Print your name and the name of your school in the boxes above. Then turn to the last page of this booklet, which is the answer sheet for Part I. Fold the last page along the perforations and, slowly and carefully, tear off the answer sheet. Then fill in the heading of your answer sheet.

Scrap paper is not permitted for any part of this examination, but you may use the blank spaces in this booklet as scrap paper. A perforated sheet of scrap graph paper is provided at the end of this booklet for any question for which graphing may be helpful but is not required. You may remove this sheet from this booklet. Any work done on this sheet of scrap graph paper will not be scored. All work should be written in pen, except graphs and drawings, which should be done in pencil.

This examination has four parts, with a total of 39 questions. You must answer all questions in this examination. Write your answers to the Part I multiple-choice questions on the separate answer sheet. Write your answers to the questions in Parts II, III, and IV directly in this booklet. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc.

When you have completed the examination, you must sign the statement printed at the end of the answer sheet, indicating that you had no unlawful knowledge of the questions or answers prior to the examination and that you have neither given nor received assistance in answering any of the questions during the examination. Your answer sheet cannot be accepted if you fail to sign this declaration.

Notice . . .

A minimum of a scientific calculator, a straightedge (ruler), and a compass must be available for you to use while taking this examination.

The use of any communications device is strictly prohibited when taking this examination. If you use any communications device, no matter how briefly, your examination will be invalidated and no score will be calculated for you.

DO NOT OPEN THIS EXAMINATION BOOKLET UNTIL THE SIGNAL IS GIVEN.
Part I

Answer all questions in this part. Each correct answer will receive 2 credits. No partial credit will be allowed. For each question, write on the separate answer sheet the numeral preceding the word or expression that best completes the statement or answers the question. [60]

1 Segment RS is parallel to segment TU. If the slope of RS = 5/8 and the slope of TU = x/24, the value of x is

- (1) 20
- (2) 15
- (3) 10
- (4) 5

Use this space for computations.

\[ \frac{5}{8} = \frac{x}{24} \]

Cross Multiply \[ 5(24) = 8(x) \]

\[ 120 = 8x \]

\[ \frac{120}{8} = x \]

\[ 15 = x \]

2 Which type of figure is shown in the accompanying diagram?

- (1) hexagon - 6 sides
- (2) octagon - 8 sides
- (3) pentagon - 5 sides
- (4) quadrilateral - 4 sides

3 At an all-county music competition, 150 students participated. If 90 students sang in the chorus and 90 played in the band, how many students both sang in the chorus and played in the band?

- (1) 0
- (2) 30
- (3) 60
- (4) 240

4 What is the value of w in the equation 0.04w + 0.6 = 2.4?

- (1) 0.045
- (2) 0.45
- (3) 4.5
- (4) 45

Check

\[ 0.04(45) + 0.6 = 2.4 \]

\[ 1.8 + 0.6 = 2.4 \]

\[ 2.4 = 2.4 \checkmark \]

\[ w = 45 \]
5 What is the sum of $x^2 - 3x + 7$ and $3x^2 + 5x - 9$?

- (1) $4x^2 - 8x + 2$
- (2) $4x^2 + 2x + 16$
- (3) $4x^2 - 2x - 2$
- (4) $4x^2 + 2x - 2$

\[
\begin{array}{c|ccc}
 & x^2 & 3x & 7 \\
\hline
3x^2 & +5x & -9 \\
4x^2 & +2x & -2 \\
\hline
\end{array}
\]

- \text{Use this space for computations.}

6 If $2n + 1$ represents an odd integer, the next larger odd integer is represented by

- (1) $2n + 3$
- (2) $2n + 2$
- (3) $2n$
- (4) $2n - 1$

\[
\begin{align*}
2n + 1 &= 1 \text{ odd} \\
2n + 2 &= 2 \text{ even} \\
2n + 3 &= 3 \text{ odd}
\end{align*}
\]

7 What is the value of the expression $2x^3y$ when $x = -2$ and $y = 3$?

- (1) $-192$
- (2) $-108$
- (3) $-48$
- (4) $48$

\[
\begin{align*}
2(-2)^3(3) &\rightarrow -16(3) \\
2(-8)(3) &\rightarrow -48
\end{align*}
\]

8 Expressed in scientific notation, the number 4,600,000,000 is

- (1) $4.6 \times 10^{-8}$
- (2) $4.6 \times 10^{-9}$
- (3) $4.6 \times 10^9$
- (4) $0.46 \times 10^{10}$

\[
4,600,000,000 = 4.6 \times 10^9
\]

9 At a department store, there are six ways to enter the building, six ways to get from the first floor to the second floor, and four ways to get from the second floor to the third floor. In how many different ways could someone enter the building and go to the third floor?

