The University of the State of New York

REGENTS HIGH SCHOOL EXAMINATION

GEOMETRY (Common Core)

Thursday, January 26, 2017 — 9:15 a.m. to 12:15 p.m., only

Student Name:

School Name:

The possession or use of any communications device is strictly prohibited when taking this examination. If you have or use any communications device, no matter how briefly, your examination will be invalidated and no score will be calculated for you.

Print your name and the name of your school on the lines above.

A separate answer sheet for Part I has been provided to you. Follow the instructions from the proctor for completing the student information on your answer sheet.

This examination has four parts, with a total of 36 questions. You must answer all questions in this examination. Record your answers to the Part I multiple-choice questions on the separate answer sheet. Write your answers to the questions in Parts II, III, and IV directly in this booklet. All work should be written in pen, except for graphs and drawings, which should be done in pencil. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. Utilize the information provided for each question to determine your answer. Note that diagrams are not necessarily drawn to scale.

The formulas that you may need to answer some questions in this examination are found at the end of the examination. This sheet is perforated so you may remove it from this booklet.

Scrap paper is not permitted for any part of this examination, but you may use the blank spaces in this booklet as scrap paper. A perforated sheet of scrap graph paper is provided at the end of this booklet for any question for which graphing may be helpful but is not required. You may remove this sheet from this booklet. Any work done on this sheet of scrap graph paper will *not* be scored.

When you have completed the examination, you must sign the statement printed at the end of the answer sheet, indicating that you had no unlawful knowledge of the questions or answers prior to the examination and that you have neither given nor received assistance in answering any of the questions during the examination. Your answer sheet cannot be accepted if you fail to sign this declaration.

Notice...

A graphing calculator, a straightedge (ruler), and a compass must be available for you to use while taking this examination.

DO NOT OPEN THIS EXAMINATION BOOKLET UNTIL THE SIGNAL IS GIVEN.

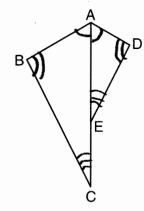
Part I

Answer all 24 questions in this part. Each correct answer will receive 2 credits. No partial credit will be allowed. Utilize the information provided for each question to determine your answer. Note that diagrams are not necessarily drawn to scale. For each statement or question, choose the word or expression that, of those given, best completes the statement or answers the question. Record your answers on your separate answer sheet. [48]

Use this space for
1 Which equation represents the line that passes through the point computations.
(-2,2) and is parallel to
$$y = (\frac{1}{2}x + 8?)$$

(1) $y = \frac{1}{2}x$
(2) $y = -2x - 3$
(4) $y = -2x + 3$
(5) $y = -2x - 3$
(4) $y = -2x + 3$
(5) $y = -2x - 3$
(4) $y = -2x + 3$
(5) $y = -2x - 3$
(5) $y = -2x - 3$
(6) $y = -2x + 3$
(7) $y = \frac{1}{2}x + 3$
(8) $y = -2x + 3$
(9) $y = -2x + 3$

2 In the diagram below, $\triangle ADE$ is the image of $\triangle ABC$ after a reflection over the line *AC* followed by a dilation of scale factor $\frac{AE}{AC}$ centered at point *A*.



Which statement must be true?

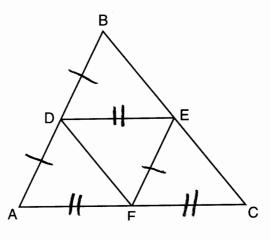
(1)
$$m \angle BAC = m \angle AED$$
 (3) $m \angle DAE = \frac{1}{2}m \angle BAC$
(2) $m \angle ABC = m \angle ADE$ (4) $m \angle ACB = \frac{1}{2}m \angle DAB$

No 3 Given $\triangle ABC \cong \triangle DEF$, which statement is *not* always true? (1) $\overline{BC} \cong \overline{DF}$ (2) $m \angle A = m \angle D$ (3) area of $\triangle ABC =$ area of $\triangle DEF$

(4) perimeter of $\triangle ABC$ = perimeter of $\triangle DEF$

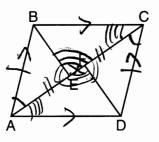
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4 In the diagram below, \overline{DE} , \overline{DF} , and \overline{EF} are midsegments of $\triangle ABC$.



