Regents Exam Questions G.SRT.B.5: Similarity 4 www.jmap.org

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## G.SRT.B.5: Similarity 4

1 In the diagram of $\triangle C A T$ below, $\mathrm{m} \angle A=90^{\circ}$ and altitude $\overline{A E}$ is drawn from vertex $A$.


Which statement is always true?

1) $\frac{C E}{A E}=\frac{A E}{E T}$
2) $\frac{A E}{C E}=\frac{A E}{E T}$
3) $\frac{A C}{C E}=\frac{A T}{E T}$
4) $\frac{C E}{A C}=\frac{A C}{E T}$

2 In the diagram below of right triangle $A B C$, altitude $\overline{C D}$ intersects hypotenuse $\overline{A B}$ at $D$.


Which equation is always true?

1) $\frac{A D}{A C}=\frac{C D}{B C}$
2) $\frac{A D}{C D}=\frac{B D}{C D}$
3) $\frac{A C}{C D}=\frac{B C}{C D}$
4) $\frac{A D}{A C}=\frac{A C}{B D}$

3 In the accompanying diagram of right triangle $A B C$, altitude $\overline{B D}$ is drawn to hypotenuse $\overline{A C}$.


Which statement must always be true?

1) $\frac{A D}{A B}=\frac{B C}{A C}$
2) $\frac{A D}{A B}=\frac{A B}{A C}$
3) $\frac{B D}{B C}=\frac{A B}{A D}$
4) $\frac{A B}{B C}=\frac{B D}{A C}$

4 In the diagram below of right triangle $K M I$, altitude $\overline{I G}$ is drawn to hypotenuse $\overline{K M}$.


If $K G=9$ and $I G=12$, the length of $\overline{I M}$ is

1) 15
2) 16
3) 20
4) 25

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5 In the diagram below of right triangle $A B C$, altitude $\overline{B D}$ is drawn to hypotenuse $\overline{A C}$.


If $B D=4, A D=x-6$, and $C D=x$, what is the length of $\overline{C D}$ ?

1) 5
2) 2
3) 8
4) 11

6 In the diagram below of right triangle $M E T$, altitude $\overline{E S}$ is drawn to hypotenuse $\overline{M T}$.


If $M E=6$ and $S M=4$, what is $M T$ ?

1) 9
2) 8
3) 5
4) 4

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7 In the diagram below of right triangle $E F G$, altitude $\overline{F H}$ intersects hypotenuse $\overline{E G}$ at $H$.


If $F H=9$ and $E F=15$, what is $E G$ ?

1) 6.75
2) 12
3) 18.75
4) 25

8 In right triangle $R S T$ below, altitude $\overline{S V}$ is drawn to hypotenuse $\overline{R T}$.

$\underline{\text { If } R} R=4.1$ and $T V=10.2$, what is the length of $\overline{S T}$, to the nearest tenth?

1) 6.5
2) 7.7
3) 11.0
4) 12.1

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9 In the diagram below of $\triangle A B C, \angle A B C$ is a right angle, $A C=12, A D=8$, and altitude $\overline{B D}$ is drawn.


What is the length of $\overline{B C}$ ?

1) $4 \sqrt{2}$
2) $4 \sqrt{3}$
3) $4 \sqrt{5}$
4) $4 \sqrt{6}$

10 In the diagram below of right triangle $M D L$, altitude $\overline{D G}$ is drawn to hypotenuse $\overline{M L}$.


If $M G=3$ and $G L=24$, what is the length of $\overline{D G}$ ?

1) 8
2) 9
3) $\sqrt{63}$
4) $\sqrt{72}$

11 Line segment $C D$ is the altitude drawn to hypotenuse $\overline{E F}$ in right triangle $E C F$. If $E C=10$ and $E F=24$, then, to the nearest tenth, $E D$ is

1) 4.2
2) 5.4
3) 15.5
4) 21.8

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12 In right triangle $R S T$, altitude $\overline{T V}$ is drawn to hypotenuse $\overline{R S}$. If $R V=12$ and $R T=18$, what is the length of $\overline{S V}$ ?

1) $6 \sqrt{5}$
2) 15
3) $6 \sqrt{6}$
4) 27

13 Kirstie is testing values that would make triangle $K L M$ a right triangle when $\overline{L N}$ is an altitude, and $K M=16$, as shown below.


Which lengths would make triangle $K L M$ a right triangle?

1) $L M=13$ and $K N=6$
2) $L M=12$ and $N M=9$
3) $K L=11$ and $K N=7$
4) $L N=8$ and $N M=10$

14 In the diagram below, $\overline{C D}$ is the altitude drawn to the hypotenuse $\overline{A B}$ of right triangle $A B C$.


Which lengths would not produce an altitude that measures $6 \sqrt{2}$ ?

1) $A D=2$ and $D B=36$
2) $A D=3$ and $A B=24$
3) $A D=6$ and $D B=12$
4) $A D=8$ and $A B=17$

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15 In $\triangle R S T$ shown below, altitude $\overline{S U}$ is drawn to $\overline{R T}$ at $U$.


If $S U=h, U T=12$, and $R T=42$, which value of $h$ will make $\triangle R S T$ a right triangle with $\angle R S T$ as a right angle?

1) $6 \sqrt{3}$
2) $6 \sqrt{10}$
3) $6 \sqrt{14}$
4) $6 \sqrt{35}$

16 In the diagram of right triangle $A B C, \overline{C D}$ intersects hypotenuse $\overline{A B}$ at $D$.


If $A D=4$ and $D B=6$, which length of $\overline{A C}$ makes $\overline{C D} \perp \overline{A B}$ ?

