$$y - 3 = -\frac{5}{4}(x + 2)$$
 (4) $y - 3 = \frac{4}{5}(x + 2)$

$$(4) \ y - 3 = \frac{4}{5}(x+2)$$

9 In circle P below, diameter \overline{AC} and radius \overline{BP} are drawn such that $m\angle APB = 110^{\circ}$.



70, TI.62 360

If AC = 12, what is the area of shaded sector BPC?

 $(1) \frac{7}{6}\pi$

(3) 11π

(4) 28π

Use this space for computations.

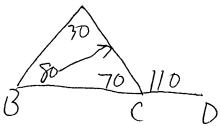
10 In $\triangle ABC$, side \overline{BC} is extended through C to D. If $m \angle A = 30^{\circ}$ and $m \angle ACD = 110^{\circ}$, what is the longest side of $\triangle ABC$?



(3) \overline{AB}

(2) \overline{BC}

(4) \overline{CD}



11 Right triangle ACT has $m \angle A = 90^{\circ}$. Which expression is always equivalent to $\cos T$?



(3) $\tan T$



 $(4) \sin T$

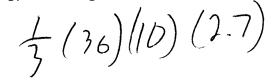
12 A regular pyramid with a square base is made of solid glass. It has a base area of 36 cm² and a height of 10 cm. If the density of glass is 2.7 grams per cubic centimeter, the mass of the pyramid, in grams, is

(1) 120

(3) 360

(2) 324

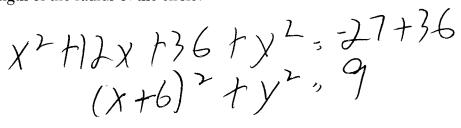
(4) 972



13 The equation of a circle is $x^2 + y^2 + 12x = -27$. What are the coordinates of the center and the length of the radius of the circle?

(1) center (6,0) and radius 3

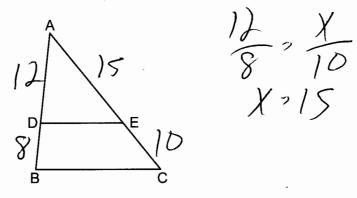
- (2) center (6,0) and radius 9
- (3) center (-6,0) and radius 3
- (4) center (-6,0) and radius 9



[5]

Use this space for computations.

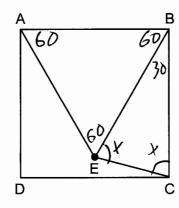
14 In triangle *ABC* below, *D* is a point on \overline{AB} and *E* is a point on \overline{AC} , such that $\overline{DE} \parallel \overline{BC}$.



If AD = 12, DB = 8, and EC = 10, what is the length of \overline{AC} ?

- (1) 15
- (2) 22

- (3) 24
- (4) 25
- 15 In the diagram below, point E is located inside square ABCD such that $\triangle ABE$ is equilateral, and \overline{CE} is drawn.



30+2x = 180 2x = 150 X=75

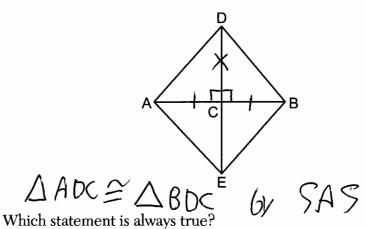
What is $m \angle BEC$?

- (1) 30°
- $(2) 60^{\circ}$

- (3) 75
- (4) 90°

Use this space for computations.

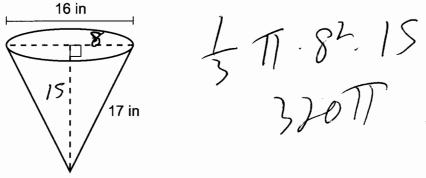
16 In the diagram below of quadrilateral ADBE, \overline{DE} is the perpendicular bisector of \overline{AB} .



- $\angle ADC \cong \angle BDC$
- (3) $\overline{AD} \cong \overline{BE}$
- $\angle EAC \cong \angle DAC$
- $(4) \ \overline{AE} \cong \overline{AD}$
- 17 What is the image of (4,3) after a reflection over the line y = 1?
 - (1) (-2,3)

(2) (-4,3)

- 18 In the diagram below, a cone has a diameter of 16 inches and a slant height of 17 inches.