The perimeter of quadrilateral *ADEF* is equivalent to

- (1) AB + BC + AC (3) 2AB + 2AC(2) $\frac{1}{2}AB + \frac{1}{2}AC$ (4) AB + AC
- **5** In the diagram below, if $\triangle ABE \cong \triangle CDF$ and \overline{AEFC} is drawn, then it could be proven that quadrilateral *ABCD* is a



- (1) square
- (2) rhombus

(3) rectangle(4) parallelogram

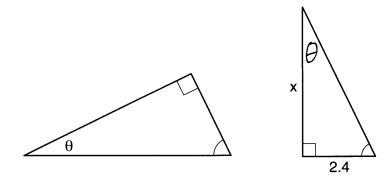
- **6** Under which transformation would $\triangle A'B'C'$, the image of $\triangle ABC$, *not* be congruent to $\triangle ABC$?
 - (1) reflection over the y-axis
 - $(2)\;$ rotation of 90^{o} clockwise about the origin
 - (3) translation of 3 units right and 2 units down
 - (4) dilation with a scale factor of 2 centered at the origin

2 rigid motions 5 preserve distance

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7 The diagram below shows two similar triangles.

Use this space for computations.

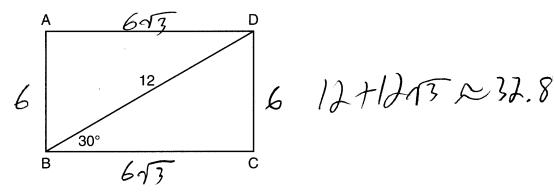


If $\tan \theta = \frac{3}{7}$, what is the value of *x*, to the *nearest tenth*? (1) 1.2(3) 7.6 (2))5.6(4) 8.8

 $fan \Theta = \frac{2.4}{\chi}$ 3 - 2.4 7 - 2.4 BX - 16.8 3 3 X:56

8 A farmer has 64 feet of fence to enclose a rectangular vegetable garden. Which dimensions would result in the biggest area for this garden?

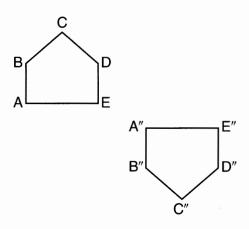
- (1) the length and the width are equal 64/4, 16(2) the length is 2 more than the width 2w + 2(w+2), 64 w, 15(3) the length is 4 more than the width 2w + 2(w+4), 64 w, 14(4) the length is 6 more than the width 2w + 2(w+6), 64 w, $13 \cdot 19$, 247
- **9** The diagram shows rectangle ABCD, with diagonal \overline{BD} .



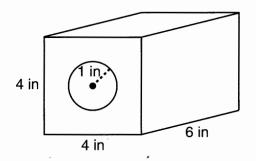
What is the perimeter of rectangle ABCD, to the nearest tenth?

(1) 28.4	(3) 48.0
(1) 28.4 (2) 32.8	(4) 62.4

10 Identify which sequence of transformations could map pentagon *ABCDE* onto pentagon *A"B"C"D"E"*, as shown below.



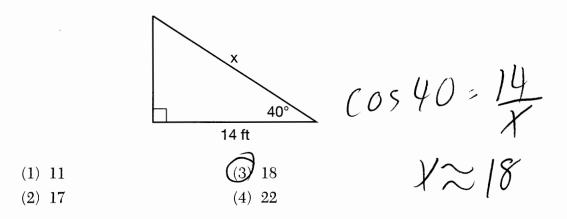
- (1) dilation followed by a rotation
- (2) translation followed by a rotation
- (3) line reflection followed by a translation
- (4) line reflection followed by a line reflection
- 11 A solid metal prism has a rectangular base with sides of 4 inches and 6 inches, and a height of 4 inches. A hole in the shape of a cylinder, with a radius of 1 inch, is drilled through the entire length of the rectangular prism.



