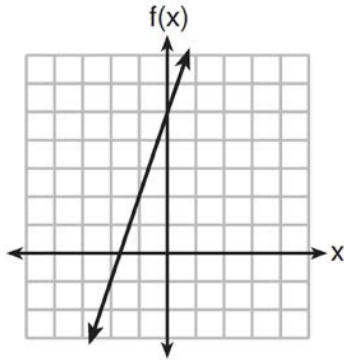


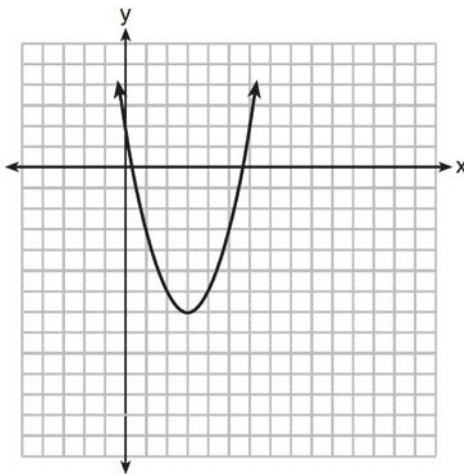
F.IF.C.9: Comparing Functions 1

- 1 Which function has the greatest y -intercept?
 - 1) $f(x) = 3x$
 - 2) $2x + 3y = 12$
 - 3) the line that has a slope of 2 and passes through $(1, -4)$



4)

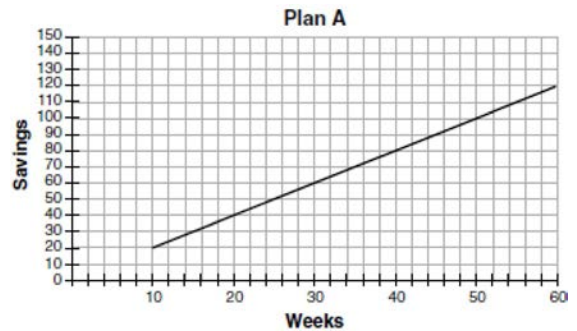
- 2 The graph representing a function is shown below.



Which function has a minimum that is *less* than the one shown in the graph?

- 1) $y = x^2 - 6x + 7$
- 2) $y = |x + 3| - 6$
- 3) $y = x^2 - 2x - 10$
- 4) $y = |x - 8| + 2$

- 3 Nancy works for a company that offers two types of savings plans. Plan *A* is represented on the graph below.

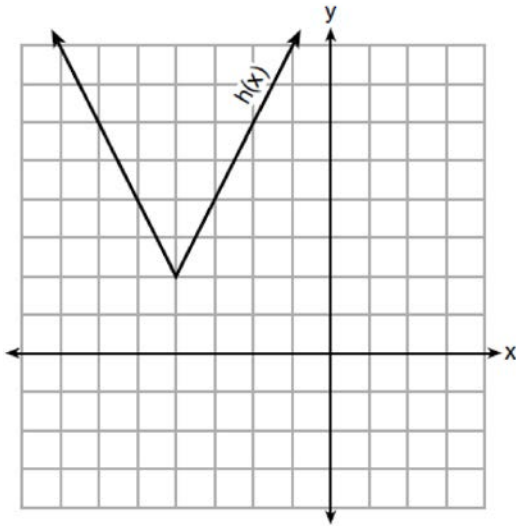


Plan *B* is represented by the function

$f(x) = 0.01 + 0.05x^2$, where x is the number of weeks. Nancy wants to have the highest savings possible after a year. Nancy picks Plan *B*. Her decision is

- 1) correct, because Plan *B* is an exponential function and will increase at a faster rate
- 2) correct, because Plan *B* is a quadratic function and will increase at a faster rate
- 3) incorrect, because Plan *A* will have a higher value after 1 year
- 4) incorrect, because Plan *B* is a quadratic function and will increase at a slower rate

- 4 The function $h(x)$, which is graphed below, and the function $g(x) = 2|x + 4| - 3$ are given.



Which statements about these functions are true?