What is the volume of the cone, in cubic inches?

 320π

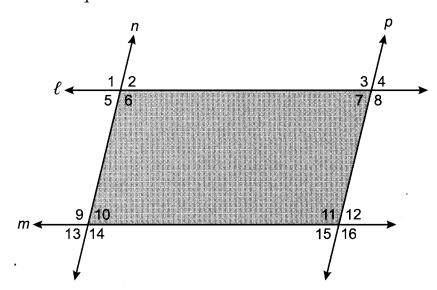
(3) 960π

(2) 363π

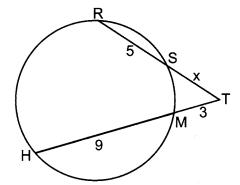
(4) 1280π

Use this space for computations.

19 In the diagram below, lines ℓ and m intersect lines n and p to create the shaded quadrilateral as shown.



quadrilateral is a parallelogram? 269244 (1) $21 \approx 26$ and $29 \approx 214$ (2) $25 \approx 210$ and $26 \approx 29$ and $26 \approx 29$ and $26 \approx 29$ and $26 \approx 211$ are corresponding angle. Since congruent, 2992411 angle.



Which equation could be used to find the value of x?

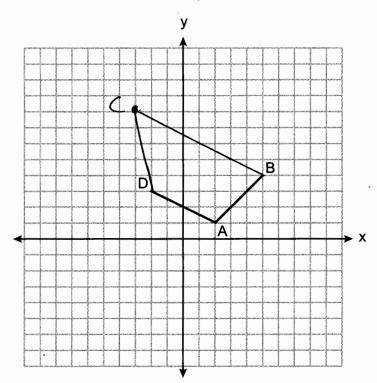
$$(1) x(x+5) = 36$$

(3)
$$3x = 45$$

$$(2) x(x+5) = 27$$

(4)
$$5x = 27$$

21 On the set of axes below, the coordinates of three vertices of trapezoid ABCD are A(2,1), B(5,4), and D(-2,3).



Which point could be vertex C?

$$(3)$$
 $(-1,6)$

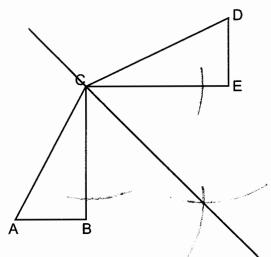
$$(2)$$
 $(4,10)$

$$(4)$$
 (-3.8)

$$M_{\overline{AD}} = \frac{3-1}{-2-2} = \frac{2}{-4} = -\frac{1}{2}$$
 $M_{\overline{BC}} = \frac{5-4}{-3-5} = \frac{4}{-8} = -\frac{1}{2}$

Use this space for computations.

22 In the diagram below, $\triangle ABC \cong \triangle DEC$.



Which transformation will map $\triangle ABC$ onto $\triangle DEC$?

- (1) a rotation
- (2) a line reflection
- (3) a translation followed by a dilation
- (4) a line reflection followed by a second line reflection

23 If $\triangle TAP$ is dilated by a scale factor of 0.5, which statement about the

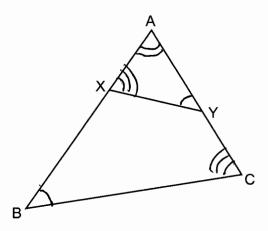
$$(1) \ \mathbf{m} \angle T'A'P' = \frac{1}{2}(\mathbf{m} \angle TAP)$$

$$(2) \ \mathbf{m} \angle T'A'P' = 2(\mathbf{m} \angle TAP)$$

(4) $TA = \frac{1}{2}(T'A')$ 5(ale factor of 2

Use this space for computations.

24 In the diagram below of $\triangle ABC$, X and Y are points on \overline{AB} and \overline{AC} , respectively, such that $m \angle AYX = m \angle B$.