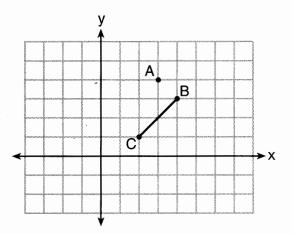
What is the approximate volume of the remaining solid, in cubic inches?

$$\overset{(1)}{(2)} \overset{(3)}{(2)} \overset{(3)}{(77)} \overset{(3)}{(4)} \overset{$$

12 Given the right triangle in the diagram below, what is the value of *x*, to the *nearest foot*?



13 On the graph below, point A(3,4) and \overline{BC} with coordinates B(4,3) and C(2,1) are graphed.



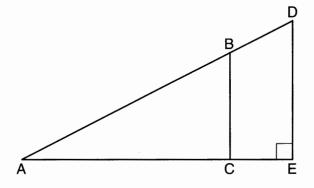
What are the coordinates of B' and C' after \overline{BC} undergoes a dilation centered at point A with a scale factor of 2?

(1) B'(5,2) and C'(1,-2) (3) B'(5,0) and C'(1,-2)(2) B'(6,1) and C'(0,-1) (4) B'(5,2) and C'(3,0)

$$\begin{array}{l} \mathsf{B}: & (4-3, 3-4) \rightarrow (1, -1) \rightarrow (2, -2) \rightarrow (2+3, -2+4) \\ \mathsf{C}: & (2-3, 1-4) \rightarrow (-1, -3) \rightarrow (-2, -6) \rightarrow (-2+3, -6+4) \end{array}$$

Use this space for computations.

14 In the diagram of right triangle ADE below, $\overline{BC} \parallel \overline{DE}$.



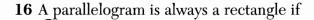
Which ratio is always equivalent to the sine of $\angle A$?



(9)	AE	(4)	$\frac{AB}{AC}$
(ム)	$\frac{AE}{AD}$	(4)	\overline{AC}

- **15** In circle O, secants \overline{ADB} and \overline{AEC} are drawn from external point A such that points D, B, E, and C are on circle O. If AD = 8, AE = 6, and EC is 12 more than BD, the length of \overline{BD} is
 - (1) 6





- (1)the diagonals are congruent
- (2) the diagonals bisect each other
- (3) the diagonals intersect at right angles
- (4) the opposite angles are congruent

Х 6 6 $\delta(x+8)$ 5 82764 = 6x+108 2x = 44 x -, 22

D

Х

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17 Which rotation about its center will carry a regular decagon onto itself?

Use this space for computations.

(1)
$$54^{\circ}$$

(2) 162°
(3) 198°
(4) 252°
(4) 252°
(4) 252°
(3) 760° , 360° ,

19 Parallelogram *ABCD* has coordinates A(0,7) and C(2,1). Which statement would prove that *ABCD* is a rhombus?

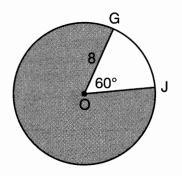
(1) The midpoint of \overline{AC} is (1,4). $\frac{7-1}{1-1}, \frac{6}{-1}, -3$ (2) The length of \overline{BD} is $\sqrt{40}$. (3) The slope of \overline{BD} is $\frac{1}{3}$. The diagonals of a rhombus are perpendicular. (4) The slope of \overline{AB} is $\frac{1}{2}$.

20 Point Q is on \overline{MN} such that MQ:QN = 2:3. If M has coordinates (3,5) and N has coordinates (8,-5), the coordinates of Q are

$$\begin{array}{c} ((1))(5,1) \\ (2)(5,0) \\ \end{array} \\ \begin{array}{c} (3)(6,-1) \\ (4)(6,0) \\ \end{array} \\ \end{array} \\ \end{array}$$

21 In the diagram below of circle O, GO = 8 and $m \angle GOJ = 60^{\circ}$.

Use this space for computations.