- (1) 16
- (2) 24
- (3) 120
- (4) 144

\[
\begin{array}{ccc}
\text{Entry Choices} & \text{1st to 2nd Floor Choices} & \text{2nd to 3rd Floor Choices} \\
6 & 6 & 4
\end{array}
\]

\[
6 \times 6 \times 4 = 144
\]
10 What is the value of $x$ in the equation $5 - 3x = -7$?

(1) $-\frac{2}{3}$  
(2) $\frac{2}{3}$  
(3) $-4$  
(4) $4$

Use this space for computations.

$5 - 3x = -7$
$-3x = -12$
$x = 4$

11 Which expression is equivalent to $7\sqrt{90}$?

(1) $16\sqrt{10}$  
(2) $21\sqrt{10}$  
(3) $70\sqrt{9}$  
(4) $\sqrt{630}$

$7 \sqrt{90}$
$7 \sqrt{9 \cdot 10}$
$7 \cdot 3 \sqrt{10}$
$21 \sqrt{10}$

12 Which transformation is illustrated by the accompanying diagram?

(1) translation  
(2) reflection  
(3) rotation  
(4) dilation

13 If $3(x + 2) - 2(x + 1) = 8$, the value of $x$ is

(1) 1  
(2) $\frac{1}{5}$  
(3) 5  
(4) 4

Check $3(4 + 2) - 2(4 + 1) = 8$
$3(6) - 2(5) = 8$
$18 - 10 = 8$

$3x + 6 - 2x - 2 = 8$
$x + 4 = 8$
$-4$
$x = 4$

14 An expression equivalent to $3!$ is

(1) $3 \cdot 3$  
(2) $3 \cdot 2 \cdot 1$  
(3) $3 \cdot 3 \cdot 3$  
(4) $-3$

$3! = 3 \cdot 2 \cdot 1$
15 The reciprocal of 5 is

(1) $\frac{1}{5}$
(2) $\frac{1}{5}$
(3) $-\frac{1}{5}$
(4) $-5$

16 What is the converse of the statement “If $x$ is an even integer, then $(x + 1)$ is an odd integer”?

(1) $x$ is not an even integer if and only if $(x + 1)$ is not an odd integer.
(2) $x$ is an even integer if and only if $(x + 1)$ is an odd integer.
(3) If $(x + 1)$ is not an odd integer, then $x$ is not an even integer.
(4) If $(x + 1)$ is an odd integer, then $x$ is an even integer.

17 How many lines of symmetry does the accompanying figure have?

(1) an infinite number
(2) 2
(3) 8
(4) 4

18 The dimensions of a rectangle are 4 and 16. What is the smallest integral value that could be the side of a square that has an area larger than that of the rectangle?

(1) 8
(2) 9
(3) 64
(4) 81

Area = $(4)(16) = 64$

$\sqrt{x^2} > \sqrt{64}$

$x > 8$

smallest integer $> 8$
19 Angle A and angle B are complementary angles. If $m \angle A = x$, which expression represents the number of degrees in angle B?

(1) $x - 180$
(2) $180 - x$

Use this space for computations.

$\triangle ABC$ with angles A, B, and C.

20 Cassandra is calculating the measure of angle A in right triangle $ABC$, as shown in the accompanying diagram. She knows the lengths of $AB$ and $BC$.

If she finds the measure of angle A by solving only one equation, which concept will be used in her calculations?

(1) Pythagorean theorem
(2) $\sin A$
(3) $\cos A$
(4) $\tan A$

21 The probability that Jinelle's bus is on time is $\frac{2}{3}$, and the probability that Mr. Corney is driving the bus is $\frac{4}{5}$. What is the probability that on any given day Jinelle's bus is on time and Mr. Corney is the driver?

(1) $\frac{2}{15}$
(2) $\frac{8}{15}$
(3) $\frac{10}{12}$
(4) $\frac{6}{8}$

Math. A – June '08
22 What is the midpoint of the line segment that joins points (4, -2) and (-2, 5)?