Which statement is not always true?

$$(1) \ \frac{AX}{AC} = \frac{XY}{CB}$$

$$(3) (AY)(CB) = (XY)(AB)$$

$$(2) \ \frac{AY}{AB} = \frac{AX}{AC}$$

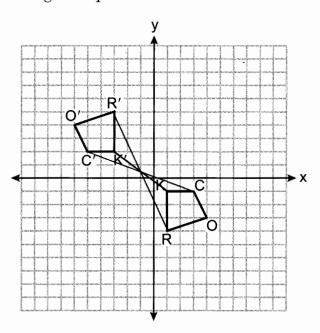
$$(4)(AY)(AB) = (AC)(AX)$$

$$(4)(AY)(AB) = (AC)(AX)$$

$$\triangle BA \subset \sim \triangle YAX$$

Answer all 7 questions in this part. Each correct answer will receive 2 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. Utilize the information provided for each question to determine your answer. Note that diagrams are not necessarily drawn to scale. For all questions in this part, a correct numerical answer with no work shown will receive only 1 credit. All answers should be written in pen, except for graphs and drawings, which should be done in pencil. [14]

25 On the set of axes below, congruent quadrilaterals ROCK and R'O'C'K' are graphed.



Describe a sequence of transformations that would map quadrilateral ROCK onto quadrilateral R'O'C'K'.

Notate 180° about (-1, 1)

26 In triangle *CEM*, CE = 3x + 10, ME = 5x - 14, and CM = 2x - 6.

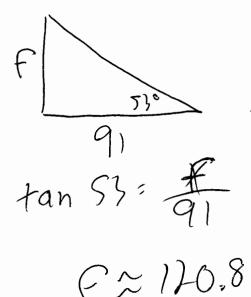
Determine and state the value of x that would make $\triangle CEM$ an isosceles triangle with the vertex angle at E.

$$5x-14.3x+10$$

 $2x-24$
 $x=12$

27 A flagpole casts a shadow on the ground 91 feet long, with a 53° angle of elevation from the end of the shadow to the top of the flagpole.

Determine and state, to the nearest tenth of a foot, the height of the flagpole.

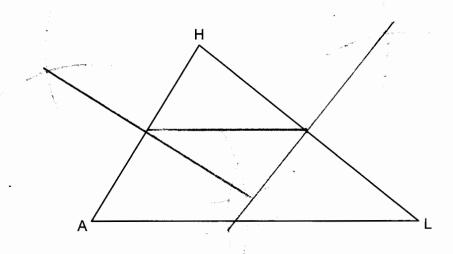


28 A man is spray-painting the tops of 10 patio tables. Five tables have round tops, with diameters of 4 feet, and five tables have rectangular tops, with dimensions of 4 feet by 6 feet. A can of spray paint covers 25 square feet. How many cans of spray paint must be purchased to paint all of the tabletops?

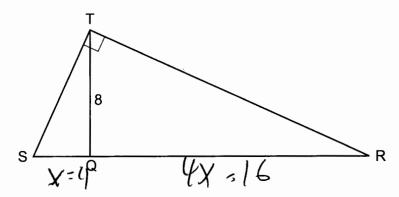
 $\frac{5(\pi)(2)^2+5(6)(4)}{25} \approx 7.3$

8 cans

29 Using a compass and straightedge, construct a midsegment of $\triangle AHL$ below. [Leave all construction marks.]



30 Right triangle STR is shown below, with $m \angle T = 90^{\circ}$. Altitude \overline{TQ} is drawn to \overline{SQR} , and TQ = 8.



If the ratio SQ:QR is 1:4, determine and state the length of \overline{SR} .

31 Line AB is dilated by a scale factor of 2 centered at point A.



Evan thinks that the dilation of \overrightarrow{AB} will result in a line parallel to \overrightarrow{AB} , not passing through points A or B.

Nathan thinks that the dilation of \overrightarrow{AB} will result in the same line, \overrightarrow{AB} .