What is the area, in terms of π , of the shaded region?

- (3) $\frac{32\pi}{3}$ (1) $\frac{4\pi}{3}$ $\frac{300}{360}$. $TT(8)^2 = \frac{16011}{3}$ (2) $\frac{20\pi}{20\pi}$ З
- **22** A circle whose center is the origin passes through the point (-5,12). V(-5)2+122 = N169 Which point also lies on this circle? (3) (11, $2\sqrt{12})$ N112+(2012)2 "N121+48 = 1169 (1) (10,3)
 - (2) (-12,13)
- 23 A plane intersects a hexagonal prism. The plane is perpendicular to the base of the prism. Which two-dimensional figure is the cross section of the plane intersecting the prism?
 - (1) triangle

(3) hexagon rectangle

- (2) trapezoid
- 24 A water cup in the shape of a cone has a height of 4 inches and a maximum diameter of 3 inches. What is the volume of the water in the cup, to the nearest tenth of a cubic inch, when the cup is filled to half its height?

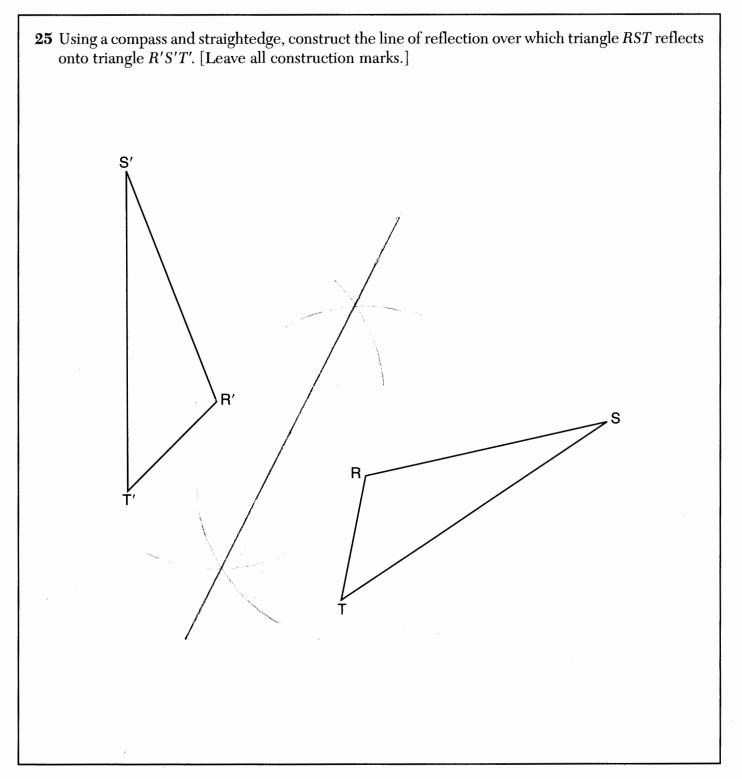
$$\begin{array}{c} (1) \\ (2) \\ (2) \\ 3.5 \end{array} (3) \\ (4) \\ (4) \\ 14.1 \\ (4) \\ 14.1 \\ (4) \\ 14.1 \\ (4) \\ 14.1 \\ (4) \\ (4) \\ 14.1 \\ (4) \\$$

