APPENDIX B: PLANE GEOMETRY

32. Two sides of a triangular plot of ground meet at an angle of 76°. One of these sides is 60 feet and the other is 140 feet.

- a. Find to the nearest tenth of a foot the altitude to the side whose length is 140 feet. [3]
- b. Find the area of the triangle to the nearest square foot. [4]
- c. If a drawing of this plot is made on a scale of 1 inch = 20 feet, find the area of this drawing to the nearest square inch. [3]

33. Equal circles O and O'are tangent to each other. OO' is extended to meet circle O' at A. AC is tangent to circle O at C and intersects circle O' at B. O'D is perpendicular to AC. The radius of each circle is 6. Find AO, O'D, AD, AC, BC. [Answers may be left in radical form.] [2, 2, 2, 2, 2, 2]

34. A shelf of a corner bookcase has the form of a square from which a quadrant, *EBF*, has been cut. [A quadrant is a quarter of a circle.] Arc *EF* is 15.7 inches. *E* is the midpoint of *AB*. Using $\pi = 3.14$,



b. find the area of quadrant EBF

c. find the area of shelf AEFCD



PART I

Answer all questions in this part. Each correct answer will receive 2 credits. No partial credit will be allowed. Unless otherwise specified, answers may be left in terms of π or in radical form.





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SPECIMEN REGENTS EXAMINATIONS

1. The sum of the interior angles of a polygon is 1,980°. Find the number of sides of the polygon.

2. An exterior angle at the base of an isosceles triangle is 105°. Find the number of degrees in the vertex angle of this triangle.

3. Chords AB and CD of a circle intersect at E. If AE is 5, EB is 6 and CE is 4, find ED.

4. In parallelogram ABCD, angle A contains x degrees and angle B contains (2x - 30) degrees. Find the number of degrees in angle A.

5. Secants ABC and ADE are drawn from external point A to a circle. If arc BD is 30° and arc CE is 100°, find the number of degrees in angle A.

6. The perimeter of a triangle is 18. Find the perimeter of the triangle formed by joining the midpoints of the sides of the given triangle.

7. In triangle ABC, a line parallel to BC intersects AB at D and AC at E. If AD is 9, DB is 6 and AE is 12, find EC.

8. A tangent and a secant are drawn from an external point to a circle. If the secant is 7 and its external segment is 3, find the tangent.

9. In right triangle ABC, CD is the altitude to the hypotenuse AB. If AD is 4 and AB is 25, find AC.

10. In rectangle ABCD, diagonal AC is 11 and side AB is 9. Find angle CAB to the nearest degree. 10.... 11. The side of a square is a. Express the diagonal in terms of a.

12. Find an altitude of an equilateral triangle whose side is 6.

13. The area of a rhombus is 60 and one diagonal is 10. Find the other diagonal.

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APPENDIX B: PLANE GEOMETRY

14....

15....

19.

14. The areas of two similar triangles are 20 and 45. If a side of the smaller triangle is 4, find the corresponding side of the larger triangle.

15. The hypotenuse of a right triangle is 6 inches. Find the number of inches in the median to the hypotenuse.

16. The circumference of a circle is 54 inches. Find the number of inches in an arc of 80° on this circle. $16.\ldots$

Directions (17-20): Indicate the correct completion for each of the following by writing the letter a, b or c on the line at the right.

17. If the greatest number of common tangents that can be drawn to two circles is three, the circles are (a) internally tangent (b) intersecting
(c) externally tangent 17.....

18. Consider scalene triangle ABC. The locus of points equally distant from A and B is (a) the bisector of the angle opposite AB (b) the median to AB (c) the perpendicular bisector of AB 18....

19. In triangle ABC, angle A is 60° and angle C is larger than angle B. The longest side of the triangle is (a) AB (b) AC (c) BC

20. If a pupil in a certain school has room 222 as a homeroom, he is a sophomore. Which of the following statements expresses a conclusion that follows logically from the given statement? (a) John is a sophomore in this school; therefore he has room 222 as a homeroom. (b) Tom is a junior in this school; therefore he does not have room 222 as a homeroom. (c) Paul has room 224 as a homeroom in this school; therefore he is not a sophomore. 20...

Directions (21-24): For each of the following, tell whether the statement is always true, sometimes true or never true by writing the word always, sometimes or never on the line at the right.

21. Two parallel lines are cut by a transversal. The bisectors of the two interior angles on the same side of the transversal are perpendicular to each other. 21....

22. The bisectors of two opposite angles of a parallelogram coincide.

23. If two angles intercept the same arc of a circle, they are equal. 23....

24. If perpendiculars from the center of a circle to the sides of an inscribed polygon are equal, the polygon is equilateral. 24.....

Directions (25): Leave all construction lines on the paper.

25. Divide line segment AB into two parts proportional to x and y.

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PART II

Answer three questions from this part.

26. Prove: The diameter perpendicular to a chord of a circle bisects the chord and its minor arc. [10]

27. In isosceles triangle ABC, CA equals CB. D is a point on CA and E is a point on CB such that AD equals BE. BDis drawn and extended its own length through D to X. AE is drawn and extended its own length through E to Y, and XAand YB are drawn. Prove:

(a)
$$BD = AE$$
 [6]
(b) $XA = YB$ [4]

28. Prove: The area of a triangle is equal to one-half the product of a side and the altitude drawn to that side. [10]

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22....

29. AB is a diameter of circle O, RB is a tangent at B, chords AEand AC are drawn on opposite sides of AB such that arc BE equals arc BC and chord AE is extended to meet RB at D.

Prove: AD:AB = AB:AC. [10]



PART III

Answer two questions from this part. Show all work.

31. In the accompanying figure, the tangent at C meets chord DB extended at F; chord AB extended meets FC at E; BD intersects AC at R.



a Find the number of degrees in arcs AB, BC, CD, DA.
[4]

b Find the number of degrees in angles 1, 2, 3. [6]



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32. In an isosceles trapezoid ABCD, AB is the longer base and DC is the shorter base. AD and BC are extended to meet in R. DC is 6, AB is 18 and AD is 5 more than DR.

a If DR is represented by x, express AD in terms of x.
[1]

- $b \operatorname{Find} AD.$ [4]
- c Find the altitude of trapezoid ABCD. [3]
- d Find the area of trapezoid ABCD. [2]

33. The radius of a regular 9-sided polygon is 14.

- a Find the apothem of the polygon to the nearest integer. [5]
- b Find a side of the polygon to the nearest integer. [3]
- c Using the results found in answer to parts a and b, find the area of the polygon. [2]

34. The perimeter of a square and the circumference of a circle are each 176. Find the amount by which the area of the circle exceeds the area of the square. [Use $\pi = \frac{22}{7}$.] [10]