1) $2 \sqrt{6}$
2) $2 \sqrt{10}$
3) $2 \sqrt{15}$
4) $4 \sqrt{2}$

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17 In the diagram below of right triangle $A C B$, altitude $\overline{C D}$ is drawn to hypotenuse $\overline{A B}, A D=2$ and $A C=6$.


Determine and state the length of $\overline{A B}$.

18 In the diagram below of right triangle $B A L$, altitude $\overline{A D}$ is drawn to hypotenuse $\overline{B D L}$. The length of $\overline{A D}$ is 6 .


If the length of $\overline{D L}$ is four times the length of $\overline{B D}$, determine and state the length of $\overline{B D}$.

19 Right triangle $S T R$ is shown below, with $\mathrm{m} \angle T=90^{\circ}$. Altitude $\overline{T Q}$ is drawn to $\overline{S Q R}$, and $T Q=8$.


If the ratio $S Q: Q R$ is $1: 4$, determine and state the length of $\overline{S R}$.

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20 In right triangle $P R T, \mathrm{~m} \angle P=90^{\circ}$, altitude $\overline{P Q}$ is drawn to hypotenuse $\overline{R T}, R T=17$, and $P R=15$.


Determine and state, to the nearest tenth, the length of $\overline{R Q}$.

21 In right triangle $A B C$ shown below, altitude $\overline{C D}$ is drawn to hypotenuse $\overline{A B}$. Explain why $\triangle A B C \sim \triangle A C D$.


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22 In the diagram below, the line of sight from the park ranger station, $P$, to the lifeguard chair, $L$, on the beach of a lake is perpendicular to the path joining the campground, $C$, and the first aid station, $F$. The campground is 0.25 mile from the lifeguard chair. The straight paths from both the campground and first aid station to the park ranger station are perpendicular.


If the path from the park ranger station to the campground is 0.55 mile, determine and state, to the nearest hundredth of a mile, the distance between the park ranger station and the lifeguard chair. Gerald believes the distance from the first aid station to the campground is at least 1.5 miles. Is Gerald correct? Justify your answer.

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Answer Section
1 ANS: $1 \quad$ REF: 012418geo
2 ANS: $1 \quad$ REF: 081916geo
3 ANS: 2
$\overline{A B}=10$ since $\triangle A B C$ is a 6-8-10 triangle. $6^{2}=10 x$

$$
3.6=x
$$

REF: 081820geo
4 ANS: 3
$12^{2}=9 \cdot G M \quad I M^{2}=16 \cdot 25$
$G M=16 \quad I M=20$
REF: 011910geo
5 ANS: 3

$$
\begin{aligned}
x(x-6) & =4^{2} \\
x^{2}-6 x-16 & =0 \\
(x-8)(x+2) & =0 \\
x & =8
\end{aligned}
$$

REF: 081807geo
6 ANS: 1
$6^{2}=4 x$
$x=9$
REF: 012412geo
7 ANS: 3

$$
\begin{aligned}
12 x & =9^{2} \quad 6.75+12=18.75 \\
12 x & =81 \\
x & =\frac{82}{12}=\frac{27}{4}
\end{aligned}
$$

REF: 062213geo
8 ANS: 4
$x^{2}=10.2 \times 14.3$
$x \approx 12.1$
REF: 012016geo

9 ANS: 2
$x^{2}=12(12-8)$
$x^{2}=48$
$x=4 \sqrt{3}$
REF: 011823geo
10 ANS: 4
$x^{2}=3 \times 24$
$x=\sqrt{72}$
REF: 012315geo
11 ANS: 1

$$
24 x=10^{2}
$$

$$
24 x=100
$$

$$
x \approx 4.2
$$

REF: 061823geo
12 ANS: 2
$18^{2}=12(x+12)$
$324=12(x+12)$
$27=x+12$
$x=15$
REF: 081920geo
13 ANS: 2
$12^{2}=9 \cdot 16$
$144=144$
REF: 081718geo
14 ANS: 2
$\sqrt{3 \cdot 21}=\sqrt{63}=3 \sqrt{7}$
REF: 011622geo
15 ANS: 2
$h^{2}=30 \cdot 12$
$h^{2}=360$
$h=6 \sqrt{10}$
REF: 061613geo

16 ANS: 2
$x^{2}=4 \cdot 10$
$x=\sqrt{40}$
$x=2 \sqrt{10}$
REF: 081610geo
17 ANS:
$6^{2}=2(x+2) ; 16+2=18$
$36=2 x+4$
$32=2 x$
$16=x$
REF: 062330geo
18 ANS:
$4 x \cdot x=6^{2}$

$$
4 x^{2}=36
$$

$$
x^{2}=9
$$

$$
x=3
$$

REF: 082229geo
19 ANS:
$4 x \cdot x=8^{2} 4+4(4)=20$

$$
\begin{aligned}
4 x^{2} & =64 \\
x^{2} & =16 \\
x & =4
\end{aligned}
$$

REF: 082330geo
20 ANS:
$17 x=15^{2}$
$17 x=225$

$$
x \approx 13.2
$$

REF: 061930geo
21 ANS:
If an altitude is drawn to the hypotenuse of a triangle, it divides the triangle into two right triangles similar to each other and the original triangle.

REF: 061729geo

## 22 ANS:

$$
\begin{gathered}
x=\sqrt{.55^{2}-.25^{2}} \cong 0.49 \mathrm{No}, .49^{2}=.25 y .9604+.25<1.5 \\
.9604=y
\end{gathered}
$$

REF: 061534geo

