

F.IF.B.4: Evaluating Logarithmic Expressions

1 The expression $\log_8 64$ is equivalent to

- | | |
|------|------------------|
| 1) 8 | 3) $\frac{1}{2}$ |
| 2) 2 | 4) $\frac{1}{8}$ |

2 The expression $\log_5 \left(\frac{1}{25} \right)$ is equivalent to

- | | |
|------------------|-------------------|
| 1) $\frac{1}{2}$ | 3) $-\frac{1}{2}$ |
| 2) 2 | 4) -2 |

3 The loudness of sound is measured in units called decibels (dB). These units are measured by first assigning an intensity I_0 to a very soft sound that is called the threshold sound. The sound to be measured is assigned an intensity, I , and the decibel rating, d , of this sound is found using $d = 10 \log \frac{I}{I_0}$. The threshold sound audible to the average person is $1.0 \times 10^{-12} \text{ W/m}^2$ (watts per square meter). Consider the following sound level classifications:

Moderate	45-69 dB
Loud	70-89 dB
Very Loud	90-109 dB
Deafening	>110 dB

How would a sound with intensity $6.3 \times 10^{-3} \text{ W/m}^2$ be classified?

- | | |
|-------------|--------------|
| 1) moderate | 3) very loud |
| 2) loud | 4) deafening |

4 If $\log_9 81 = x$, find x .

5 Find the value of n : $\log_{100} 10,000 = n$

6 If $x = \log_2 9$, find, to the *nearest tenth*, the value of x .

- 7 If $\log_3 5 = x$, find x to the *nearest tenth*.
- 8 Solve for x to the *nearest hundredth*: $\log_7 75 = x$
- 9 Find the value of $\log 58.43$ to four decimal places.
- 10 Find the value of $\log 429.7$ correct to *four decimal places*.
- 11 Find $\log 742.6$ to the *nearest ten-thousandth*.
- 12 Find $\log 1985$ to *four* decimal places.
- 13 Find $\log 2001$ to the *nearest ten-thousandth*.
- 14 The scientists in a laboratory company raise amebas to sell to schools for use in biology classes. They know that one ameba divides into two amebas every hour and that the formula $t = \log_2 N$ can be used to determine how long in hours, t , it takes to produce a certain number of amebas, N . Determine, to the *nearest tenth of an hour*, how long it takes to produce 10,000 amebas if they start with one ameba.
- 15 Evaluate $e^{x \ln y}$ when $x = 3$ and $y = 2$.
- 16 The expression $\log_2(x - 4)$ is undefined for all values of x such that
 - 1) $x > 1$
 - 2) $x > 0$
 - 3) $x \leq 4$
 - 4) $x \leq 0$
- 17 The expression $\log_3(8 - x)$ is defined for all values of x such that
 - 1) $x > 8$
 - 2) $x \geq 8$
 - 3) $x < 8$
 - 4) $x \leq 8$

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Answer Section

1 ANS: 2

$$8^2 = 64$$

REF: fall0909a2

2 ANS: 4 REF: 011124a2

3 ANS: 3

$$d = 10 \log \frac{6.3 \times 10^{-3}}{1.0 \times 10^{-12}} \approx 98$$

REF: 011715a2

4 ANS:

2

REF: 068110siii

5 ANS:

2

REF: 019407siii

6 ANS:

3.2

REF: 018941siii

7 ANS:

1.5

REF: 088637siii

8 ANS:

2.22

REF: 089940siii

9 ANS:

1.7666

REF: 018412siii

10 ANS:

2.6332

REF: 068114siii

11 ANS:

2.8708

REF: 018503siii

12 ANS:
3.2978

REF: 068507siii

13 ANS:
3.3012

REF: 088613siii

14 ANS:

$$t = \log_2 10000$$

$$2^t = 10000$$

$$13.3. \log 2^t = \log 10000$$

$$t \log 2 = \log 10000$$

$$t = \frac{\log 10000}{\log 2} \approx 13.3$$

REF: 060125b

15 ANS:

$$e^{3 \ln 2} = e^{\ln 2^3} = e^{\ln 8} = 8$$

REF: 061131a2

16 ANS: 3 REF: fall9904b

17 ANS: 3 REF: 010412b