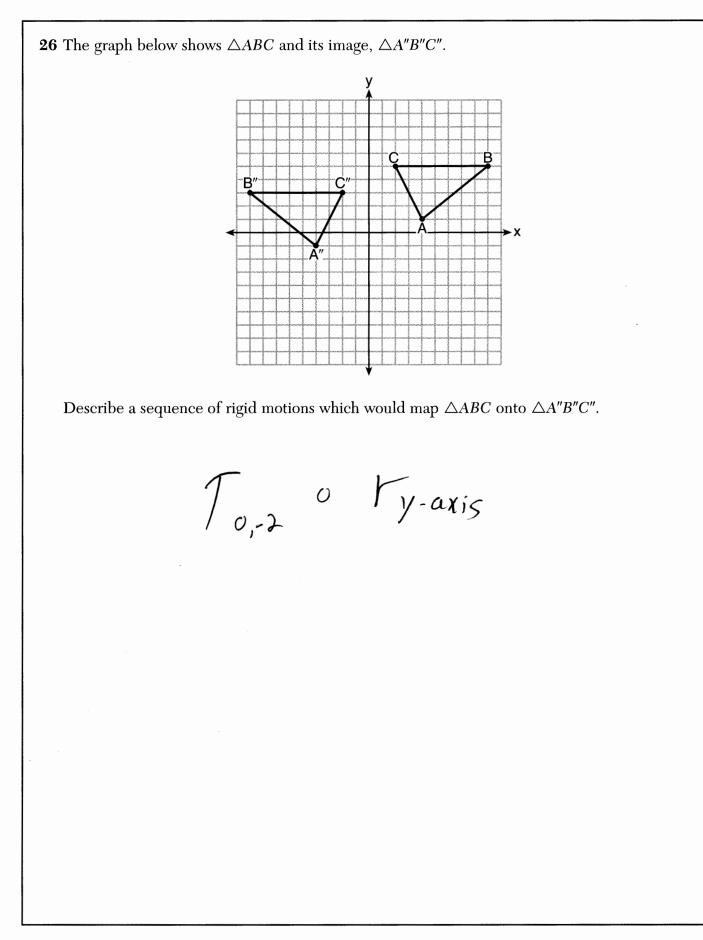
 $V = \frac{1}{2} \left(\frac{1}{2}\right)^{\prime} \left(\frac{1}{2}\right)^{\prime}$

 ≈ 1.2

Part II

Answer all 7 questions in this part. Each correct answer will receive 2 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. Utilize the information provided for each question to determine your answer. Note that diagrams are not necessarily drawn to scale. For all questions in this part, a correct numerical answer with no work shown will receive only 1 credit. All answers should be written in pen, except for graphs and drawings, which should be done in pencil. [14]

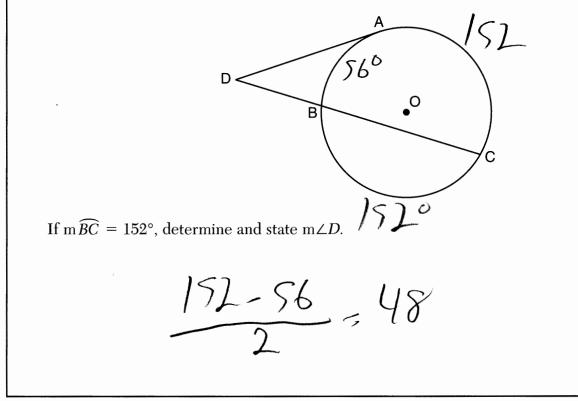




27 When instructed to find the length of \overline{HJ} in right triangle HJG, Alex wrote the equation $\sin 28^\circ = \frac{HJ}{20}$ while Marlene wrote $\cos 62^\circ = \frac{HJ}{20}$. Are both students' equations correct? Explain why.

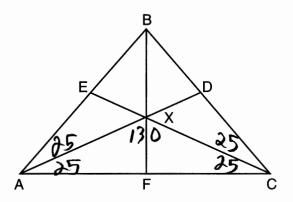
20 Yes, because 78° + 67° angles are complementary. The sine of an angle equals the osine of its complement.

28 In the diagram below, tangent \overline{DA} and secant \overline{DBC} are drawn to circle *O* from external point *D*, such that $\widehat{AC} \cong \widehat{BC}$.