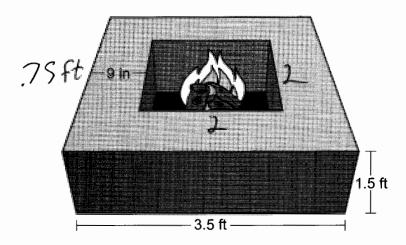
Who is correct? Nathan

Explain why.

on the like results in the same

Answer all 3 questions in this part. Each correct answer will receive 4 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. Utilize the information provided for each question to determine your answer. Note that diagrams are not necessarily drawn to scale. For all questions in this part, a correct numerical answer with no work shown will receive only 1 credit. All answers should be written in pen, except for graphs and drawings, which should be done in pencil. [12]

32 Josh is making a square-based fire pit out of concrete for his backyard, as modeled by the right prism below. He plans to make the outside walls of the fire pit 3.5 feet on each side with a height of 1.5 feet. The concrete walls of the fire pit are going to be 9 inches thick.

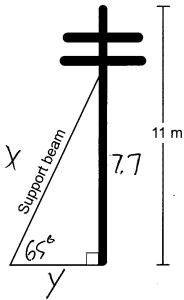


If a bag of concrete mix will fill 0.6 ft^3 , determine and state the minimum number of bags needed to build the fire pit.

 $(3.5)^2 \cdot 1.5 - 2^2 \cdot 1.5 \approx 20.6$

21 bags

33 A telephone pole 11 meters tall needs to be stabilized with a support beam, as modeled below.



Two conditions for proper support are:

- The beam reaches the telephone pole at 70% of the telephone pole's height above the ground.
- The beam forms a 65° angle with the ground.

Determine and state, to the *nearest tenth of a meter*, the length of the support beam that meets these conditions for this telephone pole.

Determine and state, to the *nearest tenth of a meter*, how far the support beam must be placed from the base of the pole to meet the conditions.

34 The coordinates of the vertices of quadrilateral ABCD are A(0,4), B(3,8), C(8,3), and D(5,-1).

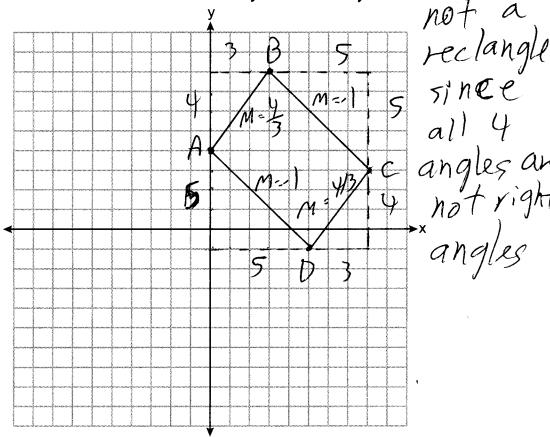
Prove that *ABCD* is a parallelogram, but *not* a rectangle.

[The use of the set of axes below is optional.]

AD & BC have equal slope, so are II

AB & CD have equal slope, so are II

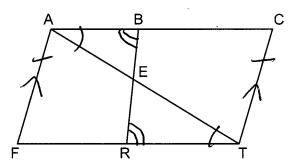
Since both pairs of opposite sides are II, ABCD is a parallelogram the slopes of AB & BC are not opposite reciprocals, so the are not perpendicular, so LB is not a right angle. ABCD is



Part IV

Answer the question in this part. A correct answer will receive 6 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. Utilize the information provided to determine your answer. Note that diagrams are not necessarily drawn to scale. A correct numerical answer with no work shown will receive only 1 credit. All answers should be written in pen, except for graphs and drawings, which should be done in pencil. [6]

35 In the diagram below of quadrilateral FACT, \overline{BR} intersects diagonal \overline{AT} at E, $AF \mid\mid CT$, and $AF \cong CT$.



Prove: $(\overrightarrow{AB})(TE) = (AE)(TR)$

Guad FACT, BR intersection Given

DABE ~ DTHE

AB = TR

(AB) (TE) = (AE) (TA)

AT at E, AF IICT, AF = CD

A quad with one pair of

FACT is a parallelogram Dopposite sides 11 d = is a

parallelogram

AC 11 FT

BOPPOSITE sides Of a

parallelogram are 11

CABE = LATE

LABE = LATE

LABE = LATE

Transversal form alternate

interior angles that are =

Interior angles that are =

E) Corresponding sites of similar triangles are proportional of the means so product of the extremes

Work space for question 35 is continued on the next page.