(1) \(\left(\frac{3}{2}, \frac{3}{2}\right)\)  
(2) \(\left(\frac{3}{2}, -3\right)\)  
(3) \(\left(\frac{1}{2}, \frac{7}{2}\right)\)  
(4) \(\left(\frac{3}{2}, \frac{3}{2}\right)\)

midpoint = \(\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)\)

midpoint = \(\left(\frac{4 + (-2)}{2}, \frac{-2 + 5}{2}\right)\)

midpoint = \(\left(\frac{2}{2}, \frac{3}{2}\right)\)

midpoint = \(\left(1, \frac{3}{2}\right)\)

23 A conditional statement is always logically equivalent to its

(1) contrapositive  
(2) converse  
(3) conjunction  
(4) inverse

24 If \(x + y = -10\) and \(x - y = 2\), what is the value of \(x\)?

(1) -6  
(2) 6  
(3) -4  
(4) Check:

\[\begin{align*}
  x + y &= -10 \\
  x - y &= 2 \\
  -y + y &= -10 - 2 \\
  -y &= -12 \\
  y &= 12
\end{align*}\]

\[\begin{align*}
  x &= -10 - y \\
  &= -10 - 12 \\
  &= -22
\end{align*}\]

25 Point (-2, 3) is reflected in the x-axis. In which quadrant does its image lie?

(1) I  
(2) II  
(3) III  
(4) IV

The quadrants are named counterclockwise with Roman numerals.

26 The expression \((3c)^{-2}\) is equivalent to

(1) \(-6c^2\)  
(2) \(\frac{1}{3c^2}\)  
(3) \(\frac{1}{9c^2}\)  
(4) \(\frac{3}{c^2}\)

\[(3c)^{-2} = \frac{1}{(3c)^2} = \frac{1}{3c(3c)} = \frac{1}{9c^2}\]
27 Which property is illustrated by the equation \(6 + (4 + x) = 6 + (x + 4)\)?

- (1) associative property of addition
- (2) associative property of multiplication
- (3) distributive property
- (4) commutative property of addition

28 Under which operation is the set \{-1,0,1\} closed?

- (1) multiplication
- (2) division
- (3) addition
- (4) subtraction

29 The accompanying table represents the number of cell phone minutes used for one week by 23 users.

<table>
<thead>
<tr>
<th>Number of Minutes</th>
<th>Number of Users</th>
</tr>
</thead>
<tbody>
<tr>
<td>71-80</td>
<td>10</td>
</tr>
<tr>
<td>61-70</td>
<td>7</td>
</tr>
<tr>
<td>51-60</td>
<td>2</td>
</tr>
<tr>
<td>41-50</td>
<td>3</td>
</tr>
<tr>
<td>31-40</td>
<td>1</td>
</tr>
</tbody>
</table>

Which interval contains the median?

- (1) 41-50
- (2) 51-60
- (3) 61-70
- (4) 71-80

30 If the length of a side of a cube is \(7x\), which expression represents the cube’s volume?

- (1) \(7x^3\)
- (2) \(49x^3\)
- (3) \(343x\)
- (4) \(343x^3\)

\[ V = (7x)(7x)(7x) \]

\[ V = (7)(7)(7)(x)(x)(x) \]

\[ V = 343x^3 \]

\[ \text{or } V = (7x)^3 \]
31 Samuel is buying a new car. He wants either a convertible or a hatchback. Both types of cars are available in red, white, or blue and with automatic or standard transmission. Draw a tree diagram or list a sample space of all possible choices of cars that are available.
32 An 18-foot ladder leans against the wall of a building. The base of the ladder is 9 feet from the building on level ground. How many feet up the wall, to the nearest tenth of a foot, is the top of the ladder?

![Diagram of a ladder leaning against a building]

Pythagorean Theorem

\[ a^2 + b^2 = c^2 \]

\[ 9^2 + b^2 = 18^2 \]

\[ 81 + b^2 = 324 \]

\[ 81 \quad b^2 = 243 \]

\[ \sqrt{b^2} = \sqrt{243} \]

\[ b = \frac{15.58845727}{b} = 15.6 \text{ feet} \]

33 Kimberly rides her bicycle from her home to school at an average rate of 12 miles per hour. If it takes her 20 minutes to get to school, how many miles is her home from her school?

![Diagram of a bicycle ride]

12 miles per hour = \( \frac{12 \text{ miles}}{1 \text{ hour}} = \frac{12 \text{ miles}}{60 \text{ minutes}} = \frac{1 \text{ mile}}{5 \text{ minutes}} \)

\[ \frac{\text{Miles}}{\text{Minutes}} = \frac{1}{5} = \frac{x}{20} \]

Cross Multiply

\[ 5x = 20 \]

\[ x = 4 \]

Kimberly's home is 4 miles from school.
34 On the accompanying grid, draw the graph of the line whose slope is \( \frac{2}{3} \) and whose \( y \)-intercept is \(-2\).
35 Write the following numbers in order from smallest value to largest value:

\[
\sqrt{3}, \quad 1 \frac{2}{3}, \quad \frac{3}{2}, \quad 1.75, \quad 1
\]

Justify your answer.

