

G.G.43 Investigate, justify, and apply theorems about the centroid of a triangle, dividing each median into segments whose lengths are in the ratio 2:1

1. The vertices of a triangle ABC are A(4,5), B(6,1), and C(8,9). Determine the coordinates of the *centroid* of triangle ABC and investigate the lengths of the segments of the medians. Make a conjecture.

2. Using dynamic geometry software, construct the following figure in which point C is the *centroid* of $\triangle PQR$. Show that point P' is the image of point C under a dilation centered at point P with ratio $\frac{3}{2}$ (i.e. $D_{P, \frac{3}{2}}(C) = P'$). Justify mathematically that $\frac{3}{2}$ is the correct ratio for the dilation. In similar fashion show that $D_{Q, \frac{3}{2}}(C) = Q'$ and $D_{R, \frac{3}{2}}(C) = R'$.