- I. $g(x)$ has a lower minimum value than $h(x)$.
 - II. For all values of x , $h(x) < g(x)$.
 - III. For any value of x , $g(x) \neq h(x)$.
- 1) I and II, only
 - 2) I and III, only
 - 3) II and III, only
 - 4) I, II, and III

- 5 Which statement is true about the quadratic functions $g(x)$, shown in the table below, and $f(x) = (x - 3)^2 + 2$?

x	$g(x)$
0	4
1	-1
2	-4
3	-5
4	-4
5	-1
6	4

- 1) They have the same vertex.
 - 2) They have the same zeros.
 - 3) They have the same axis of symmetry.
 - 4) They intersect at two points.
- 6 Given the following quadratic functions:

$$g(x) = -x^2 - x + 6$$

and

x	-3	-2	-1	0	1	2	3	4	5
$n(x)$	-7	0	5	8	9	8	5	0	-7

Which statement about these functions is true?

- 1) Over the interval $-1 \leq x \leq 1$, the average rate of change for $n(x)$ is less than that for $g(x)$.
- 2) The y -intercept of $g(x)$ is greater than the y -intercept for $n(x)$.
- 3) The function $g(x)$ has a greater maximum value than $n(x)$.
- 4) The sum of the roots of $n(x) = 0$ is greater than the sum of the roots of $g(x) = 0$.

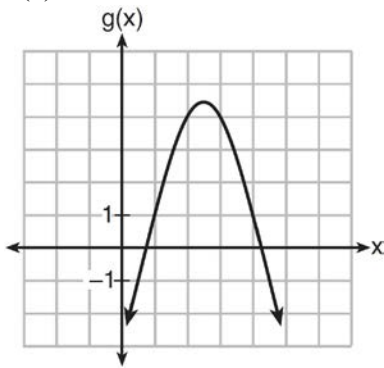
7 Which quadratic function has the largest maximum?

1) $h(x) = (3 - x)(2 + x)$

x	f(x)
-1	-3
0	5
1	9
2	9
3	5
4	-3

2)

3) $k(x) = -5x^2 - 12x + 4$



4)

8 Which quadratic function has the largest maximum over the set of real numbers?

1) $f(x) = -x^2 + 2x + 4$

x	k(x)
-1	-1
0	3
1	5
2	5
3	3
4	-1

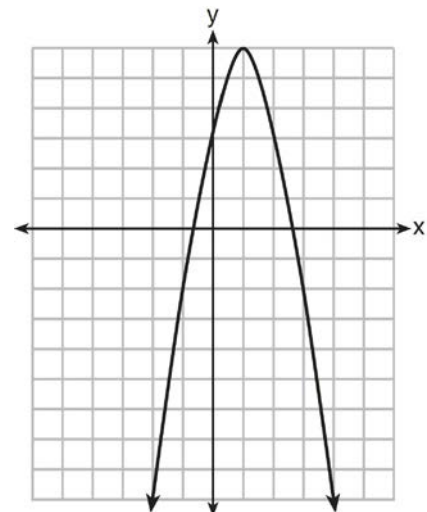
2)

3) $g(x) = -(x - 5)^2 + 5$

x	h(x)
-2	-9
-1	-3
0	1
1	3
2	3
3	1

4)

9 Let f be the function represented by the graph below.



Let g be a function such that $g(x) = -\frac{1}{2}x^2 + 4x + 3$.

Determine which function has the larger maximum value. Justify your answer.

F.IF.C.9: Comparing Functions 1

Answer Section

1 ANS: 4

1) $b = 0$; 2) $b = 4$; 3) $b = -6$; 4) $b = 5$

REF: 081611ai

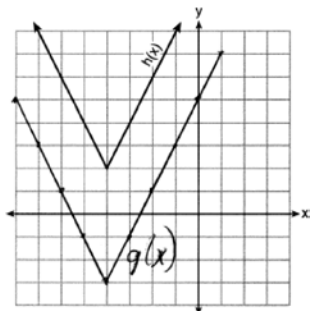
2 ANS: 3

REF: 011622ai

3 ANS: 2

REF: 011723ai

4 ANS: 2



REF: 081718ai

5 ANS: 3

 $x = 3$

REF: 061717ai

6 ANS: 4

$$1) \frac{g(1) - g(-1)}{1 - (-1)} = \frac{4 - 6}{2} = \frac{-2}{2} = -1 \quad 2) g(0) = 6 \quad 3) x = \frac{-(-1)}{2(-1)} = -\frac{1}{2}; g\left(-\frac{1}{2}\right) = -\left(-\frac{1}{2}\right)^2 + \frac{1}{2} + 6 = 6\frac{1}{4}$$