\textbf{Step 1} Convert to decimals.

\[
\sqrt{3} \Rightarrow 1.732\ldots \quad \text{Next to largest}
\]

\[
1 \frac{2}{3} \Rightarrow 1.666 \quad \text{Next to Smallest}
\]

\[
\frac{3}{2} \Rightarrow 1.500 \quad \text{Next to Smallest}
\]

\[
1.75 \Rightarrow 1.750 \quad \text{Largest}
\]

\[
1 \Rightarrow 1.000 \quad \text{Smallest}
\]

\textbf{Step 2} Arrange from small to large.
Part III

Answer all questions in this part. Each correct answer will receive 3 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. For all questions in this part, a correct numerical answer with no work shown will receive only 1 credit.

Max is paid a salary of $225 a week plus 2.5% commission on his total weekly sales.

Write an equation for \( P \), Max's pay for one week, in terms of \( T \), his weekly total sales.

\[ P = 225 + 0.025T \]

Use this equation to determine his total pay for a week in which his total sales are $4,650.

\[ P = 225 + 0.025(4,650) \]
\[ P = 225 + 116.25 \]
\[ P = 341.25 \]

$341.25
37 Express in simplest form: \[ \frac{x^2 - 5x - 24}{x^2 - 8x} \]

\[ \frac{x^2 - 5x - 24}{x^2 - 8x} = \frac{(x + 3)(x - 8)}{x(x - 8)} \]

Answer: \[ \frac{x + 3}{x} \]
Part IV

Answer all questions in this part. Each correct answer will receive 4 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. For all questions in this part, a correct numerical answer with no work shown will receive only 1 credit. [8]

38 In the accompanying diagram, isosceles $\triangle ABC \cong$ isosceles $\triangle DEF$, $\angle C = 5x$, and $\angle D = 2x + 18$. Find $\angle B$ and $\angle BAG$.

\[ m \angle C = m \angle D \]
\[ 5x = 2x + 18 \]
\[ -2x \quad -2x \]
\[ \frac{3x}{x} = 18 \]
\[ x = 6 \]

Check:
\[ 5x = 2(x) + 18 \]
\[ 5(6) = 2(6) + 18 \]
\[ 30 = 12 + 18 \]
\[ 30 = 30 \checkmark \]
39 Solve the following system of equations algebraically or graphically for $x$ and $y$:

\[ y = x^2 - 4x + 3 \]
\[ y = x - 1 \]

**Graphing Solution**

- Plot the lines $y = x^2 - 4x + 3$ and $y = x - 1$.
- The point of intersection is $(1, 0)$, which is the solution.

**Algebraic Solution**

1. Set the two equations equal to each other:
   \[ x^2 - 4x + 3 = x - 1 \]
2. Simplify the equation:
   \[ x^2 - 5x + 4 = 0 \]
3. Factor the quadratic equation:
   \[ (x - 4)(x - 1) = 0 \]
4. Solve for $x$:
   \[ x = 4 \quad \text{or} \quad x = 1 \]

**Table from Graphing Calculator**

<table>
<thead>
<tr>
<th>$x$</th>
<th>$y$</th>
</tr>
</thead>
<tbody>
<tr>
<td>-1</td>
<td>8</td>
</tr>
<tr>
<td>0</td>
<td>3</td>
</tr>
<tr>
<td>1</td>
<td>0</td>
</tr>
<tr>
<td>2</td>
<td>-1</td>
</tr>
<tr>
<td>3</td>
<td>-2</td>
</tr>
<tr>
<td>4</td>
<td>3</td>
</tr>
<tr>
<td>5</td>
<td>8</td>
</tr>
</tbody>
</table>

**Factors of 4**

- $1$ and $4$ (sum to $5$)
- $2$ and $2$ (sum to $4$)

**Two Solutions**

- $x = 4$
- $y = (4) - 1 = 3$
- $(4, 3)$

- $x = 1$
- $y = (1) - 1 = 0$
- $(1, 0)$

[(Math. A - June '08)]
Part I
Answer all 30 questions in this part.

<p>| | | | | |</p>
<table>
<thead>
<tr>
<th></th>
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<td>8</td>
<td>3</td>
<td>4</td>
<td>24</td>
<td>3</td>
</tr>
</tbody>
</table>

Your answers for Parts II, III, and IV should be written in the test booklet.

The declaration below should be signed when you have completed the examination.

I do hereby affirm, at the close of this examination, that I had no unlawful knowledge of the questions or answers prior to the examination and that I have neither given nor received assistance in answering any of the questions during the examination.

Signature