

F.LE.A.4: Exponential Growth

- A population of rabbits doubles every 60 days according to the formula $P = 10(2)^{\frac{t}{60}}$, where P is the population of rabbits on day t . What is the value of t when the population is 320?
 - 240
 - 300
 - 660
 - 960
- The growth of bacteria in a dish is modeled by the function $f(t) = 2^{\frac{t}{3}}$. For which value of t is $f(t) = 32$?
 - 8
 - 2
 - 15
 - 16
- Given a starting population of 100 bacteria, the formula $b = 100(2^t)$ can be used to find the number of bacteria, b , after t periods of time. If each period is 15 minutes long, how many minutes will it take for the population of bacteria to reach 51,200?
- Drew's parents invested \$1,500 in an account such that the value of the investment doubles every seven years. The value of the investment, V , is determined by the equation $V = 1500(2)^{\frac{t}{7}}$, where t represents the number of years since the money was deposited. How many years, to the *nearest tenth of a year*, will it take the value of the investment to reach \$1,000,000?
- Susie invests \$500 in an account that is compounded continuously at an annual interest rate of 5%, according to the formula $A = Pe^{rt}$, where A is the amount accrued, P is the principal, r is the rate of interest, and t is the time, in years. Approximately how many years will it take for Susie's money to double?
 - 1.4
 - 6.0
 - 13.9
 - 14.7
- Akeem invests \$25,000 in an account that pays 4.75% annual interest compounded continuously. Using the formula $A = Pe^{rt}$, where A = the amount in the account after t years, P = principal invested, and r = the annual interest rate, how many years, to the *nearest tenth*, will it take for Akeem's investment to triple?
 - 10.0
 - 14.6
 - 23.1
 - 24.0
- Sean invests \$10,000 at an annual rate of 5% compounded continuously, according to the formula $A = Pe^{rt}$, where A is the amount, P is the principal, $e = 2.718$, r is the rate of interest, and t is time, in years. Determine, to the *nearest dollar*, the amount of money he will have after 2 years. Determine how many years, to the *nearest year*, it will take for his initial investment to double.

- 8 In New York State, the minimum wage has grown exponentially. In 1966, the minimum wage was \$1.25 an hour and in 2015, it was \$8.75. Algebraically determine the rate of growth to the *nearest percent*.
- 9 A house purchased 5 years ago for \$100,000 was just sold for \$135,000. Assuming exponential growth, approximate the annual growth rate, to the *nearest percent*.
- 10 The number of bacteria present in a Petri dish can be modeled by the function $N = 50e^{3t}$, where N is the number of bacteria present in the Petri dish after t hours. Using this model, determine, to the *nearest hundredth*, the number of hours it will take for N to reach 30,700.

- 11 After sitting out of the refrigerator for a while, a turkey at room temperature (68°F) is placed into an oven at 8 a.m., when the oven temperature is 325°F. Newton's Law of Heating explains that the temperature of the turkey will increase proportionally to the difference between the temperature of the turkey and the temperature of the oven, as given by the formula below:

$$T = T_a + (T_0 - T_a)e^{-kt}$$

T_a = the temperature surrounding the object

T_0 = the initial temperature of the object

t = the time in hours

T = the temperature of the object after t hours

k = decay constant

The turkey reaches the temperature of approximately 100° F after 2 hours. Find the value of k , to the *nearest thousandth*, and write an equation to determine the temperature of the turkey after t hours. Determine the Fahrenheit temperature of the turkey, to the *nearest degree*, at 3 p.m.

F.LE.A.4: Exponential Growth Answer Section

1 ANS: 2

$$320 = 10(2)^{\frac{t}{60}}$$

$$32 = (2)^{\frac{t}{60}}$$

$$\log 32 = \log(2)^{\frac{t}{60}}$$

$$\log 32 = \frac{t \log 2}{60}$$

$$\frac{60 \log 32}{\log 2} = t$$

$$300 = t$$

REF: 011205a2

2 ANS: 3

$$32 = 2^{\frac{t}{3}}$$

$$\log 32 = \log 2^{\frac{t}{3}} \quad 32 = 2^{\frac{t}{3}}$$

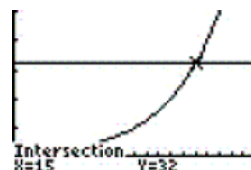
$$\log 32 = \frac{t}{3} \log 2 \quad 2^5 = 2^{\frac{t}{3}}$$

$$\frac{\log 32}{\log 2} = \frac{t}{3} \quad 5 = \frac{t}{3}$$

$$5 = \frac{t}{3} \quad t = 15$$

$$t = 15$$

Plot1 Plot2 Plot3
 $\sqrt{Y_1 = 2^{(X/3)}}$
 $\sqrt{Y_2 = 32}$
 $\sqrt{Y_3 = 3}$
 $\sqrt{Y_4 = 5}$
 $\sqrt{Y_5 = 5}$
 $\sqrt{Y_6 = 5}$
 $\sqrt{Y_7 = 5}$



