

- 14 Jack started a new fitness program. The first day he did 10 push-ups. The program required him to increase the number of push-ups each day by doing 9 less than twice the number from the previous day. Which recursive formula correctly models Jack's new program, where n is the number of days and a_n is the number of push-ups on the n th day?
- 1) $a_1 = 10$
 $a_n = 2a_{n-1} - 9$
- 2) $a_1 = 10$
 $a_n = 9 - 2a_{n-1}$
- 3) $a_1 = 10$
 $a_n = 2(n - 1) - 9$
- 4) $a_1 = 10$
 $a_n = 9 - 2(n - 1)$
- 15 A father makes a deal with his son regarding his weekly allowance. The first year, he agrees to pay his son a weekly allowance of \$10. Every subsequent year, the allowance is recalculated by doubling the previous year's weekly allowance and then subtracting 8. Which recursive formula could be used to calculate the son's weekly allowance in future years?
- 1) $a_n = 2n - 8$
- 2) $a_n = 2(n + 1) - 8$
- 3) $a_1 = 10$
 $a_{n+1} = 2a_n - 8$
- 4) $a_1 = 10$
 $a_{n+1} = 2(a_n - 8)$
- 16 The average depreciation rate of a new boat is approximately 8% per year. If a new boat is purchased at a price of \$75,000, which model is a recursive formula representing the value of the boat n years after it was purchased?
- 1) $a_n = 75,000(0.08)^n$
- 2) $a_0 = 75,000$
 $a_n = (0.92)^n$
- 3) $a_n = 75,000(1.08)^n$
- 4) $a_0 = 75,000$
 $a_n = 0.92(a_{n-1})$
- 17 After Roger's surgery, his doctor administered pain medication in the following amounts in milligrams over four days.

Day (n)	1	2	3	4
Dosage (m)	2000	1680	1411.2	1185.4

How can this sequence best be modeled recursively?

- 1) $m_1 = 2000$
 $m_n = m_{n-1} - 320$
- 2) $m_n = 2000(0.84)^{n-1}$
- 3) $m_1 = 2000$
 $m_n = (0.84)m_{n-1}$
- 4) $m_n = 2000(0.84)^{n+1}$
- 18 A tree farm initially has 150 trees. Each year, 20% of the trees are cut down and 80 seedlings are planted. Which recursive formula models the number of trees, a_n , after n years?
- 1) $a_1 = 150$
 $a_n = a_{n-1}(0.2) + 80$
- 2) $a_1 = 150$
 $a_n = a_{n-1}(0.8) + 80$
- 3) $a_n = 150(0.2)^n + 80$
- 4) $a_n = 150(0.8)^n + 80$

- 27 The population, in millions of people, of the United States can be represented by the recursive formula below, where a_0 represents the population in 1910 and n represents the number of years since 1910.

$$a_0 = 92.2$$

$$a_n = 1.015a_{n-1}$$

Identify the percentage of the annual rate of growth from the equation $a_n = 1.015a_{n-1}$. Write an exponential function, P , where $P(t)$ represents the United States population in millions of people, and t is the number of years since 1910. According to this model, determine algebraically the number of years it takes for the population of the United States to be approximately 300 million people. Round your answer to the *nearest year*.

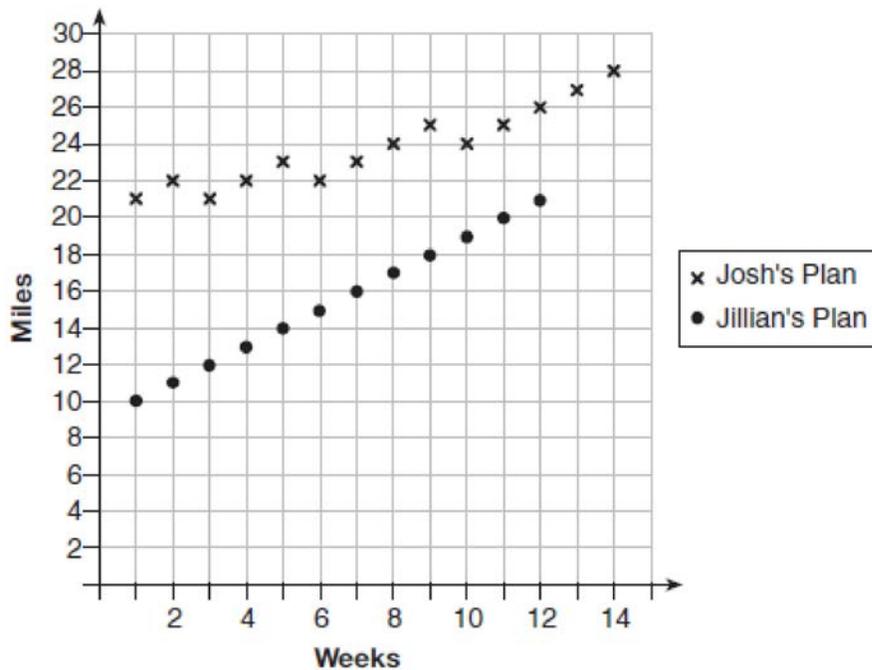
- 28 Write an explicit formula for a_n , the n th term of the recursively defined sequence below.