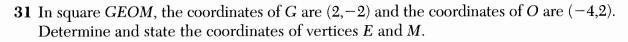
29 In the diagram below, \overline{GI} is parallel to \overline{NT} , and \overline{IN} intersects \overline{GT} at A. Prove: $\triangle GIA \sim \triangle TNA$ STAPEMENT CTILINT, IN intersects 1) Given GT at A LI=LN, LG=LT alternate interior angles))3) AA DGIA~ DTNA 3

30 In the diagram below of isosceles triangle ABC, $\overline{AB} \cong \overline{CB}$ and angle bisectors \overline{AD} , \overline{BF} , and \overline{CE} are drawn and intersect at X.

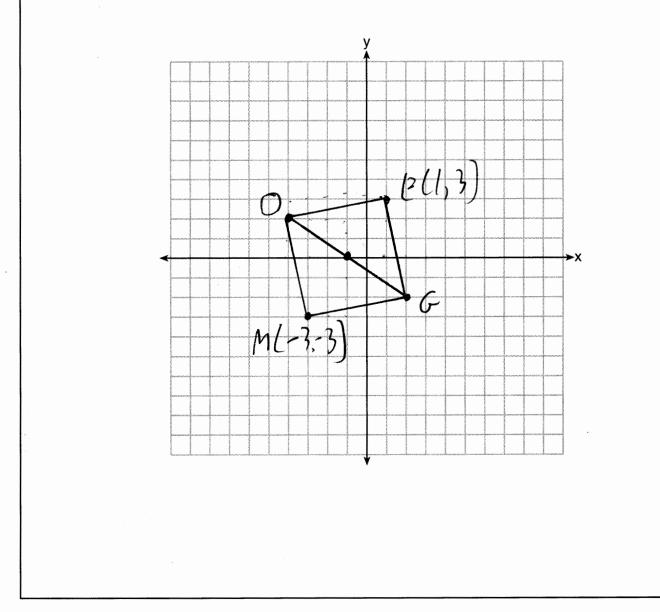


If $m \angle BAC = 50^\circ$, find $m \angle AXC$.

180 - 2(25) =130

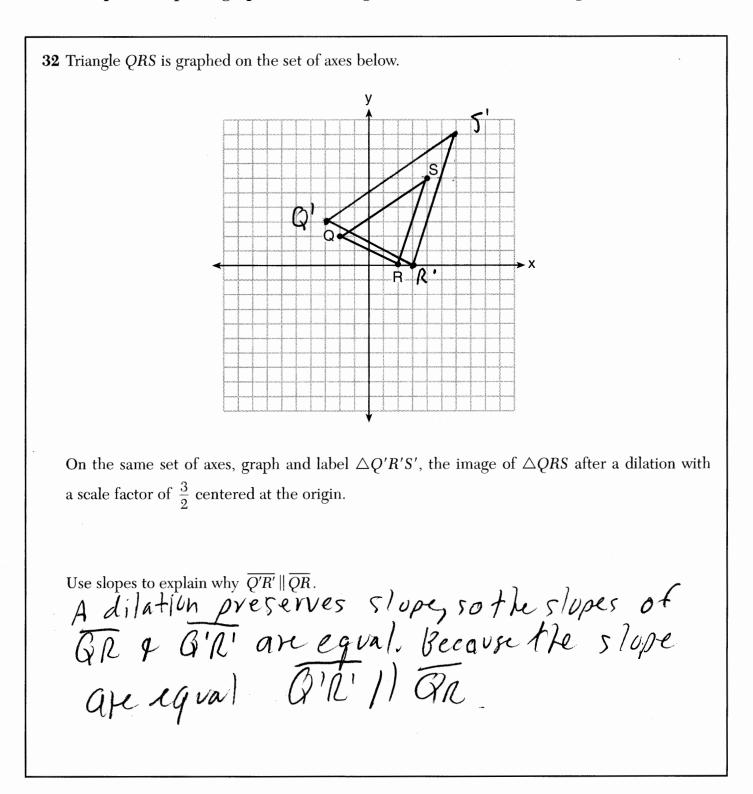


[The use of the set of axes below is optional.]