REF: 080502b

3 ANS:

$$51200 = 100(2^t)$$

$$512 = 2^t$$

$$\log 512 = \log 2^t$$

$$135. \log 512 = t \log 2$$

$$t = \frac{\log 512}{\log 2} = 9$$

$$9 \times 15 = 135$$

REF: 010923b

4 ANS:

$$1000000 = 1500(2)^{\frac{t}{7}}$$

$$\frac{1000000}{1500} = 2^{\frac{t}{7}}$$

$$\log \frac{2000}{3} = \log 2^{\frac{t}{7}}$$

$$\log \frac{2000}{3} = \frac{t}{7} \log 2$$

$$\frac{7 \log \frac{2000}{3}}{\log 2} = t$$

$$t \approx 65.7$$

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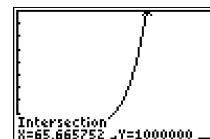
WINDOW
Xmin=0
Xmax=100
Xscl=10
Ymin=0
Ymax=1000000
Yscl=100000
Xres=1

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Plot1 Plot2 Plot3
Y1=1000000
Y2=1500(2)^(X/7)
Y3=
Y4=
Y5=
Y6=

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REF: 080729b

5 ANS: 3

$$1000 = 500e^{.05t}$$

$$2 = e^{.05t}$$

$$\ln 2 = \ln e^{.05t}$$

$$\frac{\ln 2}{.05} = \frac{.05t \cdot \ln e}{.05}$$

$$13.9 \approx t$$

REF: 061313a2

6 ANS: 3

$$75000 = 25000e^{.0475t}$$

$$3 = e^{.0475t}$$

$$\ln 3 = \ln e^{.0475t}$$

$$\frac{\ln 3}{.0475} = \frac{.0475t \cdot \ln e}{.0475}$$

$$23.1 \approx t$$

REF: 061117a2

7 ANS:

$$A = Pe^{rt}$$

$$11052, 14. \quad A = 10000(2.718)^{(0.05 \times 2)} \approx 11052$$

$$20000 = 10000(2.718)^{.05t}$$

$$2 = 2.718^{.05t}$$

$$\log 2 = \log 2.718^{.05t}$$

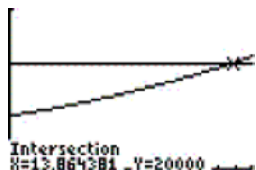
$$\log 2 = 0.05t \log 2.718$$

$$t = \frac{\log 2}{(0.05 \log 2.718)} \approx 14$$

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Plot1 Plot2 Plot3
Y1=10000*2.718^
(.05X)
Y2=20000
Y3=
Y4=
Y5=
Y6=

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REF: 060330b

8 ANS:

$$8.75 = 1.25x^{49} \quad 4$$

$$7 = x^{49}$$

$$x = \sqrt[49]{7} \approx 1.04$$

REF: 081730a

9 ANS:

$$A = Pe^{rt}$$

$$135000 = 100000e^{5r}$$

$$1.35 = e^{5r}$$

$$\ln 1.35 = \ln e^{5r}$$

$$\ln 1.35 = 5r$$

$$.06 \approx r \text{ or } 6\%$$

REF: 061632a

10 ANS:

$$30700 = 50e^{3t}$$

$$614 = e^{3t}$$

$$\ln 614 = \ln e^{3t}$$

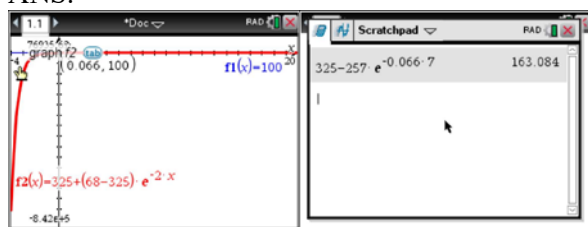
$$\ln 614 = 3t \ln e$$

$$\ln 614 = 3t$$

$$2.14 \approx t$$

REF: 011333a2

11 ANS:



$$100 = 325 + (68 - 325)e^{-2k} \quad T = 325 - 257e^{-0.066t}$$

$$-225 = -257e^{-2k} \quad T = 325 - 257e^{-0.066(7)} \approx 163$$

$$k = \frac{\ln\left(\frac{-225}{-257}\right)}{-2}$$

$$k \approx 0.066$$

REF: fall1513aii