$$a_1 = x + 1$$

$$a_n = x(a_{n-1})$$

For what values of x would $a_n = 0$ when $n > 1$?

- 29 Elaina has decided to run the Buffalo half-marathon in May. She researched training plans on the Internet and is looking at two possible plans: Jillian’s 12-week plan and Josh’s 14-week plan. The number of miles run per week for each plan is plotted below.



Which one of the plans follows an arithmetic pattern? Explain how you arrived at your answer. Write a recursive definition to represent the number of miles run each week for the duration of the plan you chose. Jillian’s plan has an alternative if Elaina wanted to train instead for a full 26-mile marathon. Week one would start at 13 miles and follow the same pattern for the half-marathon, but it would continue for 14 weeks. Write an explicit formula, in *simplest form*, to represent the number of miles run each week for the full-marathon training plan.

F.BF.A.2: Sequences 2

Answer Section

1 ANS: 2
 $d = -4$

REF: 012321ai

2 ANS: 3 REF: 061522ai
 3 ANS: 1 REF: 011708ai
 4 ANS: 3 REF: 011824aii
 5 ANS: 4
 $a_1 = 2.5 + 0.5(1) = 3$

REF: 011916aii

6 ANS: 3 REF: 081618aii
 7 ANS: 2 REF: 011919ai
 8 ANS: 1
 (2) is not recursive

REF: 081608aii

9 ANS: 4
 (1) and (3) are not recursive

REF: 012013aii

10 ANS: 4
 1) is a correct formula, but not recursive

REF: 082216aii

11 ANS: 4 REF: 062412aii
 12 ANS: 3 REF: 061623aii
 13 ANS: 4 REF: 081624aii
 14 ANS: 1 REF: 082319ai
 15 ANS: 3 REF: 062321ai
 16 ANS: 4 REF: 081810aii
 17 ANS: 3 REF: 081909aii
 18 ANS: 2 REF: 012321aii
 19 ANS: 3 REF: 081724aii
 20 ANS: 4

The scenario represents a decreasing geometric sequence with a common ratio of 0.80.

REF: 061610aii

21 ANS:
 $a_1 = 4$
 $a_n = 3a_{n-1}$

REF: 081931aii

22 ANS:

$$\frac{9}{6} = 1.5 \quad a_1 = 6$$

$$a_n = 1.5 \cdot a_{n-1}$$

REF: 061931aii

23 ANS:

$$\frac{20}{8} = 2.5 \quad a_1 = 8$$

$$a_n = 2.5 \cdot a_{n-1}$$

REF: 012531aii

24 ANS:

$$\frac{63}{189} = \frac{1}{3} \quad a_1 = 189$$

$$a_n = \frac{1}{3} a_{n-1}$$

REF: 062329aii

25 ANS:

$$a_1 = 4 \quad a_8 = 639$$

$$a_n = 2a_{n-1} + 1$$

REF: 081729aii

26 ANS:

$$a_1 = 12$$

$$a_n = a_{n-1} + 6$$

REF: 012430aii

27 ANS:

$$1.5\%; \quad P(t) = 92.2(1.015)^t; \quad \frac{300}{92.2} = (1.015)^t$$

$$\log \frac{300}{92.2} = t \log(1.015)$$

$$\frac{\log \frac{300}{92.2}}{\log(1.015)} = t$$

$$t \approx 79$$

REF: 062237aii

28 ANS:

$$a_n = x^{n-1}(x+1) \quad x^{n-1} = 0 \quad x+1 = 0$$
$$x = 0 \quad x = -1$$

REF: spr1511aii

29 ANS:

Jillian's plan, because distance increases by one mile each week. $a_1 = 10$ $a_n = n + 12$

$$a_n = a_{n-1} + 1$$

REF: 011734aii