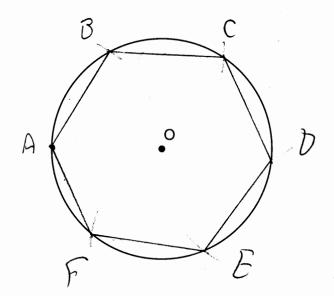
Part III

Answer all 3 questions in this part. Each correct answer will receive 4 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. Utilize the information provided for each question to determine your answer. Note that diagrams are not necessarily drawn to scale. For all questions in this part, a correct numerical answer with no work shown will receive only 1 credit. All answers should be written in pen, except for graphs and drawings, which should be done in pencil. [12]



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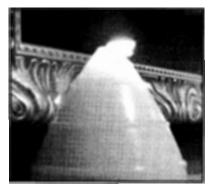
33 Using a compass and straightedge, construct a regular hexagon inscribed in circle O below. Label it *ABCDEF*. [Leave all construction marks.]



If chords \overline{FB} and \overline{FC} are drawn, which type of triangle, according to its angles, would $\triangle FBC$ be? Explain your answer.

Right triangle, because 20BF is inscribed in a semi-circle.

34 A candle maker uses a mold to make candles like the one shown below.



The height of the candle is 13 cm and the circumference of the candle at its widest measure is 31.416 cm. Use modeling to approximate how much wax, to the *nearest cubic centimeter*, is needed to make this candle. Justify your answer.

(· 2 Tr 31, 416 - 2ttr 211 211 52r

V= 5 Trzh : 1/3 TT (5)2.13 ~ 340

Part IV

Answer the 2 questions in this part. Each correct answer will receive 6 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. Utilize the information provided for each question to determine your answer. Note that diagrams are not necessarily drawn to scale. For all questions in this part, a correct numerical answer with no work shown will receive only 1 credit. All answers should be written in pen, except for graphs and drawings, which should be done in pencil. [12]

35 In quadrilateral ABCD, $AB \cong CD$, $AB \parallel CD$, and BF and DE are perpendicular to diagonal AC at points F and E. D С F Prove: $AE \cong CE$ Fatemen 1) Quadr. lateral ABCD,

 AB = CD, ABIICU, + UT

 DEune ⊥ to diagnonal AC

 1) LAED + LCFB are rt. Ls 2) ⊥ lines for rt. Ls

 3) LAED = LCFB

 3) LAED = LCFB

 3) LAED = LCFB

 3) AED = Saparallelogram 4) A guadrilateral with ore pair of situs = 4 II is a parallelogram 5. The same of situs = 4 II is a parallelogram

 AB ACD, AB 11 CD, + BF 4 5) Opposite sides of a parallelogium ADIBU 6) Il lines cot by a transversal Form congruent alternate interior Ls. LDAE = ZBCF Opposite siles of a pavallelogram que congruent IAAS 7|DA ≌BC)CBŁ PCTC

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36 New streetlights will be installed along a section of the highway. The posts for the streetlights will be 7.5 m tall and made of aluminum. The city can choose to buy the posts shaped like cylinders or the posts shaped like rectangular prisms. The cylindrical posts have a hollow core, with aluminum 2.5 cm thick, and an outer diameter of 53.4 cm. The rectangular-prism posts have a hollow core, with aluminum 2.5 cm thick, and a square base that measures 40 cm on each side. The density of aluminum is 2.7 g/cm^3 , and the cost of aluminum is 0.38 per kilogram. If all posts must be the same shape, which post design will cost the town less? How much money will be saved per streetlight post with the less expensive design? Cylinder $V = \Pi(26.7)^{2} (750) - \Pi(24.2)^{2} (750) = 95,437.5 \Pi$ 95,437.5TT cm² (2.79) (1 Kg) (10009) (10.38) ~ 307.62 $\frac{Prism}{V=40^{2}(750)-35^{2}(750):281,250}{281,250}:281,250 \text{ cm}^{3}(\frac{2.79}{cm^{3}})(\frac{1kg}{1000g})(\frac{$0.38}{kg})\approx 288.56}{\overline{8}19.06}$ Work space for question 36 is continued on the next page.