$$\frac{n(1) - n(-1)}{1 - (-1)} = \frac{9 - 5}{2} = \frac{4}{2} = 2$$

$$n(0) = 8$$

$$x = 1; n(1) = 9$$

$$4) g: S = \frac{-(-1)}{-1} = -1$$

$$n: S = -2 + 4 = 2$$

REF: 081521ai

7 ANS: 3

$$h(x) = -x^2 + x + 6 \quad \text{Maximum of } f(x) = 9 \quad k(x) = -5x^2 - 12x + 4 \quad \text{Maximum of } g(x) < 5$$

$$x = \frac{-1}{2(-1)} = \frac{1}{2}$$

$$x = \frac{12}{2(-5)} = -\frac{6}{5}$$

$$y = -\left(\frac{1}{2}\right)^2 + \frac{1}{2} + 6$$

$$y = -5\left(-\frac{6}{5}\right)^2 - 12\left(-\frac{6}{5}\right) + 4$$

$$= -\frac{1}{4} + \frac{2}{4} + 6$$

$$= -\frac{36}{5} + \frac{72}{5} + \frac{20}{5}$$

$$= 6\frac{1}{4}$$

$$= \frac{56}{5}$$

$$= 11\frac{1}{5}$$

REF: 061514ai

8 ANS: 2

$$1) x = \frac{-2}{2(-1)} = 1 \quad ; \quad 2) h = \frac{3}{2} \quad \text{Using } (0,3), 3 = a\left(0 - \frac{3}{2}\right)^2 + k; \quad \text{Using } (1,5), 5 = a\left(1 - \frac{3}{2}\right)^2 + k$$

$$y = -1^2 + 2(1) + 4 = 5$$

$$3 = \frac{9}{4}a + k$$

$$5 = \frac{1}{4}a + k$$

vertex (1,5)

$$k = 3 - \frac{9}{4}a$$

$$k = 5 - \frac{1}{4}a$$

$$5 - \frac{1}{4}a = 3 - \frac{9}{4}a \quad k = 5 - \frac{1}{4}(-1) = \frac{21}{4}; \quad 3) \text{ vertex } (5,5); \quad 4) \text{ Using } c = 1 \quad -9 = (-2)^2a + (-2)b + 1$$

$$20 - a = 12 - 9a \quad \text{vertex } \left(\frac{3}{2}, \frac{21}{4}\right)$$

$$-10 = 4a - 2b$$

$$8a = -8$$

$$b = 2a + 5$$

$$a = -1$$

$$-3 = (-1)^2a + (-1)b + 1 \quad 2a + 5 = a + 4 \quad x = \frac{-3}{2(-1)} = \frac{3}{2} \quad \text{vertex } \left(\frac{3}{2}, \frac{13}{4}\right)$$

$$-3 = a - b + 1$$

$$a = -1$$

$$b = a + 4$$

$$b = -1 + 4 = 3 \quad y = -\left(\frac{3}{2}\right)^2 + 3\left(\frac{3}{2}\right) + 1 = -\frac{9}{4} + \frac{18}{4} + \frac{4}{4} = \frac{13}{4}$$

REF: 011823ai

9 ANS:

$$g. \text{ The maximum of } f \text{ is } 6. \text{ For } g, \text{ the maximum is } 11. \quad x = \frac{-b}{2a} = \frac{-4}{2\left(-\frac{1}{2}\right)} = \frac{-4}{-1} = 4$$

$$y = -\frac{1}{2}(4)^2 + 4(4) + 3 = -8 + 16 + 3 = 11$$

REF: 081429ai