

A2.S.10: Permutations: Calculate the number of possible permutations of n items taken r at a time

- 1 Which value is equivalent to ${}_3P_3$?
 - 1) 1
 - 2) 9
 - 3) $3!$
 - 4) 27
- 2 A four-digit serial number is to be created from the digits 0 through 9. How many of these serial numbers can be created if 0 can *not* be the first digit, no digit may be repeated, and the last digit must be 5?
 - 1) 448
 - 2) 504
 - 3) 2,240
 - 4) 2,520
- 3 How many different six-letter arrangements can be made using the letters of the word "TATTOO"?
 - 1) 60
 - 2) 90
 - 3) 120
 - 4) 720
- 4 What is the total number of different nine-letter arrangements that can be formed using the letters in the word "TENNESSEE"?
 - 1) 3,780
 - 2) 15,120
 - 3) 45,360
 - 4) 362,880
- 5 How many different 11-letter arrangements are possible using the letters in the word "ARRANGEMENT"?
 - 1) 2,494,800
 - 2) 4,989,600
 - 3) 19,958,400
 - 4) 39,916,800
- 6 How many distinct ways can the eleven letters in the word "TALLAHASSEE" be arranged?
 - 1) 831,600
 - 2) 1,663,200
 - 3) 3,326,400
 - 4) 5,702,400
- 7 Which formula can be used to determine the total number of different eight-letter arrangements that can be formed using the letters in the word *DEADLINE*?
 - 1) $8!$
 - 2) $\frac{8!}{4!}$
 - 3) $\frac{8!}{2!+2!}$
 - 4) $\frac{8!}{2! \cdot 2!}$

- 8 Which expression represents the number of different 8-letter arrangements that can be made from the letters of the word "SAVANNAH" if each letter is used only once?
- $\frac{8!}{5!}$
 - $\frac{8!}{3!2!}$
 - ${}_8P_5$
 - $8!$
- 9 Which expression represents the total number of different 11-letter arrangements that can be made using the letters in the word "MATHEMATICS"?
- $\frac{11!}{3!}$
 - $\frac{11!}{2!+2!+2!}$
 - $\frac{11!}{8!}$
 - $\frac{11!}{2! \cdot 2! \cdot 2!}$
- 10 The number of possible different 12-letter arrangements of the letters in the word "TRIGONOMETRY" is represented by
- $\frac{12!}{3!}$
 - $\frac{12!}{6!}$
 - $\frac{{}_{12}P_{12}}{8}$
 - $\frac{{}_{12}P_{12}}{6!}$
- 11 Find the total number of different twelve-letter arrangements that can be formed using the letters in the word *PENNSYLVANIA*.
- 12 Find the number of possible different 10-letter arrangements using the letters of the word "STATISTICS."
- 13 Determine how many eleven-letter arrangements can be formed from the word "CATTARAUGUS."
- 14 The letters of any word can be rearranged. Carol believes that the number of different 9-letter arrangements of the word "TENNESSEE" is greater than the number of different 7-letter arrangements of the word "VERMONT." Is she correct? Justify your answer.

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Answer Section

1 ANS: 3 REF: 010713a

2 ANS: 1

$8 \times 8 \times 7 \times 1 = 448$. The first digit cannot be 0 or 5. The second digit cannot be 5 or the same as the first digit. The third digit cannot be 5 or the same as the first or second digit.

REF: 011125a2

3 ANS: 1

$$\frac{{}_6P_3}{3!2!} = \frac{720}{12} = 60$$

REF: 011324a2

4 ANS: 1

$$\frac{{}_9P_4}{4! \cdot 2! \cdot 2!} = \frac{362,880}{96} = 3,780$$

REF: 061511a2

5 ANS: 1

$$\frac{{}_{11}P_{11}}{2!2!2!2!} = \frac{39,916,800}{16} = 2,494,800$$

REF: 011518a2

6 ANS: 1

$$\frac{{}_{11}P_{11}}{3!2!2!2!} = \frac{39,916,800}{48} = 831,600$$

REF: 081512a2

7 ANS: 4 REF: fall0925a2

8 ANS: 2 REF: 080727a

9 ANS: 4 REF: 011409a2

10 ANS: 3
 $2! \cdot 2! \cdot 2! = 8$

REF: 061425a2

11 ANS:

$$39,916,800 \cdot \frac{{}_{12}P_{12}}{3! \cdot 2!} = \frac{479,001,600}{12} = 39,916,800$$

REF: 081035a2

12 ANS:

$$\frac{{}_{10}P_{10}}{3! \cdot 3! \cdot 2!} = \frac{3,628,800}{72} = 50,400$$

REF: 061330a2

13 ANS:

$$\frac{11!}{3! \cdot 2! \cdot 2!} = 1,663,200$$

REF: 011631a2

14 ANS:

$$\text{No. TENNESSEE: } \frac{{}_9P_9}{4! \cdot 2! \cdot 2!} = \frac{362,880}{96} = 3,780. \text{ VERMONT: } {}_7P_7 = 5,040$$

REF: 061038a2